# COUPLED WIND-SEA MODELS AND THEIR IMPACT ON FLUXES OF MOMENTUM, SENSIBLE HEAT AND LATENT HEAT

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1993

Canadian Technical Report of Hydrography and Ocean Sciences 149

# Canadian Technical Report of Hydrography and Ocean Sciences

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by

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Correct citation for this publication:

Wang, L. and W. Perrie. 1993. Coupled wind-sea models and their impact on fluxes of momentum, sensible heat and latent heat. Can. Tech. Rep. Hydrogr. Ocean Sci. 149: viii + 131 pp.

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#### ABSTRACT

Wang, L. and W. Perrie. 1993. Coupled wind-sea models and their impact on fluxes of momentum, sensible heat and latent heat. Can. Tech. Rep. Hydrogr. Ocean Sci. 149: viii + 131 pp.

In this report, we discuss coupled models for the atmospheric boundary layer and wind-sea in one-dimension and in two-dimensions. A coupling mechanism for the interactions between boundary layer and sea surface layer is proposed. Various characteristics of this mechanism are discussed.

The coupled wind-sea model is used to estimate, study and discuss the fluxes of momentum, sensible heat and latent heat. A new mechanism for calculating these fluxes is proposed, after considering the impacts of the sea state on calculated fluxes.

Results show that the influence of sea states on sea surface roughness Zo is very important for younger waves. The forecasted significant wave heights are clearly improved and the fluxes are increased in the coupled model, as compared to the uncoupled WAM model, particularly under stronger wind speeds.

#### RESUME

Wang, L. and W. Perrie. 1993. Coupled wind-sea models and their impact on fluxes of momentum, sensible heat and latent heat. Can. Tech. Rep. Hydrogr. Ocean Sci. 149: viii + 131 pp.

Le présent rapport traite de modèles unidimensionnels et bidimensionnels de couplage de la couche limite atmosphérique et de l'interface vent-mer. On y propose un mécanisme de couplage pour les interactions entre la couche limite et la couche de la surface de la mer. Diverses caractéristiques de ce mécanisme sont abordés.

Le modèle de couplage du vent et de la mer sert à estimer, à étudier et à analyser les flux de quantité de mouvement, de chaleur sensible et de chaleur latente. Un nouveau mécanisme est proposé pour calculer ces flux en tenant compte des effets de l'état de la mer sur ces calculs.

Les résultats montrent que l'effet des états de la mer sur la rugosité de la surface de la mer Zo est très important dans le cas des jeunes vagues. Les prévisions de la hauteur significative des vagues sont nettement meilleures et les flux sont plus grands dans le modèle de couplage que dans le modèle WAM sans couplage, surtout lorsque la vitesse du vent est élevée.

#### 1. INTRODUCTION

Experience shows that the forecasting of significant wave height using the WAM third generation model is usually lower by about 25-40 percent from the observations, especially in these cases where the wind speed is very strong or wind direction is suddenly changed (this will be presented also here). Although the wind speed and direction predicted in meteorological models may need some improvements, the WAM model should also have some improvements physically.

There are three inconsistencies the WAM model has. First of all, the WAM model uses the wind speed at 10 m height V10, to produce a friction velocity U\* which is then used to predict the significant wave height. However, this V10 is produced by a meteorological boundary layer model using the friction velocity U\*, sea surface roughness Zo and some thermal conditions. The friction velocity U\* in the wave model is produced by empirical formulae which are obtained at specific locations, specific times and for specific cases and this U\* is not the same as the U\* in the atmospheric model. Secondly, the roughness Zo, is dependent on the wind profile with height rather than the wind itself at 10 meters above the sea level. The WAM model uses the Charnock formula which states that Zo depends only on the wind speed at 10 m height. If we have two different wind profiles with height but they have the same wind speed at 10 meters above the sea level, the forecasting of significant wave height is the same in the WAM model, although it is under different conditions physically. This is unreasonable. Thirdly, the reaction of sea states on the wind profile with height is not taken into account in the WAM third generation model.

On the other hand, the geostrophic wind, in meteorology, is used to express the balance relationship between the gravitational potential field and the wind field. The thermal wind is used to express the balance relationship between the change of wind with height and the mean temperature field. The question remains as to the relationship between the wind profile with height and the sea states. The solution is to couple the wave model with the boundary layer model.

The calculated wind over the sea surface in meteorological models will be shown to be revised when the roughness of the sea surface is considered as a function of sea state. We assume that the revised wind is in such a balance state; that the roughness, friction velocity and wave age are in a balance state, that these variables have the same values in the boundary layer model as in the wind-sea model. We use such a roughness, friction velocity and revised thermal variables to calculate the revised wind. The revised wind is therefore shown to be a consequence of the sea state dependence of the sea surface roughness Zo.

#### 2. A MECHANISM ON COUPLING WIND AND SEA WAVE

The dynamic coupling between the atmosphere and the ocean has been the subject of much research. Although the effects of some characteristic properties are becoming more clear, the extremely complex processes of air-sea interaction are still not fully understood. The best-known expression for the roughness of the sea surface Zo is the one proposed by Charnock (1955), which indicated that the roughness of the sea surface depend only on friction velocity: all characteristics of the wave field are missing. Several field data sets show different constants for Charnock formula. Wu (1980) proposed a value of 0.0185 as shown in Eq.(2.1) after averaging different constants from a wide range of circumstances.

$$z_0 = 0.0185 \times \left\{ \frac{U^{\frac{2}{4}}}{G} \right\} \qquad (2.1)$$

Several studies from laboratories and from the field (Toba and Koga, 1986; Toba et al. 1990; Geernaert et al. 1987 show that the wave age  $C_P/U^*$  (in which  $C_P$  is the phase velocity of the wave at the peak of the spectrum and  $U^*$  is the friction velocity in the air) is an important parameter for the description of roughness  $Z_O$ . They claim that the roughness actually decreases with decreasing wave age as expressed in Eq.(2.2),

$$Zo = 0.025 \times \left\{ \frac{C_p}{U^*} \right\} \times \left\{ \frac{U^2}{G} \right\}$$
 (2.2)

which shows the roughness is in direct proportion to wave age.

Nordeng (1991) proposed that the roughness depends strongly on wave age with a maximum value for  $C_P/U^*$  around 5, for a young sea, and it is a function of wave age as shown in Eq. (2.3).

$$Zo = 0.11 \times \left\{ \frac{C_p}{U^*} \right\}^{-3/4} \times \left[ 1 - e^{-W} \left( 1 + \frac{W^2}{2} + \frac{W^3}{6} \right) \right]^{1/2} \left\{ \frac{U^{\frac{2}{*}}}{G} \right\} \quad (2.3)$$

where  $W = 2 \times \kappa \left\{ \frac{C_p}{U^*} \right\}$  , and  $\kappa$  is the Von Kármán constant.

From the HEXMAX 1986 field data set, Maat et al., (1991) proposed that the roughness is assumed to depend mainly on the wave age in a relationship of the form:

#### 1. INTRODUCTION

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$$Zo = \mu \times \left( \frac{U_*^2}{G} \right) \times \left( \frac{C_p}{U_*} \right)^n \qquad (2.4)$$

Several results may be summarized as follows:

- (1). Charnock (1958)  $n = 0, \mu = 0.012$
- (2). Wu (1980) n = 0,  $\mu = 0.0185$
- (3). Toba and Koga (1986) n = 1,  $\mu = 0.025$
- (4). Hsu (1974, 1986) n = -1/2,  $\mu = 0.90$
- (5). Maat et al.,(1991) proposed a relationship from HEXMAX data, which shows : n=-1,  $\mu=0.80$
- (6). Donelan (1990) reviewed several earlier published data and calculated the ratio  $\rm Zo/H_S$  as a function of wave age  $\rm C_P/U^*$ , which also implies : n  $\cong$  -1.
- (7). Theoretical studies with numerical models based on resonant wave-mean flow interaction and the quasilinear theory of wind-wave generation, Janssen (1989) calculated the effect of both gravity waves and air turbulence on the wind profile, which provides an exponent n = -1.2.

Recently, Smith et al., (1992) applied corrections to the HEXOS data for flow distortion and revised the Maat et al. formula and set  $\mu$  = 0.48 instead of 0.80. Therefore, roughness decreases with increasing wave age.

Fig.1a-c show the changes of surface roughness with wave age using different relationships as mentioned above. In these figures, "Wu" is calculated by Eq.(2.1), "RPN" is calculated using 0.032 instead of 0.0185 in Eq.(2.1). The operational model at RPN uses 0.032. Toba's result in Fig.1a shows that the older waves are rougher than younger waves. Donelan et al., (1993) pointed out that the conclusion is inappropriate and misleading. Scaling with U• is unreliable because significant variations in U• will produce a spurious correlation, masking the sought-after relation between roughness and sea state.

Hsu's result in Fig.1b seems also inappropriate. Although the roughness is decreasing with increasing wave age, the roughness is always greater than those calculated by "RPN" and "Charnock" which had support from field data. Nordeng's result is always less than Charnock's except when the wave age is less than 10.

Smith's result (see Fig.1c) seems reasonable. Wu's formula is the same as Smith's with the wave age around 26. RPN's parameterization is the same as Smith's with the wave age nearly 15. This indicates that the Charnock "CONSTANT" as selected as constant at any time or any location is unreasonable. The Charnock "CONSTANT" should be controlled by a sea state equation, such as the sea wave equation.

In this paper, we use Wu's formula Eq.(2.1) to calculate the roughness in our UNCOUPLED MODEL, and Smith's formula, which is expressed as follows:

$$Zo = 0.48 \times \left\{ \frac{C_p}{U^*} \right\}^{-1} \times \left\{ \frac{U^2}{G} \right\}$$
 (2.5)

in our COUPLED MODEL.

#### 3. WAVE AND BOUNDARY LAYER MODELS

# 3.1 Third generation wave (WAM) model

We integrate the spectral energy balance equation for wind-generated waves in time. We use the formulations of the WAM model (Hasselmann et al., 1989) for non-linear transfer, energy input due to the wind, and energy removed due to dissipative breaking.

The spectral energy density for surface gravity waves in deep water  $E(f,\theta)$  evolves in space and time according to the relation

$$\frac{\partial E(f,\theta)}{\partial t} + \underline{c}_{q} \cdot \nabla E(f,\theta) = \varphi_{in} + \varphi_{nl} + \varphi_{ds}$$
 (3.1)

where  $\varphi_{\rm in}$  is the spectral energy input by the wind,  $\varphi_{\rm ds}$  is the dissipation due to wave breaking and white-cap formation and  $\varphi_{\rm nl}$  is the change in spectral energy due to non-linear transfer resulting from wave-wave interactions.

Parameterizations for wind input energy  $\varphi_{\rm in}$  are heavily motivated by the observations of Snyder et al (1981). The form is

$$\varphi_{in} \cong \beta E(f, \theta)$$
 (3.2)

where  $\beta$ , as specified by Hasselmann et al (1989), is given by

$$\beta = \max \left\{ 0, \ 0.25 \frac{\rho_{a}}{\rho_{w}} \left( 28 \frac{U^{*}}{\zeta} \cos \theta - 1 \right) \right\} \omega \tag{3.3}$$

where  $\rho_{\rm a}$  and  $\rho_{\rm w}$  are air and water density respectively, the friction velocity in the wave direction is U\* cos  $\theta$  with  $\theta$  the direction of the wind relative to the wave propagation direction, phase velocity is  $\zeta = \omega/k$  and angular frequency  $\omega$  is related to wavenumber k through the deep water dispersion relation.

Dissipation due to wave breaking  $\varphi_{\rm ds}$  is assumed to have a simple form, motivated by Hasselmann (1974), as well as numerical experiments completed in Hasselmann et al (1989), and may be written as follows:

$$\varphi_{ds} \cong g k^{-4} \mathcal{F}(k^{4}F(\underline{k}))$$
 (3.4)

where  $k=|\underline{k}|$ ,  $F(\underline{k})$  is the energy spectrum in vector wavenumber space  $\underline{k}$  and  $\mathcal{F}$  is an appropriate functional. It is usually taken as

$$\mathcal{F}_{ds} = -2.33 \times 10^{-5} \hat{\omega} \left(\frac{\omega}{\hat{\omega}}\right)^2 \left(\frac{\hat{\alpha}}{\hat{\alpha}_{pm}}\right)^2 \quad E(f,\theta)$$
 (3.5)

where

$$\hat{\omega} = \left( E_0^{-1} \iint E(f,\theta) \omega^{-1} df d\theta \right)^{-1}$$
 (3.6)

$$\hat{\alpha} = E_0 \hat{\omega}^4 g^{-2}$$
,  $E_0 = \int \int E(f,\theta) df d\theta$  (3.7)

and

$$\hat{\alpha}_{pm} = \frac{2}{3} E_0 g^{-2} \left( E_0^{-1} \iint E(f,\theta) \omega df d\theta \right)^4 \Big|_{Pierson-Moskowitz}$$

$$\approx 0.003$$

The complete representation for non-linear transfer due to wave-wave interactions  $\varphi_{\rm nl}$  can be represented in term of a 6-fold Boltzmann integral in wavenumber space by Hasselmann (1961),

$$\mathcal{F}_{n1} (\underline{\mathbf{k}}_{1}) = \iiint \zeta^{2}(\underline{\mathbf{k}}_{1}, \underline{\mathbf{k}}_{2}, \underline{\mathbf{k}}_{3}, \underline{\mathbf{k}}_{4}) \mathcal{D}(\underline{\mathbf{k}}_{1}, \underline{\mathbf{k}}_{2}, \underline{\mathbf{k}}_{3}, \underline{\mathbf{k}}_{4})$$

$$\delta(\underline{\mathbf{k}}_{1} + \underline{\mathbf{k}}_{2} - \underline{\mathbf{k}}_{3} - \underline{\mathbf{k}}_{4}) \delta(\omega_{1} + \omega_{2} - \omega_{3} - \omega_{4}, \underline{\mathbf{k}}_{2} \underline{\mathbf{d}} \underline{\mathbf{k}}_{3} \underline{\mathbf{d}} \underline{\mathbf{k}}_{4})$$

$$(3.9)$$

The WAM approximation to equation (3.9) is described in Hasselmann et al (1989) and is based on the so-called discreted interaction approximation.

The two-dimensional wave spectrum  $E(f,\theta)$  at every grid point is represented by 54 frequencies and 12 directions for a total of 648 spectral elements. The 54 frequencies range from 0.0417725 Hz to 0.65268 Hz increasing in geometric progression with a constant ratio of 1.1. The 12 directional bands have a bandwidth of 30 degrees everywhere.

The significant wave height is given by the total wave energy Eo as expressed

$$H_s = 4.0 \sqrt{E_0}$$
 (3.10)

The total energy Eo can be obtained by summing  $E(f,\theta)$  values over all frequency and directional bands.

# 3.2 Wave spectrum with frequency

We use an experimental spectrum (3.11) to compare with the Pierson-Moskowitz spectrum (3.12), JONSWAP -3/2 law (3.13) and JONSWAP -2/3 law (3.14). They are expressed as follows respectively:

## (1). NEW SPECTRUM

$$F(f) = 0.48 \left(\frac{C_p}{U^*}\right)^{-1} g^2 (2\pi)^{-4} f^{-5} \exp\left\{-\frac{5}{4} \left(\frac{f_p}{f}\right)^4\right\}$$
(3.11)

# (2). Pierson-Moskowitz SPECTRUM

$$F(f) = 0.0081 g^{2} (2\pi)^{-4} f^{-5} exp \left\{ -\frac{5}{4} \left( \frac{f_{p}}{f} \right)^{4} \right\} \times \left( \frac{exp}{2\sigma^{2}f^{2}} \right)$$
(3.12)

# (3). JONSWAP -3/2 law

$$F(f) = 0.57 \left( \frac{C_p}{U^*} \right)^{3/2} g^2 (2\pi)^{-4} f^{-5} \exp \left\{ -\frac{5}{4} \left( \frac{f_p}{f} \right)^4 \right\} \times \left( \frac{(f - f_p)^2}{2\sigma^2 f^2} \right)$$
(3.13)

# (4). JONSWAP -2/3 law

$$F(f) = 0.054 \left(\frac{C_p}{U^*}\right)^{-2/3} g^2 (2\pi)^{-4} f^{-5} exp \left\{-\frac{5}{4} \left(\frac{f_p}{f}\right)^4\right\} \times exp \left(-\frac{(f-f_p)^2}{2\sigma^2 f^2}\right)$$
(3.14)

Equations (3.13) and (3.14) are employed by Janssen (1989), using different interpretations of the JONSWAP results of Hasselmann et al (1973). Fig. 2a-b show the wave spectrum with frequency at different wind speeds (10 m/s, Fig.2a; and 20 m/s, Fig.2b). It is shown that the energy is higher in (3.11) than the other spectra in the higher frequency region. The peak frequency will move toward lower frequency when the wind speed increases.

## 3.3 Boundary-layer model

The boundary layer model used here is quite similar to the operational boundary layer model at RPN, as documented by Delage (1988a, 1988b).

The vertical surface fluxes of momentum, sensible heat and latent heat are computed from surface (i.e., subscript s), which can be written as follows respectively,

$$\overline{|\mathbf{w}'\mathbf{v}'|_{S}} = (C_{m}|\mathbf{v}_{a}|)^{2}$$
 (3.15)

$$\overline{(\mathbf{w}'\mathbf{T}')}_{\mathbf{S}} = C_{\mathbf{p}}C_{\mathbf{m}}C_{\mathbf{T}}|\mathbf{V}_{\mathbf{a}}|(\mathbf{T}_{\mathbf{S}}-\mathbf{T}_{\mathbf{a}})$$
 (3.16)

$$\overline{(w'q')}_{s} = L C_{m}C_{T}|V_{a}|(q_{s}-q_{a})$$
(3.17)

Here  $C_m$ ,  $C_T$  are transfer coefficients for momentum and heat and are functions of the Richardson number Rib, anemometer level  $Z_a$  and roughness  $Z_0$ . The L is latent heat and  $C_p$  is specific heat at constant pressure.

In the stable case, the transfer coefficients can be written as

$$C_{\rm m} = \frac{\kappa}{\zeta_{\rm a}} F_{\rm m} \tag{3.18}$$

$$C_{T} = \frac{\kappa}{\zeta_{a}} F_{T}$$
 (3.19)

Here  $\kappa=0.035$  is Von Kármán constant and  $\zeta_a=\ln\left(\frac{Z_a+Z_0}{Z_0}\right)$ ,  $Z_a$  is the reference level and  $F_m$  and  $F_T$  are transfer functions given below. Empirical expressions for  $F_m$  and  $F_T$  were selected for their ability to simulate the Wangara data (Delage, 1988a, 1988b).

$$F_{\rm m} = 1 - \frac{\text{Rib}}{M} \left( \frac{2}{1 + (1 + \frac{2x}{M})^{1/2}} \right)$$
 (3.20)

$$F_{T} = 1 - \frac{Rib}{M} \left( \frac{2}{1 + (1 + \frac{2x'}{M})^{1/2}} \right)$$
 (3.21)

where M = Max(Ric,Rib+1/a), Ric = 0.2 and a = 10.0;  $x=\zeta_a z_*d/H$ ,  $x'=\zeta_a z_*d'/H$ ,  $z_*=$  Max(Za -10m, 0), d and d' are parameters, H is the height of boundary layer.

In the unstable case, the functions for momentum and heat exchange at the surface are calculated as follows:

$$C_{m} = 1/FQ (3.22)$$

$$C_{\tau} = 1/FH \tag{3.23}$$

where

$$FQ = \ln\left(\frac{Z_a + Z_0}{Z_0}\right) + \ln\left\{\frac{(X_0 + 1)^2 (X_0^2 - X_0 + 1)^{1/2} (X_0^2 + X_0 + 1)^{3/2}}{(X + 1)^2 (X^2 - X + 1)^{1/2} (X^2 + X + 1)^{3/2}}\right\} + \sqrt{3}\left\{\tan^{-1}\left(\sqrt{3} - \frac{(X^2 - 1) X_0 - (X_0^2 - 1) X}{(X_0^2 - 1) (X^2 - 1) + 3XX_0}\right)\right\}$$
(3.24)

$$FH = \ln\left(\frac{Z_a + Z_{OT}}{Z_{OT}}\right) + \frac{3}{2} \ln\left\{\frac{Y_0^2 + Y_0 + 1}{Y^2 + Y + 1}\right\} + \sqrt{3} \tan^{-1}\left(\sqrt{3} \frac{2(Y - Y_0)}{(2Y_0 + 1)(2Y + 1) + 3}\right)$$
(3.25)

where

$$X = \left\{1-40.0 \times \left(Z_{a}+Z_{0}\right) \times \frac{\kappa \times C_{T} \times Rib}{C_{m}^{2} \times Z_{a}}\right\}^{1/6}$$
 (3.26)

$$\mathbf{x}_{0} = \left\{1 - 40.0 \times \mathbf{z}_{0} \times \frac{\kappa \times \mathbf{C}_{T} \times \mathbf{Rib}}{\mathbf{C}_{m}^{2} \times \mathbf{z}_{a}}\right\}^{1/6}$$
 (3.27)

$$Y = \left\{1-40.0 \times \left(Z_{a}+Z_{OT}\right) \times \frac{\kappa \times C_{T} \times Rib}{C_{m}^{2} \times Z_{a}}\right\}^{1/3}$$
 (3.28)

$$Y_0 = \left\{1-40.0 \times Zot \times \frac{\kappa \times C_T \times Rib}{C_m^2 \times Za}\right\}^{1/3}$$
 (3.29)

The boundary layer model implies the drag coefficient Co depends mainly on the roughness Zo rather than the wind speed at a desired anemometer level Za under neutral conditions as in equation (6.5) below. It is important to mention this result because there are many empirical relations which attempt to show a relation between drag coefficient and wind speed, such as equation (6.4) below from Hsu (1986). Fig 3 shows the change of drag coefficient Cd with wind speed at different roughness Zo. The values for Cd (=Cm\*Cm as shown in Eq. 3.15) are all constant at a designated Zo whatever the wind speed is. On the other hand, the roughness Zo is not dependent directly on the increasing wind speed either in the UNCOUPLED model or in the COUPLED model. It is dependent on wind profile with height (in the UNCOUPLED model) and sea states, such as wave age (in the COUPLED model). It is necessary to point out that the wave age also not depends directly on wind speed. The wave age will be change with time under a constant wind speed. Therefore, empirical relationships between drag coefficient and wind speed should not be imposed upon a model without a great amount of care, or inconsistencies will result.

Fig. 4 shows the variation of the coefficient of heat exchange  $C_MC_T$  with wind speed. The coefficient of heat exchange  $C_MC_T$  (as seen in Eqs. 3.16, 3.17) also depends mainly on roughness Zo according to the boundary layer model at a desired anemometer level  $Z_A$  under neutral conditions.

Figs. 5 and 6 show the friction velocity U\* and flux of momentum FM change with increasing wind speed at different designated roughness Zo respectively.

In the unstable case, Fig. 7-10 show the changes of corresponding drag coefficient  $C_d$ , coefficient of heat exchange  $C_MC_T$ , friction velocity  $U^*$  and flux of momentum FM at different temperature differences. The Fig. 11 is for flux of sensible heat FS. It is interested to find from Figs.7-10 that the drag coefficient  $C_d$ , the coefficient of heat exchange  $C_MC_T$ , the friction velocity  $U^*$  and the flux of momentum FM are largely insensitive to the magnitude of the temperature differences at high winds. The flux of sensible heat FS, as shown in Fig. 11, is sensitive to temperature differences at all wind speeds.

Fig. 12 shows the change of drag coefficient Cd with wave age at different roughness Zo in the neutral case. It is seen that the drag coefficient is unchangeable under designated roughness not only for wind speed but also for wave age. However, the drag coefficient is indirectly changed with wave age through roughness. It will be shown that the drag coefficient is decreased when the wave age increases, and in turn, the roughness increases, as the sea state evolves and matures.

Fig. 13-15 show the changes of coefficient of heat exchange, friction velocity and flux of momentum with wave age respectively.

Fig. 16-19 show the variation of the drag coefficient, and the coefficient of heat exchange, the friction velocity and the flux of momentum respectively at different temperature difference with wave age. Fig. 20 is for the case of flux of sensible heat. From these figures, it will be seen that the drag coefficient, the coefficient of heat exchange and the flux of sensible heat change under unstable case, especially under older wave age conditions. It is also interested that only the flux of sensible heat is sensitive for the younger waves.

#### 4. COUPLED ONE-POINT MODEL

Our COUPLED ONE-POINT MODEL is essential for duration-limited waves, evolving in response to forcing by wind that is initiated at an initial time. For a very large ocean, observations at very large fetch ( $>> 10^3$  km) will not experience advective effects. We assume that

$$\underline{\mathbf{C}}_{\mathbf{q}} \cdot \nabla \mathbf{E}(\mathbf{f}, \boldsymbol{\theta}) \ll \varphi_{\mathbf{in}} + \varphi_{\mathbf{nl}} + \varphi_{\mathbf{ds}}$$
 (4.1)

then, Eq.(3.1) may be written as follows:

$$\frac{\partial E(f,\theta)}{\partial t} \cong \varphi_{in} + \varphi_{nl} + \varphi_{ds}$$
 (4.2)

which is valid for growing windsea spectra at large fetch and we

can use this simple coupled model a explore some basic characteristics in comparison with the corresponding uncoupled model.

First of all, we assume that the wind speed and direction are unchanged with time. The peak frequency will be obtained through the wave model. If a first guess roughness Zo is assumed, the friction velocity U\* or drag coefficient Cd will be obtained from the boundary layer model. Therefore, a 'new' roughness is calculated using the Charnock formula (2.1, in the uncoupled model and Eq.(2.5) in the coupled model. If this 'new' roughness is within allowable error relative to the old roughness, we may proceed to the next time step in the simulation. Otherwise we must iterate, and using Cd, U\* and the wave model recompute the peak frequency. The boundary layer model then leads to a new estimates for Cd and U\*. Thence, Eq. (2.5) leads to a re-estimate of the roughness.

Fig. 21a-c show the change of roughness Zo with wave age at different constant wind speed  $V_{10}=10$  m/s (Fig.21a),  $V_{10}=20$  m/s (Fig.21b) and  $V_{10}=30$  m/s (Fig.21c). It is seen that the roughness is decreased with increasing wave age under constant wind speed. This indicates that the roughness is not a direct function of wind speed. As we have pointed out in section 3.3, the drag coefficient is a function of only roughness under neutral conditions. The drag coefficient  $C_d$  also is changed with changed roughness even when the wind speed keeps constant in the coupled model.

