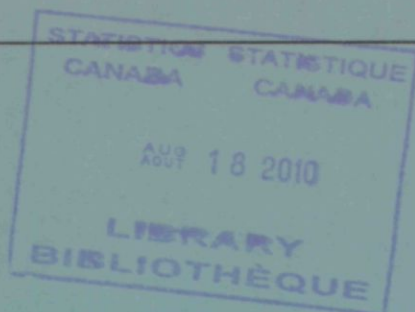


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SURVEY METHODOLOGY

TECHNIQUES D'ENQUÊTE

June - 1981 - Juin

VOLUME 7

NUMBER 1 - NUMÉRO 1

A Journal produced by
Methodology Staff
Statistics Canada

Préparé par les
méthodologistes de
Statistique Canada

SURVEY METHODOLOGY/TECHNIQUES D'ENQUÊTE

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SURVEY MAINTENANCE - PHILOSOPHY AND PRACTICE¹F. Mayda and P. Timmons²

An aspect of surveys not always given adequate consideration is maintenance.

The scope and importance of survey maintenance are discussed and a case is made for a more scientific methodological approach. Practical applications to various stages of surveys are illustrated by examples from the Canadian Labour Force Survey.

1. INTRODUCTION

Survey maintenance is an indispensable part of any continuing survey; however, its components are usually treated as separate activities rather than as an overall program. This ad hoc approach can result in gaps in the program, inadequate documentation or dissemination of results, inefficiency, and lack of funding due to inadequate understanding of the problems addressed by maintenance. The recognition of survey maintenance as a distinct methodological domain can encourage the application of a more scientific approach. One such example is the cost-benefit approach to controls in surveys of Platek and Singh [1]. This paper will deal with a philosophy of sample maintenance and will also present some illustrations of various aspects of its application in a large scale continuous survey.

For the purposes of this paper, survey maintenance can be considered

¹ This paper was presented at the Canadian Conference in Applied Statistics (1981) at Concordia University, Montreal, April 29, 1981.

² F. Mayda and P. Timmons, Census and Household Survey Methods Division, Statistics Canada.

as the sum total of the activities and programs, both regular and occasional:

- a) which ensure that the survey design is respected in all of the operations of the survey,
- b) which measure the quality of operations and of survey data,
- c) which modify or adapt the survey process to meet changing requirements.

The maintenance aspect of the design and conduct of large scale continuing surveys seldom receives sufficient recognition. There can be many reasons for this. Theoreticians, anxious to break new ground and develop new, and in some sense better, mathematical approaches, find the concept of maintenance unglamorous and mundane. Managers, concerned with competing priorities, budgets and production, often fail to see the relationship of maintenance to operational productivity and question the need for these expenditures. The very word "maintenance" has the connotation of "just getting by" or "avoiding deterioration" and seems to imply "no change" for many people.

In spite of this lack of recognition, maintenance is a most necessary part of continuing surveys for many good reasons. The requirements of the survey may change, the conditions in the population being surveyed or the sample frame itself may change, there may be changes in policy or budget, new techniques or equipment may become available. Adapting to these changes and ensuring that quality and efficiency are not compromised is a regular part of the maintenance of a survey. Even if such obvious changes do not occur, such things as the turnover of all levels of staff, the passage of time since principles and procedures were first learned and the gradual separation of the designers and developers from the operations staff can lead to a dilution of experience and the possible degeneration of quality.

The purpose of this paper is neither to try to glamourize survey maintenance nor to develop some all-encompassing theoretical approach, model or package which can be applied to any survey. Rather, the purpose of this paper is to spotlight the role of survey maintenance, to bring to the fore and emphasize how that role applies to large scale continuing surveys and, by demonstrating its function, to encourage a more scientific and theoretical study to be brought to bear on the subject. In order to do this, it must be realized that survey maintenance is more a philosophy than a procedure. Individual programs must be tailored to the needs of the survey.

Most of the discussions on maintenance and the specific examples, which follow, although drawn from the Canadian Labour Force Survey, are relevant for many large scale continuous surveys.

2. THE MAINTENANCE PHILOSOPHY

Whenever large scale continuing surveys are planned and developed, significant effort and resources are devoted to implementing the best features that the available money can buy. This ranges from the original sample frame through data collection procedures to final estimation and data dissemination. Once the survey has become operational, especially in the case of surveys used to gather official government statistics, there is a need continually to ensure and to demonstrate the quality of the data and the efficiency of the survey methods and procedures. This ability to demonstrate the validity of the survey is required to allow for quality certification of data, to withstand criticism, to assist the organization in performing program quality audits and to encourage the development of quality improvement programs.

Perhaps the most important feature of this philosophy is to maintain programs which continue in an organized fashion to question operations, procedures and survey materials in order to verify their adequacy.

The anomaly of a good maintenance program is that the more effective it is in maintaining high quality in the survey process, the less recognition it may receive as a necessary program. A simple hypothetical example could be cited. Suppose in a personal interview survey the interviewers and supervisory staff all know that there is a continuous and prescribed program of reinterview. This mere presence of the reinterview program may result in a better standard of data collection. The more effective this program is, however, the less dramatic will be the results of the reinterview. When faced with the requirement to reduce costs it is very tempting for managers to assume that the interview process is properly conducted, as evidenced by the good reinterview reports, and therefore to cut back on the reinterview program.

The philosophy of a unified survey maintenance program approach implies a broad scope. Survey maintenance touches on every facet of a survey from the initial planning to the final dissemination of the survey data.

Many steps or stages can be identified in the process of a survey according to the degree of detail one wishes. For convenience, we will broadly divide the survey process into the following five stages:

- a) Survey Planning and Design
- b) Sample Selection and Control
- c) Data Collection
- d) Data Capture and Processing
- e) Estimation and Dissemination

All of the above can be recognized as common to any large scale survey. When the survey is continuous the planning and design stages are frequently replaced by periodic improvements and occasional redesigns and revisions.

3. ASPECTS OF MAINTENANCE

Various maintenance programs, to be discussed in detail later, are operative at each of these five stages of a survey. These programs can be classified as Measuring, Controlling and Adapting.

The distinction as to which aspect of maintenance a particular maintenance program falls under is not essential. This is so because often a quality measure, for example, can be used both for diagnostic purposes and as feed-back to operations. What is important is the recognition of the necessity of these aspects in a maintenance program.

Measuring

Maintenance programs, classified as Measuring, provide certain indicators of performance at various stages of the survey. The measures may be used as a guide to operational control or by data analysts to improve their insight into the reliability of the data and its suitability for particular purposes.

Measurement programs can be identified according to their use:

regulatory: those which serve to measure the conduct of specific aspects of the survey operations.

diagnostic: those which measure how well the survey functions in relation to the survey output.

metadata: measurements of aspects of the survey data used by analysts and managers to evaluate the data itself.

It is understood, of course, that the same measurement may serve more than one of these purposes.

Controlling

Maintenance programs used in controlling provide measures of survey performance for comparison against standards to identify aspects

requiring correction. This implies a feed-back mechanism which will adjust operations to ensure that these standards are met.

Adapting

These programs are essentially means of coping with change, whether due to changes of objectives or conditions or to the availability of new methods or equipment.

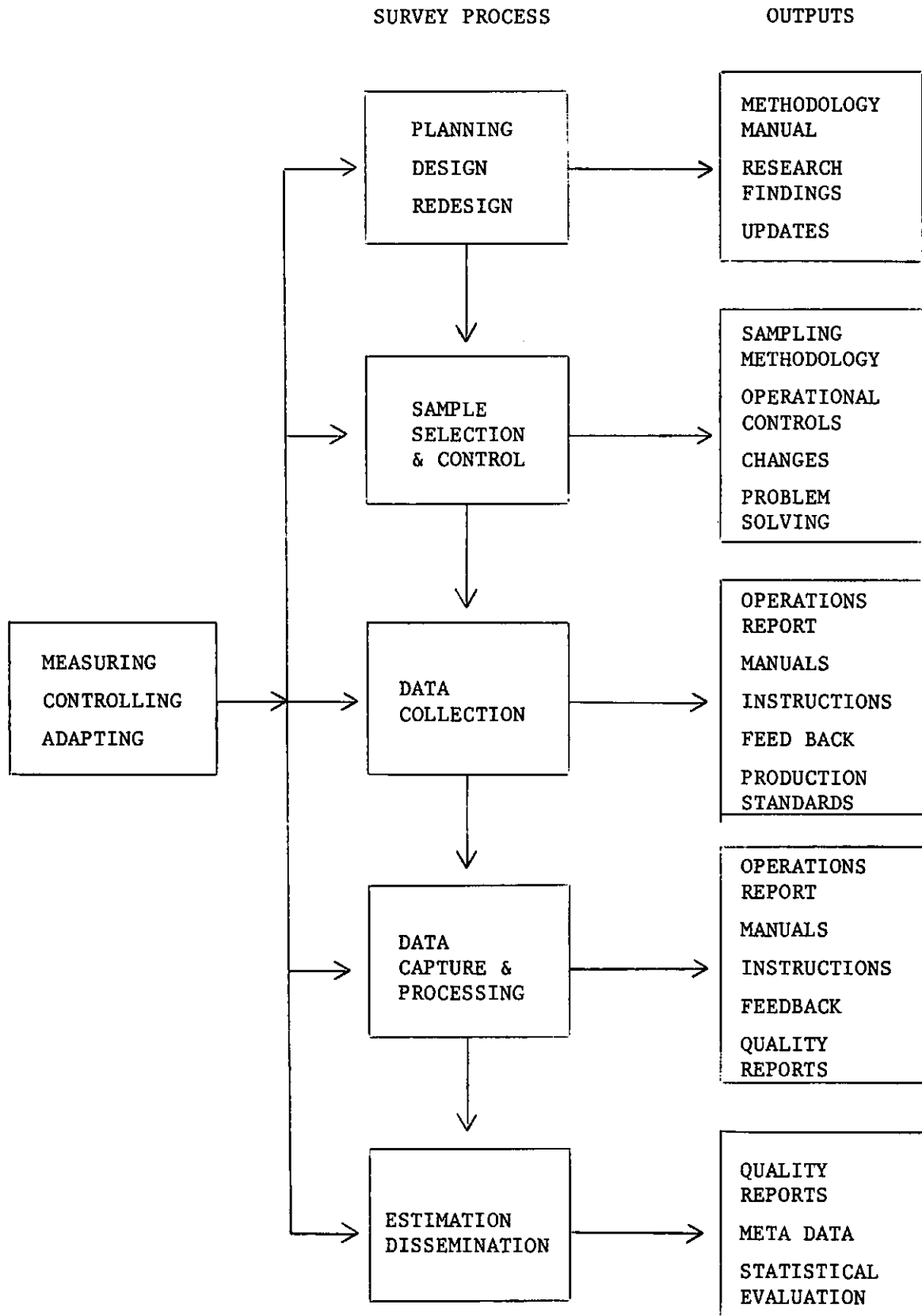
Examples of maintenance activity in the Canadian L.F.S. for the purpose of adapting to changed conditions or requirements:

- Parallel run. The running of two surveys in parallel, the old design and the new, to explain any differences and to link up the old and new time series.
- Sample size increase. Differential increase in sample size to improve provincial estimates.
- Stabilization program. To maintain a stable sample size while allowing for natural population growth.
- Sample Update. Partial redesign of new sample units to account for unequal growth.
- Sub-sampling in growth clusters. Reducing the interviewing burden on Field operations while allowing for growth.

Data from Maintenance Programs

Data from maintenance programs, whether in the form of quality measures, feed-back for remedial action or methods review and evaluation can be considered as outputs from the survey process. The following schematic diagram, although by no means complete, serves to illustrate how the maintenance program can influence all the stages of the survey process.

SURVEY MAINTENANCE



4. MAINTENANCE PROGRAMS AND THE SURVEY PROCESS

In order to control and minimize the impact of errors in large scale surveys, numerous quality control and evaluation programs are traditionally used. Most of these are familiar to survey methodologists and variations of them appear in almost any ongoing survey. The more obvious programs include tabulation and evaluation of non-response, undercoverage, cost of enumeration, observation, reinterview, variance/covariance, error rates and so on.

What we would like to do is demonstrate how survey maintenance impacts on every stage of the survey process. Examples are drawn from the Canadian Labour Force Survey.

a. Planning and Design

Obviously if a totally new survey is being planned and designed, there can be no maintenance program which affects the exercise directly. However, maintenance programs play two roles in the planning and design of a continuous survey. The first is in the fact that survey designers will draw on their own previous experience and that of others in the area of survey maintenance in order to evaluate possible features of the survey design. For example, the type of frame chosen will depend not only on what is available but also on what experience the designer has been exposed to in regard to frame maintenance.

The second way in which maintenance programs influence survey design is in periodic re-designs or programs of survey updating. For example, the LFS is normally redesigned every 10 years, shortly after the Decennial Census. The re-design after the 1971 Census was particularly extensive, incorporating many changes which were suggested based on the experience of maintenance on the older survey. Details

of the changes made are elaborated in [2]. It is expected that more changes, based on maintenance experience with the current survey, will be introduced in the 1981 Redesign.

No on-going survey regardless of how adequate its initial design was, can remain without change for an extended period of time without some deterioration. Populations of study change, concepts and objectives are modified, parameters which govern the sample selection become out of date and new procedures and technologies are developed. To prevent deterioration in the level of reliability of survey output, the survey maintenance function must evaluate these new factors constantly and implement required changes.

A specific example of this concerns the up-to-dateness of the LFS sample frame in large cities (SRU areas). After the 1976 Census it became possible to identify population growth in SRU areas from 1971 to 1976. The effect of this growth, which was not uniform even within individual SRU areas, was that size measures used in unequal probability of selection of sampling units became out of date, resulting in increased sampling variances. The changes made to the survey in the 1971 redesign allowed the development of methods to update the design in the SRU areas [3]. By using the information provided from the population comparisons, a special program was introduced to redesign specified sub-units within the SRU [4]. The impact of the re-specification of size measures can be seen in table 1. The effect of the program is to avoid increases in sampling variability due to highly clustered growth. This is particularly significant for estimates at the Census Metropolitan Area level.

TABLE 1

Increase in number of Random Groups due to SRU Update

December 1977 to March 1981

Province	No. of sub-units up-dated	Resulting no. of sub-units	Original no. of groups	New no. of groups
NFLD	4	4	42	60
PEI	5	5	90	112
NS	15	12	102	128
NB	12	13	144	214
QUE	26	32	162	252
ONT	46	53	300	402
MN	9	8	96	154
SASK	6	8	108	194
ALTA	23	39	276	518
BC	25	27	174	250
CANADA	170	204	1494	2284

Note: a sub-unit is a contiguous area stratum within a Self-Representing area comprising a number of Random Groups. A Random Group is a random collection of clusters (usually city blocks). The total number of sub-units in the initial design was 734.

b. Sample Selection and Control

Numerous activities are involved in the selection and control of a sample. In the case of a continuing survey, these relate to the maintenance of the sample frame and the selection and rotation of sample units at various stages.

In the LFS the second last stage of selection is a small well-defined area called a cluster. All of the dwellings located in the cluster are identified and listed in the field. The list is stored on a computerized data base in Ottawa and the final sample consists of a systematic sample of dwellings drawn by computer from the clusters. Comparisons of the expected number of dwellings based on the count when designing the area, to those actually listed frequently show significant differences. Most often the differences are due to construction or demolition of dwellings since the time that the cluster was first defined. In a number of cases, however, differences were due to incorrect listing or boundary errors. Such errors result in under or over sampling. To minimize the possibility of errors in listing clusters, a special program called "Cluster Yield Monitoring" was established.

Each month, Regional Offices are asked to identify reasons for significant differences between the design count of dwellings and the actual number listed for all newly introduced clusters. The timing of the program is such that field or design errors can frequently be corrected before interviewing in selected dwellings has begun. The following table illustrates some results of the program.

TABLE 2

Cluster Yield Monitoring Program
Number of Exception Clusters Checked (October 1979-December 1980)

<u>Type of discrepancy</u>	<u>No. of Clusters</u>
Valid differences	968
No correction necessary or no correction possible	244
Correctable errors	62
Not determined	24
<hr/>	
Total Exceptions	1298

This evaluation is based on a total of 11804 clusters entering the active sample during the period.

Another example of maintenance in the Sample Selection and Control stage is stabilization of the sample size. Because of the self-weighting feature of the LFS design and the fact that the Canadian population continues to grow, the sample size would normally continue to grow at the same rate. As a means of holding down survey costs an automated procedure known as Sample Size Stabilization has been developed to keep the sample size from growing [5]. Each month for a specific rotation group and type of area within a province, the number of dwellings selected is compared to a predetermined base figure. Should the number selected be less than or equal to the base, nothing further is done. However, should the number selected exceed the base then the excess of dwellings is systematically dropped from the set of selections. A compensating weight is calculated and applied to all the non-dropped dwellings.

Fluctuations in sample size, due to sampling variability among clusters and unequal growth rates, introduce slight changes in the actual number of dwellings selected each month. However, due to the stabilization program, the net sample size remains fairly stable. The following table illustrates the net sample reductions per month. It can be seen that although the net decrease due to stabilization varies somewhat from month to month, there is an increasing reduction through time compensating for the natural growth in the sample.

TABLE 3

SAMPLE SIZE STABILIZATION: OCTOBER 1979 TO MARCH 1981

SURVEY DATE	NUMBER OF DWELLINGS DROPPED
1079	521
1179	544
1279	519
0180	610
0280	544
0380	598
0480	643
0580	667
0680	548
0780	740
0880	677
0980	693
1080	745
1180	868
1280	755
0181	861
0281	847
0381	897

At the current rate this amounts to a direct saving in interviewing costs of around \$4,500 per month. There are also additional savings due to reduced processing and hiring and training of additional interviewers.

c. Data Collection

This phase of the survey process encompasses all collection activities and the materials used. In the case of the LFS, data is collected by personal and telephone interviews by a large staff of highly trained interviewers. The forms used by interviewers are preprinted for specific households and often the second and subsequent Interview show certain data reproduced from the month before. There are many opportunities in this stage of the survey process for

the effective use of maintenance programs to maintain quality and to improve methods and procedures. For example, tabulation and examination of edit changes can lead to improvements in training, changes in questionnaire design or changes in edit rules depending on the results of such analyses. This operation, in the LFS, is called the Field Edit Module and is maintained on a monthly basis.

Other significant modifications can derive from re-interview, observation and cost monitoring programs. It is essential to make results from such programs visible so that their importance can be recognized in order to ensure their continued support.

A phenomenon in large scale probability surveys is the problem of under-coverage. In the LFS the extent to which the survey underrepresents the population is called slippage. Slippage is the accumulated result of many things such as errors in clusters or cluster lists, missed dwellings, missed persons within dwellings, errors in coding and inaccurate population estimates to which the survey estimates are compared.

