## ENERGY LOSSES AT JUNCTION MANHOLES

## WITH A LATERAL

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#### Abstract

Head losses at sewer junctions of a main pipe with a lateral were studied for various junction geometries and pressurized flow characteristics. The junction parameters studied included the manhole base shape, the size and angle of entry of the lateral pipe, and various benchings installed in the junction manhole. The most important flow variable was the relative lateral inflow ( $=$ Q lateral/ Qoutlet). The junction head losses were affected most by the lateral pipe size and the relative lateral inflow.


## RESUME

On étudié les pertes d'énergie aux raccordements entre un Egout principal et un egout lateral en fonction de la forme du raccordement et des régimes d'écoulement forcé. Pour ce qui est du regard proprement dit, voici les parametres que nous avons retenus: forme de la base de l'ouvrage, divers types de banquettes de circulation dont il est muni, ainsi que diametre et angle d'arrivee de l'égout latéral. Quant au régime d'écoulement, la variable la plus importante a été le debit relatif de l'egout lateral (correspondant au rapport $\left.Q_{1 a t e ́ r a l} / Q_{\text {sortie }}\right)$. On a conclu que les chutes d'énergie de l'écoulement dans les raccordements tiennent surtout au diametre de l'égout latéral et au débit relatif de celui-ci.

## TABLE OF CONTENTS

PAGE
ABSTRACT ..... i
1.0 INTRODUCTION ..... 1
2.0 EXPERIMENTAL APPARATUS AND PROCEDURES ..... 1
2.1 Experimental Apparatus ..... 1
2.2 Experimental Procedures ..... 2
3.0 DATA ANALYSIS ..... 3
3.1 Energy Grade Lines for Test Pipes ..... 3
3.2 Calculation of Energy Losses at Junctions ..... 3
4.0 EXPERIMENTAL RESULTS ..... 5
4.1 Data Presentation ..... 6
4.2 Combined Head Loss Coefficients for Various Junction Configurations ..... 7
5.0 DISCUSSION OF RESULTS ..... 8
6.0 SUMMARY AND CONCLUSIONS ..... 10
7.0 REFERENCES ..... 12

## LIST OF TABLES

Table 1. Coefficients of Quadratic Regression Polynomials
Table 2. Combined Head Loss Coefficients for Various Lateral Inflows
Table 3. Comparison of Head Loss Coefficients from Various Sources

## LIST OF FIGURES

Figure 1. General Layout of Experimental Apparatus
Figure 2: Junction Box with a Lateral Pipe Inlet Assembly
Figure 3. Junction Manhole with Benchings Tested
Figure 4. Notation Sketch
Figure 5. Head Loss Coefficient vs the Relative Lateral Inflow

### 1.0 INTRODUCTION

Head losses at sewer pipe junctions have been investigated in the Hydraulics Laboratory of the Hydraulics Divison of the National Water Research Institute during the last several years. While the first phase of these investigations dealt with head losses at straight-flow-through junctions (4) the phase described in this report deals with head losses at junctions of a main pipe with a single lateral.

The main objectives of these studies were to evaluate junction head losses caused by a lateral inflow at various angles, and to investigate flow guidance devices for reduction of such losses. The basic junction structure studied was a square-base manhole with a main pipe and a lateral pipe entering the junction at three diferent angles $45^{\circ}, 60^{\circ}$ and $90^{\circ}$. A round-base manhole was investigated only for a $90^{\circ}$ lateral. In all experiments, the flow in the pipe was pressurized.

### 2.0 EXPERIMENTAL APPARATUS AND PROCEDURES

2.1 Experimental Apparatus

A general layout of the experimental apparatus is shown in Figure 1. The apparatus consists of two water supply tanks, the main pipe, the lateral pipe, the junction box, and a measuring weir box. The junction assembly is shown in Figure 2.

Both the main and lateral pipes were clear acrylic pipes. The internal diameter of the main pipe was 152 mm throughout the installation. Four lateral pipe sizes were used, with internal radii of 76 , 102, 127 and 152 mm , respectively. Both main and lateral pipe branches consisted of a number of sections which were typically 1.82 m long. The individual sections were connected by means of rubber sleeves and metal band clamps. The main pipe branches upstream and downstream of the junction were 16.47 m and 9.15 m long, respectively. The lateral pipe
was 3.80 m long. The hydraulic resistance of the main pipe was characterized in the earlier tests (4) by the roughness factor of $K=$ 0.034 mm (after the Colebrook-White equation).

The acrylic pipes were supported by a TV antenna beam resting on 13 scissor jacks. The pipe slope was changed manually by gradually adjusting individual jacks. In all runs, the pipes were set at slope of 0.01 . Piezometer openings were formed by drilling 3 mm diameter holes in pipe inverts at 0.6 m intervals. A total of 47 piezometer openings were drilled; 20 openings in the upstream pipe, 16 openings in the downstream pipe, and 11 openings in the lateral pipe. The lateral pipe piezometers were spaced at 0.305 m intervals. The piezometer openings were connected to a manometer board by Tygon tubing. On the board, piezometer heads were read with an accuracy of $\pm 0.5 \mathrm{~mm}$.

The dimensions of the square-base junction manhole are shown in Fig. 2. A round-base manhole was obtained by installing a cylindrical insert in the basic manhole. In all tests, the ends of the test pipes attached to the junction manhole had square edges.