Fig. 22a-c show the change of roughness Zo with time at different constant wind speed V10=10 m/s (Fig.22a), V10=20 m/s (Fig.22b) and V10=30 m/s (Fig.22c). It is very interested to see from Figures 21 and 22 that Wu's roughness formula Eq.(2.1) is the same as Smith's formula Eq.(2.5) at wave age about 26 in wind speed V10=10 m/s, 20 m/s cases and takes about 17 hours at V10=10 m/s and 22 hours at V10=20 m/s case. However at V10=30 m/s even in 100 hours (see fig. 21c and 22c) Wu's formula has no crossover with that of Smith. This seems to indicate that the Wu's formula is suitable only at older wave age. It seems unsuitable for younger waves, especially under very strong wind speed as simulated by the coupled model. Alternately the integration grid used in this computation is probably not adequate to model 30 m/s winds.

Fig. 23a-c and 25a-c show the change of drag coefficient Cd and friction velocity U\* with wave age. Fig. 24a-c, 26a-c show their changes with time respectively. In these figures, the a, b and c represent wind speed at V10=10 m/s, V10=20 m/s and V10=30 m/s respectively. It can be seen that in the coupled model the drag coefficient and friction velocity change at constant wind speed condition and they have a same value with uncoupled corresponding cases at wave age at about 23 under V10=10 m/s and V10=20 m/s (see Figs. 23a, 23b and 25a, 25b). This is corresponding to about 14 hours at V10=10 m/s (see Figs. 24a and 26a) and about 19 hours at V10=20 m/s (see Figs. 24b and 26b). The

coupled model never return to Wu's case when the wind speed is at  $V_{10}=30\,$  m/s (see Figs. 23c and 25c), even after 100 hours (see Figs. 24c and 26c), which may be a problem of the computational grid that needs further work.

Fig. 27a-c show the change of forecasted significant wave height  $H_{\rm S}$  with time at constant wind speed using logarithmic coordinate for  $V_{10}=10$  m/s (Fig.27a),  $V_{10}=20$  m/s (Fig.27b) and  $V_{10}=30$  m/s (Fig.27c) respectively. Fig. 28a-c is the same with Fig. 27a-c, but using linear coordinates. All calculations mentioned above are under the neutral stable condition. The differences in forecasted significant wave height by means of the coupled and uncoupled models are obvious, especially under strong wind speed.

From table 1, we can see that the maximum difference between using coupled and uncoupled model for the forecasted significant wave height reaches about three meters under strong wind at the neutral stable case.

In the unstable case, the influences of instability on the changes for roughness Zo, drag coefficient Cd, coefficient of heat exchange CMCT and friction velocity with wave age are shown on Figs. 29a-c to 32a-c respectively. The signs a, b, c on these figures are expressed at wind speed  $V_{10}=10~\text{m/s}$ ,  $V_{10}=20~\text{m/s}$  and  $V_{10}=30~\text{m/s}$  respectively. The DT on these figures is the difference between air temperature  $T_a$  and sea surface temperature  $T_s$  (DT= $T_a$ - $T_s$ ).

In the unstable case, the differences in forecasted significant wave height between the coupled and uncoupled model are more obvious. Fig. 33a-b show the differences under various conditions. In these figures, the DT= $T_a$ - $T_s$ , DQ= $Q_a$ - $Q_s$  at wind speed V10=20 m/s. The influences of unstable conditions are greater in coupled model (Fig.33b) than the corresponding ones in the uncoupled model (Fig.33a).

Another important fact, which influences the forecasted significant wave height, is the selection of anemometer level  $Z_a$ ,  $Z_a=10$  meter is used in this paper except where noted. Fig. 34a-b shows the differences at  $V_{10}=30$  m/s (Fig. 34a for log coordinate and 34b for linear coordinate). The maximum difference is about 3.5 meter between  $Z_a=5$  m and 50 m). Table 2 shows corresponding forecasted significant wave height at various cases.

Fig. 35a-b show the change of spectral density with frequency at different time for coupled model (Fig.35a) and uncoupled (Fig.35b) respectively. From these figures we can seen the peak frequency is decreasing with increasing time, so that the wave age will increase and the roughness will decrease with time.

The vertical profile of wind speed with time is unchanged in the uncoupled model. In the coupled model due to the changes of roughness and friction velocity the vertical profile of wind speed changes with time. Figs. 36a-c (log coordinate) and 37a-c (linear

coordinate) show these variations corresponding to wind speed (36a, 37a),  $V_{10}=20$  m/s (36b, 37b) and  $V_{10}=30$  $V_{10}=10 \text{ m/s}$ (36c, 37c) and t=10, 20 and 30 hours respectively.

#### 5. COUPLED WIND-SEA MODEL

In this paper, the uncoupled model is the third generation WAM model (Hasselmann et al., 1989). In this wave model the spectral energy balance equation (Eq.3.1) is integrated for wind-generated waves in time for duration-limited growth and the roughness is calculated by Wu's formula Eq. (2.1). Since the roughness is a constant at constant wind speed and it is independent on sea states, such as wave age, significant wave height etc, we call it an uncoupled model. In the coupled model, the roughness is calculated by Smith's formula Eq. (2.5) and it is changed as the wave age changes, even at constant wind speed. The coupled method is described in section 4 (one-point model).

The model's grid is selected in the northwest Atlantic, on a transverse Mercator projection with an assumed equator at 51°W and a grid spacing of 119 km near Halifax, Nova Scotia. The grid consists of 160 points of which 139 are water points, at which model parameters are generated. These grids coincide with the coarse grids of the Canadian Spectral Ocean Wave Model (CSOWM). Fig. 38a shows the coarse grid of the CSOWM covering the northwest Atlantic. The points in a box with thick line are used in this model. Fig.  $38\hat{b}$  shows the grids we used in this report. The sign "  $\blacktriangleright$  " is the location of buoy number 44138 and sign "  $\bullet$  " for 44139.

The input data for every grid point are as follows:

- 1. WDDR—— wind direction.

- WDSP— wind speed.
   ZANG— the zenith.
   ALAT— the latitude of grids.
- 5. ALONG—— the longitude of grids.
- 6. DEPTH—— the water depth

The main output two dimension (x and y direction) data are as follows:

- 1. USTYX—two dimensional friction velocity (every 12 hours).
- ZOYX——two dimensional roughness (every 12 hours).
   CDYX——two dimensional drag coefficient (every 12 hours).
   FPYX——two dimensional peak frequency (every 12 hours).
- 5. HTYX——two dimensional forecasted significant wave height (every 12 hours).
- 6. FQYX——two dimensional flux of momentum (every 12 hours).
- 7. FVYX——two dimensional flux of latent heat (every 12 hours).
- 8. FCYX—two dimensional flux of sensible heat (every 12 hours).
- 9. FL3 ——two dimensional frequency-direction spectrum, which is printed out at any time you want.

You must write FL3, USTYX, Z0YX and FPYX at the last time step when you want to continue to calculate the next time step and change some parameters related with time in this model.

# 6. A MECHANISM OF IMPACT ON FLUXES OF MOMENTUM, SENSIBLE HEAT AND LATENT HEAT

What does the drag coefficient (Cd) depends on? There are several empirical formulae about the relationship between Cd and wind speed V10 at 10 meters above the sea level. As we discussed in section 3.3, the drag coefficient Cd depends mainly on the roughness Zo rather than the wind speed at a desired anemometer level Za under neutral condition in this model. It (Cd) is unchanged at a designated roughness Zo although the wind speed may be increasing. It is also noticed that the roughness Zo is a function of friction velocity U\* and wave age rather than wind speed and that the roughness Zo can also be changed under constant wind speed. This seems to indicate that the drag coefficient Cd is not a direct function of wind speed.

Therefore, the drag coefficient (Cd), which influences the fluxes of momentum, heat and water vapour, depends on

- 1. the changes of wind speed with height  $\left(\frac{\partial u}{\partial x}\right)$ , not the wind speed itself at 10 meters.
- 2. Sea states, such as wave height, wave age and so on.
- 3. the thermal conditions or instability.

We use 
$$C_d = C_d(Z_0, Z_{0T})$$
 (6.1)

where  $Z_0 = Z_0(U^*, SEA STATE)$  (6.2)

Zor is expressed as thermal conditions

U\* is the friction velocity

IN NEUTRAL OR STABLE CASES, the drag coefficient only depends on ROUGHNESS Zo, which means

$$Cd = Cd (Zo) (6.3)$$

HSU has a relationship between Cd10 and V10 (Hsu, 1986 Eq. 35).

$$C_{d10} = \left\{ \frac{0.4}{14.56 - \ln V_{10}} \right\}^2 \tag{6.4}$$

but, according to Hsu's Eq.(7) and (8) in the same paper under neutral condition, we have:

$$C_{d} = \left(\frac{U^{*}}{U_{z}}\right)^{2} = \left\{\frac{\kappa}{\ln\left(\frac{z}{z_{0}}\right)}\right\}^{2}$$
 (6.5)

which shows that the drag coefficient  $C_d$  also only depends on roughness  $Z_0$  at desired level Z.

In this paper we discuss only the case  $Z_0 = Z_{07}$ . The general expression and characteristics of the thermal roughness  $Z_{07}$  will be discussed in another paper. The coefficient of heat exchange calculated by Eq.(3.21) shows that it is also only dependent on roughness  $Z_0$  in the neutral stable cases and at a designated level  $Z_2$ .

In the unstable case, from Eqs. (3.15) to (3.17) and from Eqs. (3.22) to (3.29) it is seen that although these expressions are more complex, the drag coefficient  $C_d$  and the coefficient of heat exchange  $C_MC_T$  are also the functions of roughness  $Z_0$  (or thermal roughness  $Z_{0T}$ ) directly and indirectly at a designated level  $Z_a$ .

The precise calculations of the drag coefficient and the coefficient of heat exchange are very important and complex. They will directly influence the calculations of momentum, sensible heat and latent heat fluxes. There is a reaction of the sea state (wave age) on roughness, and the roughness changes with changing sea state. As we discussed above, the fluxes of momentum, sensible heat and latent heat will change with changing sea state.

Figs. 39a-c to 42a-c show the various fluxes calculated by our coupled one-point model at constant wind speed. Fig. 39a-c shows momentum flux changes with wave age under neutral stable case at different wind speed  $V_{10}=10~\text{m/s}$  (fig.39a),  $V_{10}=20~\text{m/s}$  (Fig.39b) and  $V_{10}=30~\text{m/s}$  (Fig.39c). Fig. 40 shows the same but with time and the a, b, and c on figures are the same as described in Fig. 39a-c.

Figs. 41a-c show the same as in Fig. 39a-c, but in the unstable case. Fig. 42a-c show the same as in Fig. 41a-c, but for the flux of sensible heat. The DT on these figures are the difference between air and sea surface temperature (DT= $T_a$ - $T_s$ ). It is seen that these fluxes are no longer a constant as calculated by uncoupled model at constant wind speed.

Table 3 lists estimates for these different cases for fluxes of momentum, sensible heat and latent heat. Under special cases, such as  $T_a$ - $T_s$ =20 degrees or  $Q_a$ - $Q_s$ =20 g/kg or both, these fluxes can change by a factor two. This may be useful to study the suddenly developing cyclone over the eastern coast of Canada and it seems to be worthy to couple the coupled wind-sea model with an atmospheric model to consider the changing roughness with changing sea state.

#### 7. AN EXAMPLE FOR UNCOUPLED AND COUPLED MODEL

As a example, we use the uncoupled and coupled models mentioned above for one-point and wind-sea models. The wind data are provided by Recherche en Prévision Numérique (RPN) every three hours for the CAL/VAL period from Nov. 8 to 25, 1991. The hourly wind data are obtained by linear interpolation. The time step is 20 minutes for the one-point models and one hour for wind-sea models. The buoy data are provided by Atmospheric Environment Services (AES) in Bedford Nova Scotia.

# 7.1 One-point model

Fig. 43 shows the observations at buoy station number 44138 for winds (Fig.43a) and temperatures (Fig.43b). Fig. 44a shows the comparisons of observational wave heights (solid line) with the ones calculated by uncoupled model (dotted line) and coupled model (dashed line). It is seen that the forecasted significant wave heights calculated by the coupled model are closer to the observations than the ones calculated by the uncoupled model. It is interesting to notice from Fig.44b that if we use a weighted wind speed V as follows:

$$v = (v_{ave} \times 2.0 + v_{gust}) / 3.0$$
 (7.1)

the forecasted significant wave heights (dot dash line) are even closer to the observations (solid line) than either the ones calculated by coupled model (dashed line) or the ones calculated by uncoupled model (dotted line).

Fig. 45a, 45b and 46 are the same as Fig. 43a, 43b and 44a respectively but at buoy station 44139.

## 7.2 Wind-sea model

Two dimensional wind-sea uncoupled and coupled models are calculated using the wind data provided by RPN during the CAL/VAL period. The hindcast is done for Nov. 8-25, 1991. A cyclone was just over the region between Nova Scotia and Newfoundland on Nov. 15. Fig. 47a and 47b are the wind fields at that region for Nov. 15 and 16 respectively. Fig 48a and 48b are the wind speeds corresponding to Fig. 47a and 47b respectively.

Fig. 49 shows the forecasted significant wave heights with the uncoupled model (Fig.49a) and the coupled model (Fig.49b). It is worth noticing that the maximum wave height is 7.0 meters in the coupled model and 5.9 meters in uncoupled model. The observational maximum wave height is 7.1 meters in the cyclone region, where the wind direction and wind speed are changing rapidly and the wave age is very young. In other regions, the wave

age is older, so the forecasted significant wave heights in the coupled model are almost the same as the ones in uncoupled model.

Fig 50a and 50b show the forecasted significant wave heights at grid point number 1464 and 1465 (the coarse grid number of the Canadian Spectral Ocean Wave Model in northwest Atlantic region) near the buoy station number 44138 and Fig. 51a, 51b are at grid point number 1518 and 1519 near buoy station number 44139. The forecasted results are more in accord with observations, especially on Nov. 16, 1991. The maximum wave height in the coupled model is almost the same as the observations.

Figs. 52a-b to 54a-b show the distributions of fluxes for momentum (Fig.52a,b), sensible heat (Fig.53a,b) and latent heat (Fig.54a,b) on Nov. 16, 1991. The a and b on the figures correspond to the uncoupled model and coupled model cases respectively. It is seen from these figures that the fluxes of momentum, sensible heat and latent heat in the coupled model are higher in the cyclone region and almost the same in the other region as the fluxes in the uncoupled model.

# 7.3 Calibrations of wind

As mentioned in meteorology, the observational wind can not be directly used in a numerical weather forecast model, it is necessary to calibrate the wind according to some equilibrium relationships, such as geostrophic balance or thermal-wind balance which expresses the balance between geopotential height and wind field or the vector difference of wind and mean temperature field between two designated levels.

We have to find a balance state between sea state and the wind near the sea. The coupled wind-sea model makes it possible to do this kind of calibration. A forecasted or observational wind can be calibrated through changing the friction velocity U\* and roughness Zo at a required level Za.

Fig. 55 shows that the observational winds (dotted line) and the calibrated winds (solid line) at buoy station number 44138. Fig. 56 is the same with Fig. 55, but at buoy station number 44139. It seems to be necessary that the calibrated wind rather than observational wind may be useful for data assimilation.

## 8. CONCLUSIONS AND DISCUSSION

- 1. The effects of sea states, such as wave age, on roughness in the boundary layer are very important for the improvement of the forecasted significant wave height. The WAM model developed by Hasselmann et al (1989) seems only to describe the Fully-developed wind sea at the cases where the WAVE AGE ( $C_P/U^*$ ) is very old. If the wind speed is not so strong, the changes in predicted significant wave height between the coupled and uncoupled models is negligible. If the wind speed is very strong ( $V_{10} \ge 30 \text{ m/s}$ ) or the wave age is very YOUNG, the reactions of sea state on the boundary layer and its coupling mechanisms are very important to improve the wave forecasts.
- 2 The drag coefficient Cd is a direct function of only roughness Zo rather than wind speed under neutral case and the roughness is a function of friction velocity and wave age (as seen in Eq. 2.5) rather than wind speed in the coupled model. This indicates that the drag coefficient Cd is not a direct function of wind speed. Cd is changed when the roughness changes with wave age. Under very strong wind speed conditions, such as 30 m/s, the drag coefficient can change by a factor two.
- 3. The effects of the sea states, such as wave age, on fluxes of momentum, sensible and latent heat are also very important. The fluxes are changed not only by the differences of temperature and water vapour between sea surface and air, but also by transfer coefficients, which are changed with roughness and thermal conditions rather than wind speed. The roughness is changed with vertical wind profile and wave age, so that the coefficients are changed with changing wave age. This may be very important for simulating the CANADIAN ATLANTIC STORMS over the east coast of Canada.
- 4. It may be very important in doing the four-dimensional data assimilation to use coupled wind-sea models, which make the sea states, such as wave age, and vertical wind profile reach a balance state with corresponding atmospheric boundary layer model values. This is a very important condition in doing data assimilation, especially in estimating the wind over sea surface.

#### 9. ACKNOWLEDGEMENT

The Federal Panel on Energy Research and Development (PERD) of Canada provided funding for this research. The Northern Cod Fund supported L. Wang's visit to BIO.

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TABLE 1 : FORECASTING WAVE HEIGHT (in neutral case)

WIND SPEED (m/s)	10	20	30	40	50
t=10 hours UNCOUPLED COUPLED	1.14 1.31	3.06 3.49	<b>4.21</b> 5.86	8.56 9.32	11.10 13.00
t=20 hours UNCOUPLED COUPLED	1.45 1.60	5.44 6.40	9.03 12.00	13.80 16.90	16.30 19.20
t=30 hours UNCOUPLED COUPLED	1.62 1.73	7.34 7.94	11.90 13.90	15.50 17.40	16.60 19.50
t=40 hours UNCOUPLED COUPLED	1.75 1.83	8.65 9.09	13.40 14.30	15.50 17.40	16.60 19.90
t=50 hours UNCOUPLED COUPLED	1.86 1.93	9.63 10.00	13.60 14.30	15.50 17.50	16.60 19.90

TABLE 2. FORECASTING SIGNIFICANT WAVE HEIGHT AT VARIOUS ZA

TIME (hours)	10	20	30	40	50
Za=5	5.74	10.80	13.60	14.30	14.30
Za=10	5.43	9.69	12.30	13.50	13.60
Za=20	5.11	8.67	11.10	12.60	12.90
Za=50	4.79	7.98	10.10	11.60	12.30

TABLE 3. FLUXES OF MOMENTUM, SENSIBLE HEAT AND LATENT HEAT

	DT=0 DQ=0	DT=20 DQ=0	DT=0 DQ=20	DT=20 DQ=20
FLUX OF MOMENTUM UNCOUPLED MODEL COUPLED MODEL	1.1614 2.0648	1.2033 2.1578	1.1926 2.1219	1.2188 2.1898
FLUX OF SENSIBLE HEAT UNCOUPLED MODEL COUPLED MODEL	0 0	1.2927 2.3196	0	1.3126 2.3608
FLUX OF LATENT HEAT UNCOUPLED MODEL COUPLED MODEL	0 0	0	0.7519 1.3377	0.7801 1.4031

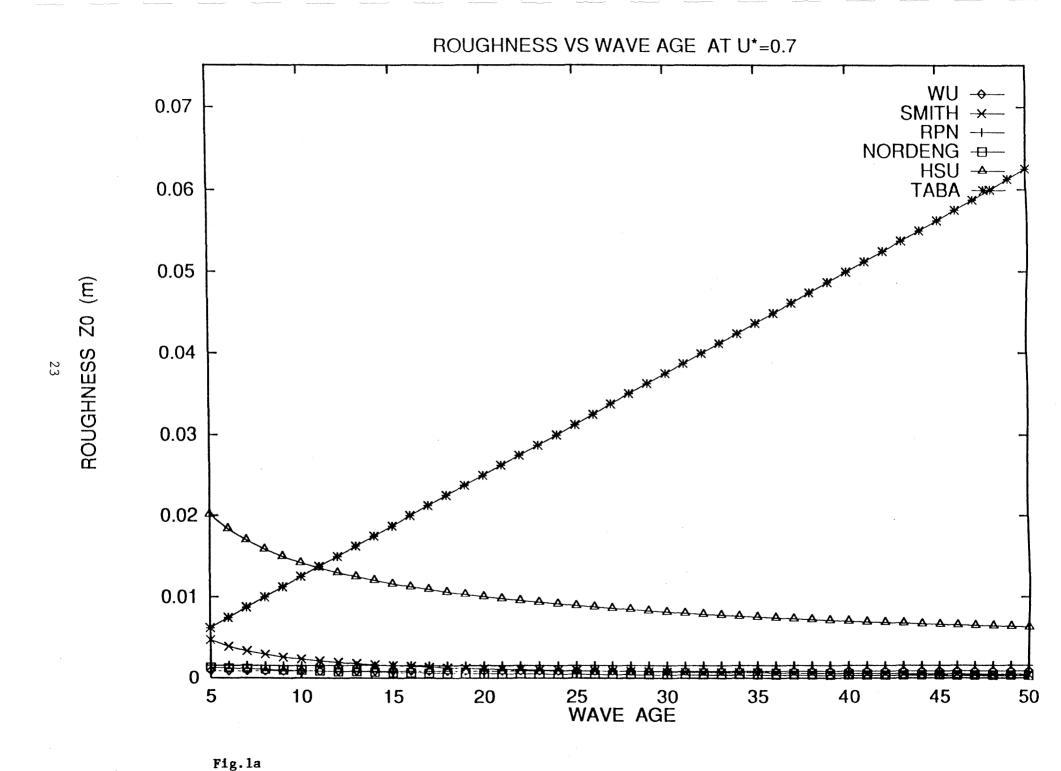


Fig.1b

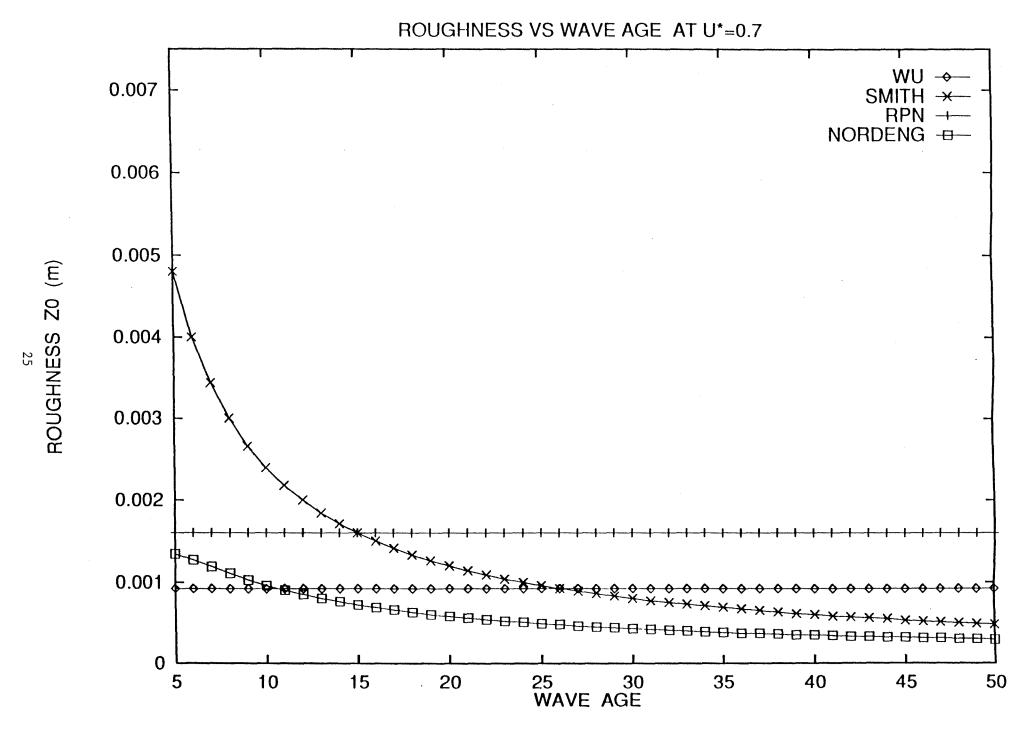
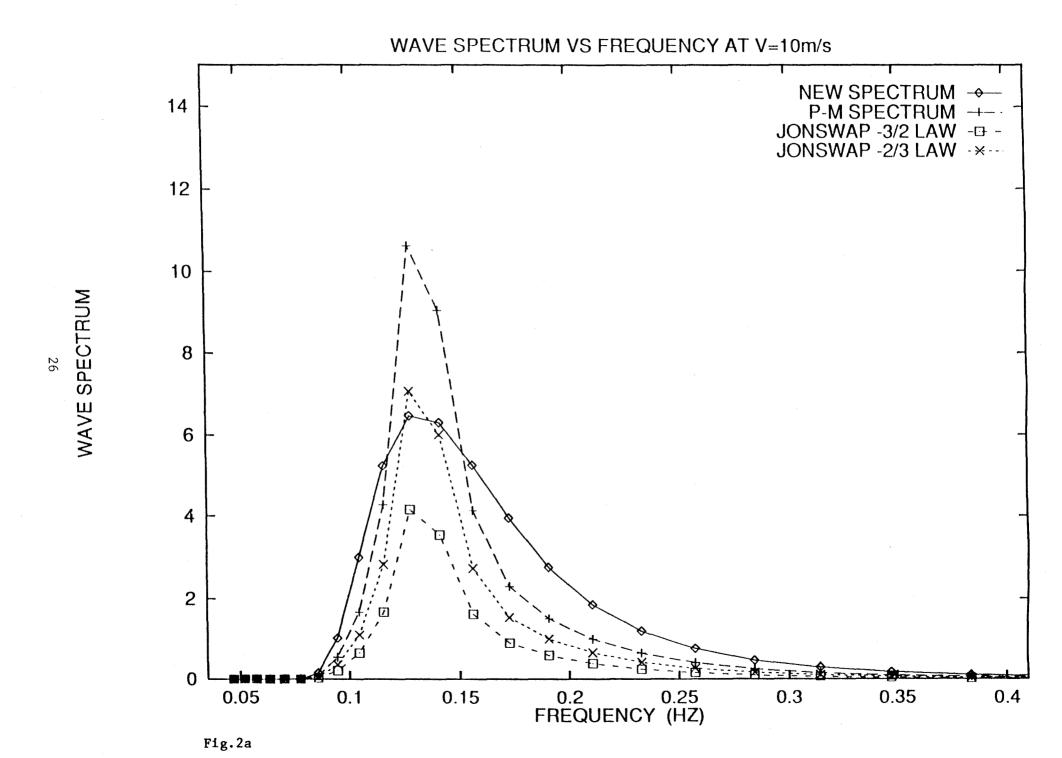


