





DISCUSSION PAPER NO. 52

Rates of Return on Life Insurance Savings

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RESUME

La fonction première des compagnies d'assurance-vie est évidemment de procurer une certaine protection à l'égard des pertes résultant du décès. Parallèlement à cette fonction, elles procurent aussi aux agents économiques diverses possibilités quant au placement de leurs épargnes. Ainsi, elles offrent toute une gamme de régimes de pension, une grande variété de polices d'assurance-vie avec composante épargne et, enfin, elles acceptent de garder en dépôt contre remunération la valeur de rachat de ces polices une fois qu'elles sont échues. Les compagnies informent généralement leurs clients potentiels des rendements qu'ils sont en mesure d'attendre des fonds de pension et des dépôts. Par contre, l'information quant au rendement sur la composante épargne des polices d'assurance-vie avec valeur de rachat laisse beaucoup à désirer.

L'évaluation de ce rendement pose des difficultés et le présent document porte précisément sur ces problèmes. Après une revue de la littérature sur le sujet (Partie I), nous proposons une technique permettant de mesurer ce rendement et nous l'appliquons à divers types de polices (Partie II).

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# ABSTRACT

The main business of life insurance companies is obviously to provide protection against loss resulting from death. Besides that, they also play an important role in supplying the economy with various types of savings media; namely deposit facilities, annuity contracts and life insurance policies embodying a savings element. While the rates of return on deposits and annuity contracts are made available to potential customers by the companies themselves, the assessment of the return on the savings element of most life insurance contracts, however, remains a partially open issue.

The purpose of this paper is to throw some light on the assessment of this yield as it pertains to savings accumulated as part of life insurance contracts written by some of the major companies doing business in Canada. A survey of the literature on the topic will be presented in <u>Part I. Part II</u> will include our own approach to the issue and our results.

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# Part I

From the survey to follow, it will become clear that most of the controversy over the merits of savings accumulation through life insurance contracts results from a very specific point; that is, there is disagreement about the proper division of insurance premiums paid into a pure *insurance cost component* and a *savings component*.

# LINTON

Although Linton is known to most students of insurance for his persistency studies, he was also a pioneer in his responses to those who criticized life insurance when it was viewed as an investment opportunity. In this regard, he devised a method to calculate the investment rate of return that would be necessary for a separate investment fund (along with term insurance, which is an example of insurance without a savings element) to match the cash value accumulation in a standard life insurance policy.<sup>1</sup>

Linton describes his approach as follows:

Assuming that the amounts to be invested in each program (standard life vs term plus separate investment fund) are equal, the figure we are seeking is the net rate of

Results obtained by means of his method are revised periodically. For a summary and discussion of these results, see LINTON (1964), pp. 238-245

compound interest that must be earned on the investment fund so that at the end of a given period, such as twenty years, the fund will equal the twentieth-year guaranteed<sub>2</sub>cash value of the life insurance policy.

The main constraint under which the calculations are performed is that the financial position of the insured at the time of death should be strictly equivalent under the two alternative programs. It can be shown that this is achieved if the term insurance purchased is equal to the sum of 1/ the difference between the separate fund accumulation and the face value of the standard life policy, plus 2/ an amount equal to the term premium.

Results arrived at for a twenty-year period when using the 1963 financial data of ten mutual companies are as follows:

Jssue age	Return
	(net of taxes and expenses)
. 25	4.80 %
35	4.78 %
45	5.17 %
55	6.37 %

### Table 1

RATE OF RETURN TO BE EARNED ON THE

Source LINTON (1964) reported in FERRARI (1968), p. 183.

<sup>2</sup> LINTON (1964), p. 241.

## FERRARI

FERRARI (1968) shares Linton's concern with assessing the compound rate of return on the savings component of standard life insurance contracts. No longer is the constraint simply that the financial position should be strictly equivalent at the time of death. The approach is rather to compare the financial position at a number of durations through equivalent outlays or either standard insurance or term insurance plus a separate investment fund. As we go on, it will become clear that, with such an approach, equivalence of financial positions over the early years of a standard life policy is to be ruled out.

The criticisms addressed by Ferrari to Linton's approach have to do with both the use of the premium on oneyear term insurance as a proxy for the cost of pure insurance and the complexity of the computations involved. A normal insurance program would call for a guaranteed insurability clause which extends over a period longer than the usual nine years of renewability attached to most one-year term plans. The pure cost of insurance as approximated by premiums on oneyear term would then understate the lifetime cost of pure insurance: Ferrari uses premiums on five-year term insurance. As for computational complexities, the problem can be alleviated without any great loss of generality. This, then, is the major departure from Linton's approach. In Ferrari (1968), the

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insurance protection which corresponds to the amount of term insurance to be purchased for each duration is simply set equal to the face amount of a given standard life policy less the cash surrender value at the same duration.