Sketches of all junction geometries tested are shown in Fig. 3. The main variables included the manhole base shape, the lateral pipe size and angle, and the benching (mould and deflectors) inside the junction.

### 2.2 Experimental Procedures

When studying head losses in individual junction configurations, the main experimental variable was the relative discharge defined as $\psi_{13}=Q_{3} / Q_{1}$, where $Q_{3}$ is the lateral discharge, and $Q_{1}$ is the outlet discharge $\left(Q_{1}=Q_{3}+Q_{2}\right.$, where $Q_{2}$ is the main pipe discharge). To obtain various relative discharges, a constant main pipe discharge was established first and then the lateral discharge was varied over a fairly wide range. For each setting of the relative discharge, the flow rates through the lateral and outlet pipes were measured by taking
measuring weir readings, and all the piezometer readings were photographically recorded.

Using the observed piezometric readings and the velocity heads calculated from observed discharges, energy grade lines were determined for all pipe reaches and projected to the junction. The drops in the grade line, at the junction, for the main and lateral pipes were then taken as junction head losses for the main and lateral pipes, respectively.

Altogether 40 junction configurations were tested using the experimental procedures outlined above. Each junction configuration tested is referred to by a test series number in the following sections.

It should be emphasized that, in order to simplify the testing procedures, only the discharge through the lateral pipe was varied.

### 3.0 DATA ANALYSIS

3.1 Energy Grade Lines for Test Pipes

The first step in the processing of experimental data was to plot energy heads for individual piezometers. Using the least-squares method, straight lines were fitted through the plotted points in order to obtain energy grade lines for all three test pipes. Such a fitting procedure helped to reduce effects of random errors in individual piezometer readings. A typical plot of least-squares fitted energy grade lines is shown in Figure 4.

### 3.2 Calculation of Energy Losses at Junctions

To determine the energy losses across the junction, the upstream and downstream grade lines, for both the main and lateral pipes, were projected to the centreline of the junction and the difference between the upstream and downstream grade lines, measured at the junction centreline, was taken as the junction loss. The same
procedure has been used earlier by many other researchers (2, 4, 5, 7 and 9).

Following the customary procedures, the measured energy head losses were expressed as the head loss coefficient, one for the main pipe,

$$
\begin{equation*}
K_{12}=\frac{\Delta \dot{E}_{12}}{\frac{\bar{v}_{1}^{2}}{2 g}} \tag{1}
\end{equation*}
$$

and the other one for the lateral pipe

$$
\begin{equation*}
K_{13}=\frac{\Delta E_{13}}{\frac{\bar{v}_{1}{ }^{2}}{2 g}} \tag{2}
\end{equation*}
$$

where $K_{12}$ and $K_{13}$ are the head loss coefficients for the main and lateral pipes, respectively,
$\Delta E_{12}$ and $\Delta E_{13}$ are the junction energy head losses for the main and lateral pipe, respectively (see Fig. 4),
$\overline{\mathrm{V}}_{1} \quad$ is the mean velocity in the outlet pipe, and g is the acceleration due to the gravity.

Furthermore, in order to compare the effect of different junction configurations on the overall energy loss, a combined energy head loss coefficient was calculated as follows $(2,3)$ :

$$
\begin{equation*}
K_{c}=K_{12} \psi_{12}+K_{13} \psi_{13} \tag{3}
\end{equation*}
$$

where $K_{C}$ is the combined energy loss coefficient at the junction, $K_{12}$ and $K_{13}$ were defined before, and

$$
\psi_{12}=Q_{2} / Q_{1} \text { and } \psi_{13}=Q_{3} / Q_{1}
$$

where $Q_{2}$ is the main pipe discharge, $Q_{3}$ is the lateral discharge, and $Q_{1}$ is the outlet discharge. Note that $\psi_{12}+\psi_{13}=1.0$.

### 4.0 EXPERIMENTAL RESULTS

Head loss coefficients observed in the junction model were plotted against the flow ratios in Figure 5. There are altogether 40 graphs shown in Figure 5, representing 40 different junction configurations tested. The graphs numbers correspond to the earlier listed test numbers from 1 to 40 . Each graph indicates the angle between the main and lateral pipes (lateral angle), lateral pipe diameter ( $\phi$ ), and the junction benching geometry ( $M$ ). The main and outlet pipes sizes were identical in diameter ( 152 mm ).

The head loss coefficients, $\mathrm{K}_{12}$ and $\mathrm{K}_{13}$, which are plotted against the relative discharges, $\psi_{12}$ and $\psi_{13}$, in Fig. 5, typically varied from -0.5 to 12.0 . This range of values indicates that head loss coefficients can be either positive or negative depending on whether energy is transferred to or from the lateral flow. Thus negative values of both head loss coefficients are plausible under certain circumstances and have been reported earlier by several investigators (3, 6, and 8).

The negative values of the lateral head loss coefficient $K_{13}$ have been found for both $45^{\circ}$ and $90^{\circ}$ laterals for very small values of $\psi_{13}$ (say $\psi_{13}<0.3$ ), when almost all flow is passing through the main pipe. Under such circumstances, the water in the lateral appears to be drawn out by the main flow in a manner resembling ejector action. For these small lateral flows, the pressure in the lateral outlet is equal to that at the junction and the flow velocity is very small. As the water from the lateral is drawn into the main stream, an apparent energy gain takes place when basing the downstream pipe energy on the mean flow velocity in this pipe. However, this energy gain is only apparent, because the water flowing from the lateral must enter into the main flow region in which the velocity is below the mean value. In
connection with this discussion, two other points should be made negative head losses (apparent energy gains) are neglected in practical design, and the combined head loss coefficient described by Eq. 3 is always positive.