Fig.1c



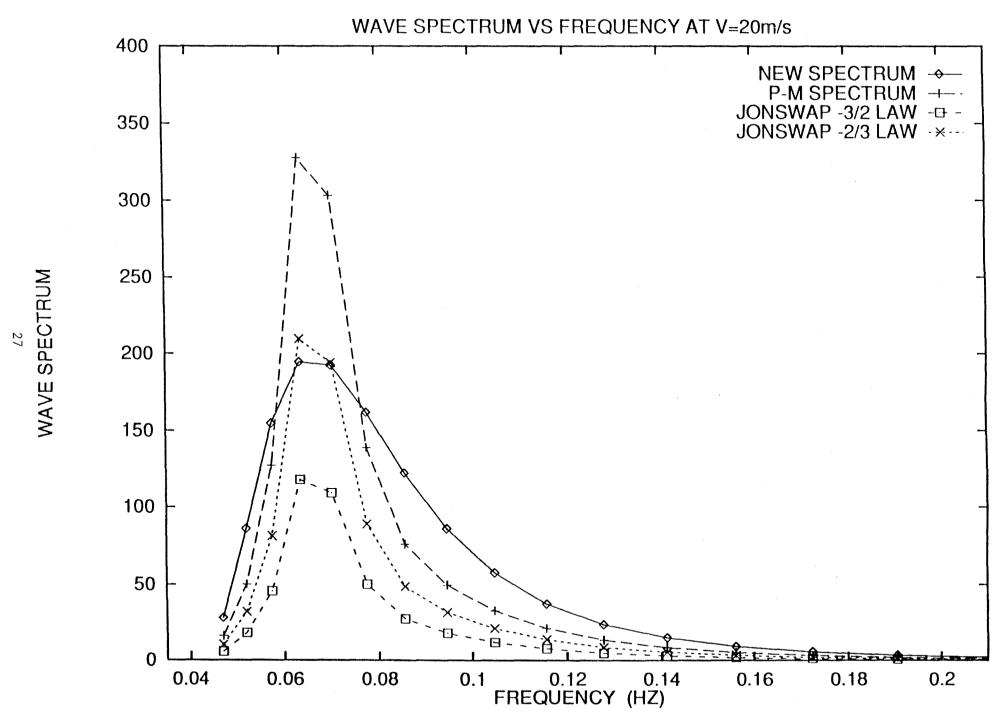
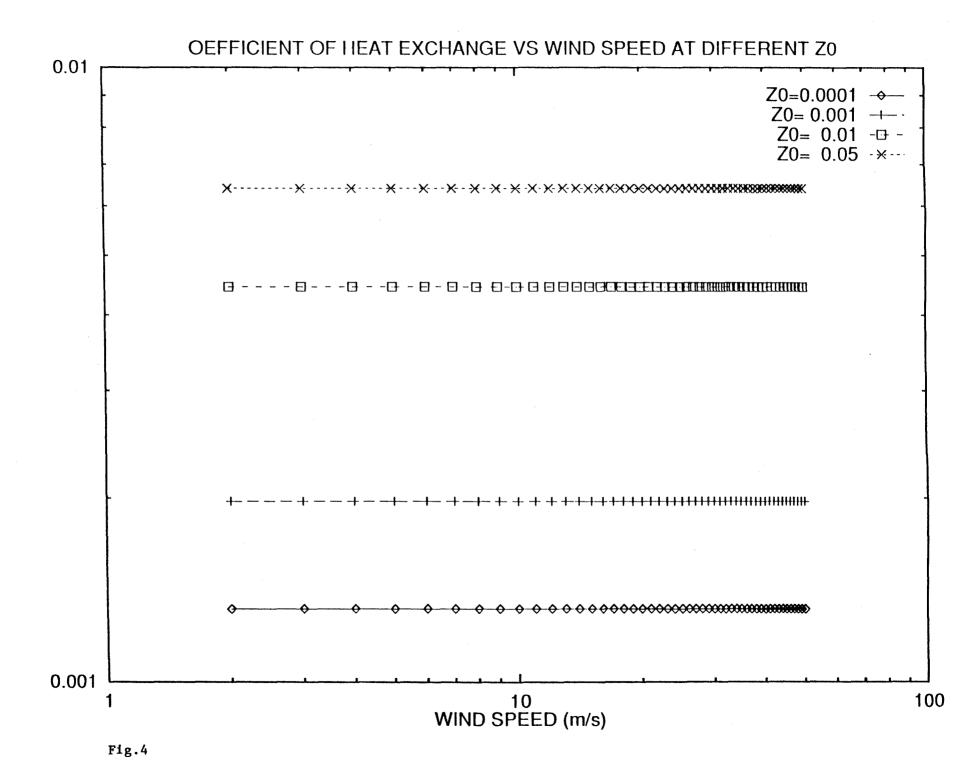
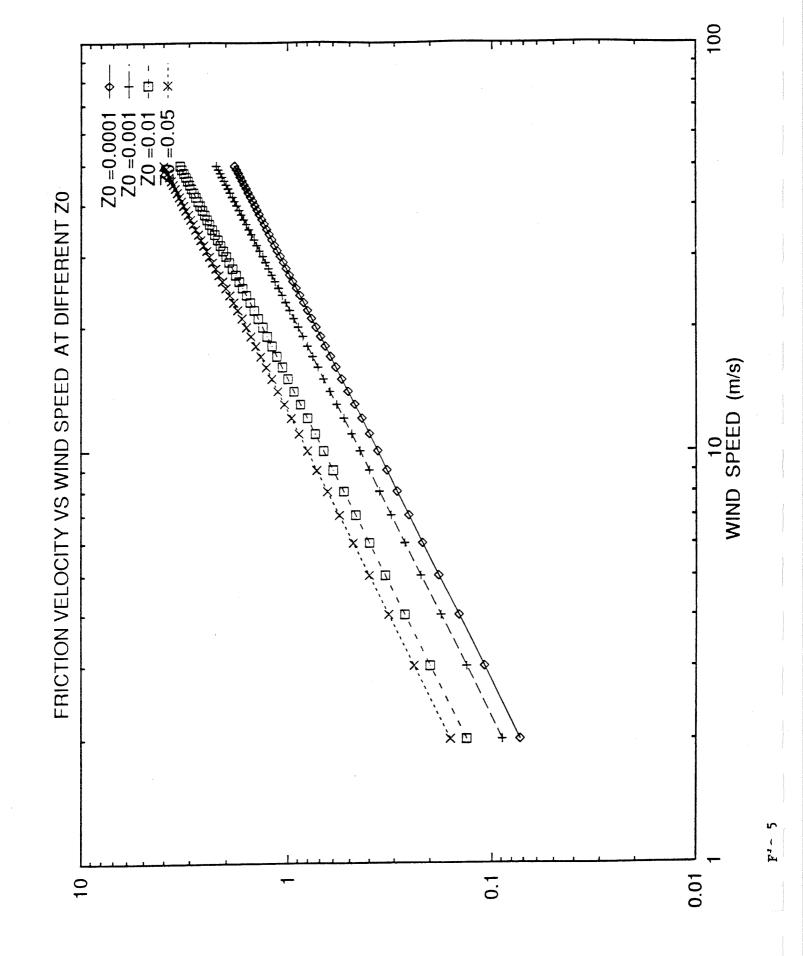


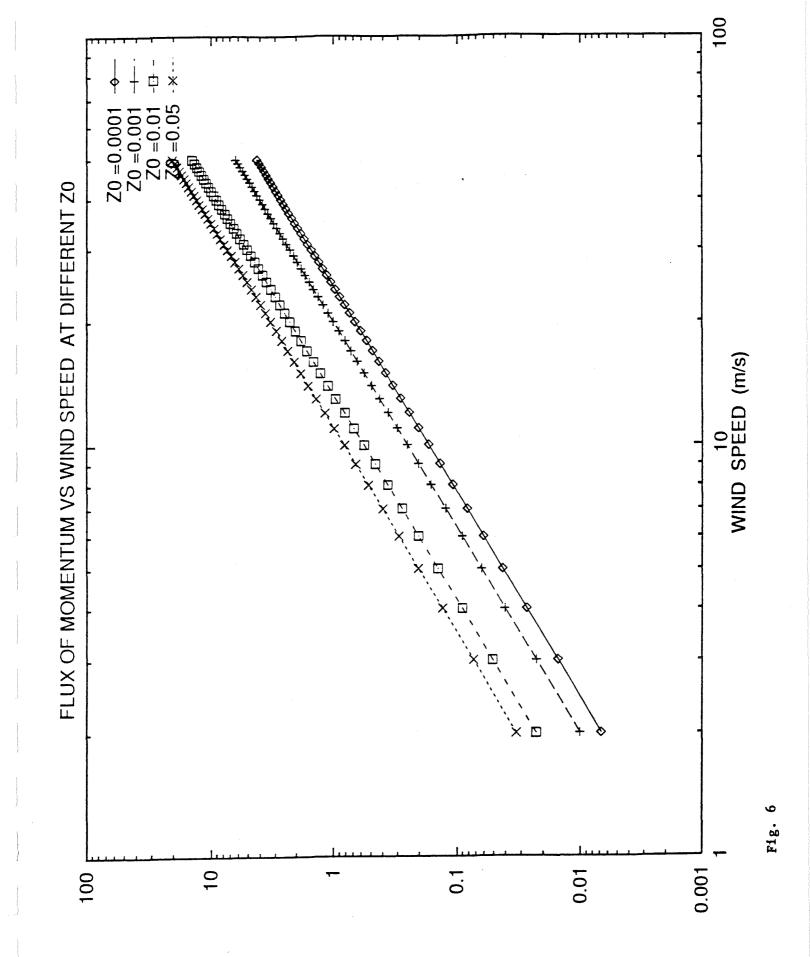
Fig.2b

Fig. 3



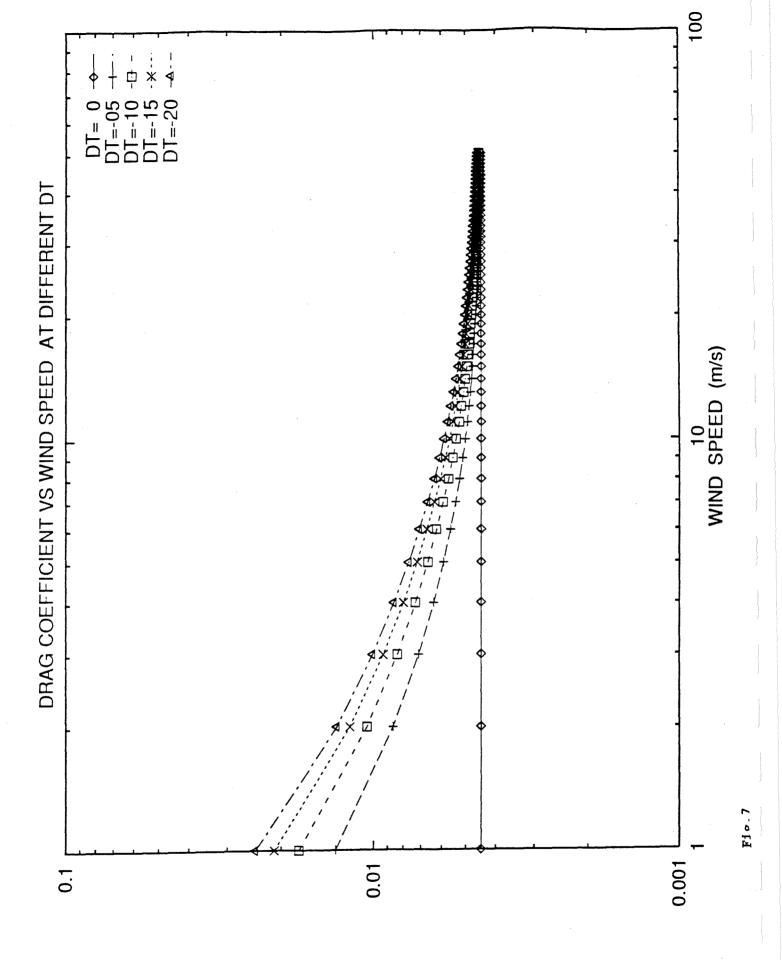


FRICTION VELOCITY U\*



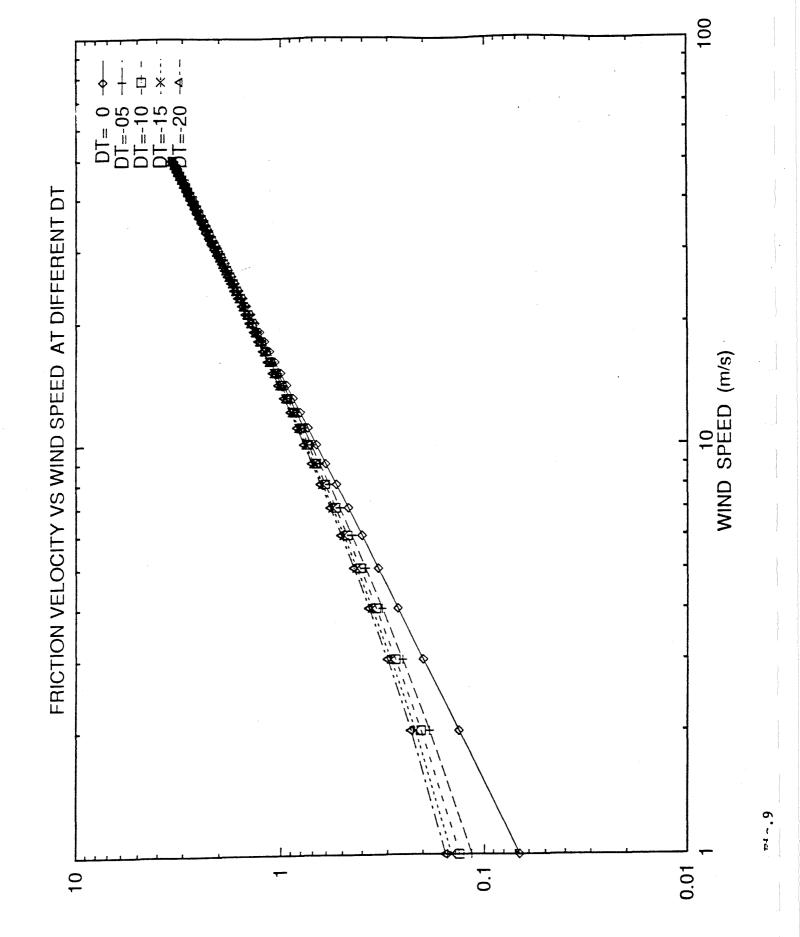
ELUX OF MOMENTUM FM

## DRAG COEFFICIENT CD

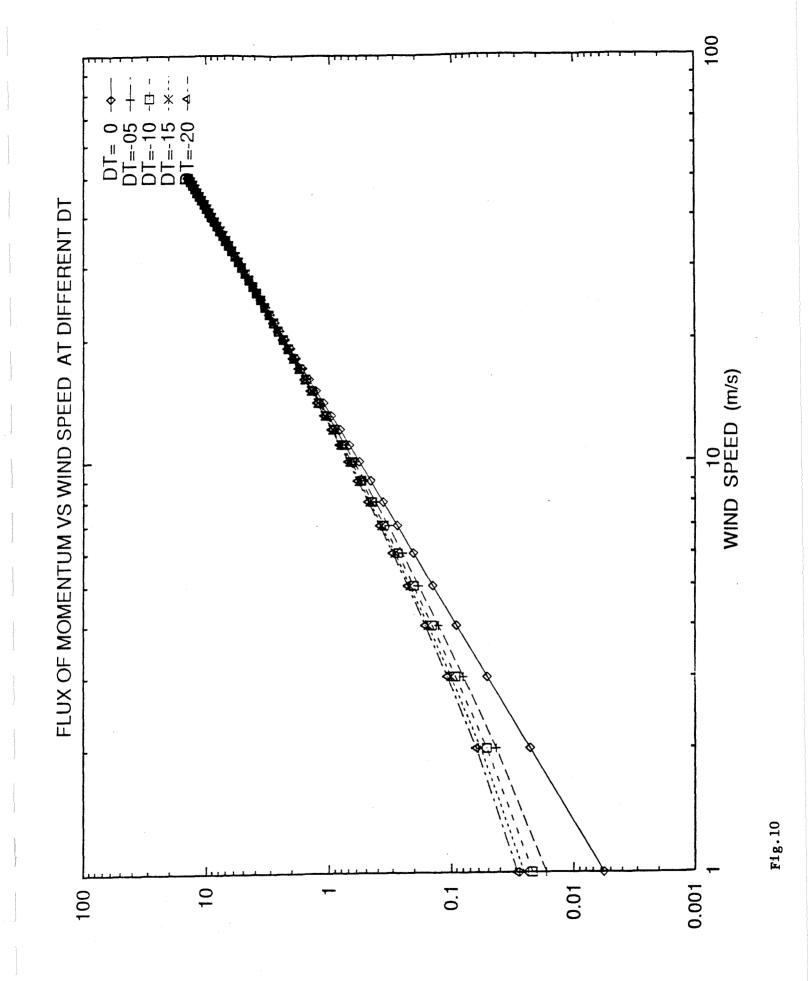


## 100 4 **OEFFICIENT OF HEAT EXCHANGE VS WIND SPEED AT DIFFERENT DT** 10 WIND SPEED (m/s) 0.001 0.01 0.1

COEFFICIENT OF HEAT EXCHANGE CMCT



FRICTION VELOCITY U+



FLUX OF MOMENTUM FM

## FLUX OF SENSIBLE HEAT FS

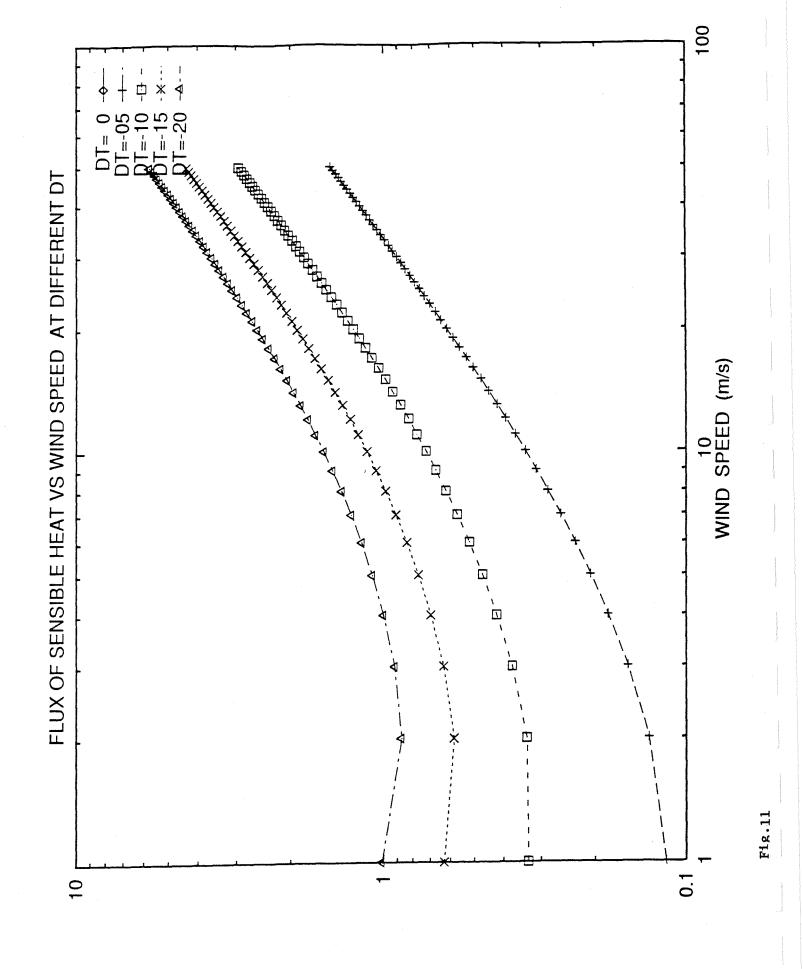


Fig.12

Fio. 13

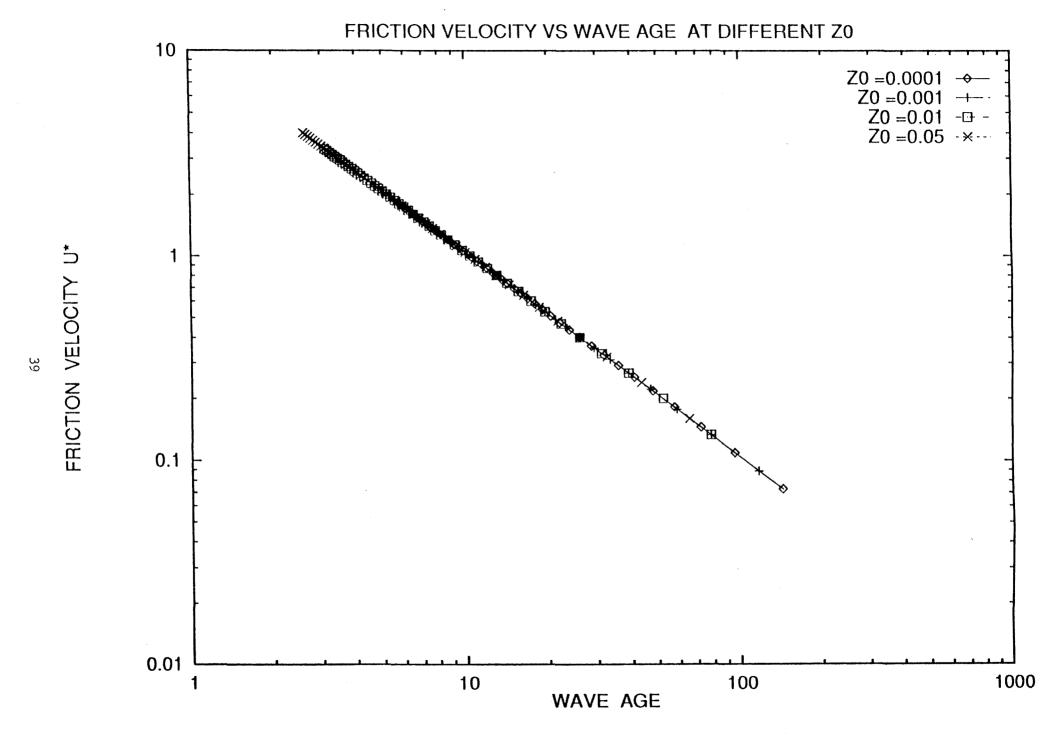


Fig.14

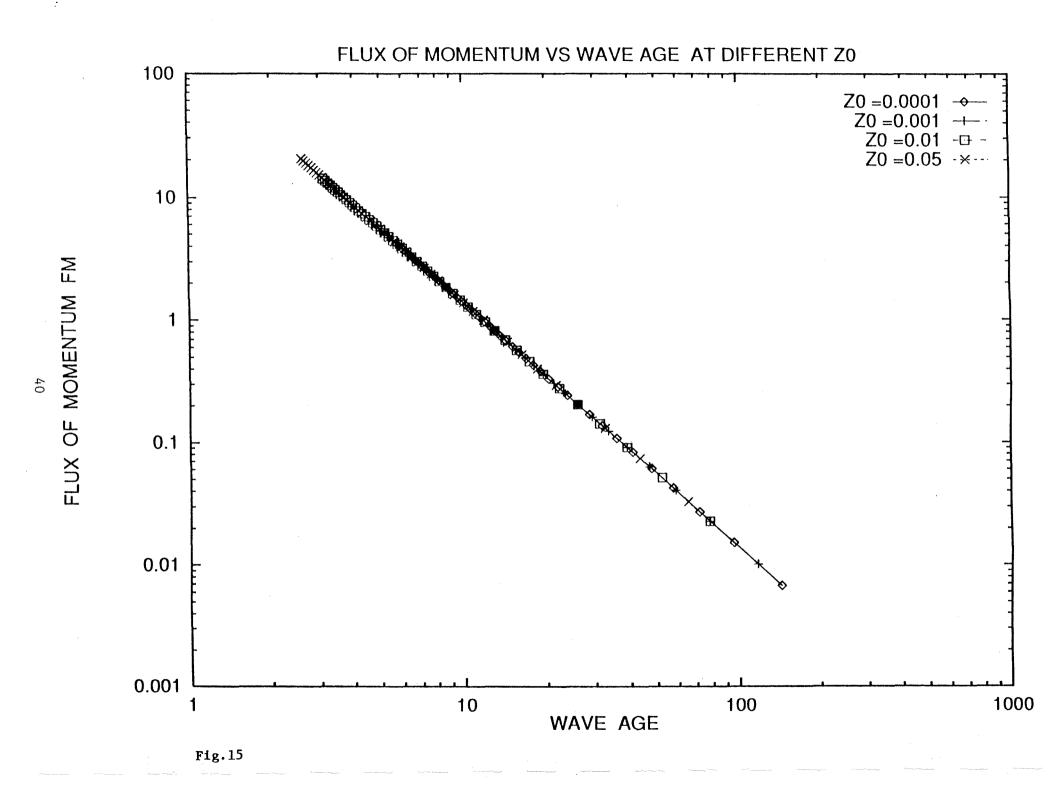
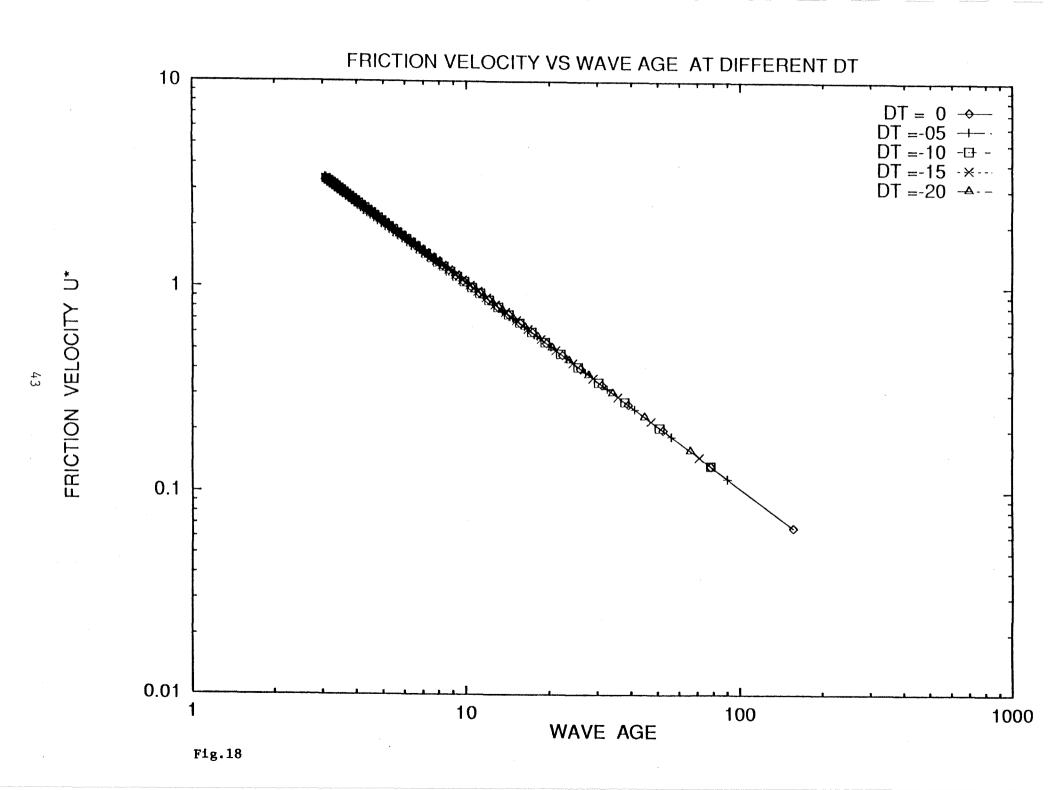
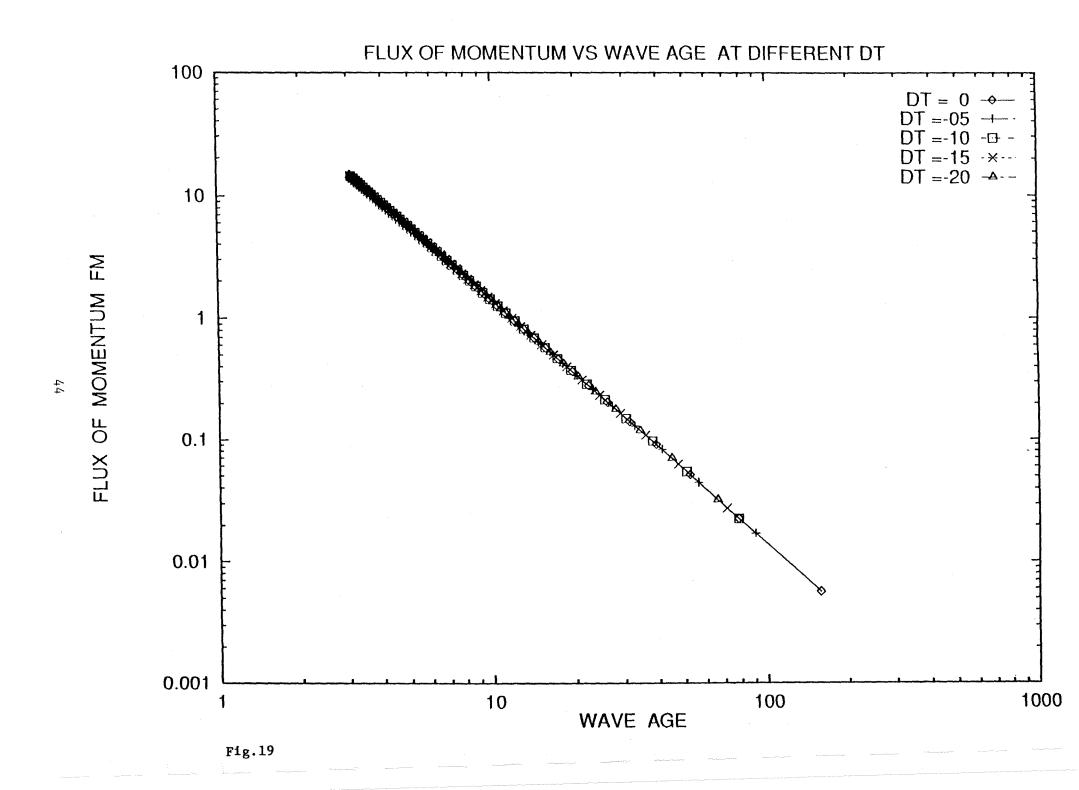