The continual monitoring of slippage is part of the maintenance program of the LFS. A significant change in the slippage rate triggers remedial action, for example: special list checks or special interviewer instructions.

Another problem in Data Collection is non-response. Continuous monitoring of response rates has shown a consistent trend toward higher non-response due to higher no one at home and temporary absent category during the summer months. In an effort to improve response a procedure known as "Post Survey Week Follow Up" has been developed [6]. In essence this is a special procedure of contacting, mostly by telephone, as many non-responding dwellings as possible one or two days after the normal survey period. Due to considerations such as timeliness, recall length and cost, the procedure is only used within specific restrictions and essentially during the summer months. On occasion, the procedure is also permitted where there are special situations where non-response is expected to be exceptionally high. An example of the sort of improvement that is obtained is shown in the following, Table 4.

TABLE 4

POST SURVEY WEEK FOLLOW-UP OTTAWA R. O.

JULY 1978

Type of Non-Response	Number			Reduction in Non-response Rate (%)
	At end of Survey Week	Followed Up	Successful Follow-Up	
T	160	117	43	1.61
N	46	36	11	0.47
K	4	2	2	0.04
TOTAL TOTAL	210	155	55	2.12

T = The household was temporarily absent for the entire week.

N = The occupants could not be contacted after several attempts.

K = Circumstances within the household, e.g. sickness, language problems.

d. Data Capture and Processing

The next step of the survey process consists of data capture and processing. In any large scale survey, the survey data are transformed into machine readable form; the data are edited and coded and imputations are made. In the LFS, in order to ensure the accuracy of the data capture, a quality control program using complete and sample verification is maintained. The program is designed to ensure that data entry errors do not exceed 3%. Continued monitoring of the program results in very high levels of data capture accuracy and ensures the efficiency of data entry operators.

Even when high levels of data capture accuracy are maintained, the data are still subject to errors which may have been introduced during the field collection. These would represent enumerator or respondent errors and they are detected in the edit process. In the LFS there is a program to identify all data fields where changes have been made during editing. The program is called the Field Edit Module and, as has been mentioned earlier, is used as a feed-back to interviewers, questionnaire designers and editors.

The FEM does not include all errors that might have been made but only those where the data entered (or omitted) causes an edit failure. Nevertheless the FEM results have been shown to be a very good measure of the relative number of errors made. The error rates generated by the FEM are a sensitive indicator of the quality of interviewers' work and also a measure of the awareness of field staff of survey requirements. Since the implementation of the program, there has been steady improvement in the error rates to a currently stable level. Even this stable level shows some improvement, however, each time efforts are made to emphasize accuracy in completing the questionnaire. For example, each time special training sessions for field staff focus on improving accuracy, there is a corresponding improvement in error rates for several occasions immediately after the sessions.

In addition to the FEM analysis of edit failures, the editing section monitors the number of error-containing records each month. Results of this monitoring are regularly discussed with field staff to keep them aware of the need to minimize these errors. In cases where error rates show abnormal increase, there is feed-back to individual Regional Offices with identification of the specific types of errors and suggestions for eliminating them in future.

Table 5 shows how the maintenance of this program has contributed to reducing the error rates over time for the household record (F03) and individual questionnaire (F05).

TABLE 5
EDIT ERROR RATES BY FORM TYPE
1977 - 1980

F03	JAN.	FEB.	MAR.	APR.	MAY	JUNE	JULY	AUG.	SEP.	OCT.	NOV.	DEC
1977	5.8	4.7	4.8	5.2	5.1	5.3	5.3	5.4	5.4	5.1	4.9	4.6
1978	4.8	4.2	4.0	3.4	3.6	3.3	3.1	3.0	3.1	2.9	2.8	2.9
1979	2.3	2.3	2.3	2.6	2.3	2.6	2.3	2.5	2.3	1.9	2.1	2.2
1980	1.8	1.9	1.8	1.9	1.9	1.9	2.1	1.8	N/A	1.9	1.8	1.9

F05	JAN.	FEB.	MAR.	APR.	MAY	JUNE	JULY	AUG.	SEP.	OCT.	NOV.	DEC.
1977	20.3	18.9	17.7	17.7	18.0	15.6	16.7	15.6	15.4	16.4	15.2	13.6
1978	14.4	13.8	13.5	14.5	14.3	11.9	12.6	11.6	11.3	12.7	11.1	9.8
1979	10.3	9.7	9.8	7.7	9.9	9.7	9.6	8.9	8.4	7.5	8.5	8.4
1980	7.7	7.4	7.1	8.6	8.0	8.0	8.1	7.1	N/A	8.2	7.6	6.4

e. Estimation and Dissemination

In this final phase of the survey process, the estimates are published and distributed to the various users. In a sense the data leave the hands of the survey methodologists and enter the domain of the data analysts and policy makers.

Survey data, especially those from large scale continuing surveys, are usually collected for two reasons. The first is to document and

chart the phenomenon of interest. Thus, in the LFS, the survey data serve to provide a comprehensive summary statement about the labour force activity of the Canadian population. The second reason is for policy makers to combine data from various sources to evaluate existing social policy, to predict trends and to devise new policy aimed at improving the social situation.

It is not immediately obvious how maintenance programs can affect this phase of the survey process. Estimation procedures are usually fixed in that they depend on the probability design of the survey. Changes are only made if the probabilities of selection change. We have an example in the LFS. As mentioned earlier, in an effort to put a limit to natural sample size growth, a procedure of "stabilization" was implemented. The effect was the requirement to add a special weight to compensate for the sample reduction. This weight was incorporated into the estimation process.

Other changes too are being incorporated which must be considered part of the regular maintenance function. A program is currently under way to expand from two-digit to three-digit occupational codes to respond to requests from users for more detail. Such a change will not be implemented without careful assessment of the impact on editing and coding operations, data processing, tabulation and printing and finally estimation of data reliability.

By carefully monitoring the data processing operations, it has been possible to improve head office processing schedules to such a degree that the press release date for LFS data has been advanced. It has moved forward four days from the Tuesday at the start of the third week after survey week to the Friday at the end of the second week.

Perhaps the most neglected aspect of survey maintenance and quality evaluation in general is its impact on the uses to which data is put after publication. Too frequently implicit assumptions are made to the effect that the published data is "true" without considering outside factors which should temper any analysis. Most data

analysts and users recognize the existence and significance of sampling errors, but may be less appreciative of the uncertainties in the data caused by non-sampling errors and non-response (missing data).

Maintenance programs are effective in reducing not-sampling errors and non-response (missing data). They also provide valuable information (metadata) which should be considered by the analyst in using the data. Difficulties in data estimation and evaluation caused by non-sampling errors and non-response are most difficult to deal with. They must then be controlled by programs of prevention and this in addition to maintaining operations is the purpose of maintenance programs.

5. CONCLUSION

This has been a rather short and not very detailed overview of some of the maintenance programs of the LFS. Particular attention has been given to some of the less well known programs in an effort to demonstrate how fundamental they can be and how they form a part of overall survey maintenance.

We hope the foregoing makes the case for the pervasiveness and importance of survey maintenance and its contribution to better and more useable statistics. We recognize that there are, however, substantial costs involved and methods need to be developed to produce dynamic indicators similar to cost-variance studies used in sample design. A start in this direction has been made by Platek and Singh [1].

The relative value and cost of the various procedures should be used to control the scope, incidence and intensity of the components of the survey maintenance program.

RESUME

La coordination est un aspect des enquêtes auquel on n'accorde pas toujours suffisamment d'attention.

Les auteurs analysent l'envergure et l'importance de la coordination des enquêtes et préconisent une approche méthodologique plus scientifique. Des applications pratiques à diverses étapes des enquêtes sont illustrées par des exemples tirés de l'Enquête sur la population active du Canada.

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IMPUTATION IN SURVEYS : COPING WITH REALITY¹I.G. Sande²

In surveys a response may be incomplete or some items may be inconsistent or, as in the case of two-phase sampling, items may be unavailable. In these cases it may be expedient to impute values for the missing items. While imputation is not a particularly good solution to any specific estimation problem, it does permit the production of arbitrary estimates in a consistent way.

The survey statistician may have to cope with a mixture of numerical and categorical items, subject to a variety of constraints. He should evaluate his technique, especially with respect to bias. He should make sure that imputed items are clearly identified and summary reports produced.

A variety of imputation techniques in current use is described and discussed, with particular reference to the practical problems involved.

1. INTRODUCTION

Everyone who has been involved in surveys knows that life would be very easy if only the respondent had read the textbook. If he had, he would know that he is allowed to respond correctly and completely, or not to respond at all. He is not allowed to respond incorrectly or incompletely. Unfortunately, the respondent has not read the textbook. Furthermore, if you call him back to correct the data or fill in missing information, he may not be very co-operative. More often than not, the cost of calling back is simply too high to be carried out generally.

¹ Presented at the annual meeting of the Statistical Society of Canada, Halifax, 23-26 May, 1981.

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So reality might look like this:

TABLE 1

IMPORTANT CANADIAN SURVEY

Record No	Identification Classification	Weight	Variables				
			1	2	3	4	5
1	X	w_1	A	a	y	3.1	4.3
2	X	w_2	A	a	z	4.6	2.8
3	X	w_3	A	b	y	-	1.1
4	X	w_4	B	b	z	2.3	4.6
5	X	w_5	B	c	y	4.9	2.3
6	X	w_6	B	b	-	3.2	3.6
7	X	w_7	C	-	x	3.0	-
8	X	w_8	C	-	y	-	1.2
9	X	w_9	C	a	-	0.0	2.4
10	X	w_{10}	-	b	y	-	1.4

Edits: $A \wedge a \Rightarrow$ Not x.

$B \wedge b \Rightarrow$ Not y.

$\text{Var } 4 + \text{Var } 5 \leq 10.$

$\text{Var } 4 \geq 0, \text{Var } 5 \geq 0.$

This survey has both categorical and numeric items, and there are three constraints (edits) on the items which must be satisfied. We notice that of 10 records, four (1, 2, 4, 5) are complete. If we look hard, we might also notice that the 'missings' are informative: a low value of Variable 5 is associated with a missing Variable 4.

Our primary problem is that we have to produce tabulations of population estimates, e.g. Variable 1 x Variable 2 x Classification Variables, or Variable 4 x Classification variables. Although we might be able to write down all the estimates we think we have a need for in our publication, we know that after the publication comes out, we are going to get a large number of requests for tabulations and estimates which we have not anticipated.

How, then, are we to deal with the partial non-response? The possibilities are:

- (i) Ignore all the records with missing values. This may result in loss of a great deal of data, since many records may be affected. Furthermore, 'missings' are seldom random and the procedure would almost certainly lead to biased estimates.
- (ii) Publish "unknowns" as a category. This is a little better than (i); but still ignores the partial information about the missing value which may be available in the other variables. Frequently, the users of the data will make adjustments for the "unknown" categories without being able to look at the microdata and with little knowledge of the data collection process.
- (iii) Adjust (reweight) each table or estimate, ignoring the missings in each case. This is a variation of (i) which may give rise to inconsistent tables in the sense that no complete data set corresponds to the set of estimates because of the constraints on the data.

- (iv) Fill in the blanks in each record with plausible and consistent values. This is called imputation.

To sum up, partial non-response arises in two ways:

- (i) A record (i.e. the total response for a single survey unit) contains one or more missing values because (after all possible checking and follow-up) the data are unavailable.
- (ii) A record is inconsistent in the sense that its component items do not satisfy natural or reasonable constraints (known as edits) and one or more items are designated unacceptable (and therefore are artificially 'missing').

To cope with the "missing value" problem in an expeditious manner, values are frequently imputed for the missing items so that the data set is "completed".

The estimation of individual values in a data set is not a new problem. It is the direct descendant of the "missing observation" problem in ANOVA and the "incomplete data" problem in multivariate analysis. However, though imputation is not an optimal solution to the "missing value" problem in surveys when any particular estimates are considered, it may just be the least bad of the feasible solutions for general purposes.

2. THE GENERAL IMPUTATION PROBLEM

What are the "facts of life" facing the unwilling imputer? No matter what method of imputation he opts for, the following problems must be dealt with:

(i) The close relationship between editing and imputation.

- (a) If a record fails an edit, it is not always obvious which fields are faulty, but some basis must be established for deciding which fields to change. Does one change all the fields involved in a failed edit? Some of them may be involved in other edits which do not fail. Does one change the least number of items, as recommended by Fellegi and Holt [9], or adopt a policy of "least change", whatever that means? Or does one adopt the "principle of expedience" : deleting that configuration which makes imputation easy?

These are non-trivial problems. The mathematical analysis of edits and the identification of fields to be changed when several edits have been failed, is a very subtle problem. Fellegi and Holt did the first systematic work on categorical or coded data and their methods have been implemented at Statistics Canada and used (with modifications, see [11]) in the Census of Population. The parallel work for numerical data with linear edits has been carried out by Gordon Sande at Statistics Canada using optimization techniques [20] and the development of techniques for the combined numerical and categorical data problem is seen as feasible.

- (b) When it has been decided which fields must be imputed (because they are missing or must be changed) it is obvious that the imputed data must satisfy the edits, i.e. the completed record must be consistent. This requirement often eliminates the mathematically elegant imputation schemes and reduces the mathematical tractability of the problem to zero. Since complex edits make the imputation procedure hard, the theoretical analysis of such procedures is virtually impossible. Therefore edits are usually ignored in theoretical work on the properties of imputation techniques.

- (ii) The marginal and joint distributions of responses are almost certainly different from those of the underlying population. In the case of numeric data, such distributions are unlikely to be normal. Transformations to normality (or less pronounced skewness) result in transformations of the edits which makes them more difficult to deal with.
- (iii) The pattern of missing fields varies from record to record. In an n -field record (excluding the identifiers and classification variables), there are $2^n - 1$ possible patterns of fields to impute. Some imputation schemes (I do not know if any have been seriously implemented) seek to specify a separate imputation procedure for each pattern; but if n is large, this idea soon gets out of hand.
- (iv) The imputer does not usually have much time to fiddle with the data after they have come in. Most survey data should be processed promptly to be useful and in some cases (such as many at Statistics Canada) the time constraints are severe. Therefore the method of imputation should be precisely specified before the processing begins. Furthermore, the statistician usually has little, if any, test data to work on before the data collection begins. Historic data cannot always be trusted to look like current data in any but the most general respects. For example we may believe that X is proportional to Y on the basis of historic data; but the proportion $\frac{X}{Y}$ may change from year to year. On the other hand, the circumstances governing the joint occurrence or non-occurrence of X and Y may be similar over time, a fact which can be exploited in testing imputation procedures.
- (v) Imputation does not solve any specific estimation problem more satisfactorily than classical estimation techniques for incomplete data, and it may do a lot worse. The trouble is that if one can optimally estimate a particular θ using some (correct) distributional assumptions and a (correct) model, one hasn't solved the problem for θ . One has to start again. If one combines θ and θ ,

one may have an unwieldy problem. By the time one has optimally estimated all the parameters one can think of, one may have a set of estimates which is not consistent with any possible data set. And then someone may find a ψ to be estimated. By imputing a consistent value for each missing item one can estimate any of the usual population parameters (means, totals, ratios, differences, proportions, correlations) very easily, although possibly with no guaranteed precision.

- (vi) It is generally hard to know how to estimate the variance of estimates when some data is imputed. If the amount of imputed data is very small, the usual estimates will do. In some circumstances, mathematical or empirical studies in a vaguely related situation may be available.
- (vii) The imputer is faced with ethical problems if the microdata are ever going to be given out. At the very least, he must plan to identify the imputed items on all copies of the data and publish the proportions of imputations in each field as part of a discussion of data quality when the primary results are published. Alternatively, he may choose to give out edited, but unimputed, versions of the data set. In this case, the secondary users may do their own imputations and get results which are inconsistent with each other and the original.

Which data set should be analyzed? The question really is: What do you mean by analysis? If one wants to explore relationships between variables, the use of imputed data could be prejudicial, not to mention misleading. For simple estimation purposes, as we have pointed out, the imputed set reduces the headache. And we could argue that if the data are so bad that the presence of imputed data could influence the analysis significantly, then the data are not worth analyzing.

After considering these problems we may conclude that the imputer needs a procedure which

- (i) will impute plausibly and consistently provided only that the non-missing data satisfy the edits;
- (ii) will preserve the underlying distributions in the data or, at least, reduce the response bias and preserve the relationships between items as far as possible;
- (iii) will work for (almost) any pattern of missing items;
- (iv) can be set up and tested ahead of time;
- (v) can be evaluated in terms of data quality and impact on precision of the estimates.

Particular techniques of imputation vary in their ability to meet these requirements.

3. METHODS OF IMPUTATION

Planning ahead is to be recommended. If one can guess the fields most likely to cause problems, it will pay to pick up a correlated variable on the questionnaire or from auxiliary sources. For example, it may be hard to get information about household income, but easy to get an estimate of square feet of living space or some other correlate of income. The store manager may not want to disclose his gross income; but one can count the number of cash registers. How this information is used depends on the circumstances.

Techniques of imputation vary from naive to sophisticated.

- (i) Use of ad-hoc values. Each case may be treated differently in a manual procedure, or a few rules of thumb are formulated on the basis of 'experience' and hunches, and often without the encumbrance of real facts. These are used to fill in the blanks.

For example, in a business survey we may have the rule for imputing the value of closing inventory: if gross income (GI) is less than or equal to \$25,000, set closing inventory (CI) to 0; if GI is greater than \$25,000, set CI equal to 5% of GI minus net income or 0, whichever is larger. In many ways this rule appears quite reasonable, provided GI and net income are always available, especially if the 5% came from last year's survey. If it is dirty it is at least quick and not too damaging if only a small percentage of the records are affected.

Rules of this type can be formulated to force compliance with the edits. They are also compatible with the simplest of data processing systems. However, they are subjective and may not reflect reality. The effects on the underlying distributions are often unpredictable and non-response bias is not necessarily reduced. Evaluation may be impossible.

- (ii) Post-stratify and use the post-stratum marginal mean or another typical value (e.g. the mode in the case of a categorical variable), making sure that there are sufficient data in each post-stratum. In the numeric case, this is equivalent to item by item reweighting.

In the closing inventory example of (i), we might post-stratify by gross income, net income, industry, region, etc. If we create too fine a grid or too many data are missing, some collapsing may be necessary to ensure that there are enough good data in each cell (see [8]).

This technique may run into trouble with the edits. If this seems likely, some modification may be in order (such as letting the edits define the post-strata). Like the method of ad-hoc values, it is very simple, if it works; but will create spikes in the marginal distributions and may be biased. However, in the numeric case variance estimates are generally available.

- (iii) Model the relationships between the variables. A popular idea has been to use the conditional mean given the items present, modified to account for the information in the incomplete records assuming normality, or some generalization of this idea (e.g. [3], [7], [12]). However, normality is not usually a plausible assumption and it does not take the edit structure into account. I have not seen any theory worked out for non-normal cases and I am not aware of any application to missing survey data except for test purposes (e.g. Huddleston and Hocking in [1], pp. 88-93).