The after tax rates of return on the separate investment fund as assessed by means of this method are only slightly higher than Linton's rate due to the fact that more term insurance is purchased under the simplified approach. Smaller provisions entering the separate fund mean that its rate of return must be higher to match the cash value accumulation in a given standard life insurance contract. Table 2 shows two sets of rates of return; the first results from an extension of Linton's method

Table 2

		RATE OI	F RETURN ON SEPAR	RATE INVESTMENT
		FUND NEO	CESSARY TO MATCH	SURRENDER VALUE
IN	۸	\$10,000	PARTICIPATING ST	TRAIGHT LIFE POLICY,
		ISSUE	AGE 35, 1964 DIV	/IDEND SCALE,
			ANNUAL PREMIUM	234.20

Duration in years	Linton's method	Linton's method : simplified for term insurance determination
}	9428	9424
1 2	2571	2540
3	0857	0820
4	0145	0120
4 5 6	.0162	.0186
6	.0314	.0335
7	.0395	.0414
8	.0455	.0486
8	.0490	.0505
10	.0509	.0523
11	.0504	.0516
12	.0500	.0511
13	.0501	.0511
14	.0502	.0510
15	.0501	.0509
16		.0508
17	.0500	.0508
18	.0500	.0507
19	.0500	.0506
20	.0500	.0506

Source Ferrari (1968), p. 186.

to cover a number of durations and the second shows the rates of return based on Linton's method as simplified by Ferrari for the amount of term insurance to be purchased.

As can be seen from Table 2, the extension of Linton's approach to a number of durations including the early years of a standard life policy casts doubt on the relevance of starting with the constraint of equivalent financial positions under the various insurance programs to be compared. This table shows negative rates of return on savings in early years. Should a policy terminate in those early years, (either because of voluntary withdrawal or because of death), equivalence of financial positions would then require a negative return on the separate investment fund. Over those years, any reasonable separate investment and appropriate term insurance would, for equal outlays, lead to a better financial position than would standard life insurance alone.

Ferrari's own results appear in the last column of Table 2. Equal outlays are assumed and the stream of annual savings (i.e., the difference between the premiums on standard life insurance and the premiums on appropriate five-year term insurance) is invested in a fund at the available "reasonable" rate. The second step is to compare financial positions attainable under the two alternatives. This comparison is

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twofold: 1/ the separate investment fund accumulation at the end of each year under the assumed rate of return is compared to the accumulated cash value plus dividends available at the end of that same year to ascertain the relative financial position at each duration if the insured should surrender and 2/ the term insurance death proceeds plus the separate investment accumulation are compared against the face amount plus post-mortem dividends of standard life insurance to ascertain the relative financial position at each duration should the insured die. Those two sets of relative financial positions ranked along duration are discounted by an assumed discount factor and then weighted by the appropriate probability of termination (voluntary or by death) for each duration. The last step of the procedure involves the summing up of the resulting, expected, discounted values and the search, through trial and error and interpolation, for a rate which produces an expected discounted value of zero.

Results obtained by means of this method show the expected return on a separate investment fund necessary for term insurance plus separate investment to provide for a financial position comparable to that which at all durations would be attainable through standard life insurance. Those results are positively linked to persistency and although they tend towards Linton's estimates, they never quite reach them.

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# CAMERON

Cameron's method differs from both Linton's and Ferrari's in that the assessment of the rate of return on savings through life insurance is straightforward. In other words, no reference is made either to a separate fund in which the appropriately defined savings component of annual premiums would accumulate or to the rate of return which could be considered as the opportunity cost (expressed in percentages) of savings channelled through life insurance.

Cameron's approach consists first of isolating the savings component of premiums on life insurance and then of searching for the rate of return which will cause this stream of annual savings to accumulate to the known terminal cash value of the contract.

The savings element in each year is found as the residual of the net premium on standard life after deduction of the protection element. The latter is defined as the product of the average amount of protection provided during the year, and its unit cost. The average amount of protection is defined as the difference between the face value of the contract and the accumulated cash value. The unit cost of protection is the mortality cost of insuring a given type of policy holder plus

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other fixed charges. In Cameron's paper, this cost of protection is covered by the use of a proxy which is the sum of the term premiums charged by Sun Life of Canada on a five-year renewable term insurance plus a policy fee charged by this same company for each policy issued.

Results of computations for 265 policies using data from 1972 Stone and Cox Life Insurance Tables are as follows, (a twenty-year holding period is assumed):

### Table 3

	Participating	Nonparticipating
Canadian companies	4.35	3.10
British companies	3.74	2.75
Foreign companies	4.07	2.86

AVERAGE RATE OF RETURN ON SAVINGS THROUGH DIFFERENT TYPES OF STANDARD LIFE INSURANCE CONTRACTS

Source CAMERON, Table 1, p. 10a.