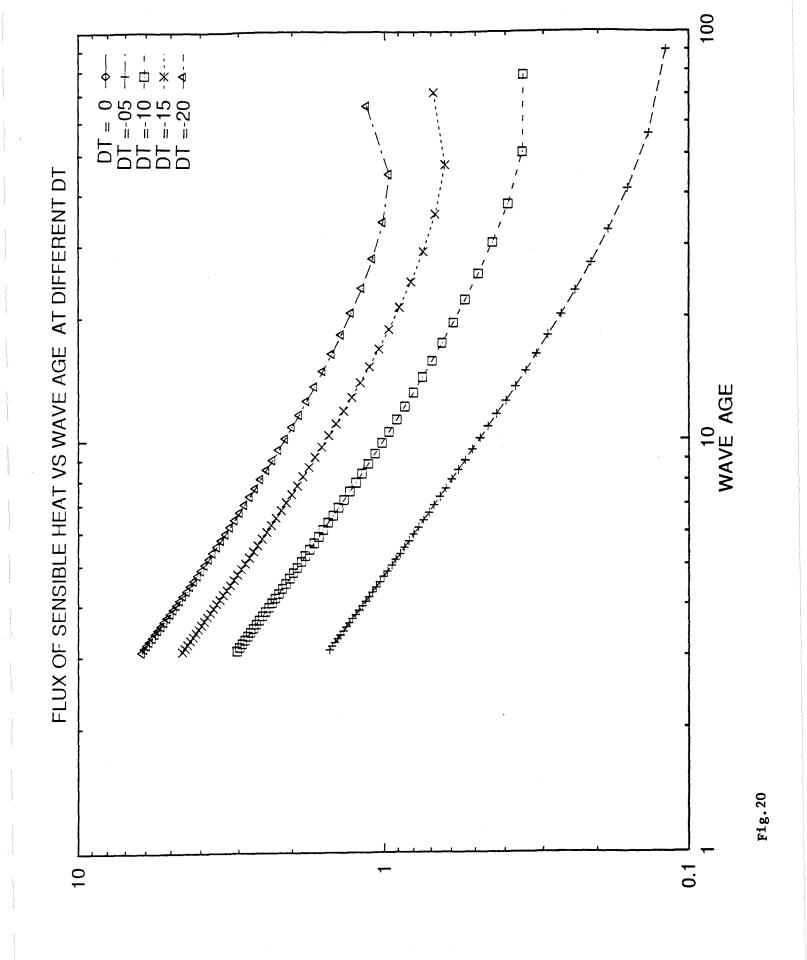
Fig.16

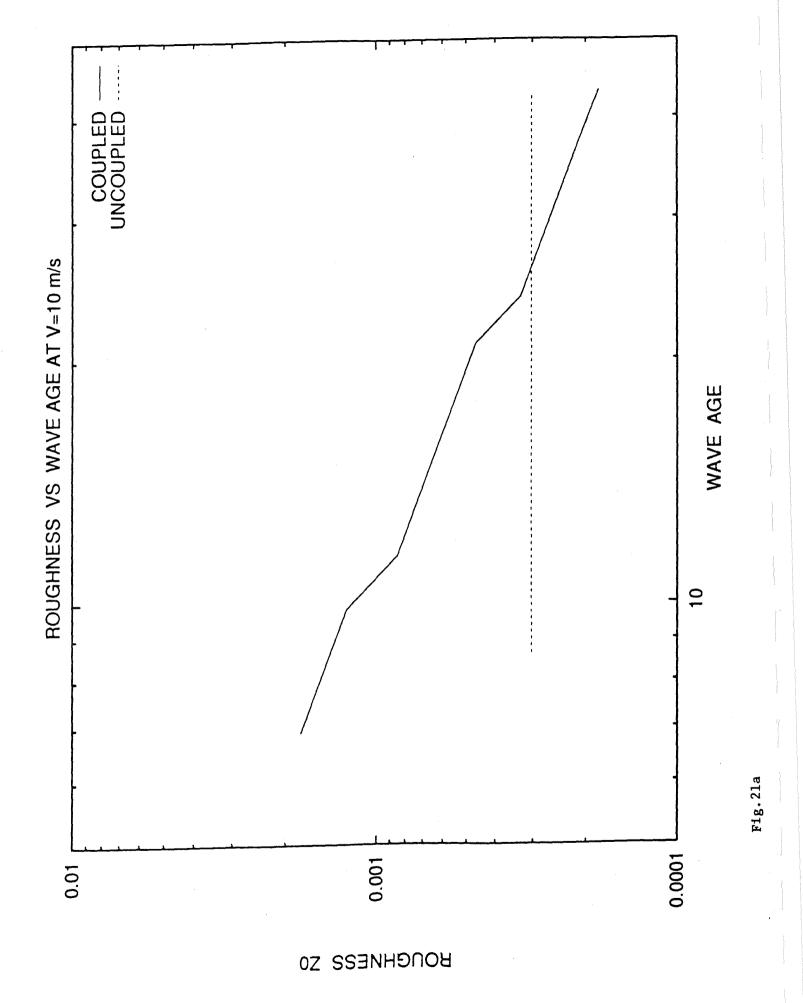
Fig.17

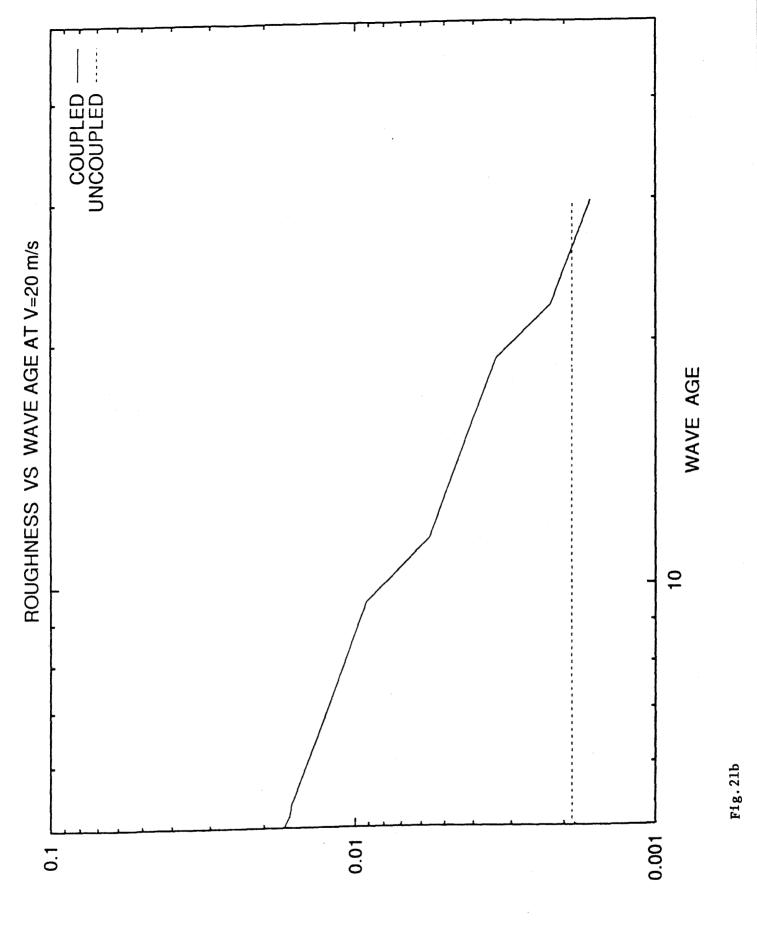




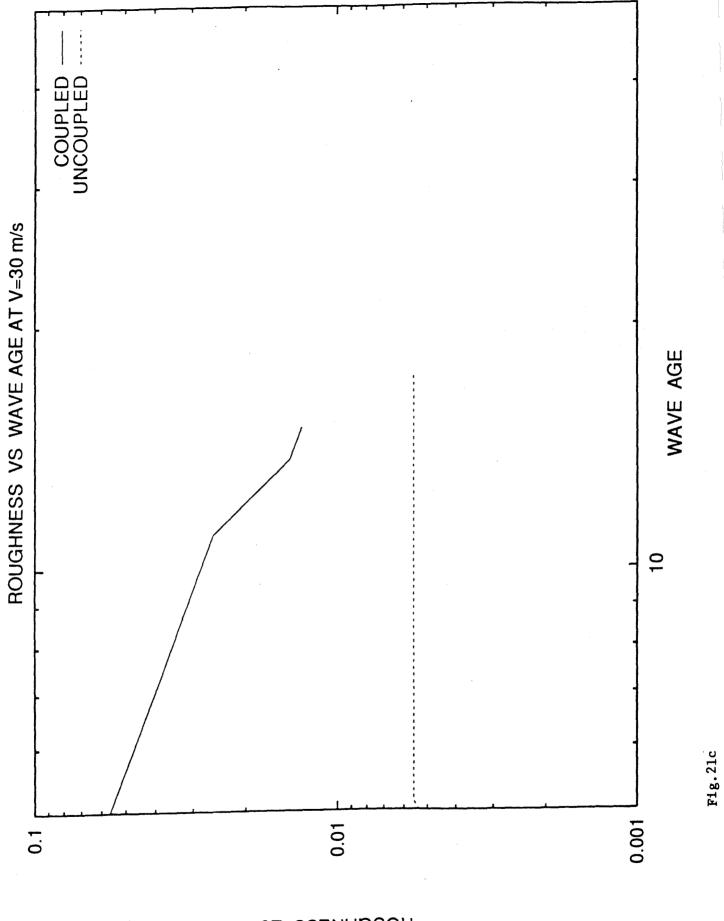
FLUX OF SENSIBLE HEAT FS



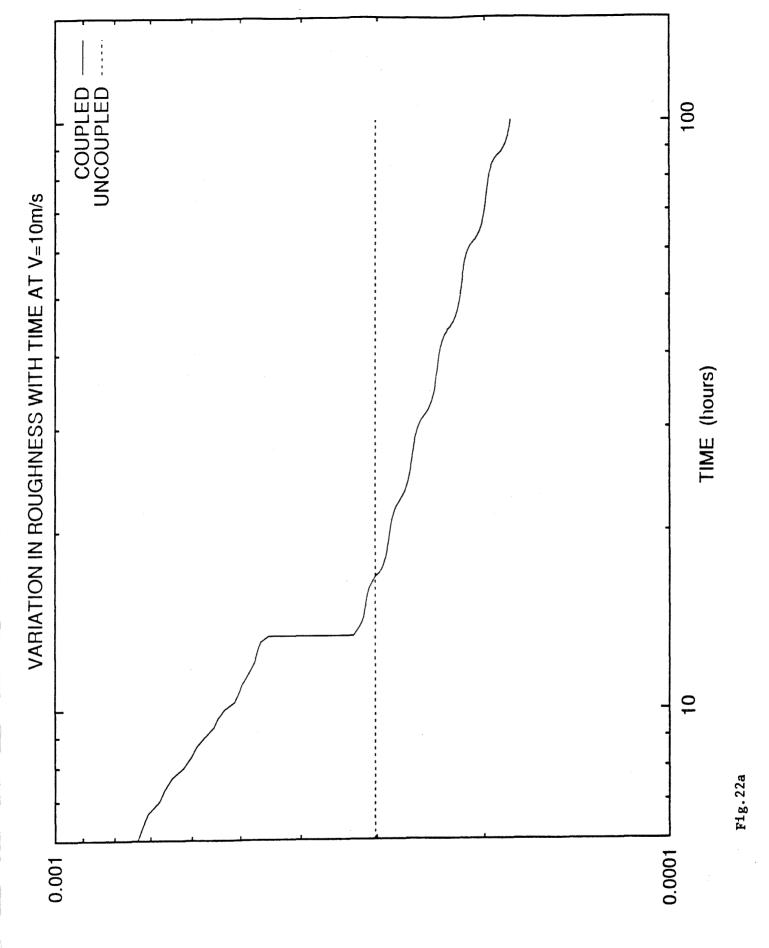




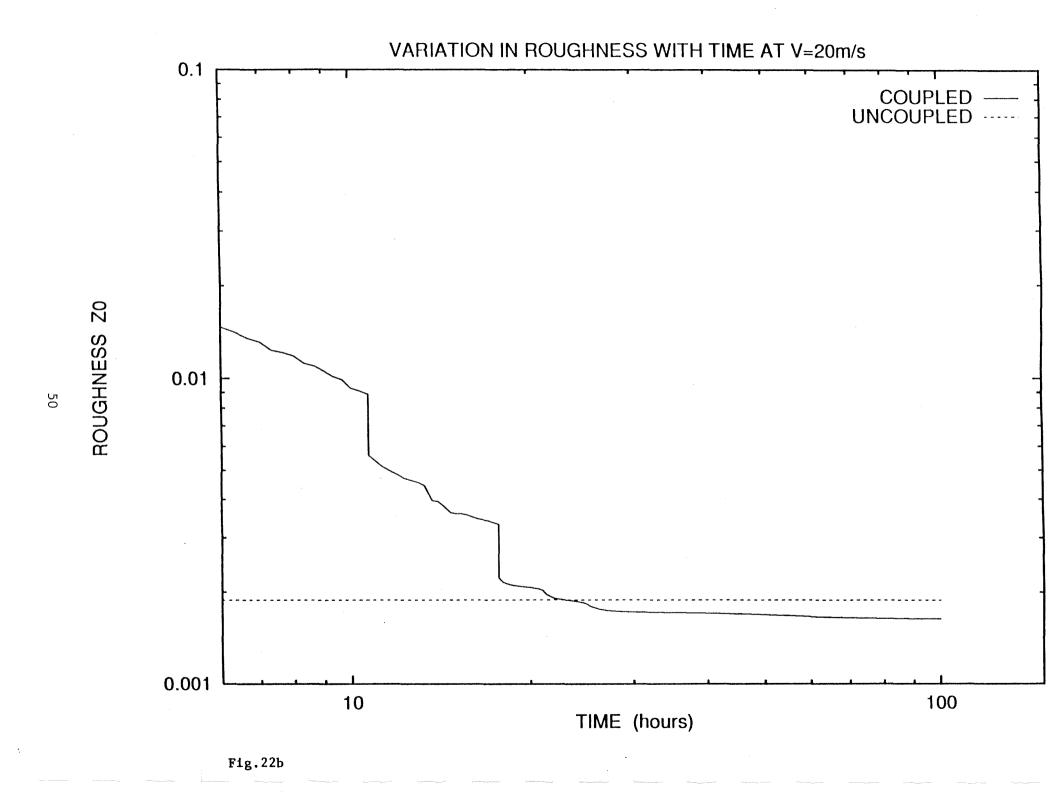
BONGHNESS ZO

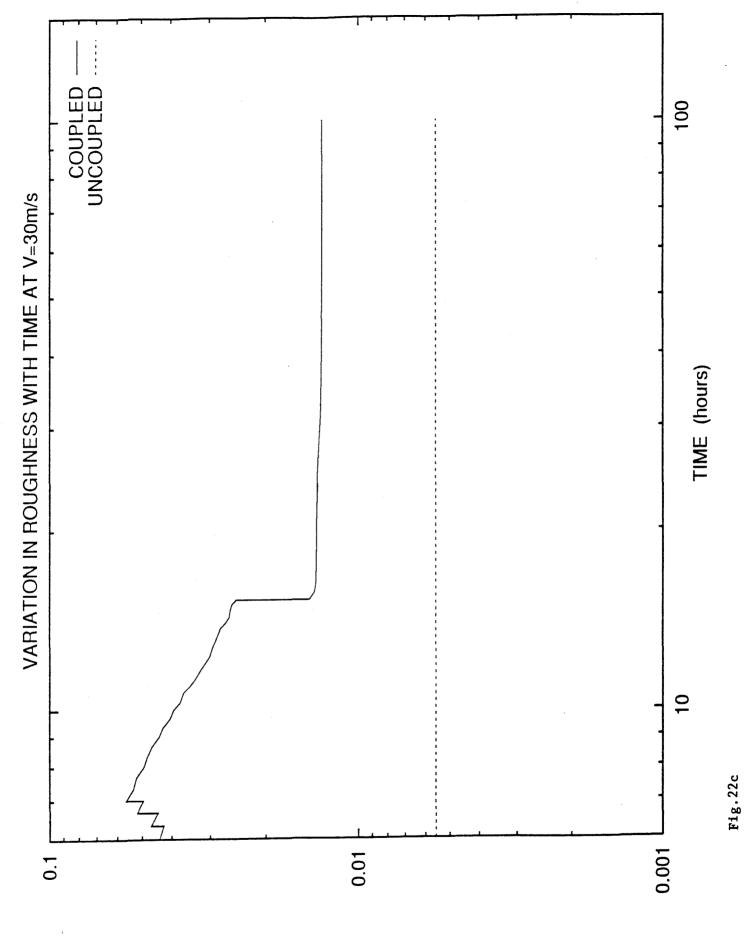


BONGHMESS ZO



ROUGHNESS ZO





BONGHNESS ZO



DRAG COEFFICIENT CD

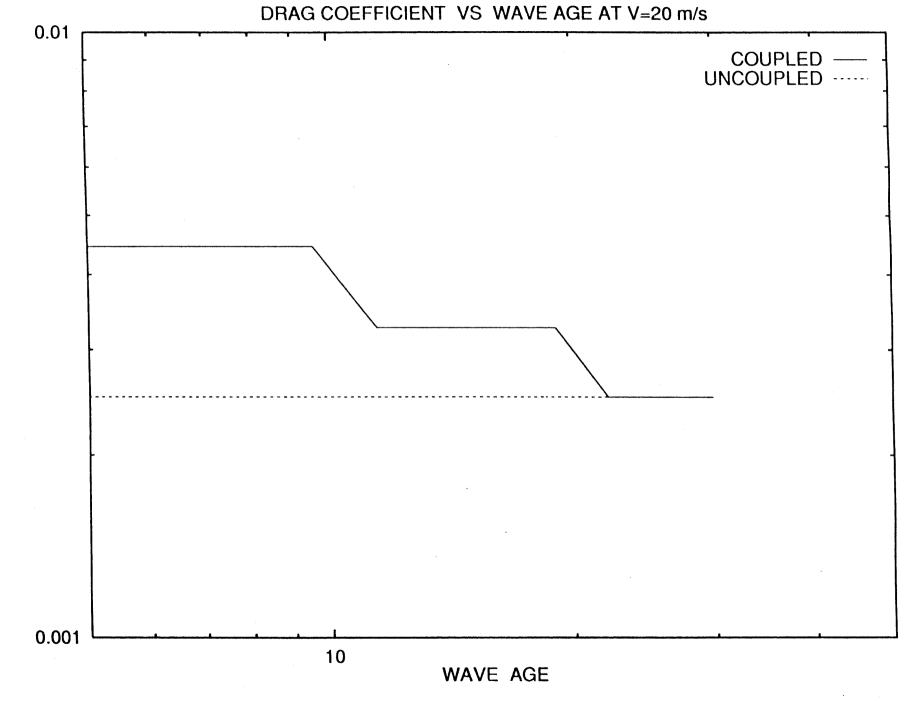
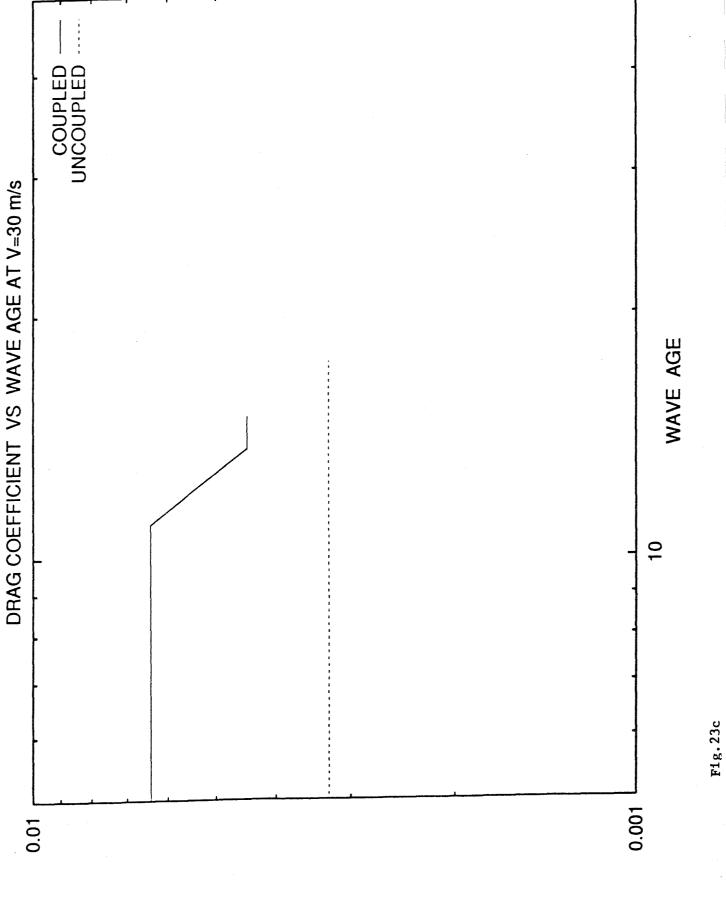