In one survey at Statistics Canada, about 160 items are collected (from administrative documents) for a fairly small sample of businesses and 5 major items are collected from other sources for the entire population. For various reasons (mainly the ease of arbitrary tabulation of estimates) it is desired to impute the 160 items for the non-sampled businesses. A ratio-type imputation is used, after stratification by size and industry:

$$\hat{x}_i = \frac{\sum_P x_j}{\sum_P y_j} y_i$$

where x is related to major item Y and the i th record requires imputation. P is the sample of complete records with all 160 items present. Because of the structure of the data, the edits are automatically satisfied; but the imputations do not reflect the real structure of the data which have a lot of zero values. In other words, the imputed records are not realistic and the marginal

distributions are distorted. On the other hand, the principal estimates (which are just ratio estimates) are quite acceptable and permit variance estimation. In this case the ratio-type imputation is used because it is easy and convenient, not because it is a good model. The effort that would go into fitting a model would be prodigious and one may well never achieve a good fit.

Thus modelling is an elegant solution which will probably reduce bias. On the other hand achieving a good fit may require a great deal of effort or one may have to tolerate a bad fit, and there may be problems with edits. Furthermore, one may find that the assumed model becomes "built into" the data and may be recovered by other researchers later, unless steps are specifically taken to prevent this.

- (iv) Use of historic data, such as last month's or last year's response for the same unit, if available. This technique is in common use in monthly surveys where the same units are surveyed in consecutive months, for variables which are not expected to change often. Of course, the assumption is that one did get a response for the particular item at some stage and when one has carried a value forward for several months in a row, one perhaps ought to do some investigation into what is going on.
- (v) Use a proxy data from another source. This means that another file, perhaps of administrative data such as medical or tax records, is available with the unique identifiers required for matching to the survey file and that this file includes an equivalent item which can be used as a proxy for the missing survey item (e.g. [10]).

If an exact match is not available (possibly because the identifiers have been removed for reasons of confidentiality), one may be content with a statistical match on classification fields such as age, sex,

and place of birth. For example, one may use last year's sample survey as a source of data for statistical matching and imputation for this year's survey.

Most statistical matching is used for linking different data files to extend data sets (see e.g. Radner in [1], pp. 108-113). The idea of statistical matching is closely related to the hot deck and nearest neighbour techniques discussed in (vi) and (vii) below.

- (vi) Use of the current survey data as a source of matched individual data records from which one (the donor) is selected at random to supply values for missing items in a particular deficient record. Procedures of this type are often called hot deck procedures; but there is no agreement on the definition of hot deck procedures in the literature. I will take it to mean an imputation procedure which uses records from the current survey to supply missing values and involves a random or pseudo-random choice. There seem to be two main variants currently in use, both directed mainly at categorical data:
 - (a) The sequential hot deck, used in the U.S., for example, in the Current Population Survey and the Census of Population. Here the data are processed one record at a time. To impute a field or group of fields A, a cross-classification (matrix) of several other related fields (B,C,D...) is defined. For each cell in this classification, that value of A is retained which occurred in the last record processed with the corresponding values of B,C,D.... . Thus, as the file is processed, the values in the individual cells of the B,C,D... matrix change. When a record lacking a value for A occurs, it receives the value currently in the cell of the matrix which matches its own values of B,C,D... If two such records (missing A, but with the same values of B,C,D...) occur consecutively, the same value of A will be imputed in each case.

The ordering of the file may not be random, so that the record used as a donor is not chosen at random. In fact, it may not be advantageous to randomize the file, thereby exploiting the correlations between nearby records to improve the imputation.

The matching fields (and therefore the imputation matrix) vary with the fields to be imputed, so that many matrices must be maintained. In those cases where imputation of a single field might result in an edit failure after imputation, a set of related fields is deleted and imputed together.

Because different fields are imputed from different imputation matrices, several donors may be involved in completing a single deficient record and this may be a source of some concern.

Each imputation matrix must be initialized, using historic data or ad-hoc values. On the other hand, the imputation can be done at one pass and is not difficult computationally.

- (b) The random choice procedure used by the Canadian Census and Labour Force Survey. Here an imputation matrix is not maintained; but the set of records with the required values in the matching fields is identified and the donor is chosen at random from these to supply the missing items to the deficient record.

In the Canadian Census, an attempt is made to impute all missing items on a deficient record using a single donor. If this fails, a field-by-field hot deck is tried, in which several donors may be involved [11].

The choice of matching fields in both sequential and random choice procedures must be made considering likely sources of variation, linkage through edits and the number of complete or eligible records available as potential donors in each cell. If too many fields are used for matching, the number of

potential donors may be too small; if too few fields are used for matching, there is a risk of a poor match or edit failure in the imputed record.

With hot deck methods, the variance of the estimates in simple cases is known to be larger than the variance of the usual expansion estimates of means and totals (e.g. [2]). However, there may be a reduction in bias.

- (vii) Use of the current survey data as a source of individual data records with similar characteristics to supply values for missing items. Unlike the hot deck procedures in (vi), these procedures are appropriate for use with numeric data. I shall call them nearest neighbour procedures rather than hot deck procedures because the value in the matching fields must be similar (not the same) and the element of randomness in the choice of donor may be absent.

The hot deck procedures discussed in (vi) run into trouble when numeric fields are linked by edit constraints and matching must be done on them. Occasionally the problem can be dealt with by splitting the range of the variable, e.g. age, into intervals and coding the intervals; but consider the problem of imputing the age of a child from the age of a parent.

For purely numeric data with linear edits, a prototype system at Statistics Canada locates the m "nearest" complete records to a particular deficient record. An attempt to complete the deficient record using fields from the nearest of the m neighbours is made. If the tentatively completed recipient record passes the edits, the imputation is complete. Otherwise, the next nearest neighbour is tried, and so on. If none of the m neighbours will do, the imputation fails and further processing is required [20].

In this type of imputation, the use of suitable data transformations can make the imputation proceed more smoothly. It also helps to insert additional edits so that extreme observations are not admitted as donors (special arrangements can be made for them).

The method requires an efficient search algorithm; but the choice of distance function is not crucial and one which is simple computationally is advisable.

It is possible that particular records will be used as donors much more often than others. Another nearest neighbour type of imputation system developed at Statistics Canada for the imputation of mixed numeric and categorical data, incorporates the number of times a particular record has been used as a donor into the distance function, so that the distance increases with the number of previous donations [5].

Nearest neighbour procedures can be converted into hot deck procedures by choosing the donor record at random from m nearest neighbours instead of taking the nearest satisfactory record. Both types of procedure can be regarded as a form of non-parametric regression.

With numeric matching, the variance would be hard to calculate since the match is deterministic given the data.

- (viii) Use of hybrid methods. In fact, to my knowledge, no complex imputation problem is handled by a single imputation procedure. Some ad hoc imputations are usually combined with more sophisticated methods so that the job gets done expediently. Typically, some items are imputed one way and others another way and then some cleaning up is done. In one case [22], the occurrence of zeros in a particular variable was modelled. Those missing cases not imputed as zero through the model were imputed by hot deck.

Various devices may be employed to expedite the imputation. Among these are:

- (i) Formulation of the edit procedures to reduce the number of possible missing configurations. More fields than necessary

are deleted, but consistent imputation is easier. For example, if the edit is $A + B + C \leq X$, failure of the edit may result in the deletion of all fields A,B,C and X or just A,B,C rather than only one of these fields. Obviously this is an option to be used with extreme caution since information is destroyed.

- (ii) Transformation of the data. It is sometimes more natural to impute proportions than absolute numbers and often the edits transform neatly to permit this. For the purpose of numerical hot decks or nearest neighbour procedures, the distance function is often better formulated in terms of transformed variables than the originals which may be very skew. In terms of the original variables, "nearness" in one part of the space may be quite different from "nearness" in another.
- (iii) Dividing the record into segments and imputing one segment at a time. Each pass is conditional on the preceding ones being complete. This makes the imputation task less formidable and, in those cases where matching is required, allows different appropriate matching procedures to be used at each stage [5]. A related device is to attempt a global imputation first and, where this fails, to try a stage by stage imputation [11]. If all else fails, we can end with an ad-hoc procedure to tie up the loose ends.

IV EVALUATION OF IMPUTATION PROCEDURES

In evaluating an imputation procedure, the relevant concerns are bias and variance of the estimates (means, ratios, etc.) not the ability of an imputation procedure to guess missing values of individual items correctly.

The theoretical treatment of imputation procedures is generally confined to fairly simple cases, ignoring edit constraints (e.g. Bailer and Bailer in [2] and [15], pp. 422-447; Schaible in [15], pp. 170-187; Platek and Gray, [17]; Szameitat and Zindler, [23]). Empirical work deals either with the comparison of different imputation methods (e.g. [6], [8], [22]); or with the performance of a particular technique under different conditions ([5], [10]). Various edit and imputation strategies are compared by Nordbotten in [13]. Other studies simply attempt to examine the impact of imputation [14], or summarise current practice [18].

Since the scope for theoretical work is limited to fairly simple data and imputation procedures, it seems that, in general, imputation procedures must be evaluated by simulation. This usually means selection or creation of a clean data set (no items missing) to act as a population, the creation of artificial "missings" in biased and unbiased modes and at different rates, and studying the performance of the imputation process over several replicates of each case. The quality (bias, variance), in relationship to the rate and bias of "missings", of the resulting estimates may then be assessed. Particular imputation procedures will allow variants of this basic recipe: for example, in a sequential hot deck, replicates may be generated by re-ordering the data set rather than by regenerating a complete set of "missings" as required by nearest neighbour techniques.

Rubin [19] advocates the routine production of several sets of imputed values under different models or sets of assumptions, as part of the regular data processing. This leads to estimates of the "imputation error", that part of the error due to imputation, in the actual data and the effects of different models can be studied. The method which is applicable to only a limited variety of imputation techniques, including hot deck, has been used experimentally.

In general, the estimation of the "imputation error" under normal production conditions will be very difficult; but it is better to use

approximations obtained from a simulation study than nothing at all.

Whatever the method of imputation, the actual imputation process should be carefully monitored. In the simplest cases this means recording data about the missing items which were subsequently imputed : the number of records in which any imputation is made, the number requiring one (two, three, etc.) item(s) to be imputed, the number of records missing specific variables (or possibly combinations of variables), statistics breaking down the imputations into those due to item non-response and those due to edit failure. For imputations made using a decision tree (the imputation being conditional on other fields and the relationships between them), the number of imputations made in each branch of the tree should be recorded. For a nearest neighbour procedure one also wants to know, for example, how many times each record was used as a donor, which donor was involved in a particular imputation, how many attempts were required to complete a record and what the value of the distance function was. And of course one wants a listing of any records failing to be completed. (It is also equally important to monitor the editing process which precedes the imputation).

V. CONCLUSION

This is not the first paper on imputation in surveys (e.g. [4], [16], [18], [23]) nor will it be the last. The activity has been going on for a long time under such disguises as "automatic error correction" and used to be considered as part of data processing rather than statistical methodology. Now the survey statisticians are getting involved and the subject is being discussed in the literature and at meetings. Predictably, the open discussion of imputation has dismayed some of the more classical statisticians.

Reality does not consist of the data at the end of the chapter (like the iris data) and normal distributions: it consists of 20,000 long

forms filled out by 20,000 businessmen with other things on their minds, or several million census returns filled out by individuals who want to get back to the newspaper or the TV. These people want to be co-operative; but if the information requested isn't handy or has been forgotten, they omit the question or make up a response, and they also make mistakes. The survey people have to extract as much sense as possible from the results and they try to do a respectable and ethical job.

Reality also consists of the almost unlimited and unpredictable demands which are made on some data sets. These should be satisfied in a consistent way. And reality is the fact that even the simplest survey, properly run, is a complex operation and one does not want to increase the complexity any more than one has to.

I believe that the real problem of imputation is the interaction with editing. Very little of the literature deals with this problem. Szameitat and Zindler [23] and Nordbotten [13] touch on the subject. The "Canadian School" led by Fellegi and Holt ([9]; [5], [11], [20] and even [21]) discuss it (with little empirical work), while, by and large other writers do not, preferring to simplify the problem so that it is amenable to mathematical analysis or empirical study. This does not suggest to me that the effort is wasted, but that the problem of studying the properties of imputation procedures under realistic conditions is a very difficult one. And one must admit that there are some one-question surveys to which the available results might be applicable.

I hope that we will see more empirical work on data sets with complex edit constraints. We need to know much more about how imputation procedures compare with each other and we need guidance about how to optimize the performance of a specific type of procedures. So far, we have only scratched the surface.

RESUME

Dans les enquêtes, il arrive qu'une réponse soit incomplète ou que certains éléments soient incompatibles ou encore, que des éléments puissent manquer, comme dans le cas de l'échantillonnage à deux phases. Il peut alors être utile d'imputer des valeurs aux éléments manquants. Même si cette méthode n'offre pas une solution particulièrement bonne à un problème d'estimation donné, elle permet cependant la production d'estimations arbitraires d'une façon cohérente.

Le statisticien enquêteur sera peut-être aux prises avec un mélange d'éléments numériques et qualitatives qui seront assujettis à une variété de contraintes. Il doit évaluer sa technique, en particulier en ce qui concerne le biais, et veiller à ce que les éléments imputés soient nettement identifiés et que des rapports sommaires soient produits.

L'auteur décrit diverses techniques d'imputation utilisées à l'heure actuelle et elle accorde une attention particulière aux problèmes pratiques en cause.

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REDESIGNING CONTINUOUS SURVEYS IN A CHANGING ENVIRONMENT

M.P. Singh and J.D. Drew¹

Survey organizations undertake periodic redesigns of continuous surveys. Reasons for such redesigns related to changes in information needs to be satisfied by the survey and changes in public awareness and attitudes towards surveys are discussed in the context of the redesign of the Canadian Labour Force Survey following the 1981 Census. In particular, the importance of close dialogue between users of the survey data and design statisticians at the early stages of the redesign process in order to establish survey objectives is stressed.

1. INTRODUCTION

Data from decennial censuses in addition to serving the need of their primary users, serve as one of the frequently used tools in designing new surveys and by far the most important tool for redesigning (designing) large scale continuous surveys of population and housing. For instance, the Canadian Labour Force Survey (CLFS), a monthly survey of 55,000 households across Canada [12], has been redesigned following each decennial Census. Two of the primary reasons for these post-censal redesigns are to update the sample design to reflect changes in population characteristics and boundaries of Census units, and to incorporate improved methodologies such as sample selection and estimation procedures. Also the redesigns provide a unique opportunity to respond to a) changes in information needs to be

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satisfied by the survey, and b) changes in public awareness and attitudes towards surveys and other factors affecting data collection. In this paper, the discussions are focused on items a) and b) in the context of the redesign of the CLFS following the 1981 Census. They may be found relevant for other similar surveys.

With regard to information needs, it should be mentioned that at the time of the revision of the CLFS carried out during the 1970's [10], a great deal of emphasis was placed on more data and increased reliability of data at the provincial level. However, new and important uses of CLFS data have emerged since that time, such as the legislated use of CLFS estimates in determining the eligibility for benefits under the Unemployment Insurance Program, administered by Employment and Immigration Canada. The redesign currently being planned for will represent the first occasion to consider such new data requirements. Along with the uses of labour force data, uses of the Labour Force Survey vehicle itself for obtaining other socio-economic data have greatly increased in recent years. After briefly discussing the process of identifying the survey objectives in general terms, the discussion in section 2 will cover the following three specific situations for meeting data demands:

- i) Improved monthly data at sub-provincial levels through reallocation of sample within the provinces.
- ii) Reliable data on quarterly and annual basis at smaller levels of aggregations through alternate rotation patterns.
- iii) Increased demand for socio-economic data vis-à-vis current survey capacity.

The third section of the paper discusses the impact of the data collection method-item (b)- on development of the design of the survey, and emphasizes the importance of timely decisions on the procedure to be

adopted. The seventies have witnessed significant changes in the general conditions in which surveys have been undertaken, including increased respondent resistance and sensitivity to response burden, emphasis on voluntary surveys, increased incidence of proxy response, relatively higher travel costs, and as a result increased and more refined techniques of using telephone in conducting surveys, mail surveys, etc. In such an environment, it is essential for a continuous survey to maintain a capacity for testing various new options (or to study the effects of changing conditions) with the view to developing and maintaining a cost-efficient design. Basic requirements for such a capacity together with the planning for a telephone experiment and its implications on the current design are discussed in this section.

Lastly, some projects related to updating of the sample and development of improved methodologies [16] are highlighted in the final section.

It should be noted that research into the areas of alternative sample allocations and rotation patterns discussed in sections 2.2 and 2.3 are in very initial stages. For that reason, the tables presented are the results of preliminary investigations only, but they do indicate various possibilities depending on the requirements and priorities of users for the survey data.

2. DATA REQUIREMENTS

2.1 Establishment of Information Needs

It has now become a standard practice when designing a new survey or redesigning an existing survey to determine the information needs for establishing survey objectives at an early stage in the project. For a continuous survey, failure to determine these needs on the assumption that general objectives have remained unchanged would defeat one of the most important purposes of the redesign exercise, namely evaluation of the survey from the viewpoint of its uses and effectiveness.

During the period between successive redesigns, information needs of users who participated in the earlier setting of objectives may have changed, and in addition new uses of the survey data other than those considered in the design of the survey may have emerged. It is incumbent upon the methodologists and the sponsors to discuss jointly with survey users the detailed information needs and priorities and to set up objectives for the redesign in clear and specific terms.

It is only when specific objectives have been agreed upon, that the design statisticians can properly discharge their responsibility of developing the most efficient survey design taking account of the operational constraints and the cost specified for the survey. The importance of this close dialogue at the initial stages cannot therefore be overemphasized. This is particularly so in the case of large-scale continuous surveys where major changes cannot usually be incorporated in midstream due to such factors as continuity of the time series, complexities of operations, and cost benefit considerations. Hence any failure at the outset in establishing survey objectives may continue to affect the survey results for the life of the design.

In an environment of fiscal restraint such as currently exists, a seemingly legitimate concern on the part of the survey sponsoring agency may be that initiation of discussions with the users might spark the type and degree of demands which could reach well beyond the scope of the survey. However, as long as the importance of budgetary constraints are clearly realized by both, there should be a definite advantage to such discussions. Not only would they enable the statisticians to take stock of and prioritize demands, but also they would serve to identify and inform users of those requirements which cannot be met by the survey and alert them to the consequences of misuse of the survey data. For fuller discussions on the role of user consultations in analysis of requirements, and on identification of feasibility, priority and method, we refer the reader to a paper by Fellegi and Ryten [5].