The above explanation of apparent negative head losses also applies to the main pipe head loss coefficient $K_{12}$ for the tested lateral angles $45^{\circ}$ and $60^{\circ}$, and low values of $\psi_{12}$ (i.e., almost all flow passing through the lateral).

Besides the physically plausible negative head loss coefficients, some extrapolations of observed $K_{12}$ 's also yielded small negative values for the lateral angle of $90^{\circ}$. Such negative values are not physically plausible and these extrapolations were omitted from the final plots shown in Fig. 5.

### 4.1 Data Presentation

In each experimental series, the head loss coefficients $K_{12}$ and $K_{13}$ were determined for about 5 to 8 different values of the relative discharges $\psi_{12}$ and $\psi_{13}$. Consequently, it was desirable to approximate such data by regression lines which could be used for data interpolation and extrapolation. After testing several regression models, a second degree polynomial model was found satisfactory for all 40 test series. This model was defined as follows:

$$
\begin{align*}
& K_{12}=a+b \psi_{12}+c \psi^{2}{ }_{12}  \tag{4}\\
& K_{13}=d+e \psi_{13}+f \psi_{13}^{2} \tag{5}
\end{align*}
$$

where $a, b, c, d, e$ and $f$ are fitted coefficients.
Equations (4) and (5) were derived with an assumption that the head loss coefficients do not vary with the Reynolds number which can be defined as $\operatorname{Re}=v D / \nu$, where $v$ is the mean combined flow velocity, $D$ is the pipe diameter, and $v$ is the kinematic viscosity. Thus for the experimental conditions studied, the head loss
coefficients are not affected by the combined discharge magnitude, but only by the division of discharges between the main and branch pipes. This assumption was based on extensive experimental evidence (5, 6 and 8) which indicated that, for Reynolds numbers greater than a certain threshold value, the head loss coefficients are independent of the Reynolds number. Although this threshold value was reported as low as $5 \times 10^{3}$, the more commonly accepted value is $10^{5}(6)$.

All the experiments reported here were performed in the range of Reynolds numbers from $1.8 \times 10^{5}$ to $3.4 \times 10^{5}$. The head loss coefficients derived from these experiments are directly applicable to sewer design which can be characterized by Reynolds numbers greater than $1.4 \times 10^{5}$. This minimum Re value follows from standard design practices which specify the minimum pipe diameter ( $D=0.305 \mathrm{~m}$ ) and the minimum flow velocity ( $v=0.61 \mathrm{~m} / \mathrm{s}$ ), and from assumed kinematic viscosity of $1.3 \times 10^{-6} \mathrm{~m}^{2} / \mathrm{s}$. In applications to laminar and transitional flow, which are outside of the scope of this report, the head loss coefficients are affected by the Reynolds number (1) and equations (4) and (5) are no longer applicable.

Using Eqs. (4) and (5) and the regression coefficients given in Table 2, the head loss coefficients $K_{12}$ and $K_{13}$ can be calculated for arbitrary relative discharges $\psi_{12}$ and $\psi_{13}$.

### 4.2 Combined Head Loss Coefficient for Various Junction Configurations

In order to compare the effect of different junction configurations on the overall energy loss, a combined head loss coefficient was calculated for each test series using Equation (3) and the data from Table 1. The results of such calculations are shown in Table 2.

The calculated $K_{c}$ values shown in Table 2 range from a low of -0.533 (test seriés 36 ) to a high value of 17.82 (test series 15 ). Because of such large variations, the comparisons of results for
various junction configurations are difficult. To facilitate such comparisons, the mean $\bar{K}_{C}$, the standard deviation about the mean, and the coefficient of variation $c_{V}=\sigma / \bar{K}_{c}$ were calculated for all test series and also presented in Table 2.

### 5.0 DISCUSSION OF RESULTS

The discussion which follows is based on the results of extensive tests of head losses at sewer junctions with a lateral. Forty different junction configurations with various lateral sizes and angles, junction benchings (moulds), and manhole bases were tested for pressurized flow conditions. Considering the need to test each configuration for a range of flow divisions, more than 250 experiments had to be conducted.

The head loss coefficients $K_{12}$ and $K_{13}$ shown in Fig. 5 varied with the relative discharges $\psi_{12}$ and $\psi_{13}$. Such variations were found nonlinear and for practical purposes could be approximated by polynomials of the second degree. The fitted coefficients of such polynomials were given in Table 2 and could be used to calculate head coefficients for the relative discharges $\psi_{12}$ and $\psi_{13}$ varying from 0 to 1.0. Such calculated head loss coefficients should be fairly reliable within the range of flow divisions which was used in the experiments. The coefficient values extrapolated outside of this range are less reliable because of inherent uncertainties. These extrapolated values were therefore underlined in Table 2 and caution or further verifications are recommended when using such data.

Comparisons of various junction configurations were made possible by calculating the mean combined head loss coefficient for each test series and such coefficients were used in the following discussion of effects of various junction parameters on the head losses.