Fig.23b

## DRAG COEFFICIENT CD



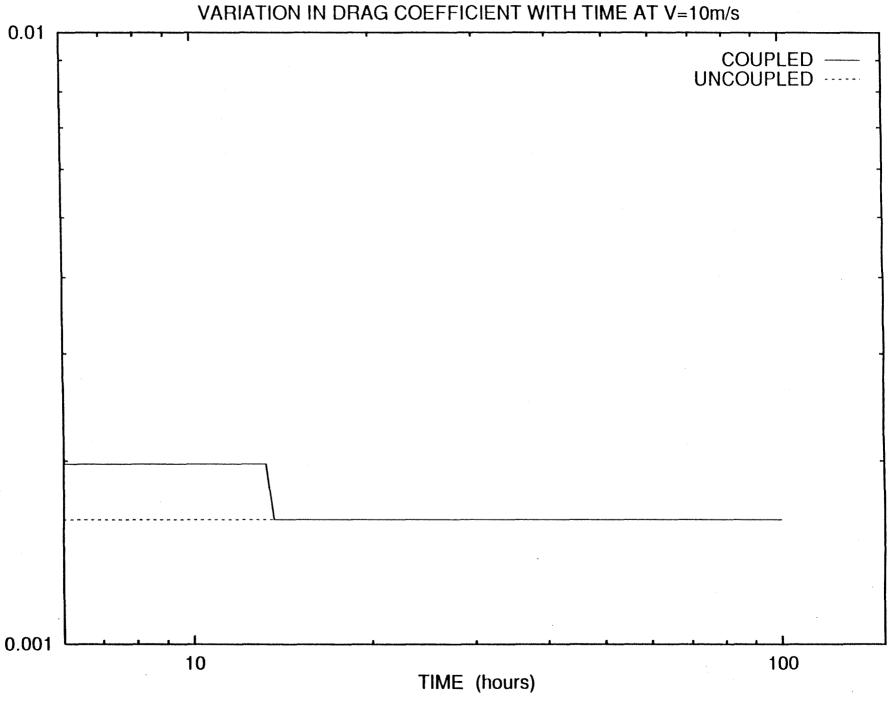
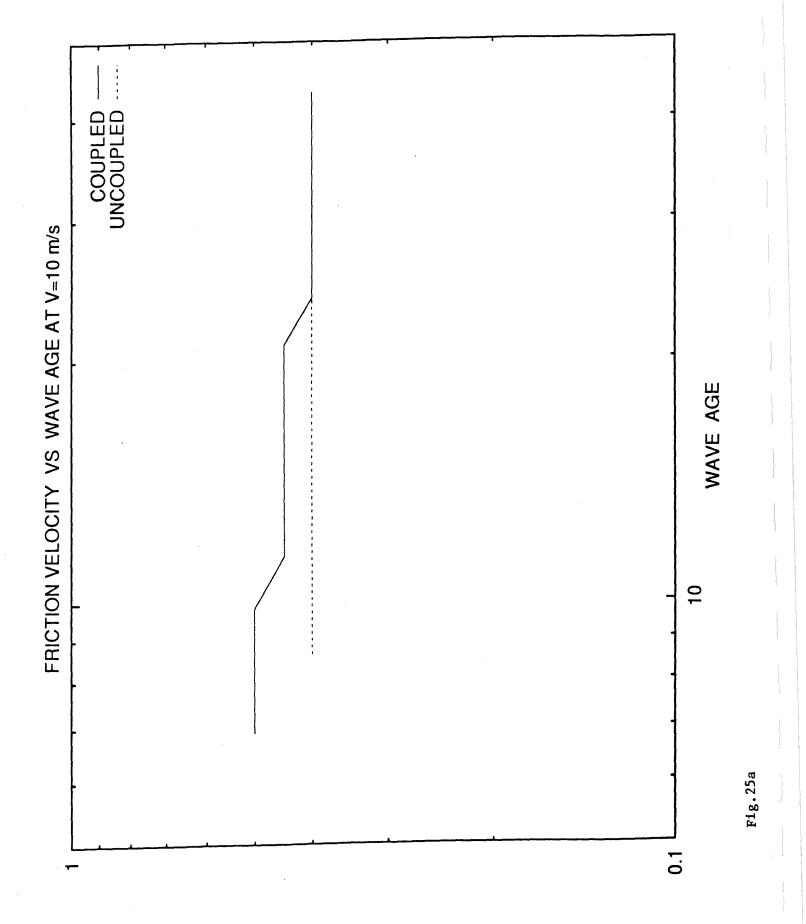


Fig.24a

Fig.24b

Fig.24c



FRICTION VELOCITY U\*



FRICTION VELOCITY U\*

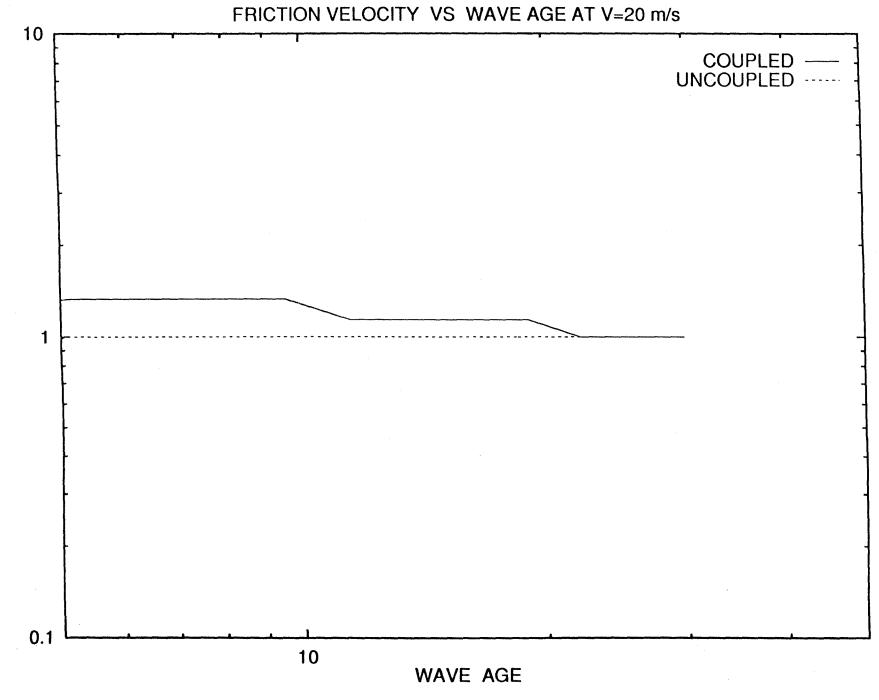
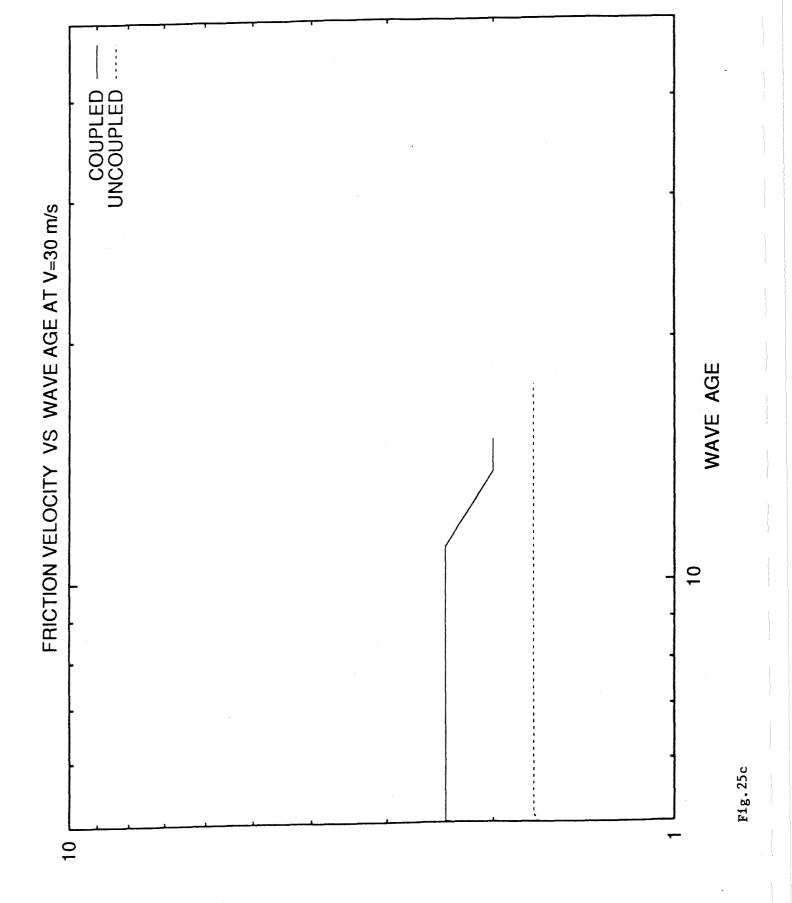
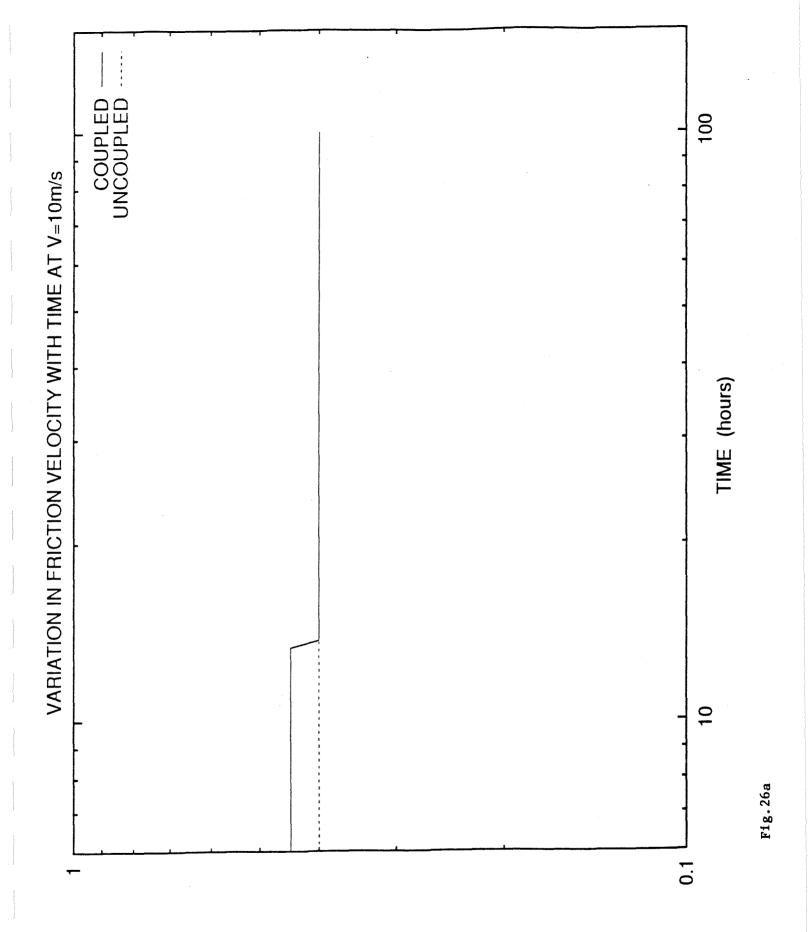


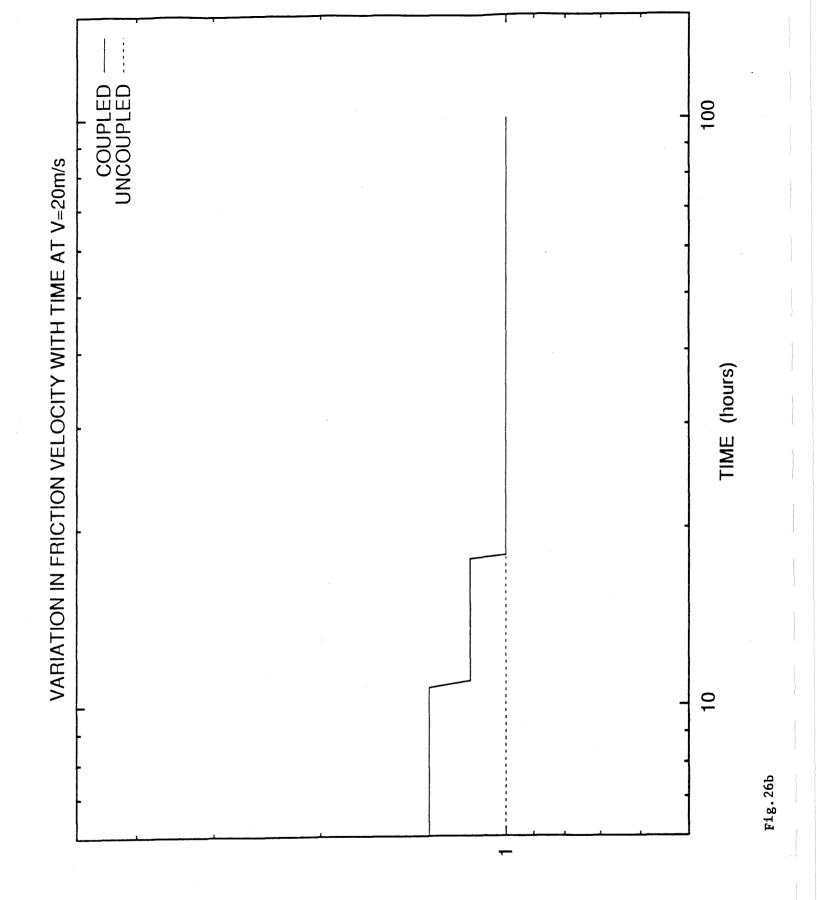
Fig. 25b



FRICTION VELOCITY U\*



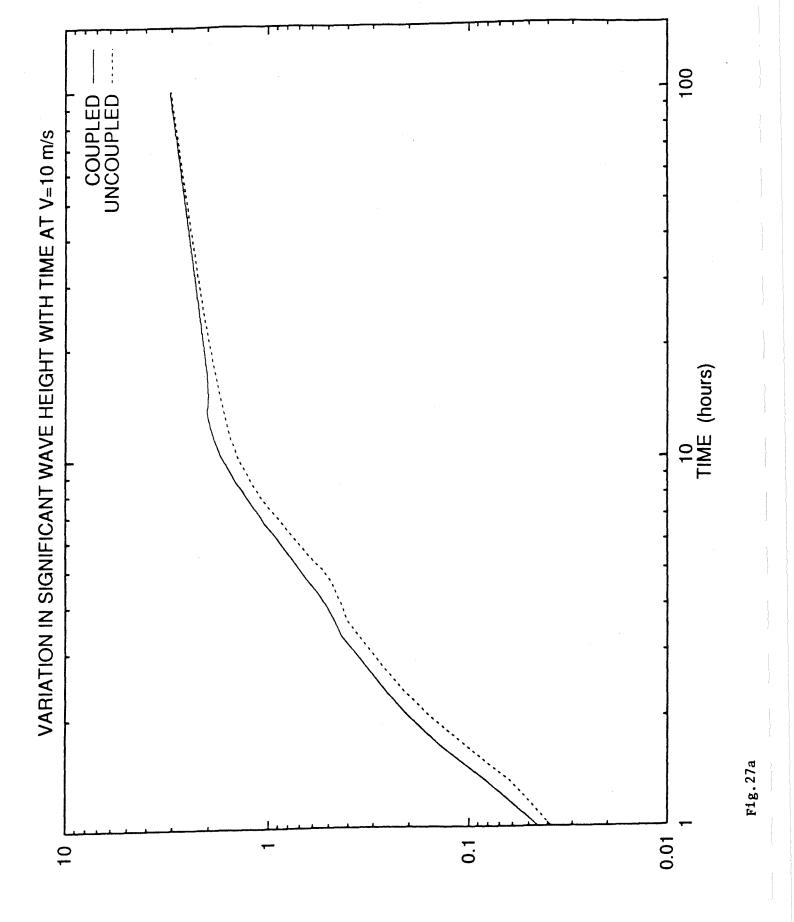
FRICTION VELOCITY U\*



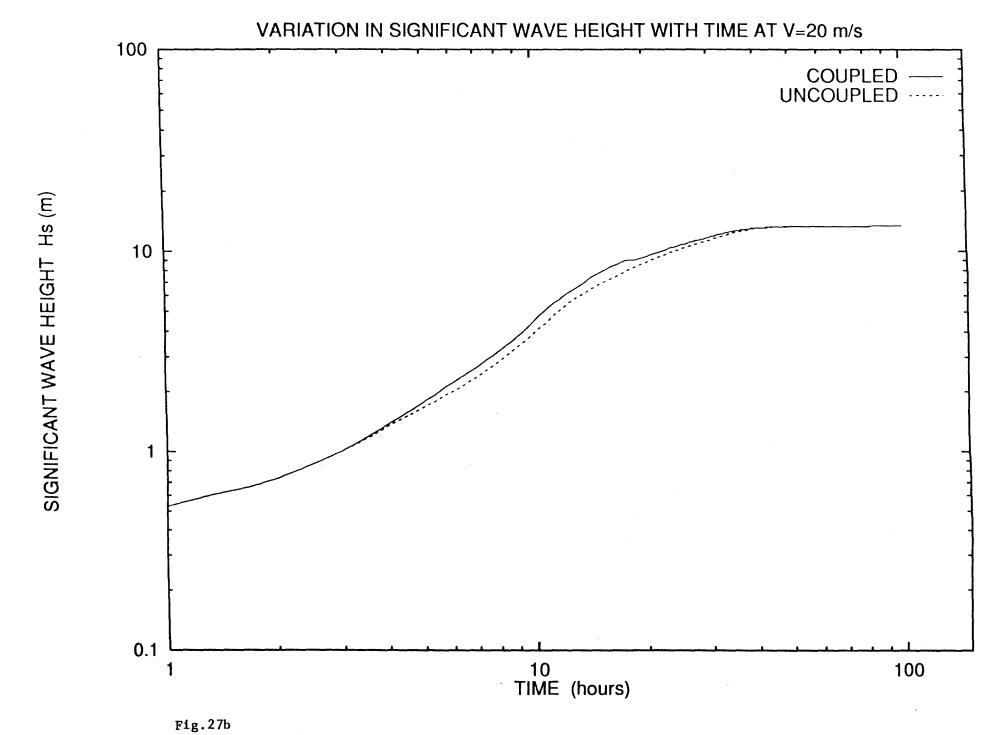
FRICTION VELOCITY U\*

Fig.26c

SIGNIFICANT WAVE HEIGHT Hs (m)







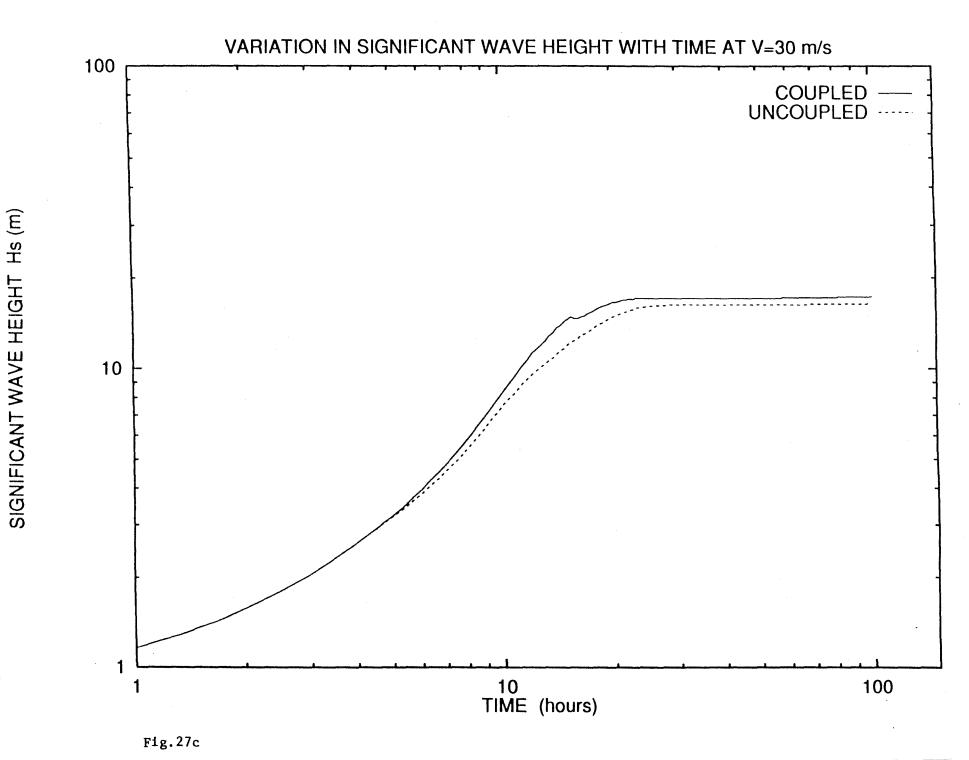
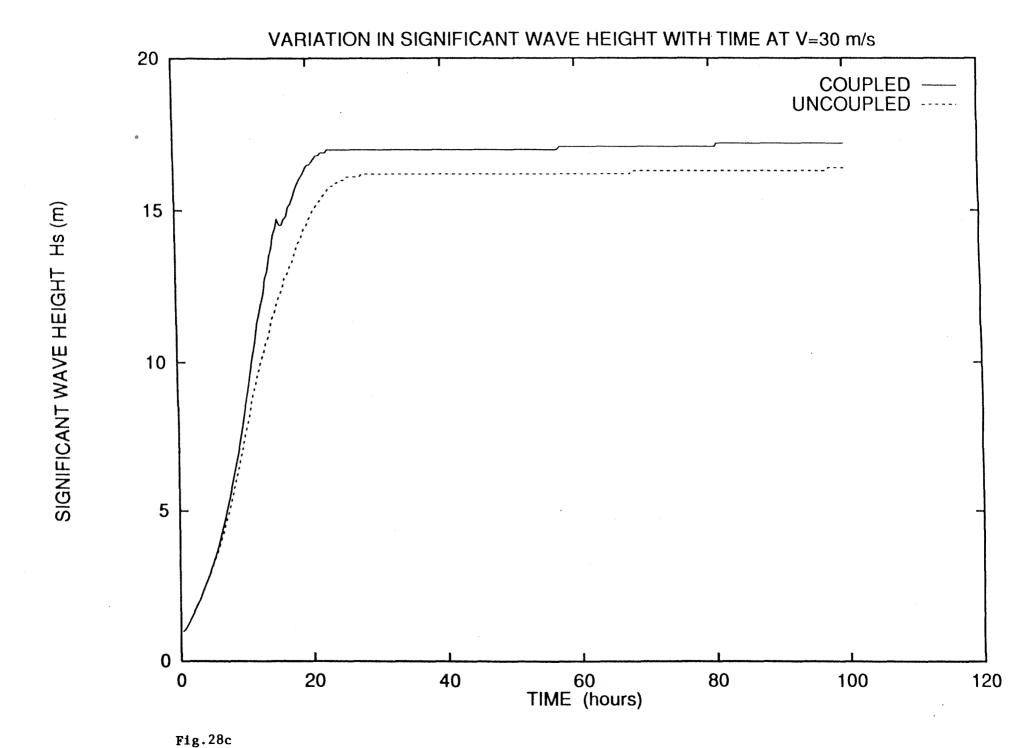
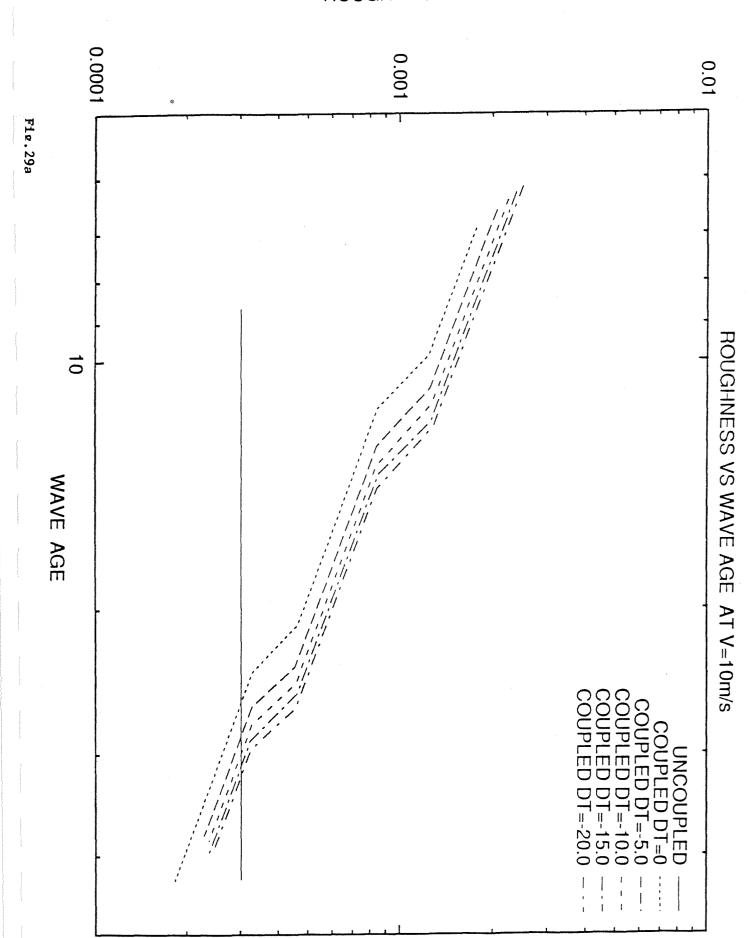