Another point to be emphasized is the lead time required in redesigning a continuous survey and the importance of input from survey users at the early stages of this process. In contrast with adhoc surveys where normally design activities may be completed in a couple of months to about a year, the lead time needed for continuous surveys is much longer. By the same count, payoffs as well as stakes are higher. For the CLFS redesign, while the detailed research plans are currently being formalized, some initial studies have already been in progress since the middle of 1980 and the introduction of a redesigned sample is scheduled for 1985.

As a beginning step in the process of determining information needs for the coming CLFS redesign, members of a recently established Evaluation Program For the LFS [15] will meet with all the major users of CLFS data and a sample of other users, for the purposes of identifying users' needs and how well the existing LFS satisfies these needs. Based on these findings, the design statisticians will intensively follow up cases where new information needs have emerged or earlier information needs have changed. Success of the redesign program thus becomes heavily dependent upon the timely specification of the requirements so as to provide the survey designers sufficient time to evaluate alternatives and choose the most appropriate strategy for a given situation.

The specification of information needs should include a specification of; characteristics of interest; the types of estimates required-rates, levels, changes in rates, or changes in levels; required frequency of estimates; cross classifications (if any) desired for the characteristic at different area levels of interest; and finally associated data reliability requirements.

The specifications should also include a description of the uses of the data, and their bearing on decision-making processes or allocation of funds. Equally essential is an assessment by the users of the importance

of the survey data for their program. Where information needs of a user are diverse, the user should also be asked to indicate priorities for them. Having received this input from users, overall priorities would be established and, subject to budgetary and other restrictions, would be translated into specific survey objectives. It should be emphasized that a primary responsibility of the design statistician in the process of user consultation is to provide assistance to the users in understanding what input is required of them and to provide technical guidance, for instance in the determination of reliability requirements, and identification of possible means of meeting their requirements.

It is worth drawing attention to a note by Platek [11], to papers by Cahoon, Kniceley and Shapiro [1], in which the importance of establishing clear survey objectives at an early stage of the survey has been emphasized.

To illustrate the importance of precise specification of survey objectives in deciding upon the choice of survey strategy, we present below three alternate means of meeting demands for more data. The choice of a particular strategy or combination of strategies should depend upon the type of data needed and the priorities set out for them. In the following sections alternatives will be presented with respect to reallocation of the sample (sect. 2.2), use of alternate rotation patterns (sect. 2.3) and lastly, expansion of the scope of the survey (sect. 2.4).

2.2 Sample Reallocation for Improved Monthly Subprovincial Estimates

Before discussing the implications of sample reallocation on data reliability, the expression for the coefficient of variation used in calculations is briefly discussed with relation to sample size, frequency of a characteristic, and design effect.

For the LFS, the coefficient of variation for monthly estimates for the characteristic unemployed (u), and for an area (a) of interest, can be expressed as

$$CV_a(u)\% = 100 \frac{SD_a(u)}{u_a}$$

where $SD_a(u) = \left(\sum_{t \in a} F_t (W_t - 1) P_t p_t q_t \right)$

where \sum_t = sum over strata or collection of strata for which sample design and sampling rate are the same.

and P = estimated persons 15 years of age or over
 W = inverse sample rate ($= P/n$, where n = sample size)
 p = proportion unemployed
 $q = (1 - p)$
 F = design effect
 $u_a = \sum_{t \in a} P_t p_t$

From the above formulation, it can be seen that the reliability of estimates of level for a characteristic are primarily dependent on three factors:

- i) Sample size: since $W = P/n$, other factors being constant, the CV% decreases proportionately to increases in the square root of the sample size. That is to reduce the CV in half, the sample size would have to be quadrupled.
- ii) Frequency of the characteristic: the coefficient of variation is approximately inversely proportional to the square root of the proportion of persons having the characteristic. Thus for unemployed, the lower the unemployment rate, the larger the sample size required to obtain reliable estimates.
- iii) Design effect: The design effect provides an overall comprehensive measure of the combined effect of all the design features, such as

stratification, multistage sampling and estimation. It is defined by the variance estimate obtained from the survey divided by the variance that would have resulted had the sample been taken in the form of a simple random sample of persons. The interpretation of a design effect of 2 for unemployed, would imply that, cost consideration aside, the sample design was only half as effective for measuring the characteristic unemployed as a simple random sample would have been. For the LFS, design effects are generally greater than one for most characteristics, due to the need for concentrating the sample in a relatively few selected areas as a means of reducing data collection costs.

Historically for the LFS, the characteristic unemployed has usually been considered of primary importance, and the total size and allocation of the sample have been determined to achieve specified reliability requirements for monthly estimates of unemployed. Prior to a sample size increase during the 1970's, the sample of 36,000 households was allocated with the primary objective of providing good monthly estimates for unemployed at the national level. When the sample was increased to 55,000 households, the additional sample was allocated on the basis of achieving more uniform reliability between provinces for unemployed. Because the increase was carried out after the redesign of the sample there was an additional restriction imposed by the sample design, namely that in Self Representing (SR) strata (i.e. larger cities) the sample could only be increased by multiples of the existing sample size, and in remaining (NSR) areas, increases had to be half-multiples of the existing sample size (i.e. 50%, 100%, 150%, etc.)

In increasing the sample size, uniform sampling rates by type of area (NSR and SR) within provinces were retained, as this provided an effective allocation scheme for improving provincial estimates for unemployed. Table 2.1 illustrates the impact of the increase on monthly CV's for the characteristic unemployed for the period Jan 75 to Dec 1980. The uniform sampling rates have the additional advantage of providing a good general purpose allocation considering the broad range of characteristics

on which information is collected, not only for the LFS, but by other surveys utilizing the LFS capacity.

Table 2.1 Pre-Increase and Post-Increase
CV% for Monthly Estimates of Unemployed

Province	Post Increase Sample Size (households) (2)	% Increase (3)	CV% for unemployed	
			pre-increase (4)	post-increase (5)
Newfoundland	3056	70.30	8.44	6.23
Prince Edward Island	1418	200.00	18.12	9.61
Nova Scotia	4021	29.80	6.55	5.34
New Brunswick	4217	67.78	8.23	5.44
Quebec	8541	17.06	4.56	3.54
Ontario	10850	14.24	4.31	3.65
Manitoba	4719	141.34	11.13	6.55
Saskatchewan	5724	200.00	14.42	7.56
Alberta	6709	100.00	8.65	6.49
British Columbia	6124	42.20	5.76	4.99
Canada	55379	52.12	2.33	1.88

With provincial CV's currently at acceptable levels, there has been an increased demand for more reliable subprovincial data. In the remainder of this section we examine how the reliability levels for subprovincial monthly estimates of unemployed could be improved by means of within province sample reallocations.

A disadvantage of the self-weighting design (uniform sampling ratio) is that for subprovincial regions variability in population sizes translate

into variations in the reliability of estimates. Currently monthly estimates of unemployed are published separately for 47 LFS Economic Regions for which the CV's are 25% or less. The remaining 19 ER's have been collapsed into groups of 2-4 to ensure that the reliability levels for the groups meet publication criteria.

It has been recently determined [17] that an additional sample of approximately 3000 dwellings would be required to achieve a 25% CV for each of the individual ER's where collapsing is carried out. It was also shown that these dwellings could be achieved by reallocating samples from the larger CMA's in the respective provinces. Refinements on such within province reallocations are currently being investigated using more months of survey data in the calculations and also taking into consideration reliabilities of estimates for other subprovincial areas as discussed in section 2.3 .

For illustration purposes, below we consider what could be achieved by within-province sample reallocations for the province of Manitoba. Present reliability levels for Manitoba's 8 Economic Regions based on data for the period Feb 78 to May 79 are shown in column 5 of Table 2.2. It might be noted that currently ER's 65 and 68, and ER's 61-64 are collapsed for publication purposes. The sample was reallocated to NSR and SR portions of individual Economic Regions so as to minimize data collection costs while achieving a fixed CV (22%) for unemployed following a general approach suggested by Fellegi et al [4], for all the ER's except 67 (Winnipeg), for which the sample size had to be reduced by 288 households. It should be noted that under the sample reallocation the provincial CV remains virtually unchanged, although costs would increase somewhat due to heavier sampling in NSR areas.

Table 2.2 Within Province Sample Reallocation for
Manitoba Economic Regions
(period Feb 78 - May 79)

Economic Regions (1)	existing sample allocation				reallocation of sample			
	W_{NSR} (2)	W_{SR} (3)	Hhlds (4)	CV(u)% (5)	W'_{NSR} (6)	W'_{SR} (7)	Hhlds (8)	CV(u)% (9)
61	41.67	-	477	25.98	30.16	-	659	22.00
62	41.67	-	308	25.89	30.33	-	423	22.00
63	41.67	90.00	690	17.55	92.55	74.54	399	22.00
64	41.67	90.00	242	30.84	25.48	36.37	435	22.00
65	41.67	-	404	22.36	40.40	-	417	22.00
66	41.67	90.00	426	20.18	52.69	65.30	353	22.00
67	-	90.00	2030	7.73	-	104.88	1742	8.35
68	124.00 ¹	90.00	142	36.44	33.37	92.70	288	22.00
Manitoba	43.27	90.00	4719	6.15	39.37	100.52	4716	6.19

¹ remote area sample

There are some potential problems with an allocation scheme optimized for the subprovincial estimates for the characteristic unemployed, that have yet to be fully addressed, however. For instance, it may be less efficient for other surveys utilizing the LFS capacity. While for other surveys the desired allocations could be achieved by sub-sampling the LFS selections, this would nevertheless reduce the sample size available to such surveys. Additionally the robustness of such an allocation against changes in the unemployment levels over time would have to be studied further.

2.3 Alternate Rotation Patterns

In a rotating panel survey such as the LFS, the monthly sample size determines the reliability of monthly estimates of levels and rates; however, it is primarily the rotation pattern which determines:

- i) the reliability of estimates of change, whether month to month, quarter to quarter, or for a calendar month from one year to the next and
- ii) the reliability of estimates obtained by combining monthly data to arrive at quarterly, semi-annual or annual estimates.

In general, rotation patterns which are better for i) are not as good for ii) and vice versa. Thus the choice of a rotation pattern should be governed by the relative priorities attached to these types of estimates.

At the time of earlier redesigns of the LFS, there was little demand for estimates of type ii) and therefore the choice of the current LFS rotation pattern has reflected a predominant importance for estimates of month to month change. Under the current LFS rotation pattern, households remain in the sample for six consecutive months, and each month one-sixth of the households rotate out of the sample and are replaced by new ones. This scheme is very efficient for measuring month to month changes as the 5/6 households in common from one month to the next results in moderate to high correlations between successive months' samples for most characteristics.

The same correlations between successive months' samples which are advantageous for estimates of change are disadvantageous for average estimates of level. As a result, the current LFS rotation pattern is not as efficient for quarterly, semi-annual or annual estimates of rates or level as some other schemes. It is of interest to compare the performance of the LFS rotation pattern for combining data over months and for estimates of month to month change with that of the Current Population Survey (CPS), the counterpart of the LFS in the United States. In the

CPS households remain in the sample for 4 consecutive months, are out for 8 months, and then rotate back in again for 4 more months. Thus each month 1/4 of the households rotate.

If we denote V_m as the variance of estimate for a given month m and V_{cm} as the corresponding variance for estimates obtained by combining data for c months, then the variance reduction factor due to combining data, K , is defined as:

$$K = \frac{V_{cm}}{V_m}$$

Similarly, if we let $V_{(m, m+1)}$ denote the variance for estimates of change between months m and $m+1$, then the variance reduction factor for month to month change, K' , is defined as

$$K' = \frac{V_{(m, m+1)}}{V_m + V_{m+1}}$$

It should be noted that K' is approximately equal to $(1 - \text{the correlation coefficient between the months' estimates})$. Table 2.3 presents values of K and K' for the two rotation schemes for the characteristic unemployed. The smaller value for K for the CPS rotation scheme indicates that it is more efficient for combining data, while the smaller value of K' for the LFS rotation scheme indicates it performs better for estimates of month to month change. It should be noted that the figures presented in the table for the LFS are the result of preliminary investigations only [7], and results for the CPS are taken from [18].

Table 2.3 Comparison of LFS and CPS Rotation Schemes for Unemployed

	Variance reduction factor due to combining months data (K)			Variance reduction factor for month to month change (K')
	3 mo	6 mo	12 mo	
CPS	.50	.31	.20	.50
LFS	.67	.48	.29	.44

Research studies are planned to confirm the results of Table 2.3 for the LFS, to consider similar variance factors for a broader range of characteristics, and also to consider the implications on combined estimates and estimates of change for other rotation patterns such as 3 - 9 - 3 (three months in the sample, 9 months out, and 3 months in) and 1 - 2 - 1 - 2 - 1, (one month in, 2 months out, one month in, etc.)

To further illustrate the impact of rotation pattern on average estimates of level, Table 2.4 presents the sample sizes necessary to achieve 25% CV's for annual estimates of unemployed for individual Census Divisions for the LFS and CPS rotation patterns under two different allocation schemes.

The augmentation allocation is based on retaining the present sample allocation and adding to it whenever necessary to produce the required reliability level for individual Census Divisions (CD's). The reallocation strategy on the other hand is based on a complete reallocation of the sample to achieve the required reliability levels for CD's. On practical considerations, both of these are extreme options and are used only for illustrative purposes. The reallocation strategy in some cases would result in a deterioration of monthly provincial estimates, while the augmentation strategy is clearly too expensive. A comprehensive strategy taking into consideration annual reliability levels for Census

Divisions, simultaneously with monthly reliability levels at the Province, Metropolitan Area, and Economic levels is currently under investigation.

Table 2.4 Additional Dwellings Required Monthly for
25% CV for Annual Estimates for
Unemployed for Census Divisions

Province	LFS ROTATION PATTERN		CPS ROTATION PATTERN	
	Augmentation	Reallocation	Augmentation	Reallocation
NFLS	--	--	--	--
PEI	--	--	--	--
NS	90	--	12	--
NB	7	--	--	--
QUE	2,520	--	1,055	--
ONT	2,300	--	952	--
MAN	3,578	1,411	1,887	--
SASK	2,080	--	877	--
ALTA	1,357	--	647	--
B.C.	370	--	184	--
Canada	12,302	1,411	5,614	--

It should be noted that the calculations are based on the assumption of the current LFS design and the unemployment level at the time of the 1976 Census. Further, assumed density factors of 1.5 and 3 are used for SR and NSR areas, and the variance reduction factors used are those given in table 2.3. Thus the figures in Table 2.4 should be considered only for the purpose of illustration and relative comparisons, as changes in any of the above factors including the design, will result in changed allocations.

The point clearly illustrated by Table 2.4 is that if sufficient priority is attached to improved quarterly, semi-annual or annual average estimates, then for cost-efficiency reasons, there would be a strong case for changes in the rotation pattern. In this event, apart from the theoretical investigations of various rotation patterns, including the study of the impact of rotation group biases on them, a detailed examination of response burden and other operational aspects would have to be tested through the field experimental capacity described in section 2.4. If, on the other hand, higher priorities are given to the estimates of month to month change, then the LFS rotation pattern should remain unchanged.

2.4 Current Survey Capacity

Recent years have witnessed an increased demand for more detailed labour force data and data on a wide variety of characteristics influencing the labour market situation. During the 1970's Statistics Canada successfully responded to these demands by undertaking a major survey revision [10] which included an expanded capacity for use of the LFS as a vehicle for conducting other surveys. The current redesign will provide the opportunity to re-evaluate the role of the LFS in this regard.

Since the LFS is the only continuous household survey program carried out by Statistics Canada, integration of other household surveys with the LFS is desirable in the sense that these surveys can take advantage of the investment the LFS represents in terms of sample frame, design, data collection, and processing systems to obtain data more quickly, at less cost and greater reliability than would be possible through independent surveys. With the increased flexibility and capacity of the LFS achieved through the revision and through methodological improvements made at the last redesign, demands for use of the LFS as a vehicle for conducting household surveys have continued to increase in recent years. Examples of such surveys include: Survey of Consumer Finances, Asset and Debt, Family Expenditure, Annual Work Pattern, Household Facilities and

Equipment, Student Identification, Job Opportunity, Travel, Education, Smoking Habits, and Leisure Time Activities. Integration of these occasional surveys takes three different forms.

First, in the majority of cases, these surveys are conducted as supplements to the LFS due to cost and timeliness considerations. In such cases the most commonly adopted procedure is to collect data during the same visit, immediately after the LFS interview. In the case of enquiries with longer questionnaires, such methods of data collection as drop-off/pick-up are also utilized.

A second level at which the LFS has been utilized by other surveys is to select a different set of households in the same sampled areas as the LFS and to utilize labour force interviewers but at a different time period from the LFS. This is somewhat more costly than a supplement, but nevertheless represents a considerable saving over an independent survey. Examples of such use include; the Survey of Consumer Finances in odd years, when the survey content is expanded to include in depth questioning, for instance on Assets and Debts, and the program of Family Expenditure Surveys which consists of a recall survey and a diary survey.

The other situation in which LFS frame has been used is to select an 'independent sample' from the LFS frame, but in areas not currently being sampled by the LFS. The advantages over a totally independent sample are saving in sample design and implementation costs and also the control to avoid overlapping with the LFS and surveys associated with it. The Canada Health Survey for instance followed this approach in its survey design in cities, although in the remainder of the country a separate design was called for due to unique operational constraints.

Currently along with the LFS redesign activities, methodological aspects of other major surveys are also being researched. Just as it is important for the primary subject of enquiry using the continuing survey vehicle to

re-evaluate and re-establish its own objectives, it is equally incumbent on the other major users of the vehicle to follow the same course of action.

This will provide an opportunity for such surveys to maximize to the extent possible their benefits from the redesigned capacity of the vehicle, by determining optimal designs for their surveys, by being aware of implications of redesign alternatives, and by providing input to the decision processes.

Sponsors of each such major survey and the associated methodologists have recently begun this undertaking. Major studies in the optimization process would include stratification, sampling stages, allocation at various level of aggregations, determination of sampling and sub-sampling fractions, rotation patterns, response rates and their adjustments and other factors in the estimation process. It is not unlikely that these studies would result in a collection of optimal designs differing to a varying degree for different surveys.

Depending upon the importance attached to the major surveys using LFS vehicle and the degree to which the optimal designs differ, one of the three options may be followed, namely:

- a) to redesign the current vehicle as a continuing household survey primarily for the LFS taking account of other surveys to the extent possible,
- b) to redesign the current LFS vehicle as a general purpose survey or
- c) to redesign the vehicle only for the LFS and develop a separate vehicle for conducting other major socio-economic surveys

The current situation is somewhere between a) and b); design features are optimized for the LFS, particularly in Non Self Representing Areas, (sect. 4.2); nevertheless the capacity is used extensively in a general purpose sense, as has already been described. It will be noticed that there is a very fine distinction between the options a) and b) and that

the difference mainly lies in the degree of importance associated to various subjects of enquiry using the redesigned vehicle.