Among the junction parameters studied, the relative lateral size expressed as $D_{3} / D_{1}\left(=D_{3} / D_{2}\right.$ because the main and outlet pipe
diameters were identical) had the greatest influence on junction head losses. In this notation, $D$ is the pipe diameter and indices 1, 2 and 3 refer to the outlet, main and lateral pipes, respectively. The lowest losses were found for $D_{3} / D_{1}=1.0$ (in other words, $D_{1}=D_{2}=$ $D_{3}$ ). In this case, the mean combined head loss coefficient varied from 0.305 to 0.719 . For $D_{3} / D_{1}=0.7$, the mean head loss coefficient varied from 0.678 to 1.143 . For $D_{3} / D_{1}=0.45$, the range of mean combined head loss coefficients was from 1.28 to 2.019 and, finally, for $D_{3} / D_{1}=$ 0.25 , the range was from 4.713 to 5.902 .

The lateral size affects the momentum of the lateral flow. For a particular discharge, the lateral flow momentum will increase proportionately with $\left(1 / D_{3}\right)^{2}$. Since most of the lateral flow momentum is lost at the junction (particularly for $\theta=90^{\circ}$ ), the configurations with small laterals and the resulting high lateral flow momentum yield the highest head losses.

The effects of the remaining junction parameters, such as the benching type, manhole base shape and lateral angle were rather minor. The benching had some effect on the losses for $D_{3} / D_{1}=1.0$ and 0.7 , and the lateral angle $\theta=90^{\circ}$. The benchings providing better flow guidance, such as those described as moulds $2 A$ and $2 B$, produced somewhat lower losses.

The head loss coefficients $K_{12}$ and $K_{13}$ varied with the relative discharges $\psi_{12}$ and $\psi_{13}$ (see Fig. 5). The variations in $K_{12}$ are moderate and this coefficient seems to increase slightly with the increasing relative discharge. The maximum values of $K_{12}=1.0$ are obtained in the range of $\psi_{12}$ from 0.5 to 1.0 . For the lateral pipe, the head loss coefficient $K_{13}$ varies sharply with $\psi_{13}$ and the maximum values of about 16.0 are found for $\psi_{13}=1.0$.

The combined head loss coefficients $K_{c}$ obtained in this study are compared with those reported by others in Table 3. Such comparisons for similar junctions were made for a selected typical value of $Q_{3} / Q_{1}=0.6$. A fair agreement among the results from various studies is obvious from Table 3.

### 6.0 SUMMARY AND CONCLUSIONS

Extensive tests of 40 different configurations of junction manholes with the main pipe and a lateral indicate the following findings:
(1) Head losses at junctions of the main and lateral pipes are affected by both the junction geometry and the relative lateral discharge $\psi_{13}\left(=Q_{1_{\text {ateral }}} / Q_{\text {outlet }}=1-\psi_{23}=1-Q_{\text {main }} / Q_{\text {outlet }}\right)$.
(2) Among the junction geometry parameters, the relative lateral size ( $D_{\text {lateral }} / D_{\text {outlet }}=D_{3} / D_{1}$ ) had the strongest influence on the mean combined head loss coefficient of a particular junction configuration. The smaller the ratio $D_{3} / D_{1}$, the larger the junction head losses. The effects of the remaining parameters, such as the junction benching, lateral angle and the manhole base shape on the mean combined head loss coefficient were relatively minor.
(3) Large differences between head loss coefficients for the main and lateral pipes were observed. Although both coefficients generally increased with the increasing relative discharges $\psi_{12}$ and $\psi_{13}$, the increases in the lateral head loss coefficient were much larger. For very low relative discharges, energy gains rather than losses were observed under some circumstances.
(4) For practical applications of the results presented above, it is recommended to reduce junction head losses by designing the junction of the main and lateral pipes with the following features:
(a) $D_{3}=D_{2}=D_{1}$.
(b) Ideally, the discharges should be in the range $0.7 \leq \psi_{12}<$ 1.0 and $0<\psi_{13} \leq 0.3$.
(c) Both square, and round base manholes are acceptable.
(d) Because the effects of the lateral angles $\theta$ on the mean combined head losses were minor, any of the angles studied $\left(45^{\circ}, 60^{\circ}\right.$ and $90^{\circ}$ ) is acceptable.
(e) The junction benching should be used, particularly for large lateral angles $\left(90^{\circ}\right)$. The benching described as mould $2 B$ and its modified version with benches at the pipe crown level are recommended.