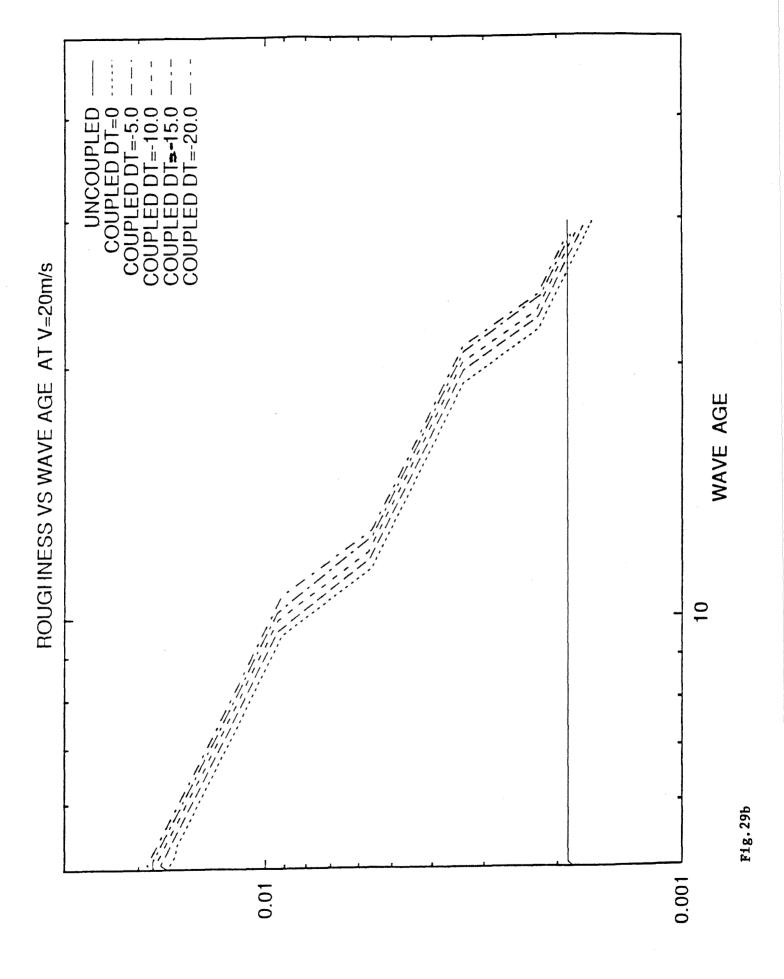
Fig. 28a

Fio. 28b

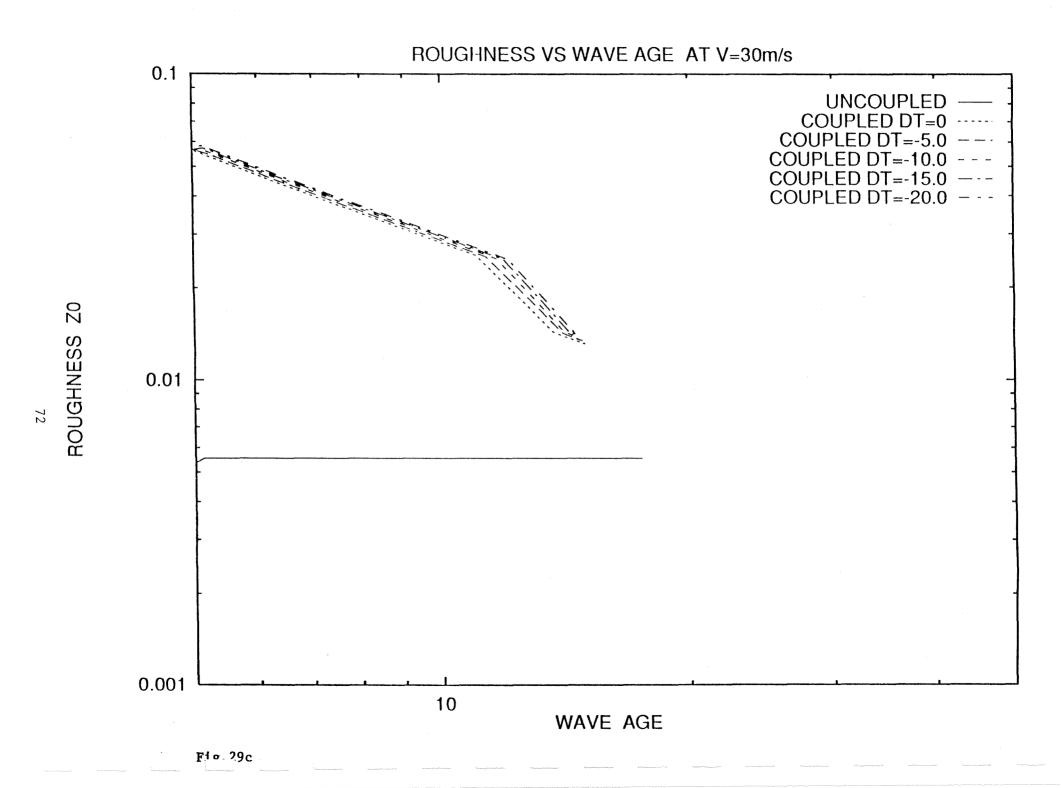


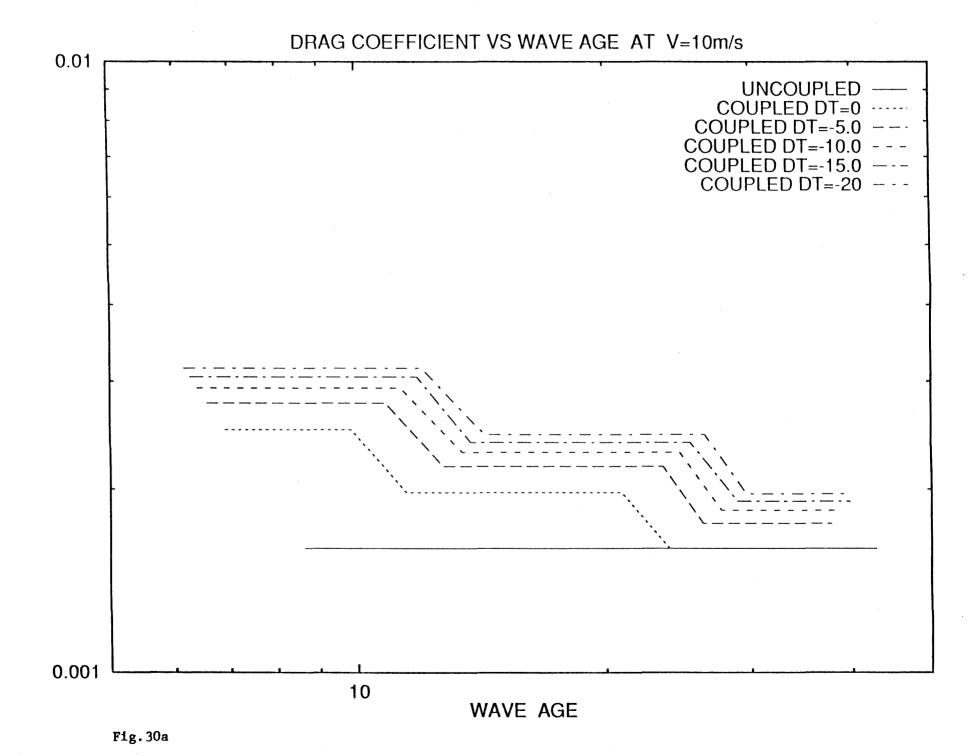
## ROUGHNESS ZO





BONGHNESS ZO

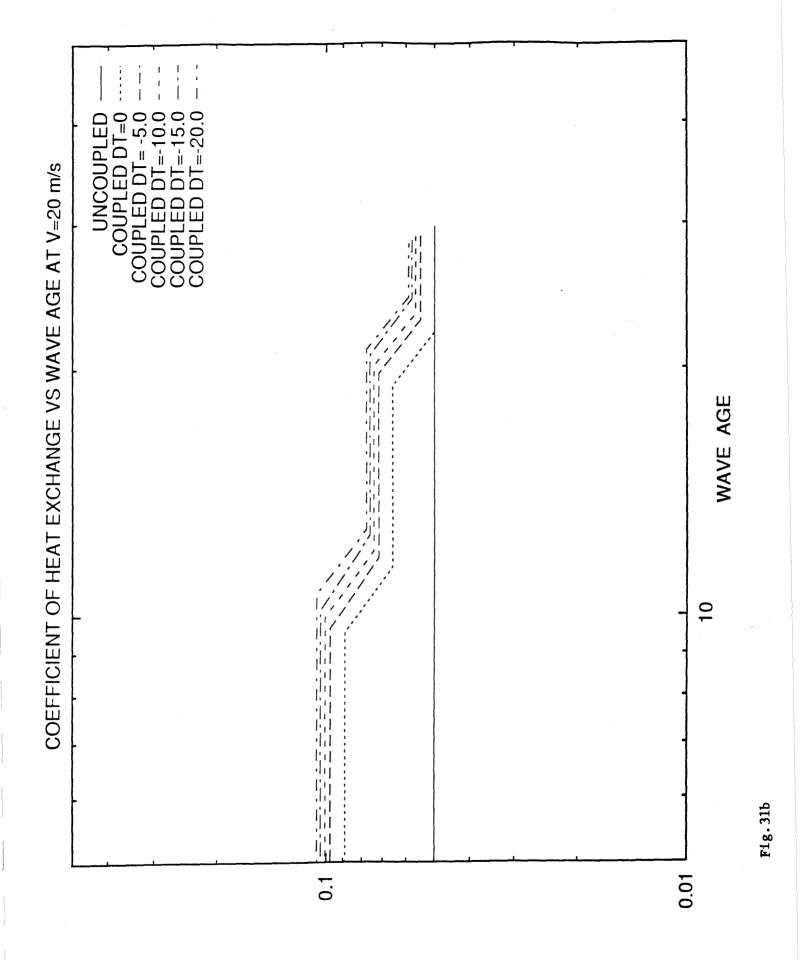


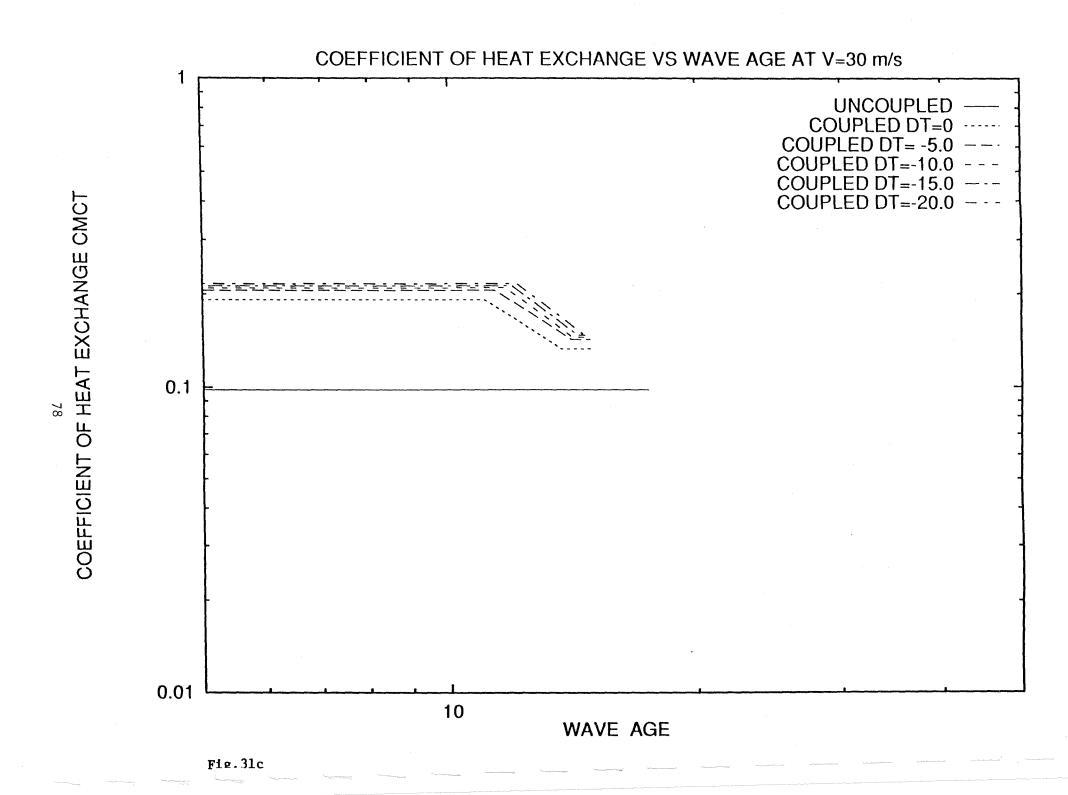


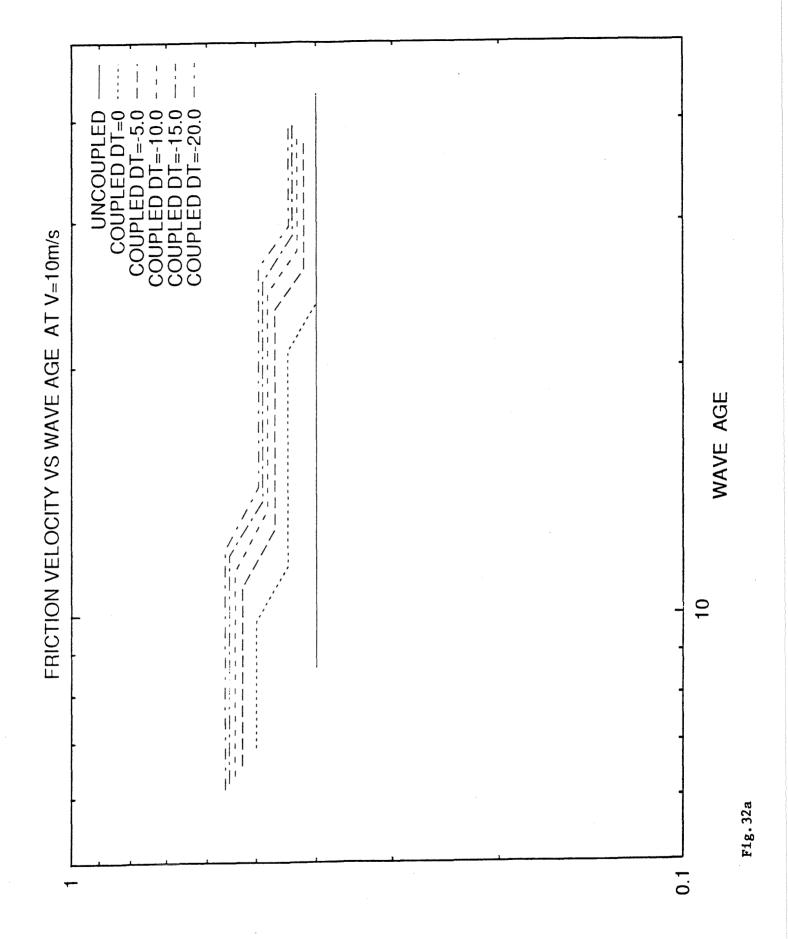
COEFFICIENT

Fig. 30c

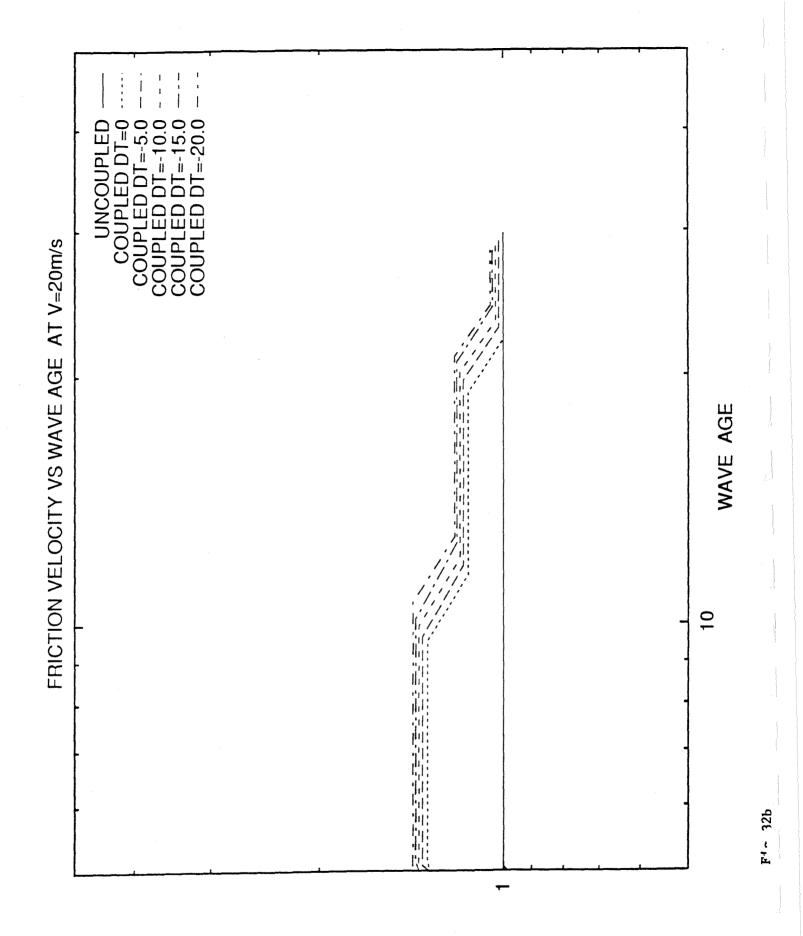
COEFFICIENT OF HEAT EXCHANGE CMCT

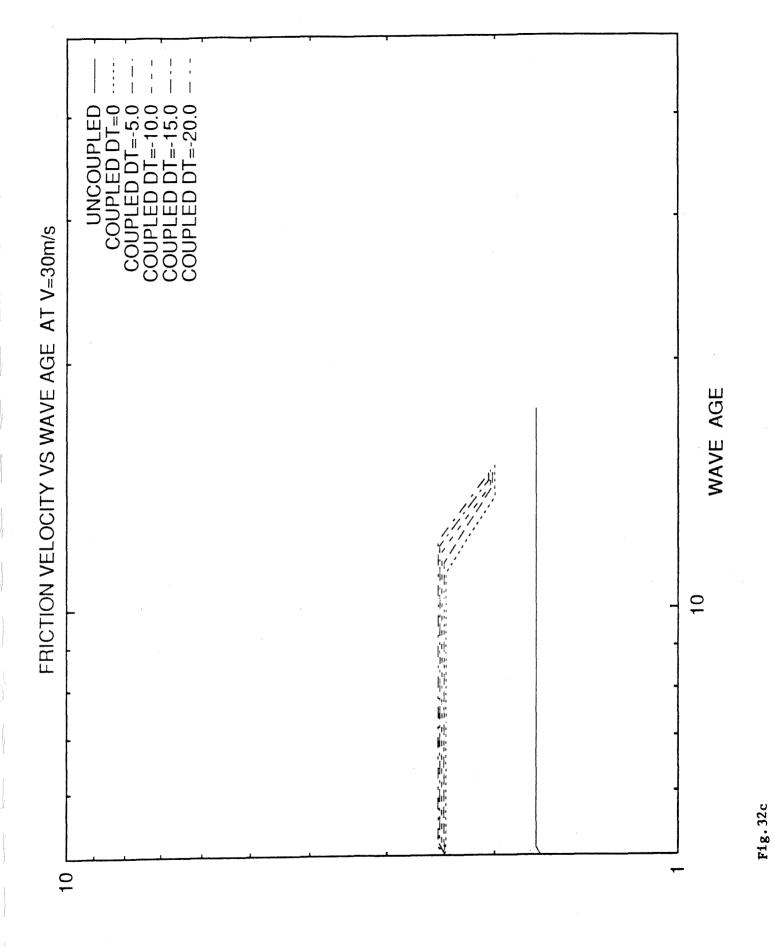




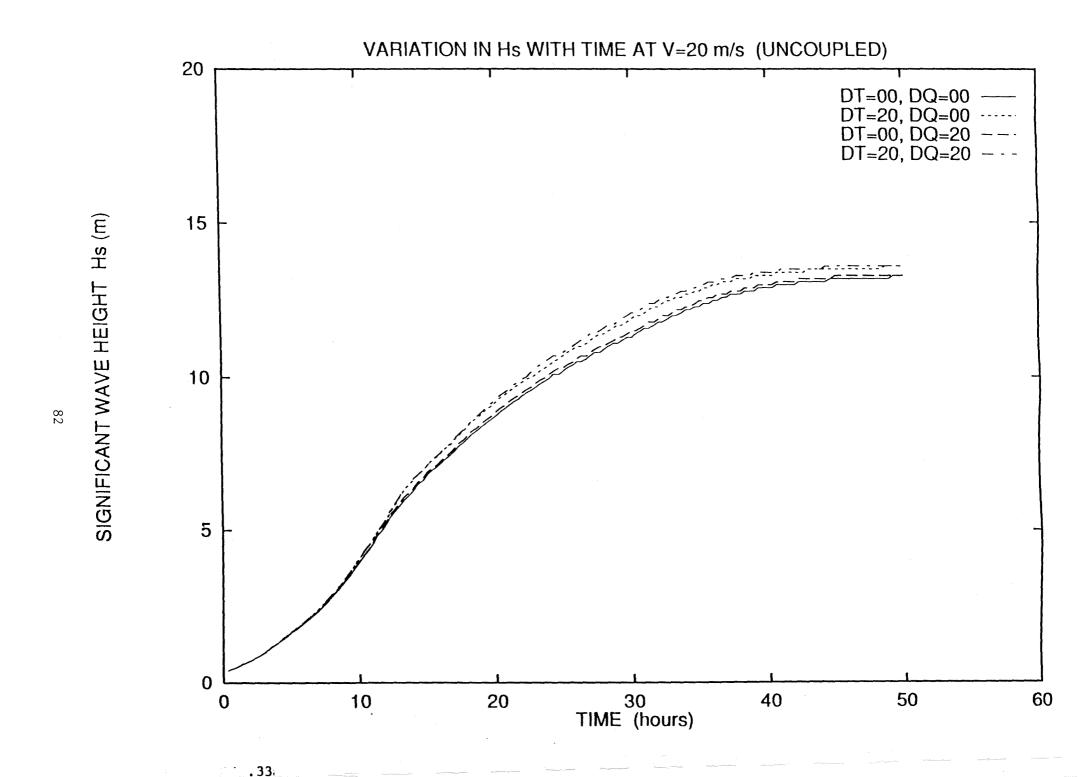


FRICTION VELOCITY U\*

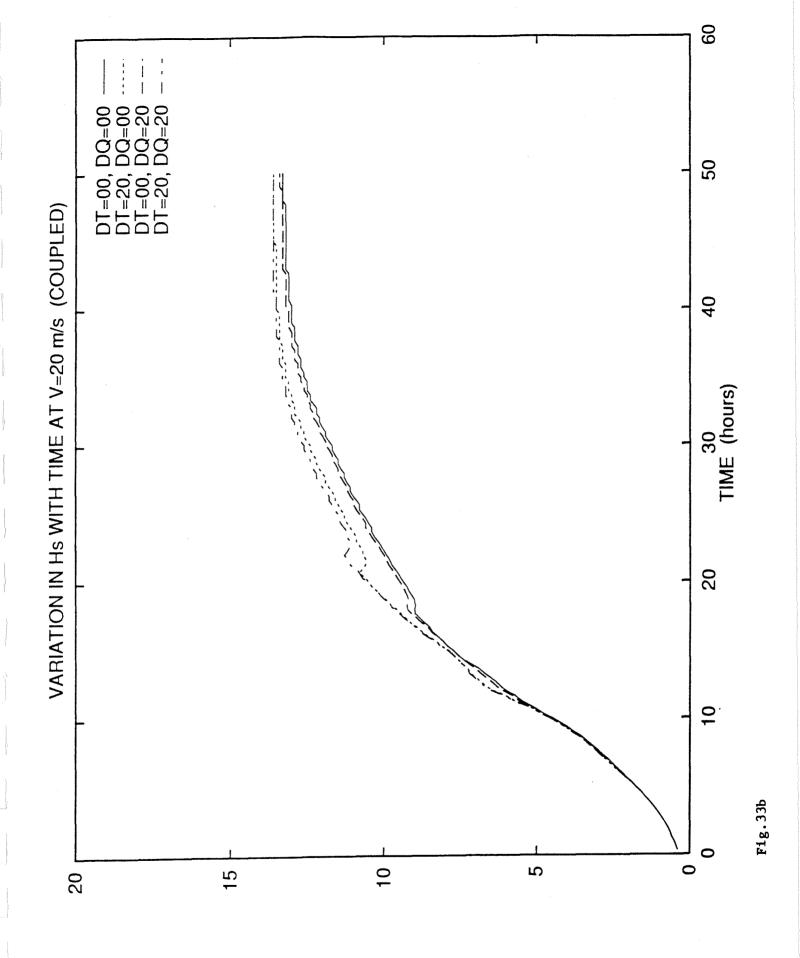




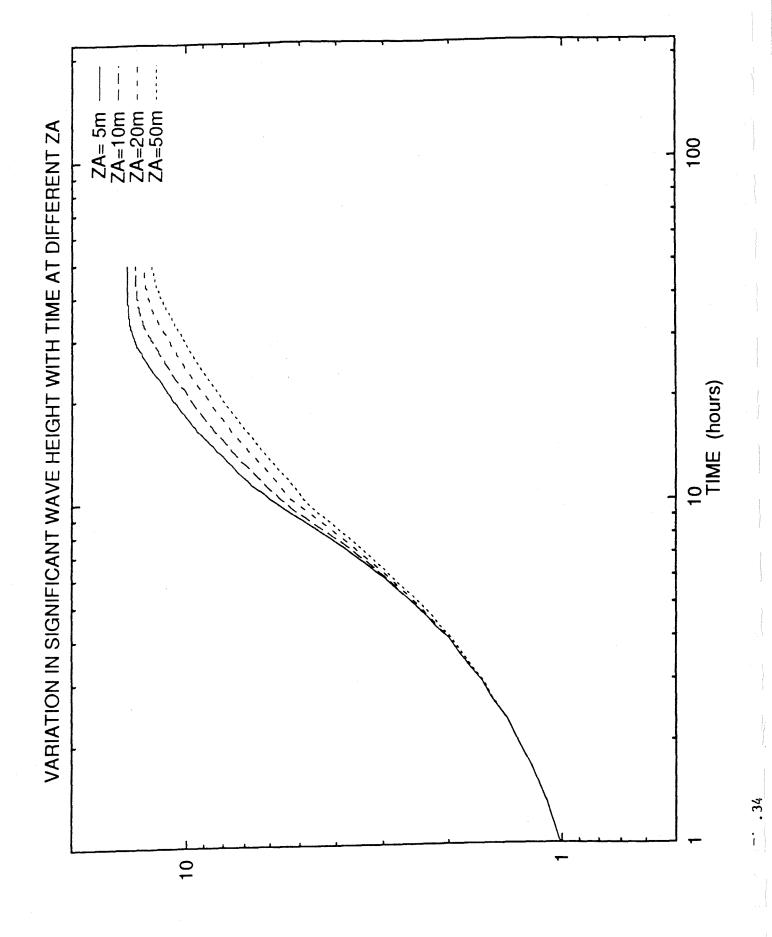
FRICTION VELOCITY U\*



## SIGNIFICANT WAVE HEIGHT Hs (m)



## SIGNIFICANT WAVE HEIGHT HS (m)



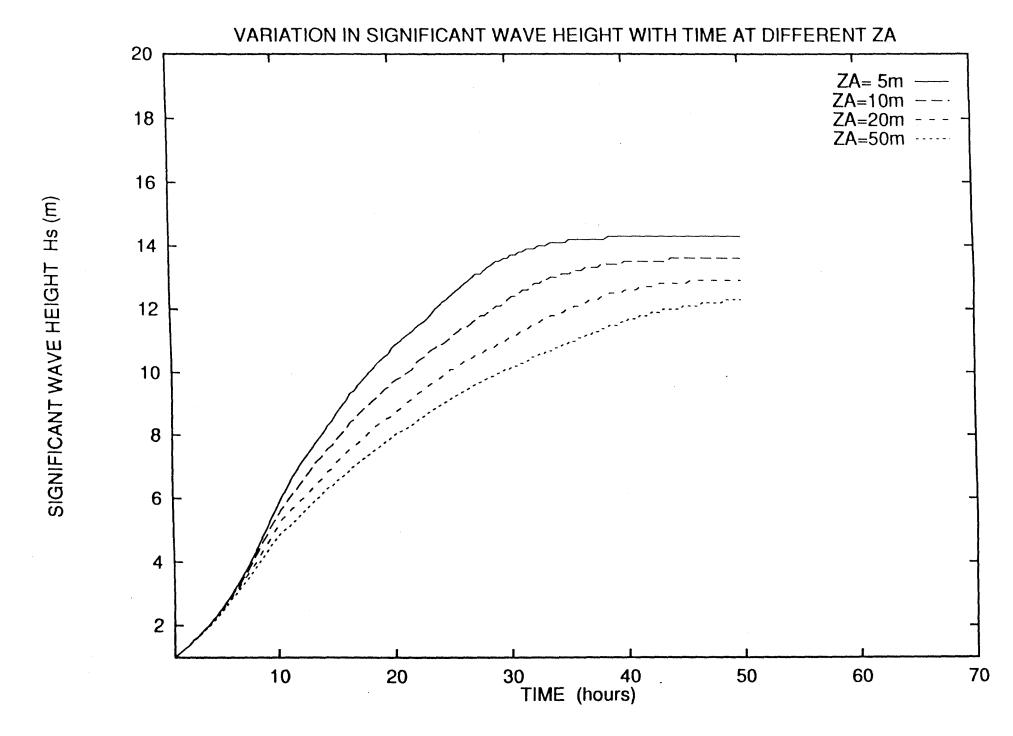
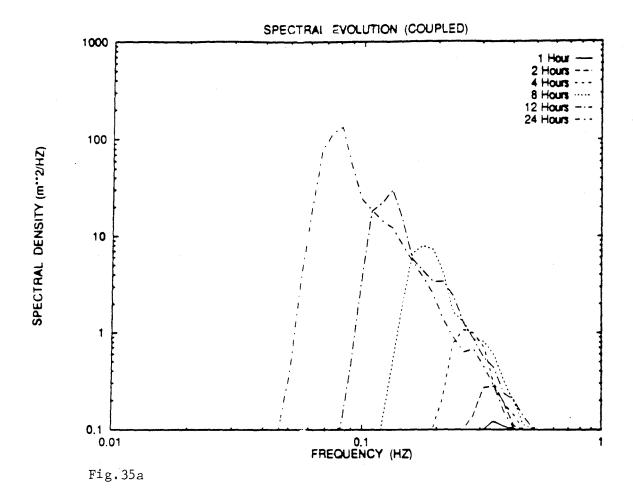
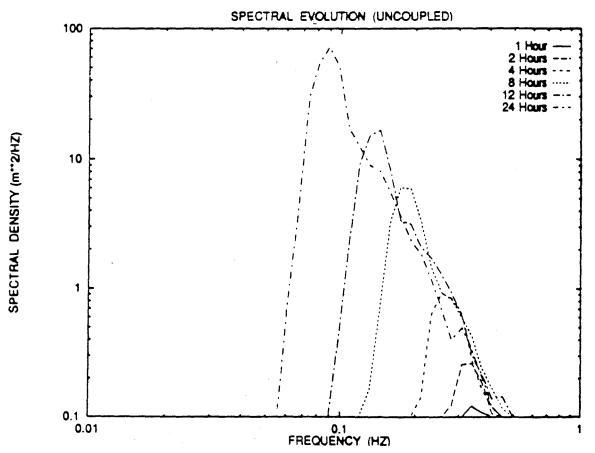