In order to illustrate the distinction between the two approaches let us consider the problem of allocation of sample at a given level of aggregation (say R). Suppose there are m enquiries ($m=1, 2, \dots, M$) with the corresponding optimum allocation as n_m at level R, with the LFS allocation being denoted by n_ℓ . Say their magnitudes are as follows:

$$n_1 \leq n_2 \leq \dots \leq n_\ell \dots \leq n_m \dots \leq n_M$$

indicating that the subject M requires largest sample at level R.

Note that this may happen at level R even if the total sample size for subject M may be smaller than that of the LFS.

In the case of option b) the approach would be to aim at a compromise allocation (say n^*) such that $n_1 \leq n^* \leq n_m$. In case of option a) however, the allocation would always be n_ℓ determined to be optimum for the LFS, and in order to accommodate other surveys, flexibility would have to be introduced into the vehicle to allow for over-sampling or sub-sampling as required. Option c) while having some technical merit, suffers from operational problems, such as co-ordination of the two vehicles to prevent overlapping samples. Even if such problems are taken care of, this option as such can be ruled out on the grounds of being very expensive unless some enquiries equally important and complex as the LFS come along.

Discussions and studies are being carried out in order to make a final decision on these options. It seems at this stage that the requirements of most surveys currently using the vehicle would be met under option a) by incorporating minor changes in various aspects of the LFS design and increasing the capacity of the survey vehicle as described below.

In order to meet the data requirements, studies are being undertaken to develop an alternate small scale survey capacity in addition to increasing the capacity for the current LFS vehicle. One component of this program would be a collection of statistics on new subject matters in anticipation of future requirements. This would thus serve as a 'pilot' for full scale enquiries for more detailed data. As well the small scale survey capacity would provide an opportunity for analytical studies to examine inter-relationships between various social and economic phenomena. The capacity may frequently be used for surveys where it is necessary to react quickly in response to data associated with policy concerns of the federal government. The third area where this capacity would be useful is the development of new techniques through well designed field experimentation. This last aspect is discussed in more detail in the following section along with data collection.

3. DATA COLLECTION

In a large scale survey, a single or a combination of data collection methods such as personal interview, telephone and mail may be used, depending upon the type of enquiry, available facilities, respondents' attitudes, resource situation and timing constraints. Whatever be the method adopted at the initial phase of a continuous survey, it requires regular review as changes in the environment and conditions under which data are collected will directly affect its quality. Over time, respondents' attitudes towards surveys may change due to changing life style or increased respondent burden; new tools and techniques may be developed; legal requirements, the resource situation or quality of interviewers may have changed. All these affect the quality of data collected and hence the choice of method. Although certain changes in the data collection procedure may be introduced at any time during the life of the survey design, major changes affecting the cost and quality are usually introduced along with the redesign of the vehicle. This is

because the procedure adopted for data collection affects both the type of sampling design as well as the estimation procedure, and hence to be cost effective the method of interview must be decided upon well in advance of the sampling plan. It should be noted that for a survey vehicle like the LFS, which is used by various types of enquiries, the effect of any change in the procedure of collecting data needs to be investigated, including testing in the field, for as many of the major enquiries as possible. In this respect, just as in the case of establishment of the survey objectives, close discussion and coordination among sponsor, field staff and methodologist are important at the very early stages of planning.

As mentioned in the previous section, a small scale capacity is being considered to meet the current needs of social statistics. One of the primary purposes of establishing this capacity is to provide an opportunity for testing and developing new operational and methodological procedures. Testing of alternatives will focus on the data quality through operational measures such as response rates, slippage, error rates, etc., and also the effect on the cost of the survey. This methods test capacity may be utilized depending on the purpose of the test in any of the following manners: use of same households as the LFS, separate set of households in the same area as the LFS, or a completely different sample. Also the purpose of a particular test will determine its duration, location and the spread of the sample.

It is expected that certain new methods and procedures will be tested in the field with a view to examining suitability for the ongoing LFS. As an example, one such test which deals with the extension of telephone interviewing in the rural areas and smaller urban centres is briefly discussed below.

After a period of testing, the use of the telephone interview was expanded at the time of the last redesign to cover all Self-Representing Units primarily to reduce the cost of data collection. Currently in the LFS, households are interviewed in person the first month they are in the sample. In Self-Representing Units, if the respondent agrees to the telephone, the interviews are as a rule conducted via telephone in the second through sixth month the household remains in the sample. In other areas interviews are conducted in person. A similar telephone interviewing procedure will be tested for NSRU's. However, due to concern over the confidentiality of the data, telephone interviewing will be restricted to areas with a very low incidence of party lines.

Objectives of testing telephone interviewing in NSR areas will be to determine for the LFS and other surveys using the vehicle:

- i) Effect on data collection costs and sample design implications.
Reductions in the travel component of collection costs and the potential for interviewers to handle larger assignments, could permit designs with less concentration of the sample, and hence a reduction in sampling variance. For instance, it might be possible to eliminate one or more stages of sampling.
- ii) Data quality. Acceptance of telephone interviewing, effects on non response rates, and if possible on survey estimates would be examined.

The test would be conducted on a sub-set of the ongoing LFS interviewer assignments, augmented in some cases by 10 - 20 percent to study the effects of larger assignment sizes and different concentrations of the sample.

4. OTHER DESIGN RESEARCH

In this section, we briefly highlight some of the redesign projects related to updating the sample and introduction of methodological improvements in the sample design and estimation procedure.

4.1 Redesign of Self-Representing Units

Current LFS Self-Representing Units (SRU's) correspond to those cities which were sufficiently large to yield a sample capable of supporting at least one interviewer. Minimum SRU sizes vary from a population of 10,000 in the Atlantic Region to 25,000 in Quebec and Ontario. A first step then will be a re-definition of the SR universe taking into consideration impact of the 1976-77 sample size increase, population shifts, and changes in boundaries of Census Metropolitan and Census Agglomeration areas.

Larger SRU's are divided into sub-units and within sub-units, first stage sampling units (i.e. clusters), are delineated on the basis of field counts obtained in 1973. The clusters correspond approximately to city blocks. A two stage sample of clusters, and dwellings (3 - 5 per selected cluster) is selected following a pps method based on random groups of clusters [14] . Using census data to simulate the LFS design, research is being carried out to investigate the effects on sampling efficiency and operational suitability of alternative first stage sampling units - such as census enumeration areas, blocks or block faces - and of alternative allocations of the sample between and within first stage units.

Another focus is on alternative means of achieving and maintaining an up-to-date sample in SRU areas. Due to the rapid and uneven growth which occurs in these areas, without regular updating, the variance of estimates can increase substantially [2]. Under the present sample updating program [13], [3], for sub-units being updated, revised dwelling counts for individual clusters are obtained on the basis of complete field counts. As an alternative to independently obtained field counts, the use of census units, dwelling counts and maps in the redesign of the sample is being investigated. Discussions are also in progress with Post

Canada concerning possible use of Post Canada maps and dwelling counts to provide a future means of updating the LFS sample without incurring the expense of field counts. The key to this would be the planned linking of Postal Codes to 1981 Census units, and hence to LFS sampling units.

4.2 Redesign of Non Self-Representing Units

Non Self-Representing Units correspond to the smaller urban centres and rural areas. In the present design, 1 - 5 geographically contiguous, approximately equi-sized strata are formed within the NSR portions of individual Economic Regions. Industry classifications were taken into consideration in forming strata. Within strata, approximately 15 Primary Sampling Units (PSU's) were delineated so as to be similar to the stratum with respect to stratification variables and rural to urban population ratios. To satisfy this last constraint, frequently urban centres had to be shared amongst several PSU's within the stratum, often resulting in discontinuity between rural and urban portions of PSU's.

Initially two PSU's per stratum were selected following the randomized pps systematic method [8]. The sample was increased by selecting additional PSU's [6], and at present 3 - 6 PSU's are selected per stratum. It is felt that the sample increase strategy adopted may have led to a reduction in the efficiency per unit cost of survey, although the circumstances of the increase occurring in midstream ruled out more technically desirable alternatives such as re-stratification to form an increased number of strata, each with two selected PSU's.

As data requirements and design constraints, both technical and operational, vary from province to province alternative designs will be investigated by provinces or groups of provinces taken together as opposed to seeking a uniform national design.

The NSR design is very much dependent not only on whether telephone interviewing is adopted as discussed in section 3, but also on the survey objectives. For instance, if an increased importance is attached to annual estimates for Census Divisions or to the estimates from other major surveys using the vehicle, then a design in which CD's were taken as primary strata would be seriously considered. In such a case, the design would likely feature rural/urban sub-stratification within CD's and utilization of either Census Sub Divisions or Census Enumeration Areas as first stage sampling units. Studies would be required to determine whether any loss in sampling efficiency for the LFS would be incurred under such a design, due to the reduced amount of optimal type stratification.

Additional studies in the NSR design which are planned, primarily to improve the design efficiency and facilitate updating include:

Buffer Areas

Generally growth in NSR areas is not large enough to warrant updating the sample between redesign. Exceptions, however, are the NSR areas close to the boundaries of certain Census Metropolitan Areas. During the 10 year life cycle of the design, growth frequently reaches into these areas, where a more flexible design capable of being updated is therefore required.

Stages of Sampling

Studies will be conducted to determine the implications, both operational and theoretical of reducing the number of stages of sampling. This study would be closely linked to the study on telephone interviewing.

4.3 Estimation and Variance Estimation

A number of studies are planned into estimation and variance estimation procedures used by the LFS and other household surveys. Some of these

are briefly highlighted below:

Final Ratio Adjustment

The current estimation procedure for individuals incorporates ratio estimation at the province level, using official population estimates by age-sex categories, adjusted for out of scope population (military and institutional). Research will be conducted into determining optimal age-sex post-strata, applying the ratio estimation at sub-provincial levels, and adjustment of LFS data for census undercount.

Estimation for Family Units

In the past, post censal estimates of numbers of family units have been unavailable, with the result that there has been no standard procedure from one survey to the next for producing family based estimates. This project will address both of these problems, as well as attempting to ensure consistency between family and individual based estimates.

Variance Estimation

Research will be carried out to compare alternative estimators with the Keyfitz [9] estimator currently being used from a point of view stability and extent of bias in the current estimator due to the violation of the sampling with replacement assumption. This will be examined for both seasonally adjusted as well as unadjusted sample estimates.

Small Area Estimation

Research will continue into estimation methods for non-standard areas cutting across design strata. Estimators being studied include synthetic, composite, and sample regression. Attention is also being given to the treatment of large growth clusters falling into the sample, particularly as they affect estimates for small areas.

5. SUMMARY

While redesigning continuous surveys, the importance of close discussions among users, sponsor and designers at an early stage of the program is emphasized. This will not only help to re-evaluate the effectiveness of the ongoing program but it will be a useful exercise in identifying and informing the users about the limitations of the survey. As a result of such discussions the survey objectives can be established in the light of current and future data requirements. To illustrate the importance of the precise specification of the objectives, three alternate means of meeting data demands are discussed, namely reallocation, rotation patterns and survey capacity. Choice of these or other alternative would clearly depend on the specification of the information needs.

Like the specification of survey objectives, data collection procedure plays a very significant role in deciding the survey strategy for a particular situation. Designers aim at developing the most efficient design per unit cost and since the major part of the cost relates to the data collection, an early decision in this respect is essential. A small scale capacity is being developed to list and develop new procedures and it is planned to use this capacity in examining the suitability of telephone interviews in rural and smaller urban centres.

At present steps are being taken to establish the information needs and also to decide upon the field methodology. Several research and evaluation projects in the above context have been started. In addition research related to other aspects of the design and estimation methodology has begun.

RESUME

Les organismes spécialisés révisent périodiquement leurs enquêtes permanentes. Ces révisions tiennent à l'évolution des besoins en information auxquels l'enquête doit répondre et à l'évolution de la perception et de l'attitude du public à l'égard des enquêtes; elles sont analysées dans le contexte de la révision de l'enquête sur la population active du Canada après le recensement de 1981. En particulier, les auteurs font ressortir l'importance dès le début du processus de révision du dialogue entre les utilisateurs des données de l'enquête et les statisticiens concepteurs afin de déterminer les objectifs de l'enquête.

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FOR-HIRE TRUCKING SURVEY:

SURVEY DESIGN

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The methodology of the For-hire Trucking Survey is discussed in this paper. This survey provides good examples of administrative and operational constraints faced by survey statisticians and field data collection teams.

1. INTRODUCTION

This paper presents the methodology of the For-hire Trucking Survey, a multi-stage probability survey of shipping documents retained by for-hire trucking carriers in Canada. The paper is structured as follows. In the second section, the survey context is described. In the third section, the ultimate sampling unit, namely the shipment is defined. Then the universe and the frame of the survey are depicted in the fourth section. After that, some major administrative considerations are listed in the fifth section and the stratification and sample allocation are covered in the sixth section. Then the first stage sample design and the subsequent stage(s) sample design are presented respectively in the seventh and eighth sections. In the ninth section, the field operations are discussed. The data processing and the estimation methods respectively are explained in the tenth and eleventh sections. Finally, a comment about the future of the survey concludes the paper in the twelfth section.

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2. SURVEY CONTEXT

2.1 Primary Objective and Uses of the Survey

The primary objective of this survey is to provide information about the domestic intercity movements of goods by the Canadian for-hire trucking industry. The fo-hire trucking industry covers any carrier which for compensation undertakes the transport of goods by truck. This survey measures the output of this industry in terms of revenues earned, tons carried and ton-miles performed by commodity group.

Requests for estimates from this survey come from a wide variety of sources such as government departments concerned with trade; transport regulatory officials at both federal and provincial levels; carriers; university consultants; industry associations; and many other organizations and individuals who share a common interest in transportation.

The estimates are used extensively to serve four basic requirements. First, they measure the volume of domestic trade transported by intercity for-hire carriers provincially and interprovincially. Secondly, they provide a cross-check on the rate of industrial growth reflected by intercity commodity movements and they provide information on regional development. Thirdly, they assist in transportation studies (e.g. [1], [2] and [3]). Finally, they support the presentation of briefs, submissions and other inquiries to regulatory authorities and commissions.

2.2 Background

Initial work on the For-hire Trucking Survey began in 1969. At that time, a study of various methods of collecting commodity origin and destination statistics was carried out. The study results showed that, from a cost-benefit point of view, a sample survey of shipping documents was the only viable approach to collect the data.

In 1970, a pilot survey was conducted to assess the survey approach effectiveness. The pilot survey involved the examination of the shipping documents of about 200 for-hire trucking firms throughout the country. The favourable response to the pilot survey and the availability of origin, destination, commodity, weight and revenue information of the shipping records indicated that the survey approach was feasible.

The For-hire Trucking Survey has been conducted on an annual basis since 1970 by the Transportation and Communications Division of Statistics Canada. However, the survey design has changed over time. Examples of changes mentioned in this paper are changes to the frame and changes to the sample allocation technique.

3. THE ULTIMATE SAMPLING UNIT

The 1969 study and the 1970 pilot survey mentioned in Section 2 indicated that the ultimate sampling unit be the shipment.

The principal characteristics needed from each sampled shipment are the true origin and the final destination; the description of the commodity(ies) carried; the weight; the transportation revenue earned and the interlined shipment information. An interlined shipment occurs when a consignment is moved by a carrier to an intermediate point and then moved by another carrier to another point. The interlined shipment information is used to unduplicate interlined shipments.

The secondary characteristics needed are the month and year of shipment; the quantity of commodity and the unit of measurement (e.g. 5 board feet, 20 gallons, 15 sacks, etc.); the method of movement (e.g. heated van, refrigerated van, piggyback, fishyback, container, etc.); some remarks on shipment weight transcribed (e.g. minimum weight, convenient weight used for calculating revenue, etc.); the rate charged and the rate

condition codes (e.g. code indicating where rate is minimum, per 100 lb., per hour, etc.); and the revenue condition codes (e.g. code indicating where exact transportation revenue is not available, where shipment is out of scope, etc.).

The shipment characteristics can be found on documents known in the trucking industry as Probills, Bills of Lading, Load Manifests, Trip Reports, Invoices, or a combination of the above in either a computer listing format or other media of storage.

These documents can be filed in complete numeric sequence; in broken numeric sequence; in chronological order; in alphabetical order (e.g. by customer name); by terminal; by commodity type, i.e. usually contracts; or in no order at all. The documents may even be cross-filed; for example, by serial number and by customer's name. Within a filing system, documents may be kept in a set of file drawers, in a set of binders or shannon files, on shelves, in drawers, or even in a book.

4. UNIVERSE AND FRAME

The first choice for the frame is ideally a list of all shipments. However, such a list is not available. Instead, D.S.L.P.'s (Document Storage Location Points) are used as natural clusters of shipments for the first stage sampling units of the design. A D.S.L.P. is a site at which shipping documents suitable for sampling are kept. A trucking company may have more than one D.S.L.P. in the case where shipping documents are stored at several terminals but not at the company head office. In some cases, a D.S.L.P. contains shipping documents for more than one company.

The universe and the frame of D.S.L.P.'s have changed since the survey started in 1970.

In 1970, the universe was defined to include the D.S.L.P.'s of all provincially regulated or licensed carriers, regardless of size, type or major activity. The frame for this universe was derived from provincial license lists and included about 15,000 D.S.L.P.'s.

Since 1975, the universe has been limited to the D.S.L.P.'s of the carriers earning \$100,000 or more annually from intercity trucking. Other exclusions are mentioned in the survey publication [4]. Also, the frame for a given year has been the list of the D.S.L.P.'s of the carriers whose reports to the Motor Carriers Freight and Household Goods Movers Survey for the previous year show earnings of \$100,000 or more from the domestic movement of goods over more than 15 miles of public roads.

The description of the frame of the 1978 survey and of the principal statistics estimated from the survey data are given in Table 1 at the end of the paper.

5. ADMINISTRATIVE RESTRICTIONS

The survey design consists of selecting shipments from the files of selected D.S.L.P.'s and of transcribing the characteristics of the selected shipments on coding sheets. However, administrative restrictions limit the number of transcriptions. The administrative restrictions are presented in this section and the survey design is detailed in the next sections.

5.1 Maximum Total Number of Transcriptions

The cost of the survey is relatively high. As an example, the 1977 For-hire Trucking Survey cost \$494,000. The distribution of this expenditure by function is given in Table 2 at the end of the paper.

The cost has set the maximum total number of transcriptions to 225,000 shipments. This size has remained the same since 1972 although the

number of shipments carried by the for-hire trucking industry has increased.

5.2 Minimum Number of Transcriptions per Selected D.S.L.P.

A minimum number of shipments are to be transcribed from the filing systems of the D.S.L.P.'s in the sample to justify travel and salary expenditures. Under the present design, a minimum of 200 shipments are selected from each D.S.L.P. in the sample.