### 7.0 REFERENCES

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TABLES

TABLE 1. Coefficients of Regression Quadratic Polynomials

| Test Series | $K_{12}=a+b \psi_{12}+C \psi_{2}{ }^{2}$ |  |  |  | $K_{13}=d+e \psi_{13}+f \psi_{13}{ }^{2}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a | b | c | $\mathrm{R}^{2}$ | d | e | $f$ | $\mathrm{R}^{2}$ |
| 1 | . 115 | 1.514 | -. 870 | . 900 | -. 312 | . 643 | 15.461 | 1.00 |
| 2 | . 251 | 1.427 | -. 616 | . 962 | -. 182 | . 415 | 15.743 | 1.00 |
| 3 | . 317 | . 661 | . 105 | . 988 | -. 099 | . 039 | 16.19 | 1.00 |
| 4 | . 140 | 2.097 | -1.433 | . 819 | -. 720 | 2.690 | 13.700 | 1.00 |
| 5 | . 200 | 1.568 | -. 909 | . 991 | -. 160 | . 037 | 15.880 | 1.00 |
| 6 | . 037 | 1.401 | -. 762 | . 969 | -. 283 | . 104 | 16.948 | 1.00 |
| 7 | -. 010 | 2.276 | -1.510 | . 866 | -. 308 | 1.367 | 3.878 | 1.00 |
| 8 | -. 263 | 3.044 | -1.973 | . 991 | -. 213 | 1.052 | 4.165 | . 999 |
| 9 | . 307 | . 684 | -. 221 | . 913 | -. 254 | 1.222 | 3.996 | . 998 |
| 10 | -. 062 | 2.236 | -1.354 | . 972 | -. 122 | . 444 | 5.148 | . 999 |
| 11 | -. 106 | 3.088 | -2.384 | . 992 | -. 493 | 2.457 | 2.811 | . 999 |
| 12 | . 245 | 2.524 | -2.050 | . 935 | -. 295 | 1.529 | 3.895 | . 999 |
| 13 | -. 480 | 3.719 | -2.496 | . 979 | -. 351 | 1.897 | 3.388 | . 999 |
| 14 | -. 047 | 1.999 | -1.139 | . 934 | -. 154 | . 162 | 5.089 | . 998 |
| 15 | . 414 | 1.861 | -1.683 | . 888 | -. 400 | 1.810 | 16.410 | 1.00 |
| 16 | . 721 | 1.227 | -1.099 | . 847 | -. 256 | 1.070 | 16.160 | 1.00 |
| 17 | . 617 | 1.448 | -1.501 | . 948 | . 164 | -. 253 | 14.328 | . 999 |
| 18 | -. 388 | 2.562 | -1.299 | . 988 | -. 546 | 2.273 | 2.831 | . 999 |
| 19 | -. 047 | 1.857 | -1.063 | . 975 | -. 610 | 1.766 | 3.932 | . 988 |
| 20 | -3.171 | 10.115 | -6.281 | . 948 | -. 821 | -4.833 | -1.010 | . 953 |
| 21 | . 131 | 1.331 | -. 550 | . 940 | -. 723 | 3.759 | 1.464 | . 999 |
| 22 | -. 450 | 3.969 | -2.922 | . 916 | -. 680 | 4.506 | -2.945 | . 985 |
| 23 | -. 017 | 2.540 | -1.746 | . 658 | -. 268 | 1.850 | . 631 | . 993 |

TABLE 1. (continued)

| Test No. | $K_{12}=a+b \psi_{12}+C \psi_{12}{ }^{2}$ |  |  |  | $K_{13}=d+e \psi_{13}+\mathrm{f}_{13}{ }^{2}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | a | b | c | $\mathrm{R}^{2}$ | d | e | $f$ | $\mathrm{R}^{2}$ |
| 24 | -. 021 | 2.727 | -2.065 | . 768 | -. 326 | 2.200 | . 216 | . 998 |
| 25 | -. 184 | 2.788 | -1.823 | . 942 | -. 2289 | 1.216 | 1.263 | . 997 |
| 26 | -. 793 | 5.526 | -4.045 | . 680 | -. 492 | 2.858 | -. 284 | . 998 |
| 27 | -. 059 | 2.356 | -1.541 | . 969 | -. 196 | . 921 | 1.819 | . 994 |
| 28 | -. 156 | 3.053 | -2.305 | . 862 | -. 324 | 2.122 | . 342 | . 999 |
| 29 | -. 002 | 2.176 | -1.389 | . 958 | -. 234 | 1.342 | 1.098 | . 955 |
| 30 | -1.161 | 6.137 | -4.526 | . 933 | -. 578 | 2.893 | -. 553 | . 995 |
| 31 | -. 376 | 3.432 | -2.434 | . 943 | -. 649 | 2.769 | -. 275 | . 996 |
| 32 | -. 534 | 4.201 | -3.287 | . 926 | -. 595 | 2.790 | -. 317 | . 999 |
| 33 | -1.457 | 6.009 | -4.162 | . 965 | -. 525 | 2.205 | -. 317 | . 994 |
| 34 | -1.384 | 6.485 | -4.643 | . 945 | -. 715 | 3.584 | -2.318 | . 987 |
| 35 | -. 353 | 3.868 | -2.979 | . 891 | -. 740 | 3.124 | $-1.380$ | . 995 |
| 36 | -. 648 | 3.902 | -2.605 | . 980 | -. 884 | 4.747 | -4.396 | . 998 |
| 37 | -2.755 | 9.336 | -6.135 | . 914 | -. 690 | 3.019 | $-1.898$ | . 984 |
| 38* | -. 387 | 4.167 | -3.190 | . 949 | -. 578 | 3.088 | 2.178 | . 999 |
| 39* | -. 529 | 3.825 | -2.943 | . 833 | -. 600 | 2.358 | . 060 | . 998 |
| 40* | -1.603 | 6.749 | -4.730 | . 941 | -. 644 | 2.409 | -. 553 | . 976 |