Fig. 34b





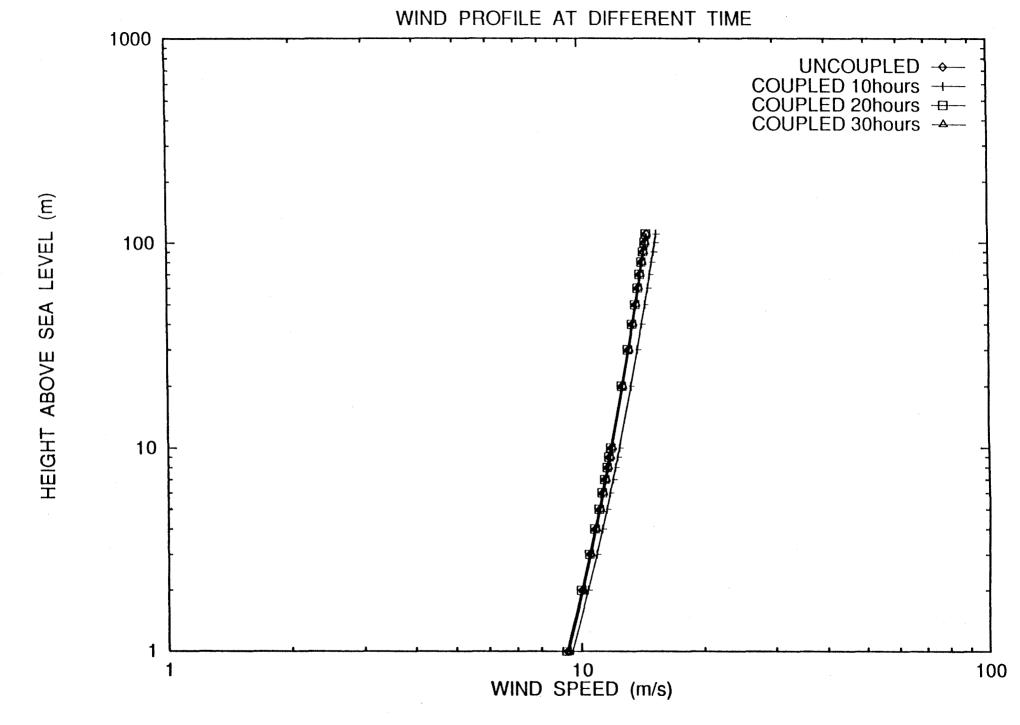


Fig.36a

Fig.36b

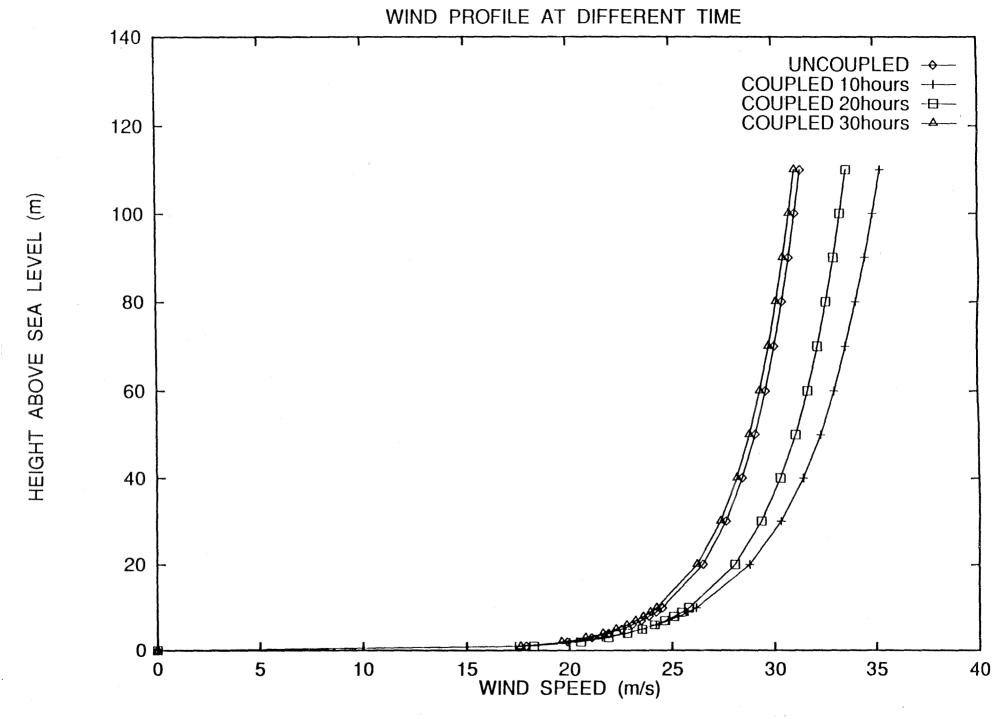
Fig. 36c

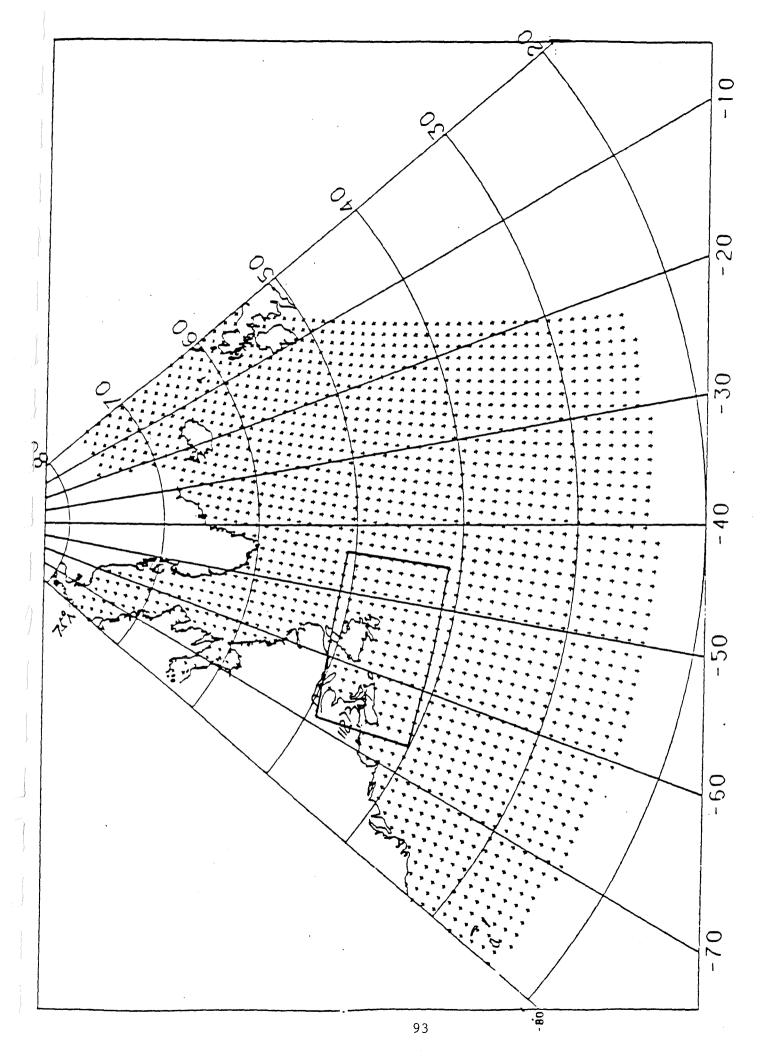
Fig.37a

WIND PROFILE AT DIFFERENT TIME

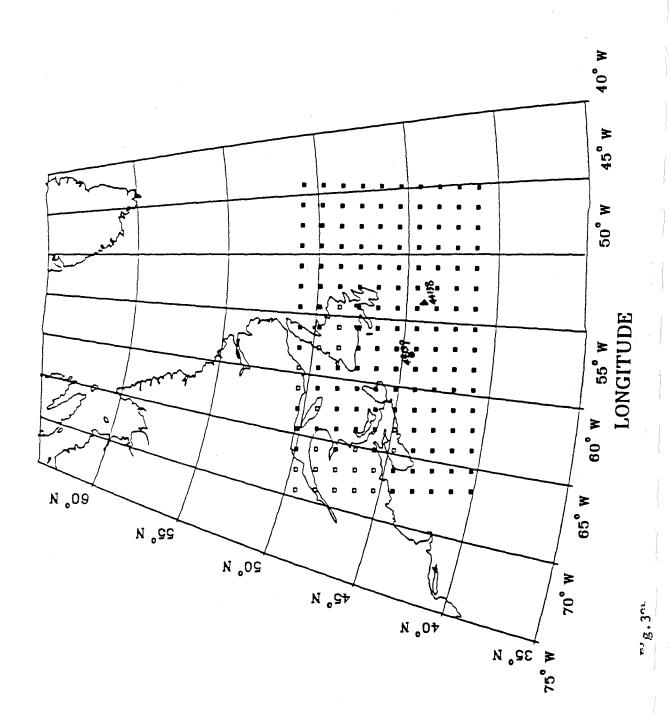


Fig. 37b





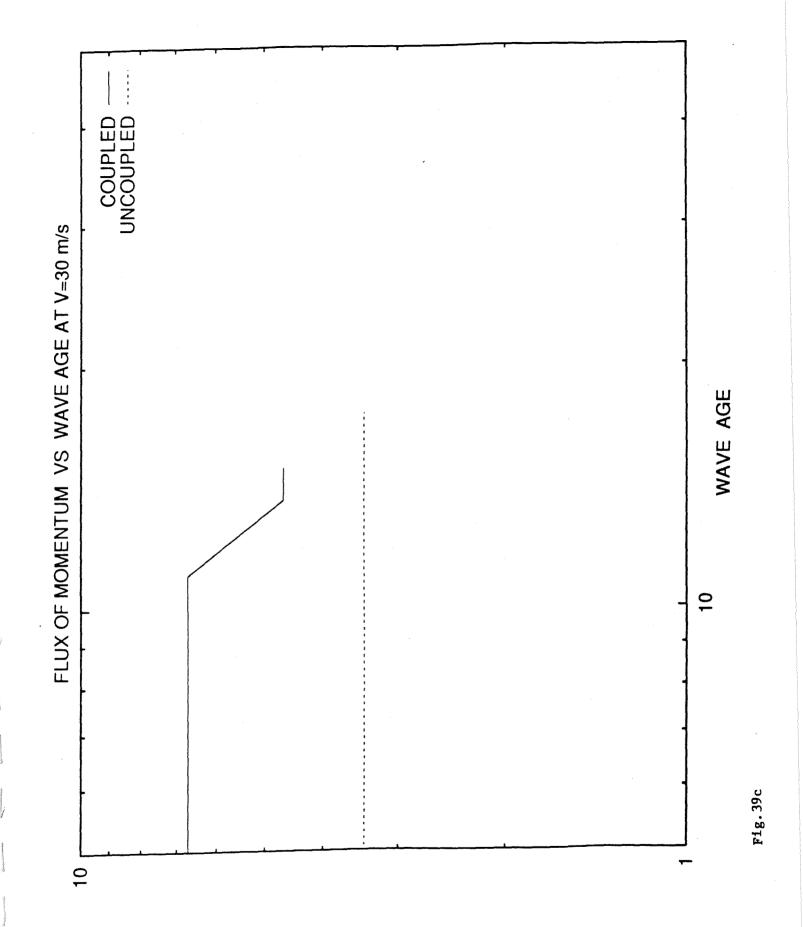
F12.38a



LATITUDE

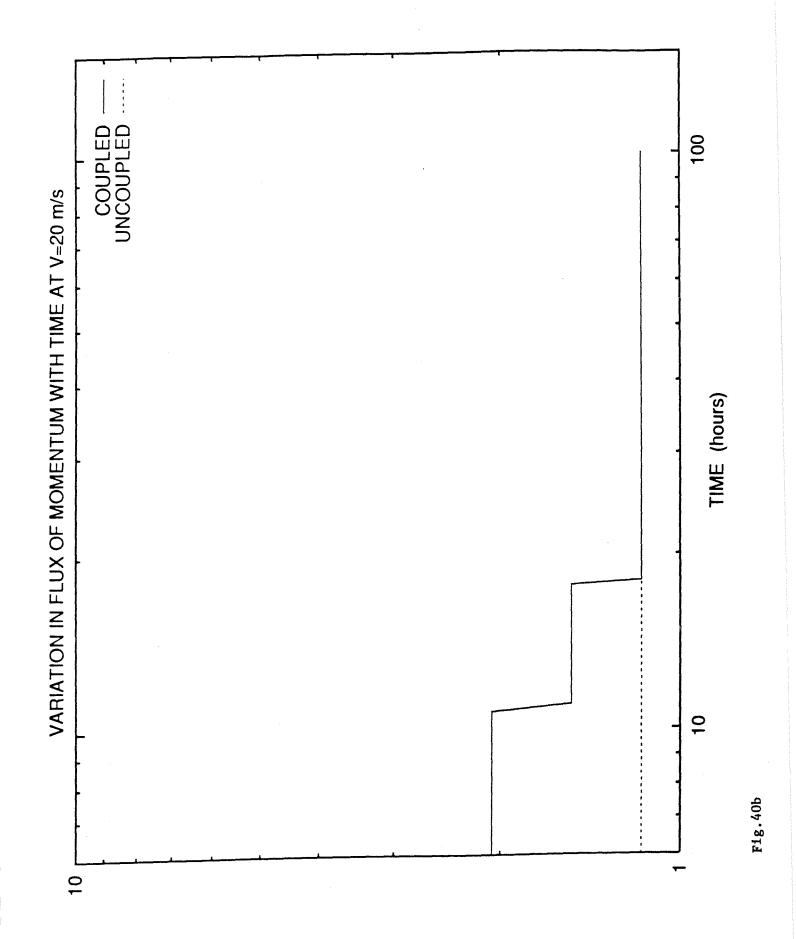
FLUX OF MOMENTUM FM

FLUX OF MOMENTUM FM

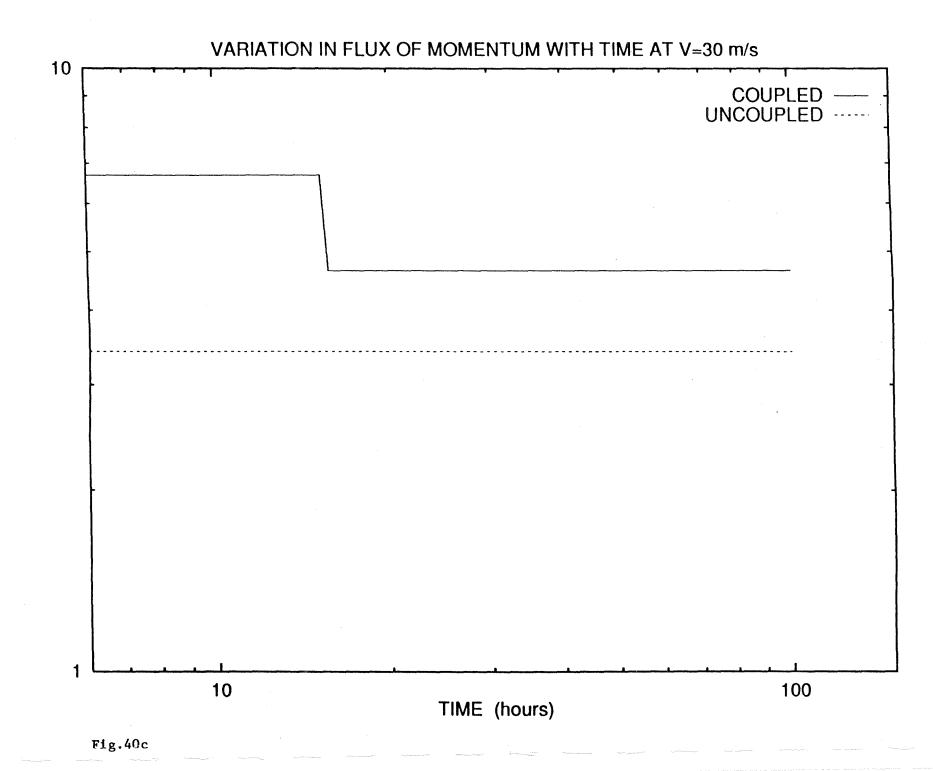


FLUX OF MOMENTUM FM

VARIATION IN FLUX OF MOMENTUM WITH TIME AT V=10 m/s



FLUX OF MOMENTUM FM





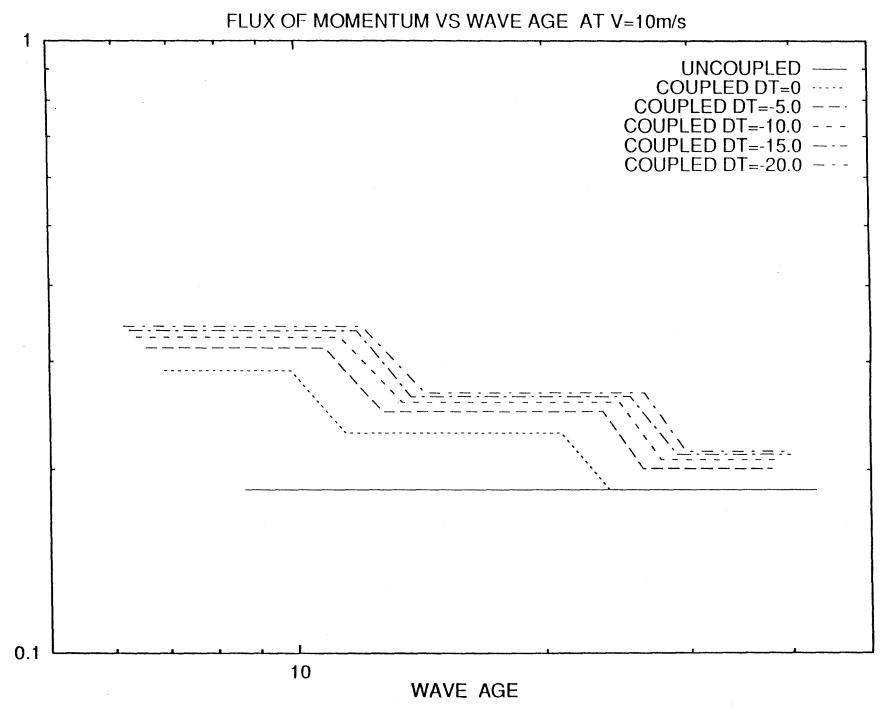
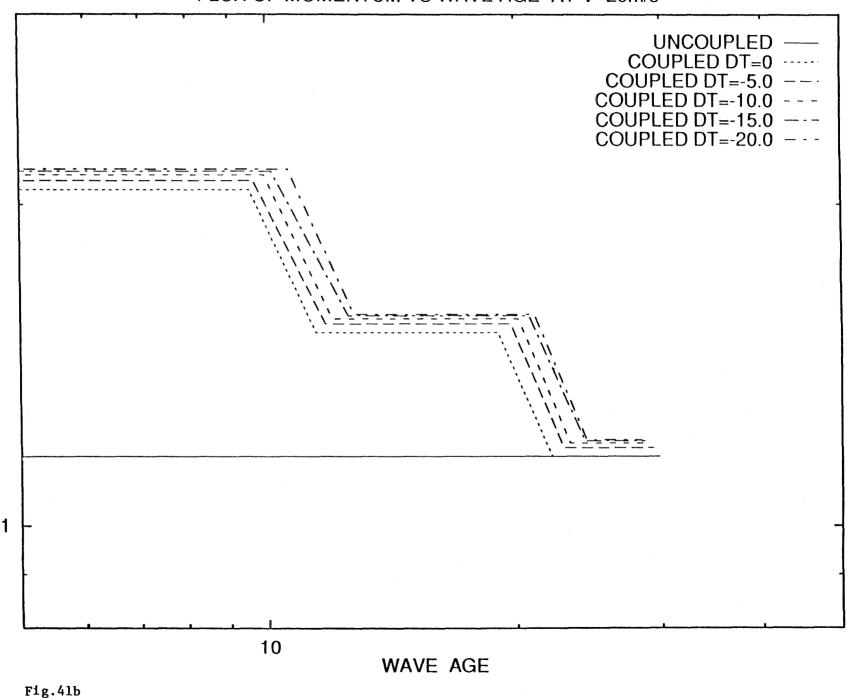


Fig.41a

#### FLUX OF MOMENTUM VS WAVE AGE AT V=20m/s

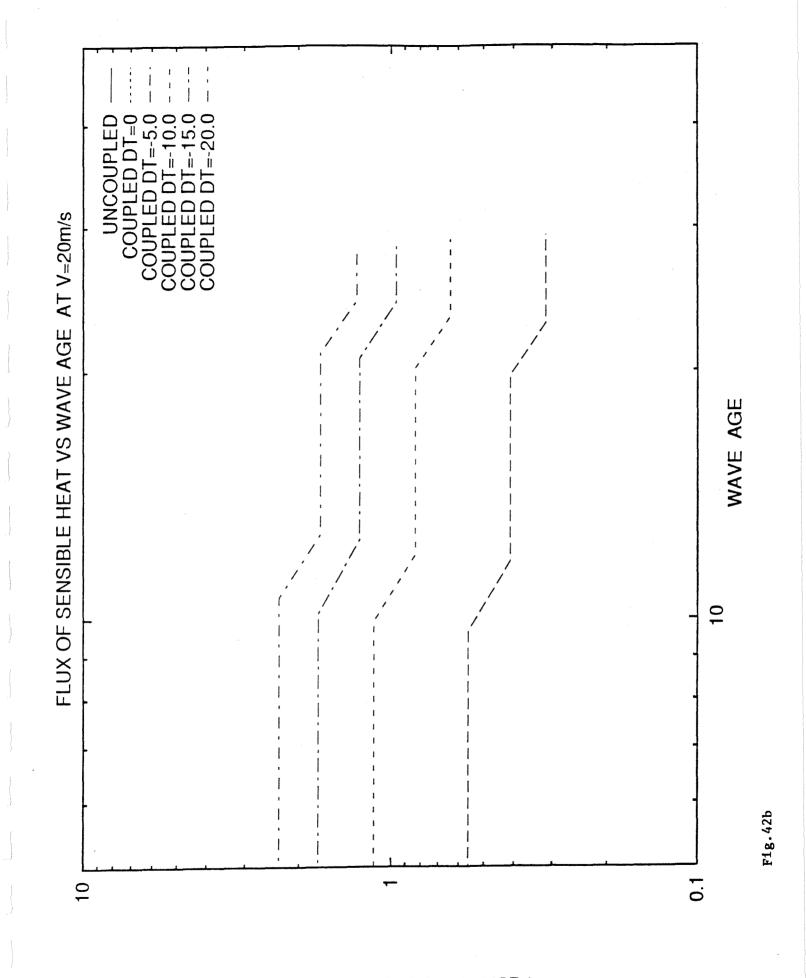


FLUX OF MOMENTUM FM

Fig.41c

Fig. 42a

FLUX OF SENSIBLE HEAT FS



# FLUX OF SENSIBLE HEAT FS

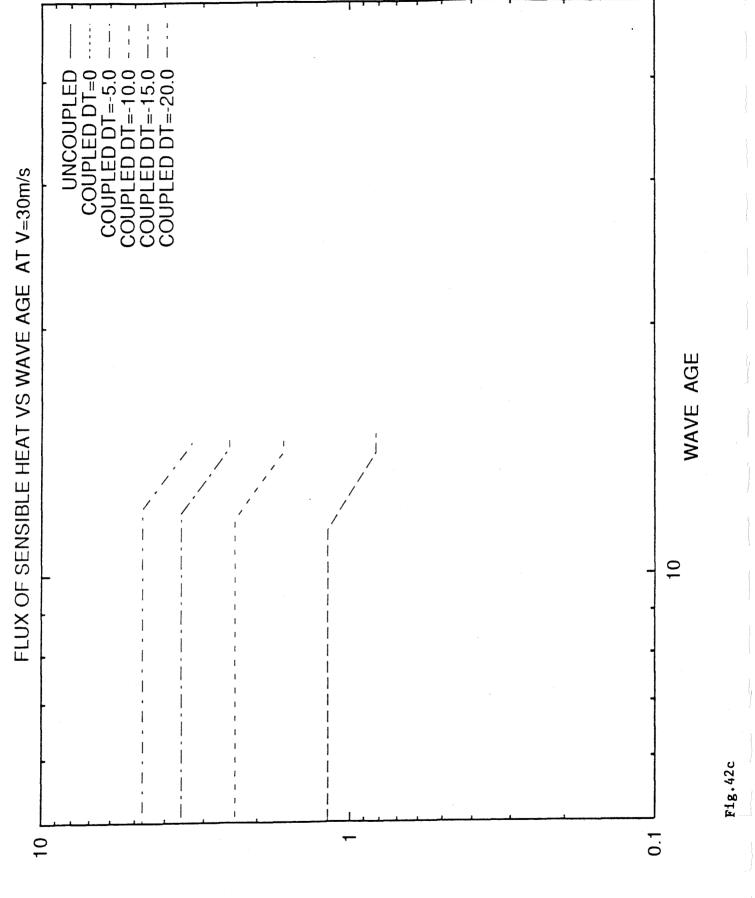


Fig.43a

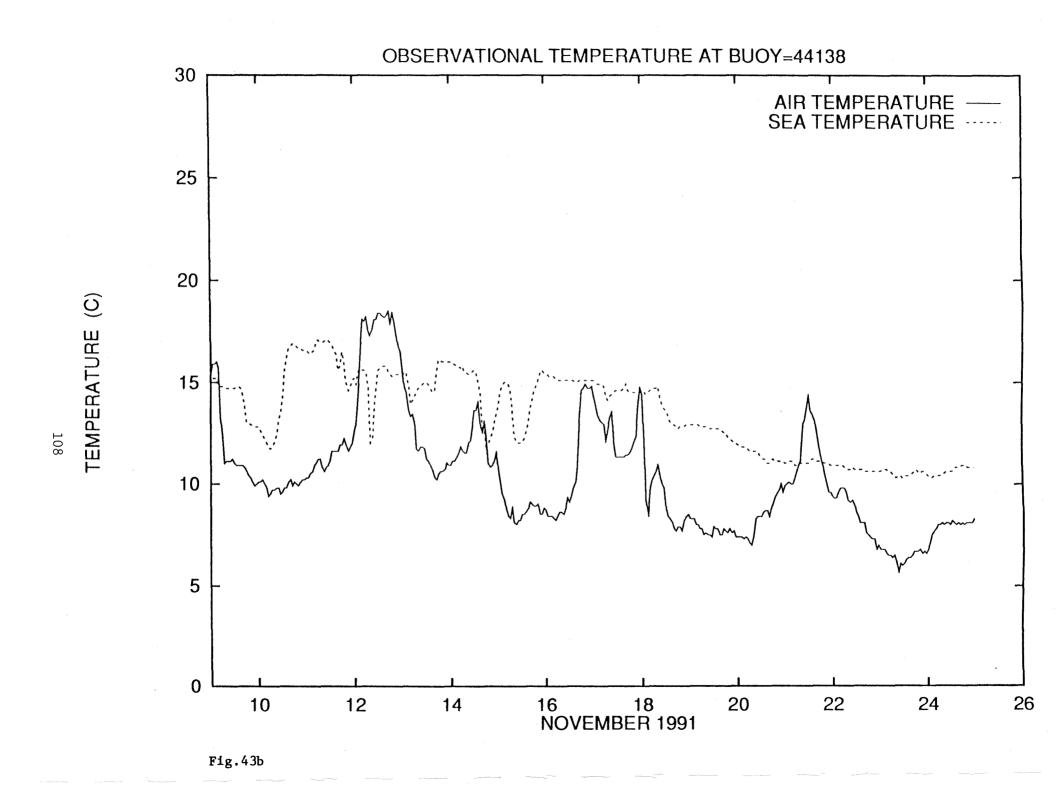


Fig.44a

WAVE HEIGHT (m)