5.3 Maximum Number of Transcriptions per Selected D.S.L.P.

Identification of shipment records in the sample and the transcription of information from these records are done at the D.S.L.P.'s. There is a constraint on the number of days the data collection team spends at a particular location, so that the respondents are not burdened by the presence of the team. This constraint translates to a maximum of 3000 shipment records to be transcribed from any one D.S.L.P.

6. STRATIFICATION AND SAMPLE ALLOCATION

Using the results of the previous year's Motor Carriers Freight and Household Goods Movers Survey, the D.S.L.P.'s are stratified according to their intercity transportation revenue class, their type of operation and their area of operation. The intercity transportation revenue class indicates if the D.S.L.P. earned \$2 million or more, between \$500,000 and \$1,999,999, or between \$100,000 and \$499,999 dollars of revenue from intercity freight transport. The type of operation says if the D.S.L.P. is a general freight carrier, an automobile carrier, a household goods mover, a van line, a bulk (e.g. petroleum, milk, etc.) carrier or an other specialized (e.g. heavy machinery, livestock, etc.) carrier. The area of operation is different depending on the D.S.L.P. total transportation revenue. If the revenue is greater than or equal to 2 million, the area of operation indicates if the revenue is between 2 and 20 million or

greater than 20 million dollars and if the predominant source of revenue is earned east of the Manitoba/Ontario border, west or from international trucking. If the revenue is less than 2 million dollars, the area of operation indicates which of the 10 provinces, the Yukon, the Northwest Territories or the international brought the predominant source of revenue to the D.S.L.P. There were 102 non-empty strata in the 1978 For-hire Trucking Survey.

Once the frame of D.S.L.P.'s is stratified, the number of shipments to be selected and transcribed ultimately from each stratum is determined by allocating the maximum total number of transcriptions to strata. The allocation technique has changed since the survey started in 1970.

Originally, the allocation was calculated in three steps. First, the total number of transcriptions was allocated to 5 domains so that the coefficients of variation were equal for ton-miles over the 5 domains. These domains were the geographic regions of origin of the shipments. The coefficients of variation were estimated using historical data. This first step gave a number of transcriptions to each domain. Secondly, the number of transcriptions to each domain was allocated to strata using essentially a Neyman allocation. This second step gave a number of transcriptions to each domain within each stratum. Finally, the numbers of transcriptions to each domain within each stratum were summed over the domains to get the total stratum allocation of transcriptions.

In 1975, the allocation scheme was revised because it was felt that the estimates of the true variance of each domain within each stratum needed for the Neyman allocation were not reliable and because the resultant strata allocations were highly variable across years and adversely affected longitudinal analyses.

The revised allocation procedure is radically different than the original one. It has been developed using years of experience and is partially a

judgement allocation based on results of the previous year's survey. It consists of allocating workloads defined as 100 transcriptions. The allocation is performed in three steps.

First, the total number of transcriptions, i.e. 2250 workloads, is allocated to the groups of strata having the same intercity transportation revenue class as follows:

Intercity Transportation Revenue Class	Workload Allocation to Groups of Strata
\$2 million or more	908
\$500,000 to \$1,999,999	832
\$100,000 to \$499,999	510
TOTAL	2,250

Secondly, the allocation of workloads to strata within a group of strata having the same intercity transportation revenue class is performed using a stratum size measure. This measure for a stratum is the total intercity transportation revenue in units of 10,000 dollars of the D.S.L.P.'s in the stratum. For the group of strata having intercity transportation revenue of \$2 million or more, the allocation is proportional to stratum size measure. For the others, the allocation is proportional to the square root of the stratum size measure. The square root is used in the latter case because otherwise some strata having little contribution to the revenue would almost be ignored in the sample.

Finally, the allocations obtained from the previous steps are adjusted as follows. The allocation is reduced to 2 workloads in the strata of the international carriers and household goods movers with intercity transportation revenue of \$2 million or more. It is increased in strata

where detailed data are needed. It is also adjusted to meet the administrative restrictions mentioned in Section 5 and to preserve consistency with previous years' allocations.

7. FIRST STAGE SAMPLE DESIGN

The current first stage consists of selecting a twice replicated stratified sample of D.S.L.P.'s. The sample selection is different in class 1 strata than in the other strata. Class 1 strata cover class 1 D.S.L.P.'s which are D.S.L.P.'s earning 2 million or more dollars of intercity transportation revenue. The two sample selection procedures are described below. The selection is done by methodologists of Business Survey Methods Division.

7.1 Selection of D.S.L.P.'s in Class 1 Strata and Allocation of Workloads to Selected D.S.L.P.'s.

All class 1 D.S.L.P.'s are selected with probability one. The reason for this approach is that these D.S.L.P.'s are known to be heterogeneous with respect to the principal statistics estimated.

Each class 1 D.S.L.P. next must be assigned a number of workloads for each replicate of the sample. This assignment has to be derived from the stratum allocation which was obtained through the procedure described in Section 6. The distribution of the stratum allocation to individual D.S.L.P.'s is done as follows. Let the stratum allocation be x workloads and let the number of D.S.L.P.'s in the stratum be d . One workload is assigned per replicate for each D.S.L.P. in the stratum so a total of $2d$ workloads are assigned. The remaining $w = (x - 2d)$ workloads are equally distributed to the two replicates. Then a probability proportional to size systematic sample of $(\frac{w}{2})$ D.S.L.P.'s is

drawn for each replicate. The measure of size used in the intercity transportation revenue. One workload is assigned per selection to the selected D.S.L.P.

7.2 Selection of D.S.L.P.'s in the Other Strata and the Allocation of Workloads to Selected D.S.L.P.'s

The selection of D.S.L.P.'s in other strata and the allocation of workloads to selected D.S.L.P.'s is done simultaneously as follows. Let the stratum allocation be k workloads. Each replicate in the stratum is assigned $(\frac{k}{T})$ workloads. A probability proportional to size systematic sample of $(\frac{k}{T})$ D.S.L.P.'s is drawn for each replicate. The measure of size used is the intercity transportation revenue. One workload is assigned per selection to the selected D.S.L.P. Finally, the workload assignments to selected D.S.L.P.'s are doubled.

7.3 Review of the Sample

The selected D.S.L.P.'s and the distribution of workloads are reviewed using the information from the previous survey, and adjustments to assignments are made, if warranted for practical reasons.

8. SUBSEQUENT STAGE(S) SAMPLE DESIGN

The subsequent stage(s) of the sample design consist(s) of selecting shipments from the files of each selected D.S.L.P. This selection is done by Statistics Canada Regional Operations Division staff at the D.S.L.P. The sample design is different depending on whether the filing system of the D.S.L.P. is small or large.

If the filing system is small (i.e. less than or equal to 2,000 shipments), then two independent systematic samples of 50 shipments are selected for each workload assigned to the D.S.L.P..

If the filing system is large, (i.e. greater than 2,000 shipments), then a sample of about 100 shipments is selected independently for each workload in two stages. For the first stage, an estimate of the number of bundles (defined as 100 shipments) is obtained and divided into 8 equal sections. Then a bundle is selected at random from each section and the selected bundle is located in the filing system. For the second stage, a systematic sample of shipments is selected from the selected bundle. The sample interval used for the systematic sampling is 8 so that 12 or 13 shipments are usually transcribed. Thus, the 8 sections provide approximately 100 transcriptions for each workload.

9. FIELD OPERATIONS

This section discusses the activities that involve the Statistics Canada Regional Operations staff: namely the training of the Regional Operations project managers, the planning of the collection, the collection itself and some special cases.

9.1 Training of the Regional Operation Project Managers

Every year, the Statistics Canada Regional Operations project managers are trained on all aspects of the survey. The training is five days long and is conducted during the month of March. The survey project manager as well as methodologists are involved in the training. A collection procedures manual is used for the in-class training. The Regional Operations project managers also receive on the job training by visiting a number of D.S.L.P.'s with different filing systems.

9.2 Planning of the Collection

Every spring, the Regional Operations project managers recruit the interviewers and administer a thorough training program. Then the interviewers with the advice of their Regional Operations project manager schedule their work, plan their itineraries and telephone D.S.L.P

officials for appointments. The collection takes place between May and September for the survey covering the shipments of the previous calendar year.

9.3 Overall Description of the Collection

When the interviewer gets on the D.S.L.P. premises, he/she has first to conduct an interview with the D.S.L.P. officials. During the interview, he/she will explain the survey, will mention the uses of the data, will estimate the time required to do the work and will complete a control form. The control form records information about the operations of the firm such as the total tonnage transported; the total number of shipments carried; the types of commodities carried and the percentage each type represents in the total transportation revenue; and the filing system(s) used.

Often, the interviewer has a choice of filing systems which provide information on the items needed in this survey. The interviewer assesses the completeness of information on principal characteristics from various filing systems, and then chooses the most appropriate system.

Then the interviewer estimates the number of shipments in the selected filing system of the carriers. This estimation is needed to be able to properly select a sample of shipments and to calculate the weights of the sampled shipments. This estimation involves measurement when the filing system is neither numeric nor broken numeric.

After then, the interviewer selects the sample shipments and transcribes their characteristics. This latter operation is often difficult because it can be hard to understand the various documents and the coding used on some documents. The interviewer often has to interpret the information on the documents and to enter on the coding sheets the data in a format that would be accepted by the computer system.

Finally, the survey project manager and the methodologists are consulted whenever necessary to assist in the field operations.

9.4 Special Cases

This sub-section discusses synthesising, abortions and cancellations.

Synthesising is the construction of hypothetical workloads when a D.S.L.P. does not keep documents suitable for sampling. In such a case, the interviewer collects through an interview with the D.S.L.P. officials macro-information about the D.S.L.P. Then this information is sent to Transportation and Communications Division who constructs shipment data in a format accepted by the computer system.

Abortions are in-scope D.S.L.P.'s for which we have not obtained transcriptions nor macro-information. Examples of abortions are a D.S.L.P. which refuses to cooperate or a D.S.L.P. on strike. The contributions of the abortions are reflected in the estimates via imputations using previous year's data or via adjustments to the weights.

Finally, cancellations are D.S.L.P.'s which are identified as out-of-scope for the reference period. In spite of the efforts made in verifying the D.S.L.P.'s in the universe against several sources on the activity of the carriers, interviewers find out that some D.S.L.P.'s in the sample are out-of-scope for the reference period. In such cases, Head Office makes adjustments to the weights when a large number of cancellations occur within a stratum.

10. DATA PROCESSING

All data processing is carried out at Head Office. Incoming data first go through a manual edit procedure which uses the data collected on the control forms. If the shipment data are correct and complete, they are sent to Key-edit. A standard data record file is created by matching the incoming transcriptions and accompanying material with a check-in list called workload master file. Out-of-scope shipments are discarded. There

were about 59,000 out-of-scope shipments in the 1978 For-hire Trucking Survey, i.e. about 26.2% of the transcribed shipments were out-of-scope. Some types of out-of-scope shipments are shipments to or from the U.S.A.; shipments transported 15 miles or less from origin to destination; shipments which were off-highway; shipments which would be double counted as a result of interlining between road carriers; shipments which would be double counted because they were recorded by household goods movers who are van line agents and by the van lines themselves; shipments which relate to a period other than the reference period; shipments which did not bring any intercity transportation revenue; and records which relate to non-transportation services such as storage, packing, equipment rental, labour loading and unloading.

The in-scope shipment records are assigned Standard Geographic Codes, Standard Commodity Codes and the distance between the origin and destination of the shipment using respective computer libraries.

Missing fields and those failing edits are imputed. There are two major imputation procedures that may take place in the system. These are prorating which is arithmetic imputation using fixed relationships and simple Hot Deck which consists of matching the record with missing data to a "similar" record with complete data. Essentially these procedures take values (or codes) to be imputed from valid or complete records and are applied to records which are incomplete. These procedures are premised on the assumption that the characteristics of records within the same workload are similar.

Weights are finally assigned and the data file is passed to the estimation module.

Detailed diagnostics produced at each stage of data processing are used as a quality check on the data passing through the system.

11. ESTIMATION METHOD

The estimates are generated from a very small sample relative to the size of the population. As an example, the 1978 sample represented only about 0.5% of the shipments in-scope to the survey.

Each workload generates an independent estimate for its stratum as follows. First, using the estimated size of the filing system in shipments, the individual shipment data of the workload are expanded to obtain an estimate at the D.S.L.P. level. Next, the relative size of the D.S.L.P. to the stratum size in terms of intercity transportation revenue is used to expand the D.S.L.P. estimate to the stratum level.

The average of estimates from all workloads in a given replicate within a given stratum provides the replicate stratum estimate. These replicate estimates are averaged to derive an overall stratum estimate. Finally, these overall stratum estimates are aggregated to provide national estimates.

Standard errors of the estimates are calculated using the two replicated estimates for each stratum.

The tabulated estimates are reviewed to ensure a check on the accuracy of the weights as well as a general check on the quality of the estimates generated. Examples of the review are the comparisons of the estimates to the previous year estimates from the For-hire Trucking Survey and to the previous year estimates from the Motor Carrier Freight Survey.

12. FUTURE OF THE SURVEY

The survey is being re-designed. One of the objectives is to develop a new approach to the data collection to reduce the cost of collection per in-scope sampled shipment so that the sample size can be enlarged. The

possibility of using computer tapes as a vehicle for the reporting firms falls into this approach. The progress of the re-design project is being monitored by an interdepartmental committee involving Transport Canada, the Canadian Transport Commission and Statistics Canada.

ACKNOWLEDGEMENT

The content of this paper is based largely in work done by R. Sugavanam, Business Survey Methods Division, Statistics Canada.

RESUME

Cet article décrit la méthodologie de l'enquête sur le Transport routier de marchandises pour le compte d'autrui. Cette enquête fournit de bons exemples de contraintes administratives et opérationnelles rencontrées par les statisticiens d'enquêtes et par les équipes de collecte de données sur le terrain.

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TABLE 1

Description of the Frame of the 1978 Survey and of the Principal Statistics Estimated from the Survey Data by Intercity Revenue Group.

Statistics	Intercity Revenue			
	\$2,000,000 and more	\$500,000 to \$1,999,999	\$100,000 to \$499,999	Total
Number of D.S.L.P.'s in the frame	218	540	1,339	2,097
Sample allocation in shipments	90,800	83,200	51,000	225,000
Number of shipments used in tabulation	69,620	62,729	33,646	165,995
Estimated number of shipments in-scope to this survey	20,146,157	7,016,909	5,261,362	32,424,428
Estimated revenue (\$,000)	1,720,578	449,781	303,575	2,473,934
Estimated number of tons (,000)	62,703	36,743	22,800	122,426
Estimated number of ton-miles (,000)	16,594,065	5,277,815	3,120,894	24,992,774

TABLE 2

1977 For-hire Trucking Survey Expenditure by Functions

<u>Function</u>	<u>Expenditure</u>
Field Data Collection	\$295,000
Mangement, Operations	\$ 98,000
Data Processing	\$ 65,000
Methodological Support	\$ 30,000
Travel, Printing, Misc.	6,000
<hr/>	<hr/>
Total	\$494,000

CONSTRUCTION OF WORKING PROBABILITIES AND
JOINT SELECTION PROBABILITIES FOR FELLEGI'S
PPS SAMPLING SCHEME

G.H. Choudhry¹

A FORTRAN Subroutine to obtain the "working probabilities" for Fellegi's (1963) method of unequal probability sampling is given. The solution is obtained by an iterative procedure where the starting values for the $(k+1)$ th draw "working probabilities" are the solutions for the k th draw "working probabilities" and the iterative procedure is terminated when a prespecified accuracy is achieved. The limitation is that the Subroutine can only be used to obtain upto and including the 5th draw "working probabilities". It was observed that the convergence occurs very fast in double precision. Therefore all real variables have been declared as double precision. The joint selection probabilities π_{ij} 's i.e. the probability that both the i th and j th units are in the sample are obtained by summing the probabilities of selecting those samples that contain both the i th and j th units. The joint selection probabilities are required for the variance estimation of the Horvitz-Thompson estimator of population total of the characteristic of interest.

1. DESCRIPTION

Fellegi (1963) has proposed a method for selecting a sample of n (≥ 2) units draw by draw and without replacement out of N units in such a way that the probability for the i -th unit to be selected is equal to p_i at each of the n successive draws ($\sum_{i=1}^N p_i = 1$). This is achieved by determining $(n-1)$ sets of selection probabilities referred to as "working probabilities". Let the $(n-1)$ sets of "working probabilities" be

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$$p_i(k) = 0, \quad i = 1, 2, \dots, N; \quad k=2, 3, \dots, n$$

$$\sum_{i=1}^N p_i(k) = 1, \quad k = 2, 3, \dots, n.$$

The $p_i(k)$, $i = 2, 3, \dots, N$ are the "working probabilities" for selecting a unit at the k -th draw. The selection probabilities at the first draw $p_i(1)$ are given by

$$p_i(1) = p_i, \quad i = 1, 2, \dots, N.$$

Then the overall (unconditional) probability $\delta_i(k)$ of selecting i -th unit at the k -th draw is given by

$$\delta_i(k) = \sum_{(k-1; i)} [p_{i_1}(1) \times \frac{p_{i_2}(2)}{1-p_{i_1}(2)} \times \dots \times \frac{p_{i_{k-1}}(k-1)}{1-p_{i_1}(k-1)-p_{i_2}(k-1)\dots-p_{i_{k-2}}(k-1)} \\ \times \frac{p_i(k)}{1-p_{i_1}(k)-p_{i_2}(k)\dots-p_{i_{k-1}}(k)}]$$

$$i = 1, 2, \dots, N;$$

$$k = 1, 2, \dots, n$$

where $\sum_{(k-1; i)}$ denotes the summation over all possible ordered $(k-1)$ - tuples of $(i_1, i_2, \dots, i_{k-1})$ such that i_1, i_2, \dots, i_{k-1} are different integers between 1 and N , and none of them is equal to i . The condition that the i -th unit be selected with probability p_i at each of the n successive draws is satisfied by setting

$$\delta_i(k) = p_i, \quad i = 1, 2, \dots, N; \quad k = 1, 2, \dots, n.$$

We have $p_i(1) = p_i$, $i=1, 2, \dots, N$. Given that $p_i(2), \dots, p_i(k-1)$ have already been found, then approximate $p_i^{(0)}(k)$ by $p_i(k-1)$ and obtain $p_i^{(1)}(k)$ from the following formula

$$p_i^{(m)}(k) = p_i \times \left\{ \sum_{(k-1; i)} [p_{i_1}(1) \times \frac{p_{i_2}(2)}{1-p_{i_1}(2)} \times \dots \times \frac{p_{i_{k-1}}(k-1)}{1-p_{i_1}(k-1)-p_{i_2}(k-1)-\dots-p_{i_k}(k-1)} \right. \\ \left. \times \frac{1}{1-p_{i_1}^{(m-1)}(k)-p_{i_2}^{(m-1)}(k)-\dots-p_{i_k}^{(m-1)}(k)} \right\}^{-1}$$

by setting $m = 1$ for $i = 1, 2, \dots, N$. Repeat for $m = 2, 3, \dots$, etc. until $p_i^{(m)}(k) = p_i^{(m-1)}(k)$ for all i up to the required number of decimal places. The procedure is carried out for $k = 2, 3, \dots, n$, thus obtaining the $(n-1)$ sets of 'working probabilities' $p_i(2), p_i(3), \dots, p_i(n)$. Since i -th unit is selected with probability equal to p_i at each of the n successive draw, this property of the scheme makes it very attractive for rotating sample designs.