* Round Base Manhole
TABLE 2. Combined Head Loss Coefficients for Various Lateral Inf lows

| Test Series | $\mathrm{K}_{\mathrm{c}}=\mathrm{K}_{12} \psi_{12}+\mathrm{K}_{13} \psi_{13} \quad\left(\psi_{12}+\psi_{13}=1.0\right)$ |  |  |  |  |  |  |  |  |  |  | Statistical Measures |  |  | Junction Configurations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\psi_{13}=$ | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 | 1.0 | $\mathrm{R}_{\mathrm{c}}$ | $\sigma$ | O/R | $\mathrm{A}_{3} / \mathrm{A}_{1}$ | $A_{2} / A_{1}$ | $\theta$ | M |
| 1 |  | . 686 | . 703 | . 906 | 1.394 | 2.265 | 3.616 | 5.547 | 8.155 | 11.547* | 15.792* | 5.060 | 5.224 | 1.033 | . 250 | 1.000 | 45* | 0 |
| 2 |  | . 934 | . 905 | 1.071 | 1.532 | 2.386 | 3.730 | 5.663 | 8.283 | $\underline{11.6887}$ | 15.976 | 5.217 | 5.219 | 1.00 | . 250 | 1.000 | 45* | 1 |
| 3 |  | . 904 | . 842 | . 993 | 1.454 | 2.321 | 3.691 | 5.660 | 8.326 | $\underline{11.783}$ | 16.130 | 5.210 | 5.297 | 1.017 | . 250 | 1.000 | $45^{\circ}$ | 4 |
| 4 |  | . 749 | . 794 | 1.030 | 1.549 | 2.440 | 3.795 | 5.705 | 8.260 | 11.552 | $\underline{15.670}$ | 5.154 | 4.659 | . 789 | . 250 | 1.000 | $60^{\circ}$ | 0 |
| 5 |  | . 788 | . 795 | . 981 | 1.446 | 2.293 | 3.620 | 5.530 | 8.122 | 11.497 | 15.757 | 5.083 | 5.178 | 1.019 | . 250 | 1.000 | $60^{\circ}$ | 1 |
| 6 |  | . 602 | . 619 | . 833 | 1.350 | 2.277 | 3.719 | 5.783 | 8.575 | 12.202 | 16.769 | 5.273 | 5.591 | 1.060 | . 250 | 1.000 | $60^{\circ}$ | 4 |
| 7 |  | . 721 | . 700 | . 726 | . 831 | 1.048 | 1.408 | 1.945 | 2.691 | 3.677 | 4.937 | 1.868 | 1.465 | . 784 | . 445 | 1.000 | $45^{\circ}$ | 0 |
| 8 |  | . 784 | . 760 | . 774 | . 862 | 1.060 | 1.406 | 1.937 | 2.689 | 3.699 | 5.004 | 1.897 | 1.466 | . 772 | . 445 | 1.000 | $45^{\circ}$ | 1 |
| 9 |  | . 660 | . 600 | . 615 | . 730 | . 971 | 1.362 | 1.929 | 2.696 | 3.690 | 4.934 | 1.819 | 1.505 | . 827 | . 445 | 1.000 | $45^{\circ}$ | 3 |
| 10 |  | . 766 | . 723 | . 730 | . 82.7 | 1.052 | 1.445 | 2.044 | $\underline{2.889}$ | 4.018 | 5.470 | 1.996 | 1.642 | . 822 | . 445 | 1.000 | $45^{\circ}$ | 4 |
| 11 |  | . 646 | . 693 | . 770 | . 909 | 1.140 | 1.495 | 2.005 | $\underline{2.701}$ | 3.614 | 4.775 | 1.875 | 1.409 | . 752 | . 445 | 1.000 | $60^{\circ}$ | 0 |
| 12 |  | . 760 | . 795 | . 859 | . 989 | 1.219 | 1.585 | 2.124 | 2.870 | 3.860 | 5.129 | 2.019 | 1.495 | . 740 | . 445 | 1.000 | $60^{\circ}$ | 1 |
| 13 |  | . 748 | . 751 | . 787 | . 892 | 1.100 | 1.447 | 1.969 | 2.701 | 3.677 | 4.934 | 1.901 | 1.444 | . 760 | . 445 | 1.000 | $60^{\circ}$ | 3 |
| 14 |  | . 738 | . 675 | . 662 | . 735 | . 933 | 1.293 | 1.852 | 2.647 | 3.717 | 5.097 | 1.835 | 1.531 | . 834 | . 445 | 1.000 | $60^{\circ}$ | 4 |

[^0]TABLE 2. Combined Head Loss Coefficients for Various Lateral Inflows (continued)