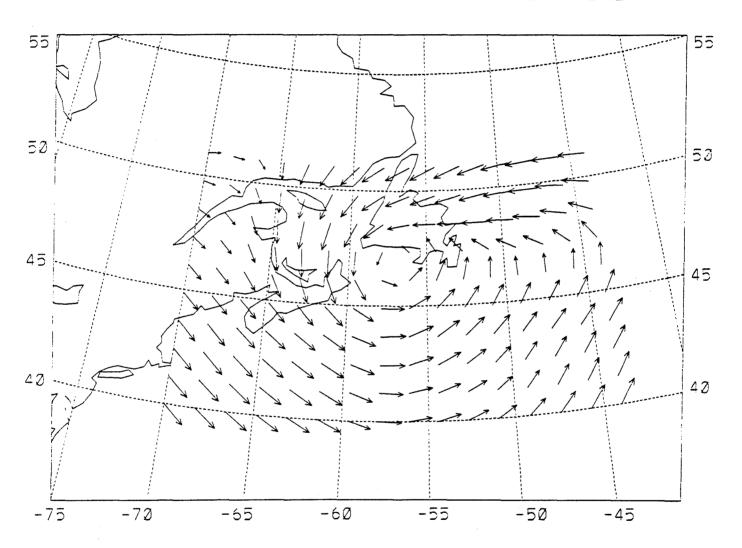
Fig.44b

Fig.45a

WAVE HEIGHT (m)

Fig.46

## WIND DATA AT: 15:00



8.265E+81 HAXIHUM VECTOR

Fig.47a

## WIND DATA AT: 16:00

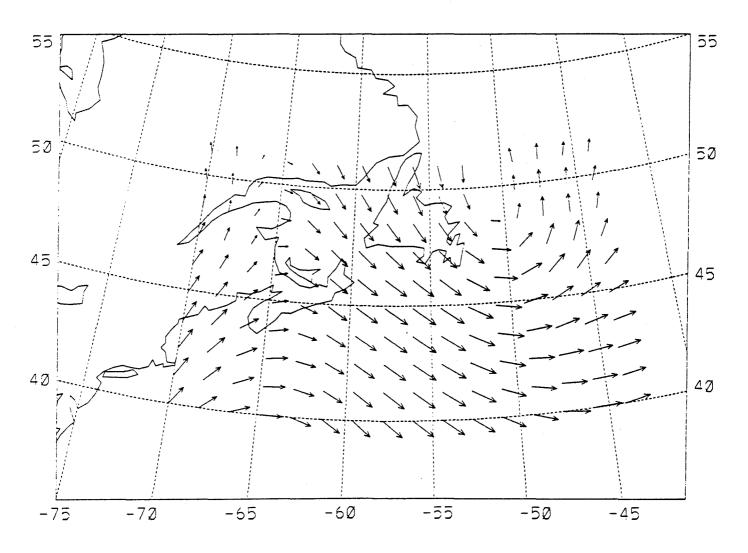


Fig.47b

Ø.286E-Ø1 MAXIMUM VECTOR

#### WIND SPEED DATA AT: 91/11/15/00

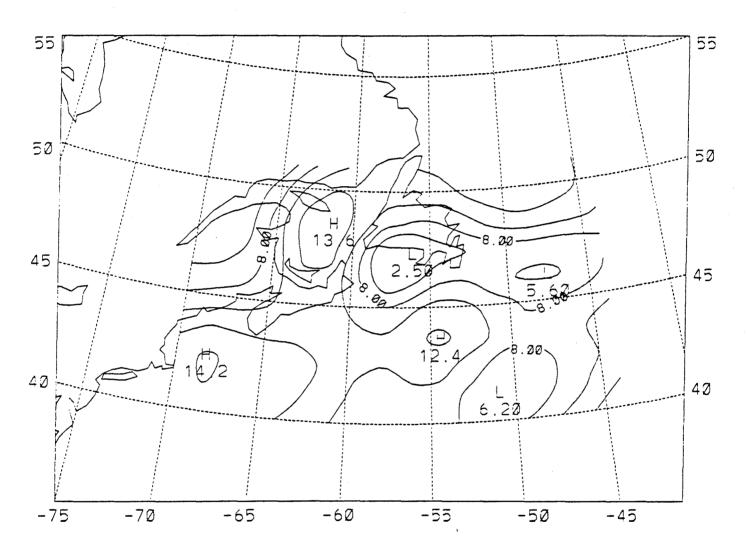


Fig. 48a contour FROM 6.0000 TO 28.000 CONTOUR INTERVAL OF 2.0000 PT(3.3)= 13.700

#### WIND SPEED DATA AT: 91/11/16/00

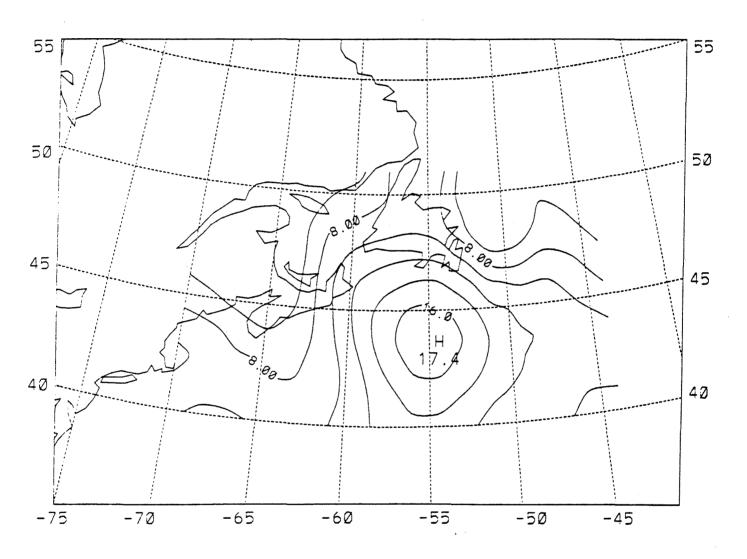


Fig. 48b

CONTOUR FROM 6.8888 TO 28.888 CONTOUR INTERVAL OF 2.8888 PT(3.3)= 8.5888

#### WAVE HEIGHT AT: 16:00 UNCOUPLED

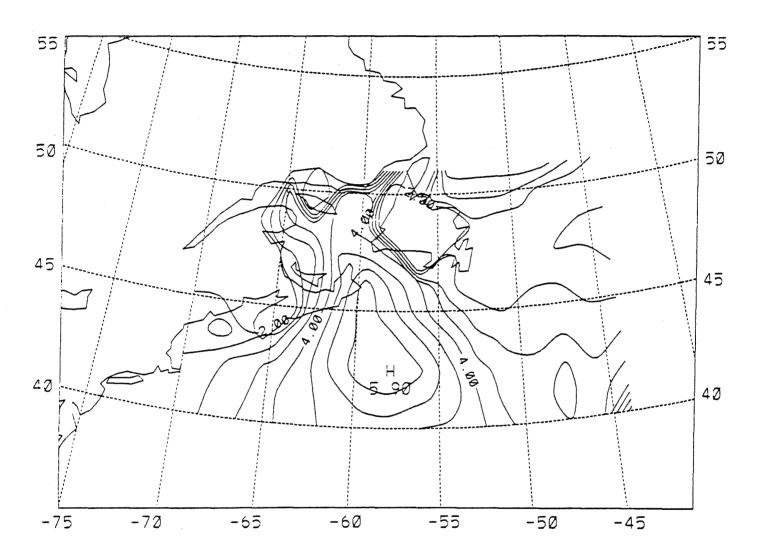
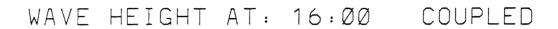


Fig. 49a

CONTOUR FROM 2.8888 TO 8.8888 CONTOUR INTERVAL OF 8.58888 PT(3,3)= 3.2888



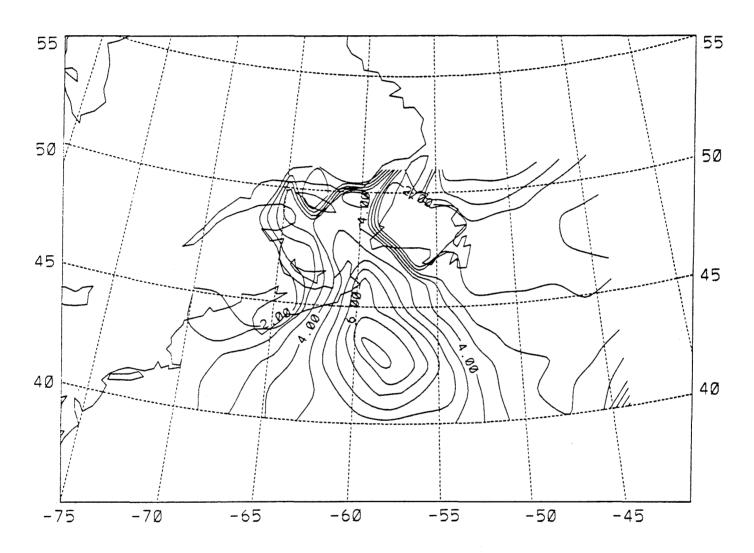
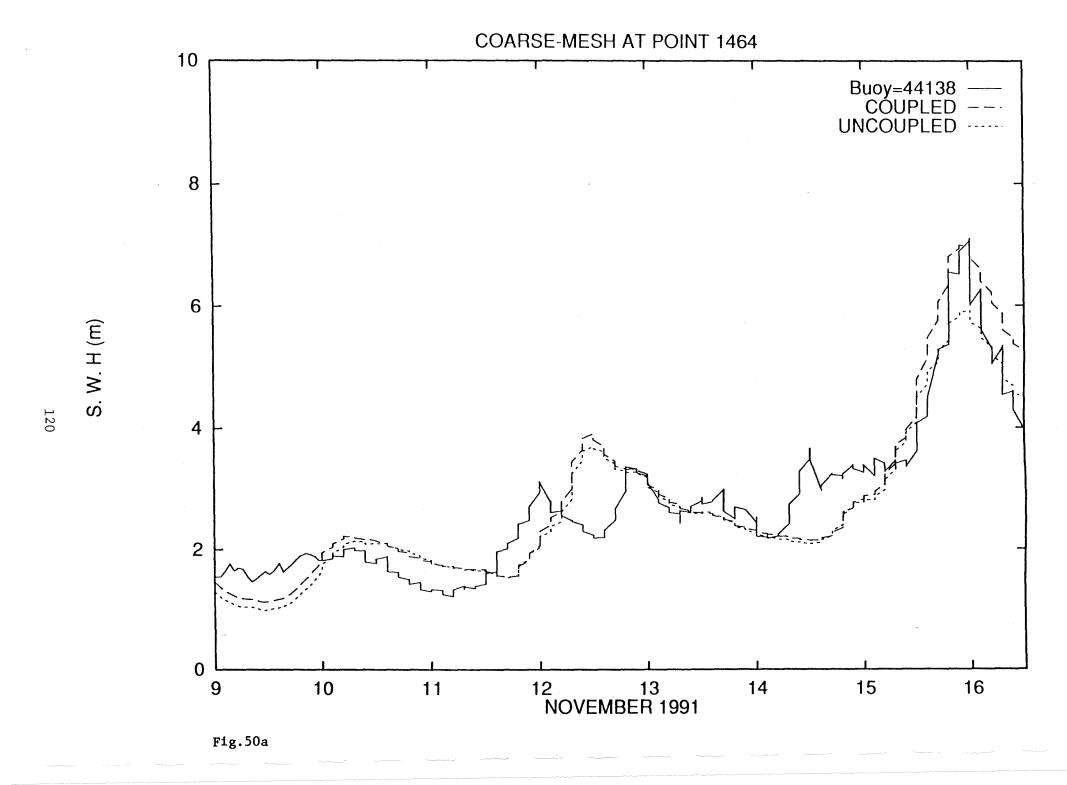


Fig. 49b

\*CONTOUR FROM 2.88888 TO 8.8888 CONTOUR INTERVAL OF 8.58888 PT(3.3)= 3.2888



S. W. H (m)

Fig.50b

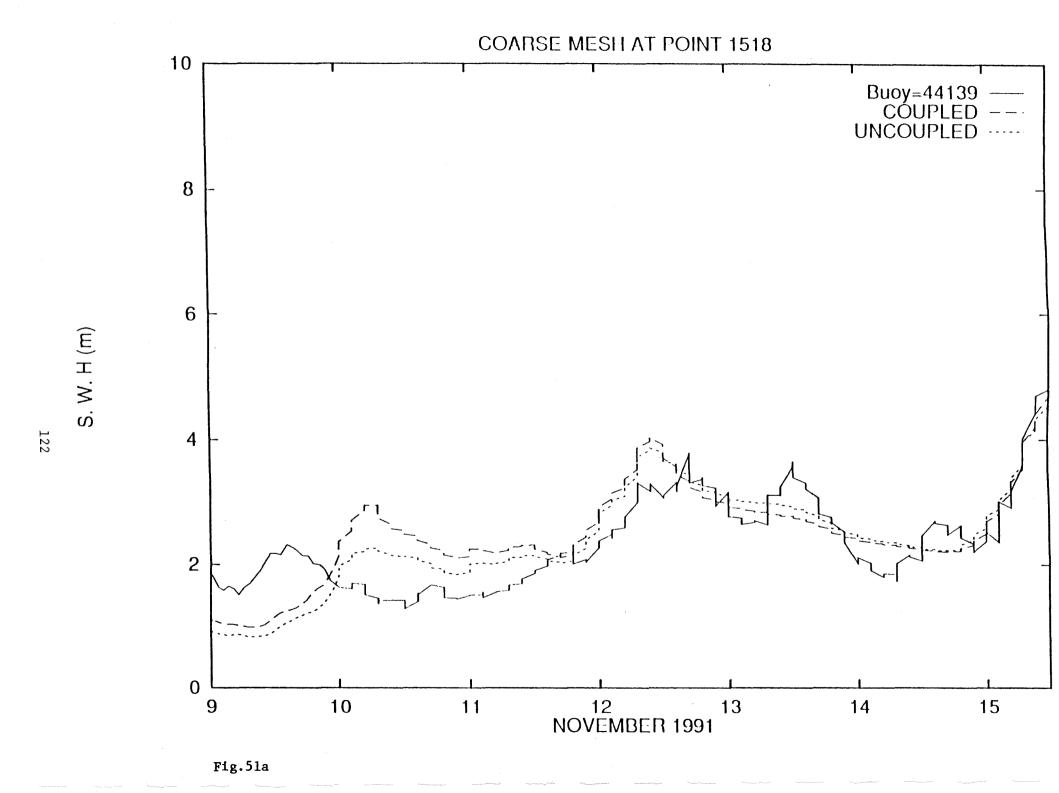


Fig.51b



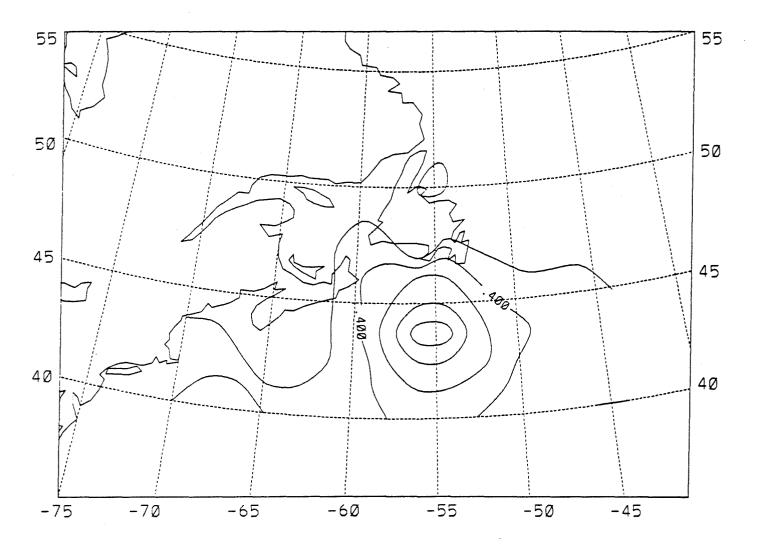


Fig. 52a

CONTOUR FROM 8.28888 TO 3.8888 CONTOUR INTERVAL OF 8.28888 PT(3.3)= 8.28888

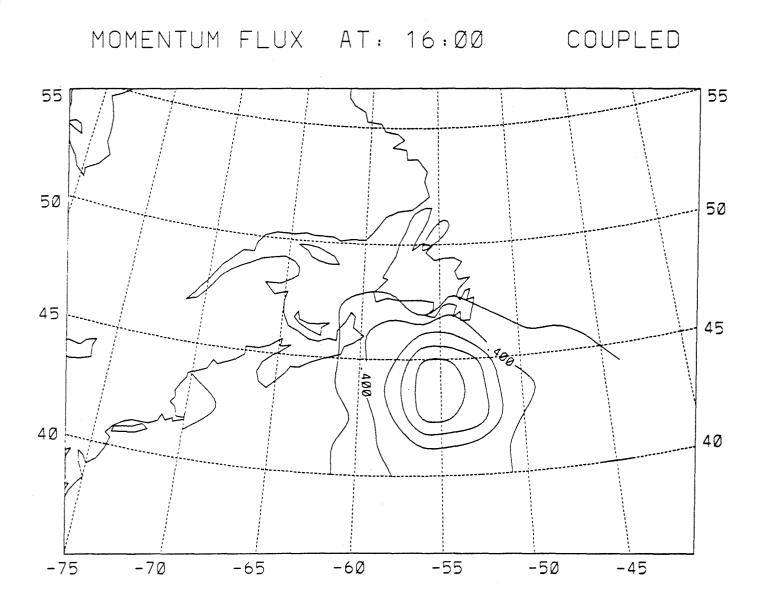


Fig. 52b

CONTOUR FROM 8.28888 TO 3.8888 CONTOUR INTERVAL OF 8.28888 PT(3.3)= 8.18888

#### SENSIBLE HEAT FLUX AT: 16:00 UNCOUPLED

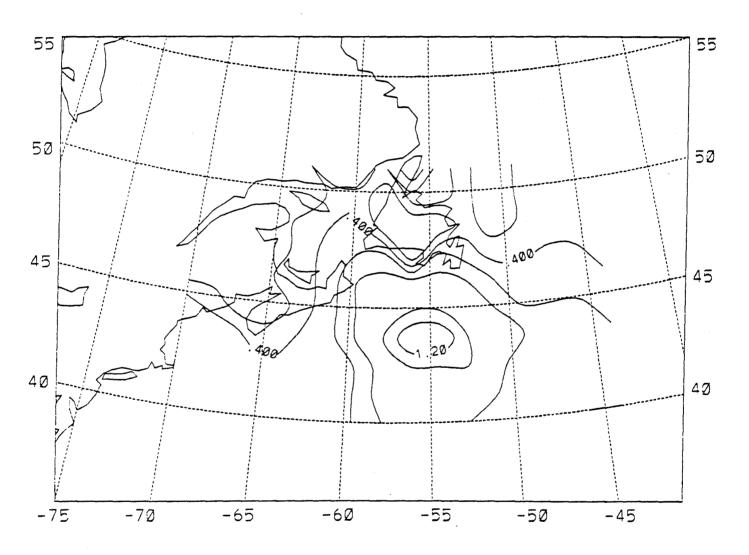


Fig. 53a

CONTOUR FROM 8.28888 TO 3.8888 CONTOUR INTERVAL OF 8.28888 PT(3.3)= 8.58888

### SENSIBLE HEAT FLUX AT: 16:00 COUPLED

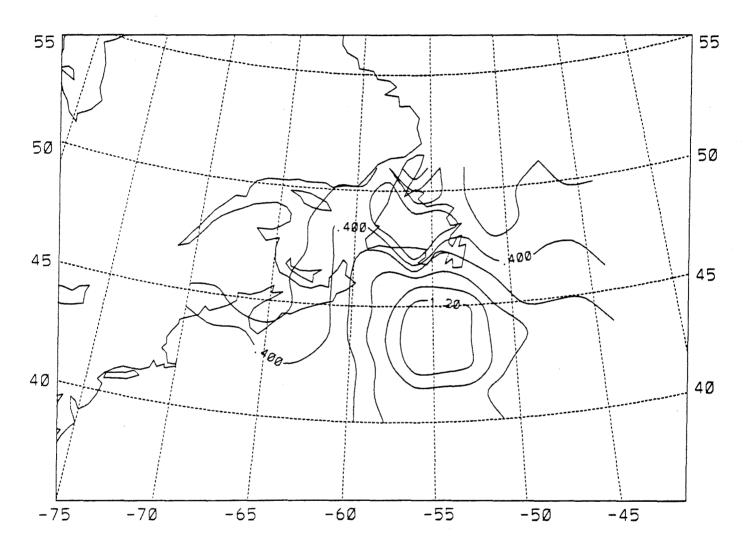


Fig. 53b

CONTOUR FROM 8.28888 TD 3.8888 CONTOUR INTERVAL OF 8.28888 PT(3.3)= 8.48888

#### LATENT HEAT FLUX AT: 16:00 UNCOUPLED

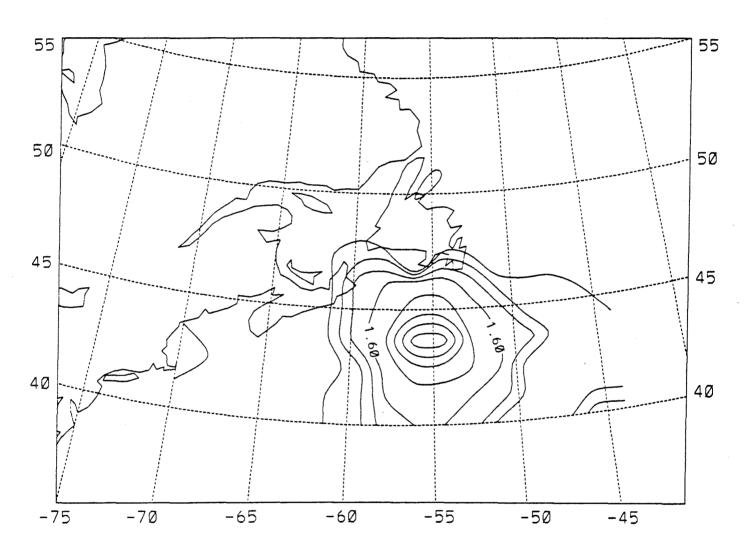


Fig.54a

#### LATENT HEAT FLUX AT: 16:00 COUPLED

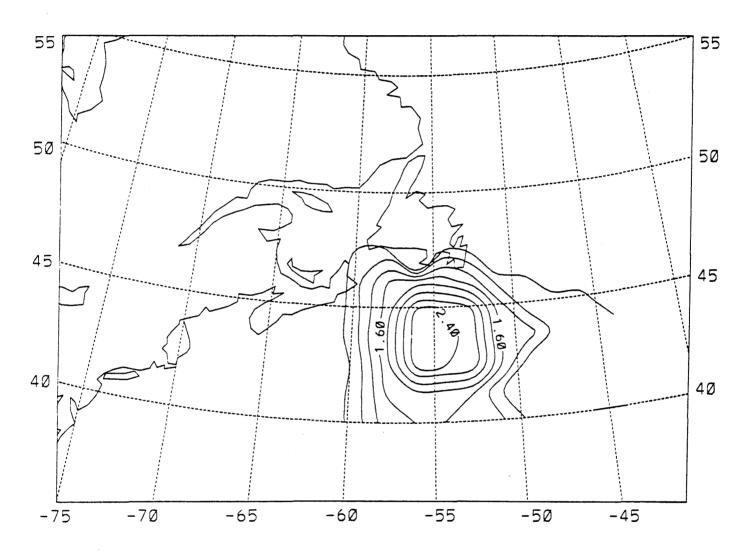


Fig. 54b

CONTOUR FROM 1.8888 TO 5.8888 CONTOUR INTERVAL OF 8.28888 PT(3.3)= 8.78888

WIND SPEED (m/s)

Fig.55

Fig.56