Bayless and Rao (1977) excluded Felleig's (1963) method from their study for $n=4$ due to convergence problems with the routine they used for obtaining the 'working probabilities'. They were not getting satisfactory answers even after a large number of iterations especially when $c.v.(x)^*$ was not small, where x -values are the sizes of the units in the population.

$$^* C.V.(x) = \frac{\left(\sum_{i=1}^N x_i^2 - \left(\sum_{i=1}^N x_i \right)^2 / N \right) / (N-1)}{\left(\sum_{i=1}^N x_i / N \right)}$$

We have used Fellegi's (1963) example for which C.V. (x) is small and two populations [Cochran (1978) and Kish (1965)] with larger values for C.V.(x) to obtain the 'working probabilities' for selecting upto 4 units. The iterative procedure was terminated when the change between two successive iterations was less than 10^{-6} for each element of the solution vector. The description of the populations and the number of iterations require to obtain the 'working probabilities' at each of the draws is given below:

Pop. No.	Source	N	C.V.(X)	No. of iterations at draw		
				2	3	4
1	Fellegi [1963, p. 198]	6	0.25	5	7	12
2	Cochran [1978, p. 152]	20	1.03	4	5	7
3	Kish [1965, p. 42]	20	1.19	4	6	8

It is noticed that for the three populations we have used, the convergence at each of the draws is obtained in a very few number of iterations although the number of iterations required at each successive draw increases. It should be remarked that the values of 'working probabilities' obtained for Fellegi's (1963) example agree with his values.

The joint selection probabilities are required for estimating the variance of the Horvitz-Thompson estimator

$$\hat{Y} = \frac{1}{n} \sum_{i \in s} \frac{y_i}{p_i}$$

of the total $Y = \sum_{i=1}^N y_i$ of y - variate of interest, where y_i is the value of y - variate pertaining to the i -th unit. Let π_{ij} denote the probability that both the i -th and j -th units are included in the sample, then π_{ij} , $i=1, 2, \dots, N-1$; $j = i+1, i+2, \dots, N$ can be obtained as follows:

Let $\delta_{ij}(k, \ell)$ denote the probability that the i -th unit was selected at the k -th draw and the j -th unit was selected at the ℓ th draw ($\ell > k$). The probability $\delta_{ij}(k, \ell)$ is given by:

$$\delta_{ij}(k, \ell) = \sum_{(\ell-2; i, j)} [p_{i_1}^{(1)} \times \frac{p_{i_2}^{(2)}}{1-p_{i_1}^{(2)}} \times \dots \times \frac{p_{i_{k-1}}^{(k-1)}}{1-p_{i_1}^{(k-1)}-p_{i_2}^{(k-1)} \dots -p_{i_{k-1}}^{(k-1)}} \times$$

$$\frac{p_{i_k}^{(k)}}{1-p_{i_1}^{(k)}-p_{i_2}^{(k)} \dots -p_{i_{k-1}}^{(k)}} \times \frac{p_{i_{k+1}}^{(k+1)}}{1-p_{i_1}^{(k+1)}-p_{i_2}^{(k+1)} \dots -p_{i_{k-1}}^{(k+1)}-p_{i_k}^{(k+1)}} \times$$

$$\dots \times \frac{p_{i_{\ell-1}}^{(\ell-1)}}{1-p_{i_1}^{(\ell-1)}-p_{i_2}^{(\ell-1)} \dots -p_{i_{k-1}}^{(\ell-1)}-p_{i_k}^{(\ell-1)}-p_{i_{k+1}}^{(\ell-1)} \dots -p_{i_{\ell-2}}^{(\ell-1)}} \times$$

$$\frac{p_j^{(\ell)}}{1-p_{i_1}^{(\ell)}-p_{i_2}^{(\ell)} \dots -p_{i_{k-1}}^{(\ell)}-p_{i_k}^{(\ell)}-p_{i_{k+1}}^{(\ell)} \dots -p_{i_{\ell-1}}^{(\ell)}}],$$

$$i \neq j = 1, 2, \dots, N;$$

$$k = 1, 2, \dots, n-1;$$

$$\ell = k+1, k+2, \dots, n$$

where $\sum_{(\ell-2; i, j)}$ denotes the summation over all possible ordered $(\ell-2)$ -tuples of $(i_1, i_2, \dots, i_{k-1}, i_{k+1}, \dots, i_{\ell-1})$ such that $i_1, i_2, \dots, i_{k-1}, i_{k+1}, \dots, i_{\ell-1}$ are different integers between 1 and N, and none of them is equal to i or j. Then π_{ij} , the probability that both i-th and j-th units are included in the sample, is given by

$$\pi_{ij} = \sum_{k=1}^{n-1} \sum_{\ell=k+1}^n [\delta_{ij}(k, \ell) + \delta_{ji}(k, \ell)],$$

$$i = 1, 2, \dots, N-1;$$

$$j = i+1, i+2, \dots, N.$$

Structure

SUBROUTINE WKPROB (N, NS, MA, P, P1, P2, P3, P4, Q1, Q2, DEL,
MAX, ACC, PI, TOL, IFAULT)

Formal parameters - all real parameters in double precision.

N Integer Input: number of units in the population
NS Integer Input: sample size, $2 \leq NS \leq 5$
MA Integer Input: dimension of PI in the calling program
P Real Array(N) Input: contains the relative measure of sizes
of units in the sequence p_1, p_2, \dots, p_N ;

$$\sum_{i=1}^N p_i = 1$$

P1 Real Array (N) Output: working probabilities for selecting a unit
at the 2nd draw
P2 Real Array (N) Output: working probabilities for selecting a unit
at the 3rd draw
P3 Real Array (N) Output: working probabilities for selecting a unit
at the 4th draw

P4	Real Array(N)	Output: working probabilities for selecting a unit at the 5th draw.
Q1	Real Array(N)	Workspace
Q2	Real Array(N)	Workspace
DEL	Real Array (MA,NS)	Workspace
MAX	Integer	Input: maximum number of iterations allowed for obtaining each set of working probabilities
ACS	Real	Input: desired accuracy of the working probabilities
P1	Real Array (MA,MA)	Output: matrix returning the joint selection probabilities π_{ij} , $i = 1, 2, \dots, N-1$ $j = i + 1, i + 2, \dots, N$
TOL	Real	Input: maximum allowed value for the absolute difference between $\sum_{i=1}^N p_i$ and the number one
IFault	Integer	Output: failure indicator

Failure Indications

- IFault = 0 normal termination
- = 1 one or more of $p_i > (1/NS)$
- = 2 $DABS(\sum_{i=1}^N p_i - 1.0) > TOL$
- = 3 both conditions 1 and 2 occur
- = 4 sample size greater than 5
- = 5 desired accuracy was not obtained in maximum allowed number of iterations

ACKNOWLEDGEMENT

The author wishes to thank the referee for some helpful comments.

RESUME

L'auteur expose un sous-programme FORTRAN visant à obtenir les "probabilités de travail" à l'aide de la méthode d'échantillonnage à probabilités inégales de Fellegi (1963). On obtient la solution par une méthode itérative dans laquelle les valeurs de départ des "probabilités de travail" du $(k-1)$ -ième tirage sont la solution du k -ième tirage des "probabilités de travail"; ce calcul prend fin lorsque l'on atteint un niveau de précision déterminé à l'avance. Le sous-programme est limité car son utilisation ne peut dépasser le 5^e tirage des "probabilités de travail". On a observé que la convergence se produit très rapidement en double précision. Par conséquent, toutes les variables réelles ont été déclarées en double précision. Les probabilités conjointes de sélection, c.-à-d. la probabilité que les i -ième et j -ième unités fassent toutes deux partie de l'échantillon, s'obtiennent par sommation des probabilités de sélection des échantillons contenant les deux unités en cause. Les probabilités conjointes de sélection sont nécessaires à l'estimation de la variance de l'estimateur Horvitz-Thompson du total de la caractéristique à l'étude dans la population.

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C.....SUBROUTINE TO OBTAIN WORKING PROBABILITIES AND	00001000
C.....JOINT SELECTION PROBABILITIES FOR FELLEGI'S PPS	00002000
C.....SAMPLING SCHEME. REF: 1963 JASA 58 , PP 183-201 .	00003000
C.....	00004000
SUBROUTINE WKPROB(N,NS,MA,P,P1,P2,P3,P4,Q1,Q2,DEL,MAX,ACC,	00005000
1 PI,TOL,IFAU1)	00006000
IMPLICIT REAL*8(A-H,O-Z)	00007000
DIMENSION P(N),P1(N),P2(N),P3(N),P4(N),Q1(N),Q2(N),DEL(MA,NS),	00008000
1 PI(MA,MA)	00009000
C.....N IS POPULATION SIZE.	00010000
C.....NS IS SAMPLE SIZE AND CAN HAVE VALUES 2 , 3 , 4 , 5 .	00011000
C.....MA IS MAXIMUM DIMENSION OF PI IN THE MAIN PROGRAM.	00012000
C.....P IS THE VECTOR OF GIVEN PROBABILITIES . SUM P = 1.0	00013000
C.....P , P1 , P2 , P3 , P4 AND P5 ARE SELECTION PROBABILITIES AT	00014000
C.....1ST , 2ND , 3RD , 4-TH AND 5-TH DRAWS RESPECTIVELY .	00015000
C.....Q1 , Q2 , DEL WORK SPACE .	00016000
CONTINUE	00017000
C.....MAX IS THE MAXIMUM NUMBER OF ITERATIONS ALLOWED TO OBTAIN	00018000
C.....THE WORKING PROBABILITIES.	00019000
C.....ACC IS THE DESIRED ACCURACY OF THE WORKING PROBABILITIES.	00020000
C.....PI IS THE OUTPUT RETURNING THE JOINT SELECTION PROBABILITIES .	00021000
C.....TOL IS THE PARAMETER SO THAT SUM P CANNOT DEVIATE FROM 1.0 BY	00022000
C.....MORE THAN THE VALUE OF TOL.	00023000
C.....IFAU1 IS FAILURE INDICATOR TAKING THE FOLLOWING VALUES:	00024000
C.....	00025000
C..... 0 IF PI COMPUTED, NORMAL TERMINATION.	00026000
C..... 1 IF NS*P .GE.1.0 FOR ONE OR MORE P VALUES .	00027000
C..... 2 IF DABS(SUM P - 1.0) IS GREATER THAN TOL.	00028000
C..... 3 IF BOTH OF THE ABOVE TWO CONDITIONS.	00029000
C..... 4 IF NS , THE SAMPLE SIZE, IS GREATER THAN 5 .	00030000
C..... 5 IF DESIRED ACCURACY NOT OBTAINED IN MAXIMUM	00031000
C..... ALLOWED NUMBER OF ITERATIONS.	00032000
C.....	00033000
IFAU1=4	00034000
IF(NS.GT.5) RETURN	00035000
IFAU1=0	00036000
IFAU2=0	00037000
IDRAW=1	00038000
XNS=NS	00039000
SUMP=0.0	00040000
DO 1 I=1,N	00041000
SUMP=SUMP+P(I)	00042000
Q1(I)=P(I)	00043000
DEL(I,1)=P(I)	00044000
IF(XNS*P(I).GT.1.0) IFAU1=1	00045000
1 CONTINUE	00046000
IF(DABS(SUMP-1.0).GT.TOL) IFAU2=2	00047000
IFAU1=IFAU1+IFAU2	00048000
IF(IFAU1.NE.0) RETURN	00049000
C.....	00050000

```
C.....SELECTING UNIT 2 .                                00051000
C.....                                                    00052000
    IDRAW=IDRAW+1                                           00053000
    A=0.0                                                    00054000
    DO 20 J=1,N                                             00055000
20  A=A+F0(N,J,P,Q1)                                       00056000
    ICOUNT=0                                                00057000
21  ICOUNT=ICOUNT+1                                         00058000
    IF(ICOUNT.GT.MAX) GO TO 999                             00059000
    DMAX=0.0                                                00060000
    DO 22 I=1,N                                             00061000
    DEN=A-F0(N,I,P,Q1)                                     00062000
    Q2(I)=P(I)/DEN                                         00063000
    DIFF=DABS(Q2(I)-Q1(I))                                 00064000
    IF(DIFF.GT.DMAX) DMAX=DIFF                             00065000
    Q1(I)=Q2(I)                                            00066000
    A=DEN+F0(N,I,P,Q1)                                     00067000
22  CONTINUE                                               00068000
    IF(DMAX.GT.ACC) GO TO 21                               00069000
    WRITE(3,24) IDRAW,ICOUNT                               00070000
24  FORMAT(1H1,////,20X,'WORKING PROBABILITIES AT DRAW    : ',15, 00071000
1      ////,20X,'NUMBER OF ITERATIONS FOR CONVERGENCE = ',16, 00072000
2      ////)                                              00073000
    DO 25 I=1,N                                             00074000
    P1(I)=Q1(I)                                            00075000
    DEL(I,2)=P1(I)                                         00076000
    WRITE(3,26) I,P1(I)                                    00077000
25  CONTINUE                                               00078000
26  FORMAT(1H0,20X,' PROB ( ',12,' ) = ',D14.6)          00079000
    IF(IDRAW.EQ.NS) GO TO 550                             00080000
C.....                                                    00081000
C.....SELECTING UNIT 3.                                    00082000
C.....                                                    00083000
    IDRAW=IDRAW+1                                           00084000
    A=0.0                                                    00085000
    DO 30 J=1,N                                             00086000
    DO 30 K=1,N                                             00087000
30  A=A+F1(N,J,K,P,P1,Q1)                                  00088000
    ICOUNT=0                                                00089000
37  ICOUNT=ICOUNT+1                                         00090000
    IF(ICOUNT.GT.MAX) GO TO 999                             00091000
    DMAX=0.0                                                00092000
    DO 31 I=1,N                                             00093000
    S1=0.0                                                  00094000
    DO 32 J=1,N                                             00095000
    S1=S1+F1(N,I,J,P,P1,Q1)+F1(N,J,J,P,P1,Q1)+F1(N,J,I,P,P1,Q1) 00096000
32  CONTINUE                                               00097000
    DEN=A-S1+2.0*F1(N,I,I,P,P1,Q1)                       00098000
    Q2(I)=P(I)/DEN                                         00099000
    DIFF=DABS(Q2(I)-Q1(I))                                 00100000
```

IF(DIFF.GT.DMAX) DMAX=DIFF	00101000
Q1(I)=Q2(I)	00102000
S1=0.0	00103000
DO 33 J=1,N	00104000
S1=S1+F1(N,I,J,P,P1,Q1)+F1(N,J,J,P,P1,Q1)+F1(N,J,I,P,P1,Q1)	00105000
33 CONTINUE	00106000
A=DEN+S1-2.0*F1(N,I,I,P,P1,Q1)	00107000
31 CONTINUE	00108000
IF(DMAX.GT.ACC) GO TO 37	00109000
WRITE(3,24) IDRAW,ICOUNT	00110000
DO 36 I=1,N	00111000
P2(I)=Q1(I)	00112000
DEL(I,3)=P2(I)	00113000
WRITE(3,26) I,P2(I)	00114000
36 CONTINUE	00115000
IF(IDRAW.EQ.NS) GO TO 550	00116000
C.....	00117000
C.....SELECTING UNIT 4.	00118000
C.....	00119000
IDRAW=IDRAW+1	00120000
A=0.0	00121000
DO 40 J=1,N	00122000
DO 40 K=1,N	00123000
DO 40 L=1,N	00124000
40 A=A+F2(N,J,K,L,P,P1,P2,Q1)	00125000
ICOUNT=0	00126000
49 ICOUNT=ICOUNT+1	00127000
IF(ICOUNT.GT.MAX) GO TO 999	00128000
DMAX=0.0	00129000
DO 41 I=1,N	00130000
S1=0.0	00131000
S2=0.0	00132000
DO 42 J=1,N	00133000
DO 43 K=1,N	00134000
S1=S1+F2(N,I,J,K,P,P1,P2,Q1)+F2(N,J,J,K,P,P1,P2,Q1)	00135000
1 +F2(N,J,I,K,P,P1,P2,Q1)+F2(N,J,K,I,P,P1,P2,Q1)	00136000
2 +F2(N,J,K,J,P,P1,P2,Q1)+F2(N,J,K,K,P,P1,P2,Q1)	00137000
43 CONTINUE	00138000
S2=S2+2.0*F2(N,I,I,J,P,P1,P2,Q1)+F2(N,J,J,I,P,P1,P2,Q1)	00139000
1 +2.0*F2(N,I,J,I,P,P1,P2,Q1)+F2(N,J,I,J,P,P1,P2,Q1)	00140000
2 +2.0*F2(N,J,I,I,P,P1,P2,Q1)+F2(N,I,J,J,P,P1,P2,Q1)	00141000
3 +2.0*F2(N,J,J,J,P,P1,P2,Q1)	00142000
42 CONTINUE	00143000
DEN=A-S1+S2-6.0*F2(N,I,I,I,P,P1,P2,Q1)	00144000
Q2(I)=P(I)/DEN	00145000
DIFF=DABS(Q2(I)-Q1(I))	00146000
IF(DIFF.GT.DMAX) DMAX=DIFF	00147000
Q1(I)=Q2(I)	00148000
S1=0.0	00149000
S2=0.0	00150000