| Test Series | $K_{c}=K_{12} \psi_{12}+K_{13} \psi_{13} \quad\left(\psi_{12}+\psi_{13}=1.0\right)$ |  |  |  |  |  |  |  |  |  |  | Statistical Measures |  |  | Junction Configurations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\psi_{13}=$ | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 | 1.0 | $\mathrm{R}_{\mathrm{c}}$ | - | $\sigma / R_{c}$ | $A_{3} / A_{1}$ | $A_{2} / A_{1}$ | $\theta$ | M |
| 15 |  | . 648 | . 784 | 1.110 | 1.735 | 2.766 | 4.312 | 6.482 | 9.384 | 13.127 | 17.820 | 5.817 | 5.898 | 1.014 | . 250 | 1.000 | $90^{\circ}$ | 0 |
| 16 |  | . 843 | . 920 | 1.185 | 1.740 | 2.689 | 4.137 | 6.185 | 8.938 | $\underline{12.500}$ | 16.974 | 5.611 | 5.558 | . 990 | . 250 | 1.000 | $90^{\circ}$ | 1 |
| 17 |  | . 662 | . 784 | 1.040 | 1.504 | 2.293 | 3.485 | 5.180 | 7.475 | 10.462 | $\underline{14.039}$ | 4.713 | 4.650 | . 986 | . 250 | 1.000 | $90^{\circ}$ | 2 A |
| 18 |  | . 750 | . 669 | . 665 | . 735 | . 933 | 1.274 | 1.782 | 2.482 | 3.399 | 4.558 | 1.724 | 1.351 | . 784 | . 445 | 1.000 | $90^{\circ}$ | 0 |
| 19 |  | . 648 | . 587 | . 595 | . 701 | . 936 | 1.329 | 1.911* | 2.712* | 3.761* | 5.088* | 1.827 | 1.561 | . 854 | . 445 | 1.000 | $90^{\circ}$ | 1 |
| 20 |  | . 726 | . 742 | . 744 | . 762 | . 830 | . 977 | 1.237 | 1.639 | 2.217 | 3.002 | 1.288 | 4.854 | 1.094 | . 445 | 1.000 | $90^{\circ}$ | 2 A |
| 21 |  | . 762 | . 693 | . 716 | . 845 | 1.091 | 1.466 | 1.982 | 2.652 | 3.487 | 4.500 | 1.819 | . 1329 | . 731 | . 445 | 1.000 | $90^{\circ}$ | 2 B |
| 22 |  | . 654 | . 705 | . 745 | . 788 | . 819 | . 844 | . 862 | . 872 | . 875 | . 871 | . 804 | . 078 | . 097 | . 694 | 1.000 | $45^{\circ}$ | 0 |
| 23 |  | . 762 | . 743 | . 737 | . 756 | . 816 | . 929 | 1.112 | 1.377 | 1.739 | 2.213 | 1.118 | . 508 | . 454 | . 694 | 1.000 | $45^{\circ}$ | 1 |
| 24 |  | . 674 | . 696 | . 719 | . 759 | . 827 | . 939 | 1.107 | $\underline{1.346}$ | 1.669 | 2.090 | 1.083 | . 479 | . 443 | . 694 | 1.000 | $45^{\circ}$ | 3 |
| 25 |  | . 754 | . 717 | . 687 | . 684 | . 725 | . 830 | 1.016 | 1.303 | 1.708 | $\underline{2.251}$ | 1.067 | . 533 | . 499 | . 694 | 1.000 | $45^{\circ}$ | 4 |
| 26 |  | . 793 | . 845 | . 867 | . 882 | . 912 | . 980 | 1.109 | 1.320 | 1.637 | $\underline{2.082}$ | 1.143 | . 421 | . 368 | . 694 | 1.000 | $60^{\circ}$ | 0 |
| 27 |  | . 723 | . 684 | . 658 | . 665 | . 727 | . 862 | 1.091 | 1.434 | $\underline{1.912}$ | 2.544 | 1.130 | . 645 | . 571 | . 694 | 1.000 | $60^{\circ}$ | 1 |

TABLE 2. Combined Head Loss Coefficients for Various Lateral Inflows (continued)

| Test Series | $K_{c}=K_{12} \psi_{12}+K_{13} \psi_{13}\left(\psi_{12}+\psi_{13}=1.0\right)$ |  |  |  |  |  |  |  |  |  |  | Statistical Measures |  |  | Junction Configurations |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | \$13 $=$ | . 1 | . 2 | . 3 | . 4 | . 5 | . 6 | . 7 | . 8 | . 9 | 1.0 | $\mathrm{R}_{\mathrm{c}}$ | $\sigma$ | $\sigma / R_{c}$ | $\mathrm{A}_{3} / \mathrm{A}_{1}$ | $A_{2} / A_{1}$ | $\theta$ | M |
| 28 |  | . 641 | . 672 | . 699 | . 739 | . 808 | . 922 | 1.096 | 1.346 | 1.689 | 2.140 | 1.075 | . 504 | . 469 | . 694 | 1.000 | $60^{\circ}$ | 3 |
| 29 |  | . 739 | . 696 | . 669 | . 674 | . 725 | . 838 | $\underline{1.028}$ | $\underline{1.309}$ | 1.697 | 2.206 | 1.058 | . 525 | . 496 | . 694 | 1.000 | $60^{\circ}$ | 4 |
| 30 |  | . 597 | . 677 | . 714 | . 731 | . 753 | . 803 | . 905 | 1.083 | 1.361 | 1.762 | . 939 | . 367 | . 390 | . 694 | 1.000 | $90^{\circ}$ | 0 |
| 31 |  | . 630 | . 628 | . 631 | . 650 | . 699 | . 791 | . 939 | $\underline{1.155}$ | 1.453 | $\underline{1.845}$ | . 942 | . 419 | . 445 | . 694 | 1.000 | $90^{\circ}$ | 1 |
| 32 |  | . 494 | . 569 | . 621 | . 670 | . 733 | . 827 | . 971 | 1.182 | $\underline{1.479}$ | 1.878 | . 942 | . 447 | . 474 | . 694 | 1.00 | $90^{\circ}$ | 2A |
| 33 |  | . 491 | . 530 | . 529 | . 513 | . 503 | . 523 | . 596 | . 745 | . 993 | 1.363 | . 678 | . 287 | . 423 | . 694 | 1.000 | $90^{\circ}$ | 28 |
| 34 |  | . 585 | . 648 | . 662 | . 640 | . 598 | . 547 | . 504 | . 480 | . 492 | . 551 | . 571 | . 067 | . 117 | 1.000 | 1.000 | $90^{\circ}$ | 0 |
| 35 |  | . 600 | . 634 | . 648 | . 653 | . 657 | . 670 | .701 | .761 | . 859 | 1.004 | . 719 | . 125 | . 174 | 1.000 | 1.000 | $90^{\circ}$ | 1 |
| 36 |  | . 633 | . 623 | . 608 | . 578 | .521* | . 427 | . 286 | . 086 | $\underline{-.184}$ | -. 533 | . 305 | . 398 | 1.307 | 1.000 | 1.000 | $90^{\circ}$ | 2A |
| 37 |  | . 570 | . 597 | . 555 | . 468 | . 362 | . 262 | . 193 | . 182 | . 252 | . 431 | . 387 | . 159 | . 411 | 1.000 | 1.000 | $90^{\circ}$ | 2 B |
| 38 |  | . 677 | . 749 | . 840 | . 981 | 1.204 | 1.541 | 2.026 | $\underline{2.689}$ | 3.563 | 4.680 | 1.895 | 1.355 | . 715 | . 445 | 1.000 | $90^{\circ}$ | 2 A |
| 39 |  | . 440 | . 493 | . 528 | . 565 | . 621 | . 714 | . 862 | $\underline{1.083}$ | 1.396 | 1.818 | . 852 | . 452 | . 531 | . 694 | 1.000 | $90^{\circ}$ | 2 A |
| 40 |  | . 535 | . 578 | . 571 | . 539 | . 506 | . 497 | . 539 | . 655 | . 871 | 1.212 | . 650 | . 226 | . 347 | 1.000 | 1.000 | $90^{\circ}$ | 2A |

* Underlined values are extrapolated and may contain appreciable uncertainties
TABLE 3. Comparison of Head Loss Coefficients from Various Sources

|  | Source | Junction Base | Junction Benching | Lateral Pipe Angle | $D_{1} / D_{3}$ | $Q_{3} / Q_{1}$ | b*/D1 | Flow Type |  |  | $\mathrm{K}_{\mathrm{c}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  | Combined or Divided | Free Surface | Pressurized Flow |  |
| 1 | Sangster <br> et al (11) | Square Round | None None | $\begin{aligned} & 90^{\circ} \\ & 90^{\circ} \end{aligned}$ | $\begin{aligned} & 1.00 \\ & 1.27 \end{aligned}$ | . 6 | $\begin{aligned} & 1.87 \\ & 2.08 \end{aligned}$ | Combined Combined |  | yes yes | $\begin{array}{r} 1.040 \\ .708 \end{array}$ |
| 2 | Townsend \& Prins (13) | Rectangular | Drop invert | $45^{\circ}$ | 1.57 | . 6 | 2.55 | Combined | Yes |  | 1.058 |
| 3 | Present Study | Square Round | ```Drop invert ditto ditto M=2A``` | $45^{\circ}$ $60^{\circ}$ 90 90 | 1.20 1.20 1.20 1.20 | .6 .6 .6 .6 | 2.26 2.26 2.26 2.23 | Combined Combined Combined Combined |  | Yes Yes Yes | .844 .980 .803 .714 |

[^1]
FIGURE, 1.
GENERAL L'AYOUT OF EXPERIMENTAL APPARATUS (not drawn to scale)


JUNCTION BOX WITH A LATERAL PIPE INLET ASSEMBLY (not drawn to scale)

LATERAL
PIPE SIZE JUNCTION ISOMETRIC
(mm) TYPE PIEW SLAN VIEW VIDEW

| $\begin{array}{r} 76\left(3^{\prime \prime}\right) \\ 102\left(4^{\prime \prime}\right) \\ 127\left(5^{\prime \prime}\right) \\ -152\left(6^{\prime \prime}\right) \end{array}$ | SQUARE <br> JUNCTION |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{array}{r} 76\left(3^{\prime \prime}\right) \\ 102\left(4^{\prime \prime}\right) \\ 127\left(5^{\prime \prime}\right) \\ 152\left(6^{\prime \prime}\right) \end{array}$ | SQUARE JUNCTION | MOULD \#2A <br> MOULD\#2B |  |  |
| $\begin{array}{r} 76\left(3^{\prime \prime}\right) \\ 102\left(4^{\prime \prime}\right) \\ 127\left(5^{\prime \prime}\right) \end{array}$ | SQUARE <br> JUNCTION | MOULD \#1 |  |  |
| $\begin{array}{r} 76\left(3^{\prime \prime}\right) \\ 102\left(4^{\prime \prime}\right) \\ 127\left(5^{\prime \prime}\right) \end{array}$ | SQUARE JUNCTION | MOULD\#3 | $\theta=45^{\circ}, 60^{\circ}$ |  |
| $\begin{aligned} & 102\left(4^{\prime \prime}\right) \\ & 127\left(5^{\prime \prime}\right) \\ & 152\left(6^{\prime \prime}\right) \end{aligned}$ | CIRCULAR JuNCTION | MOULD \# 2A |  |  |

FIGURE 3 JUNCTION MANHOLES TESTED


FIGURE 4. NOTATION SKETCH

 THE RELATIVE LATERAL



 INFLOW.













vs THE RELATIVE LATERAL






HEAD LOSS COEFFICIENT vs THE RELATIVE LATERAL
INFLOW.
FIGURE 5(e).

LOSS COEFFICIENT vs
FIGURE 5(f). HEAD


[^0]:    * Underlined values were extrapolated and may contain significant uncertainties

[^1]:    * $b$ is the width of manhole junction