DO 44 J=1,N	00151000
DO 45 K=1,N	00152000
S1=S1+F2(N,I,J,K,P,P1,P2,Q1)+F2(N,J,J,K,P,P1,P2,Q1)	00153000
1 +F2(N,J,I,K,P,P1,P2,Q1)+F2(N,J,K,I,P,P1,P2,Q1)	00154000
2 +F2(N,J,K,J,P,P1,P2,Q1)+F2(N,J,K,K,P,P1,P2,Q1)	00155000
45 CONTINUE	00156000
S2=S2+2.0*F2(N,I,I,J,P,P1,P2,Q1)+F2(N,J,J,I,P,P1,P2,Q1)	00157000
1 +2.0*F2(N,I,J,I,P,P1,P2,Q1)+F2(N,J,I,J,P,P1,P2,Q1)	00158000
2 +2.0*F2(N,J,I,I,P,P1,P2,Q1)+F2(N,I,J,J,P,P1,P2,Q1)	00159000
3 +2.0*F2(N,J,J,J,P,P1,P2,Q1)	00160000
44 CONTINUE	00161000
A=DEN+S1-S2+6.0*F2(N,I,I,I,P,P1,P2,Q1)	00162000
41 CONTINUE	00163000
IF(DMAX.GT.ACC) GO TO 49	00164000
WRITE(3,24) IDRAW,ICOUNT	00165000
DO 47 I=1,N	00166000
P3(I)=Q1(I)	00167000
DEL(I,4)=P3(I)	00168000
WRITE(3,26) I,P3(I)	00169000
47 CONTINUE	00170000
IF(IDRAW.EQ.NS) GO TO 550	00171000
C.....	00172000
C.....SELECTING UNIT 5.	00173000
C.....	00174000
IDRAW=IDRAW+1	00175000
A=0.0	00176000
DO 50 J=1,N	00177000
DO 50 K=1,N	00178000
DO 50 L=1,N	00179000
DO 50 M=1,N	00180000
50 A=A+F3(N,J,K,L,M,P,P1,P2,P3,Q1)	00181000
ICOUNT=0	00182000
59 ICOUNT=ICOUNT+1	00183000
IF(ICOUNT.GT.MAX) GO TO 999	00184000
DMAX=0.0	00185000
DO 51 I=1,N	00186000
S1=0.0	00187000
S2=0.0	00188000
S3=0.0	00189000
DO 52 J=1,N	00190000
DO 53 K=1,N	00191000
DO 54 L=1,N	00192000
S1=S1+F3(N,J,K,I,L,P,P1,P2,P3,Q1)+F3(N,J,K,J,L,P,P1,P2,P3,Q1)	00193000
1 +F3(N,J,K,K,L,P,P1,P2,P3,Q1)+F3(N,I,J,K,L,P,P1,P2,P3,Q1)	00194000
2 +F3(N,J,J,K,L,P,P1,P2,P3,Q1)+F3(N,J,I,K,L,P,P1,P2,P3,Q1)	00195000
3 +F3(N,J,K,L,I,P,P1,P2,P3,Q1)+F3(N,J,K,L,J,P,P1,P2,P3,Q1)	00196000
4 +F3(N,J,K,L,K,P,P1,P2,P3,Q1)+F3(N,J,K,L,L,P,P1,P2,P3,Q1)	00197000
54 CONTINUE	00198000
S2=S2+2.0*F3(N,I,J,I,K,P,P1,P2,P3,Q1)+F3(N,J,J,I,K,P,P1,P2,P3,Q1)	00199000
1 +2.0*F3(N,J,I,I,K,P,P1,P2,P3,Q1)+F3(N,J,I,J,K,P,P1,P2,P3,Q1)	00200000


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2      +2.0*F3(N,J,J,J,K,P,P1,P2,P3,Q1)+F3(N,I,J,J,K,P,P1,P2,P3,Q1) 00201000
3      +2.0*F3(N,I,I,J,K,P,P1,P2,P3,Q1)+F3(N,J,K,J,I,P,P1,P2,P3,Q1) 00202000
4      +2.0*F3(N,J,K,I,I,P,P1,P2,P3,Q1)+F3(N,J,K,K,I,P,P1,P2,P3,Q1) 00203000
5      +2.0*F3(N,I,J,K,I,P,P1,P2,P3,Q1)+F3(N,J,J,K,I,P,P1,P2,P3,Q1) 00204000
6      +2.0*F3(N,J,I,K,I,P,P1,P2,P3,Q1)+F3(N,J,K,I,J,P,P1,P2,P3,Q1) 00205000
7      +2.0*F3(N,J,K,J,J,P,P1,P2,P3,Q1)+F3(N,J,K,K,J,P,P1,P2,P3,Q1) 00206000
8      +2.0*F3(N,J,J,K,J,P,P1,P2,P3,Q1)+F3(N,J,I,K,J,P,P1,P2,P3,Q1) 00207000
9      +      F3(N,J,K,I,K,P,P1,P2,P3,Q1)+F3(N,J,K,J,K,P,P1,P2,P3,Q1) 00208000
A      +2.0*F3(N,J,K,K,K,P,P1,P2,P3,Q1)+F3(N,I,J,K,J,P,P1,P2,P3,Q1) 00209000
B      +      F3(N,I,J,K,K,P,P1,P2,P3,Q1)+F3(N,J,J,K,K,P,P1,P2,P3,Q1) 00210000
C      +      F3(N,J,I,K,K,P,P1,P2,P3,Q1)                                00211000
53 CONTINUE                                                                00212000
   S3=S3+6.0*F3(N,I,I,I,J,P,P1,P2,P3,Q1)                                00213000
1      +6.0*F3(N,I,J,I,I,P,P1,P2,P3,Q1)                                00214000
2      +2.0*F3(N,J,J,I,I,P,P1,P2,P3,Q1)                                00215000
3      +6.0*F3(N,J,I,I,I,P,P1,P2,P3,Q1)                                00216000
4      +2.0*F3(N,J,J,J,I,P,P1,P2,P3,Q1)                                00217000
5      +2.0*F3(N,J,I,J,I,P,P1,P2,P3,Q1)                                00218000
6      +2.0*F3(N,I,J,J,I,P,P1,P2,P3,Q1)                                00219000
7      +6.0*F3(N,I,I,J,I,P,P1,P2,P3,Q1)                                00220000
8      +2.0*F3(N,J,J,I,J,P,P1,P2,P3,Q1)                                00221000
9      +2.0*F3(N,J,I,I,J,P,P1,P2,P3,Q1)                                00222000
A      +6.0*F3(N,J,J,J,J,P,P1,P2,P3,Q1)                                00223000
B      +2.0*F3(N,J,I,J,J,P,P1,P2,P3,Q1)                                00224000
C      +2.0*F3(N,I,J,I,J,P,P1,P2,P3,Q1)                                00225000
D      +2.0*F3(N,I,J,J,J,P,P1,P2,P3,Q1)                                00226000
E      +2.0*F3(N,I,I,J,J,P,P1,P2,P3,Q1)                                00227000
52 CONTINUE                                                                00228000
   DEN=A-S1+S2-S3+24.0*F3(N,I,I,I,I,P,P1,P2,P3,Q1)                    00229000
   Q2(I)=P(I)/DEN                                                         00230000
   DIFF=DABS(Q2(I)-Q1(I))                                                 00231000
   IF(DIFF.GT.DMAX) DMAX=DIFF                                             00232000
   Q1(I)=Q2(I)                                                            00233000
   S1=0.0                                                                00234000
   S2=0.0                                                                00235000
   S3=0.0                                                                00236000
   DO 55 J=1,N                                                            00237000
   DO 56 K=1,N                                                            00238000
   DO 57 L=1,N                                                            00239000
   S1=S1+F3(N,J,K,I,L,P,P1,P2,P3,Q1)+F3(N,J,K,J,L,P,P1,P2,P3,Q1)    00240000
1      +F3(N,J,K,K,L,P,P1,P2,P3,Q1)+F3(N,I,J,K,L,P,P1,P2,P3,Q1)    00241000
2      +F3(N,J,J,K,L,P,P1,P2,P3,Q1)+F3(N,J,I,K,L,P,P1,P2,P3,Q1)    00242000
3      +F3(N,J,K,L,I,P,P1,P2,P3,Q1)+F3(N,J,K,L,J,P,P1,P2,P3,Q1)    00243000
4      +F3(N,J,K,L,K,P,P1,P2,P3,Q1)+F3(N,J,K,L,L,P,P1,P2,P3,Q1)    00244000
57 CONTINUE                                                                00245000
   S2=S2+2.0*F3(N,I,J,I,K,P,P1,P2,P3,Q1)+F3(N,J,J,I,K,P,P1,P2,P3,Q1) 00246000
1      +2.0*F3(N,J,I,I,K,P,P1,P2,P3,Q1)+F3(N,J,I,J,K,P,P1,P2,P3,Q1) 00247000
2      +2.0*F3(N,J,J,J,K,P,P1,P2,P3,Q1)+F3(N,I,J,J,K,P,P1,P2,P3,Q1) 00248000
3      +2.0*F3(N,I,I,J,K,P,P1,P2,P3,Q1)+F3(N,J,K,J,I,P,P1,P2,P3,Q1) 00249000
4      +2.0*F3(N,J,K,I,I,P,P1,P2,P3,Q1)+F3(N,J,K,K,I,P,P1,P2,P3,Q1) 00250000

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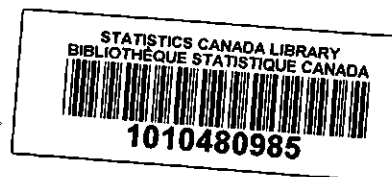
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5      +2.0*F3(N,I,J,K,I,P,P1,P2,P3,Q1)+F3(N,J,J,K,I,P,P1,P2,P3,Q1) 00251000
6      +2.0*F3(N,J,I,K,I,P,P1,P2,P3,Q1)+F3(N,J,K,I,J,P,P1,P2,P3,Q1) 00252000
7      +2.0*F3(N,J,K,J,J,P,P1,P2,P3,Q1)+F3(N,J,K,K,J,P,P1,P2,P3,Q1) 00253000
8      +2.0*F3(N,J,J,K,J,P,P1,P2,P3,Q1)+F3(N,J,I,K,J,P,P1,P2,P3,Q1) 00254000
9      +      F3(N,J,K,I,K,P,P1,P2,P3,Q1)+F3(N,J,K,J,K,P,P1,P2,P3,Q1) 00255000
A      +2.0*F3(N,J,K,K,K,P,P1,P2,P3,Q1)+F3(N,I,J,K,J,P,P1,P2,P3,Q1) 00256000
B      +      F3(N,I,J,K,K,P,P1,P2,P3,Q1)+F3(N,J,J,K,K,P,P1,P2,P3,Q1) 00257000
C      +      F3(N,J,I,K,K,P,P1,P2,P3,Q1) 00258000
56 CONTINUE 00259000
   S3=S3+6.0*F3(N,I,I,I,J,P,P1,P2,P3,Q1) 00260000
1      +6.0*F3(N,I,J,I,I,P,P1,P2,P3,Q1) 00261000
2      +2.0*F3(N,J,J,I,I,P,P1,P2,P3,Q1) 00262000
3      +6.0*F3(N,J,I,I,I,P,P1,P2,P3,Q1) 00263000
4      +2.0*F3(N,J,J,J,I,P,P1,P2,P3,Q1) 00264000
5      +2.0*F3(N,J,I,J,I,P,P1,P2,P3,Q1) 00265000
6      +2.0*F3(N,I,J,J,I,P,P1,P2,P3,Q1) 00266000
7      +6.0*F3(N,I,I,J,I,P,P1,P2,P3,Q1) 00267000
8      +2.0*F3(N,J,J,I,J,P,P1,P2,P3,Q1) 00268000
9      +2.0*F3(N,J,I,I,J,P,P1,P2,P3,Q1) 00269000
A      +6.0*F3(N,J,J,J,J,P,P1,P2,P3,Q1) 00270000
B      +2.0*F3(N,J,I,J,J,P,P1,P2,P3,Q1) 00271000
C      +2.0*F3(N,I,J,I,J,P,P1,P2,P3,Q1) 00272000
D      +2.0*F3(N,I,J,J,J,P,P1,P2,P3,Q1) 00273000
E      +2.0*F3(N,I,I,J,J,P,P1,P2,P3,Q1) 00274000
55 CONTINUE 00275000
   A=DEN+S1-S2+S3-24.0*F3(N,I,I,I,I,P,P1,P2,P3,Q1) 00276000
51 CONTINUE 00277000
   IF(DMAX.GT.ACC) GO TO 59 00278000
   WRITE(3,24) IDRAW,ICOUNT 00279000
   DO 60 I=1,N 00280000
   P4(I)=Q1(I) 00281000
   DEL(I,5)=P4(I) 00282000
   WRITE(3,26) I,P4(I) 00283000
60 CONTINUE 00284000
550 CONTINUE 00285000
C.....CALCULATE THE JOINT SELECTION PROBABILITIES . 00286000
   DO 551 I=1,N 00287000
   DO 552 J=1,N 00288000
   IF(J.EQ.1) GO TO 552 00289000
   S1=0.0 00290000
   S2=0.0 00291000
   S3=0.0 00292000
   T1=DEL(I,1)*DEL(J,2)/(1.0-DEL(I,2)) 00293000
   IF(NS.EQ.2) GO TO 590 00294000
   DO 553 K=1,N 00295000
   IF(K.EQ.1.OR.K.EQ.J) GO TO 553 00296000
   SN=DEL(I,1)*DEL(K,2)*DEL(J,3) 00297000
   SD=(1.0-DEL(I,2))*(1.0-DEL(I,3)-DEL(K,3)) 00298000
   T2=SN/SD 00299000
   SN=DEL(K,1)*DEL(I,2)*DEL(J,3) 00300000

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SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(I,3))	00301000
T3=SN/SD	00302000
S1=S1+T2+T3	00303000
IF(NS.EQ.3) GO TO 553	00304000
DO 554 L=1,N	00305000
IF(L.EQ.I.OR.L.EQ.J.OR.L.EQ.K) GO TO 554	00306000
SN=DEL(I,1)*DEL(K,2)*DEL(L,3)*DEL(J,4)	00307000
SD=(1.0-DEL(I,2))*(1.0-DEL(I,3)-DEL(K,3))	00308000
1 *(1.0-DEL(I,4)-DEL(K,4)-DEL(L,4))	00309000
T4=SN/SD	00310000
SN=DEL(K,1)*DEL(I,2)*DEL(L,3)*DEL(J,4)	00311000
SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(I,3))	00312000
1 *(1.0-DEL(K,4)-DEL(I,4)-DEL(L,4))	00313000
T5=SN/SD	00314000
SN=DEL(K,1)*DEL(L,2)*DEL(I,3)*DEL(J,4)	00315000
SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(L,3))	00316000
1 *(1.0-DEL(K,4)-DEL(L,4)-DEL(I,4))	00317000
T6=SN/SD	00318000
S2=S2+T4+T5+T6	00319000
IF(NS.EQ.4) GO TO 554	00320000
DO 555 M=1,N	00321000
IF(M.EQ.I.OR.M.EQ.J.OR.M.EQ.K.OR.M.EQ.L) GO TO 555	00322000
SN=DEL(I,1)*DEL(K,2)*DEL(L,3)*DEL(M,4)*DEL(J,5)	00323000
SD=(1.0-DEL(I,2))*(1.0-DEL(I,3)-DEL(K,3))	00324000
1 *(1.0-DEL(I,4)-DEL(K,4)-DEL(L,4))	00325000
2 *(1.0-DEL(I,5)-DEL(K,5)-DEL(L,5)-DEL(M,5))	00326000
T7=SN/SD	00327000
SN=DEL(K,1)*DEL(I,2)*DEL(L,3)*DEL(M,4)*DEL(J,5)	00328000
SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(I,3))	00329000
1 *(1.0-DEL(K,4)-DEL(I,4)-DEL(L,4))	00330000
2 *(1.0-DEL(K,5)-DEL(I,5)-DEL(L,5)-DEL(M,5))	00331000
T8=SN/SD	00332000
SN=DEL(K,1)*DEL(L,2)*DEL(I,3)*DEL(M,4)*DEL(J,5)	00333000
SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(L,3))	00334000
1 *(1.0-DEL(K,4)-DEL(L,4)-DEL(I,4))	00335000
2 *(1.0-DEL(K,5)-DEL(L,5)-DEL(I,5)-DEL(M,5))	00336000
T9=SN/SD	00337000
SN=DEL(K,1)*DEL(L,2)*DEL(M,3)*DEL(I,4)*DEL(J,5)	00338000
SD=(1.0-DEL(K,2))*(1.0-DEL(K,3)-DEL(L,3))	00339000
1 *(1.0-DEL(K,4)-DEL(L,4)-DEL(M,4))	00340000
2 *(1.0-DEL(K,5)-DEL(L,5)-DEL(M,5)-DEL(I,5))	00341000
TA=SN/SD	00342000
S3=S3+T7+T8+T9+TA	00343000
555 CONTINUE	00344000
554 CONTINUE	00345000
553 CONTINUE	00346000
590 PI(I,J)=T1+S1+S2+S3	00347000
552 CONTINUE	00348000
551 CONTINUE	00349000
N1=N-1	00350000

DO 556 I=1,N1	00351000
J1=I+1	00352000
DO 557 J=J1,N	00353000
PI(I,J)=PI(I,J)+PI(J,I)	00354000
557 CONTINUE	00355000
556 CONTINUE	00356000
RETURN	00357000
999 IFAULT=5	00358000
WRITE(3,1000) IDRAW,MAX	00359000
1000 FORMAT(1H1,////,20X,'DRAW ',I2,' DID NOT CONVERGE IN ',	00360000
1 I4,' ITERATIONS .')	00361000
RETURN	00362000
END	00363000
DOUBLE PRECISION FUNCTION FO(N,J,P,Q1)	00364000
IMPLICIT REAL*8(A-H,O-Z)	00365000
DIMENSION P(N),Q1(N)	00366000
FO=P(J)/(1.0-Q1(J))	00367000
RETURN	00368000
END	00369000
DOUBLE PRECISION FUNCTION F1(N,J,K,P,P1,Q1)	00370000
IMPLICIT REAL*8(A-H,O-Z)	00371000
DIMENSION P(N),P1(N),Q1(N)	00372000
F1=P(J)*P1(K)/((1.0-P1(J))*(1.0-Q1(J)-Q1(K)))	00373000
RETURN	00374000
END	00375000
DOUBLE PRECISION FUNCTION F2(N,J,K,L,P,P1,P2,Q1)	00376000
IMPLICIT REAL*8(A-H,O-Z)	00377000
DIMENSION P(N),P1(N),P2(N),Q1(N)	00378000
F2=P(J)*P1(K)*P2(L)/((1.0-P1(J))*(1.0-P2(J)-P2(K))	00379000
1 *(1.0-Q1(J)-Q1(K)-Q1(L)))	00380000
RETURN	00381000
END	00382000
DOUBLE PRECISION FUNCTION F3(N,J,K,L,M,P,P1,P2,P3,Q1)	00383000
IMPLICIT REAL*8(A-H,O-Z)	00384000
DIMENSION P(N),P1(N),P2(N),P3(N),Q1(N)	00385000
F3=P(J)*P1(K)*P2(L)*P3(M)/((1.0-P1(J))*(1.0-P2(J)-P2(K))	00386000
1 *(1.0-P3(J)-P3(K)-P3(L))	00387000
2 *(1.0-Q1(J)-Q1(K)-Q1(L)-Q1(M)))	00388000
RETURN	00389000
END	00390000



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