# QUIRIN AND WATERS

Part of their study on the Canadian mutual fund industry is devoted to the assessment of the rate of return on the savings part of insurance contracts which, along with mutual funds, are savings media incorporating a prepaid sales charge. Their approach is similar to Cameron's except that their premium rates, surrender values and dividend rates, are averages of the rates quoted by three companies (Crown Life, Manufacturers Life and Great-West Life). The average premium charged by the three companies on a one-year renewable term is used as a proxy of the cost of protection. The results for the three types of policies, issued at age 35, using premiums and dividends as quoted in 1967 Stone and Cox Life Insurance Tables are as follows:

### Table 4

Year	Ordinary life nonparticipating	Ordinary life participating	20-year endowment participating
1	-1.000	-1.000	-1.000
2	-1.000	-1.000	753
3	559	442	183
4	260	226	094
5	138	120	054
6	071	064	023
7	039	029	004
8	014	010	.006
9	003	.005	.013
10	.007	.013	.018
11	.016	.023	.024
12	.022	.029	.029
13	.025	.033	. 032
14	.028	. 036	.034
15	.030	.039	. 036
16	.032	.041	. 038
17	.033	.043	. 039
18	.035	.044	.040
19	.035	.046	.041
20	.036	.049	.043

RETURN ON SAVINGS THROUGH \$10,000 LIFE INSURANCE POLICIES ISSUED AT AGE 35

Source QUIRIN and WATERS, (1969) pp. 5.19-5.21.

The four approaches we briefly surveyed above suggest that the maximum rate of return which one can get on the savings element of life insurance contracts for a twenty-year holding period is approximately 5 per cent and that this rate is available on ordinary life participating contracts. When rates of return are assessed for all durations up to twenty years, computations show that those rates are very low in the early years (in fact they are negative). They also indicate that they will increase to become positive before the tenth year.

From a methodological point of view, a feature common to these four approaches is that they all make use of a decreasing amount of effective protection in their computations. Cash surrender value is then viewed as the insured's own accumulated savings which finance a part of the available death benefit should death occur before the end of the contract. Given the constant face value of a standard life contract, a rising cash value leads to a decreasing amount of effective protection.

# Part II

Our approach will be quite different from that of the previous studies in the field. We will neither make use of a separate investment fund nor will we try to split the cost of standard life insurance into its protection and savings components. Instead, we will view life insurance companies as issuers of essentially two types of life insurance contracts. (standard life contracts or insurance-savings packages and term contracts or pure insurance contracts) which, even for identical face values or death benefits, involve different outlays on the part of the insured and likely have a different impact on his wealth at the time of termination.

In our method, the differential impact on wealth will be compared to the stream of differences in outlays. Thus the compound rate of return on the savings component of standard life insurance will be the compound rate necessary to make the difference in outlays accumulate to the amount of that differential impact on wealth.

Differences in outlays will be derived as follows. For outlays on pure insurance, we will use the annual premium (including a policy fee) on five-year term renewable and convertible policies. This type of policy provides guaranteed

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insurability for entire life through successive renewals and conversion, the latter being generally available until ages 65 or 70. Only this kind of term insurance provides insurance protection which, because of its guaranteed insurability clause (without medical), may be viewed as a meaningful alternative to protection secured through standard life insurance over a relatively long horizon.<sup>3</sup> As for outlays on standard life insurance, two types of saving insurance packages will be considered: ordinary life policies (participating and nonparticipating or with and without dividends) and endowment policies. As mentioned earlier, all of those share the common feature of cash surrender value rising with effective duration of the contract. Differences in outlays will then be the difference between the premiums paid on standard life insurance and the premiums paid on five-year term insurance.

The difference impact of the two types of insurance programs on the wealth of the insured is obviously related in some way to the fact that standard policies have a cash surrender value whereas term policies do not. Cash surrender value may be thought of as an asset in that it can be withdrawn at any duration of the contract (thus bringing it to an end). The insured can also borrow from the company an amount not exceeding

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<sup>&</sup>lt;sup>3</sup> As mentioned earlier, one-year term insurance is generally renewable for a maximum of nine years and, in most cases, is not even convertible.

the cash value of his policy at a rate which used to be determined at the time of issue. Should the contract terminate because of death, however, the cash surrender value is included in the death benefit which is equal to the face value of the policy, regardless of the level reached by the cash surrender value at that time. In other words, cash surrender value is lost to the insured or to his estate whenever a standard life insurance contract terminates because of death. Cash surrender value can then be viewed as an asset with uncertain value and its expected value at any duration may be defined as the product of multiplying its predetermined value for that duration by the probability of survival of the insured to that duration.

The discussion above allows us to refer to equal and constant face values of policies when comparing the costs and benefits of the various standard life contracts to the costs and benefits of appropriate term contracts, since the contingency of death, which could reduce the value to the insured of the cash surrender value to zero, is fully accounted for through the survival rate. Then, for example, costs and benefits to the insured of a \$10,000 twenty-year endowment policy will be compared to the costs and benefits attached to a \$10,000 five-year term insurance contract renewed three times.

From a computational point of view, our approach will be as follows. The annual cost of standard life insurance will be the net premium; that is, the gross premium (basic rate x face value + policy fee) less dividends. Dividends available at the end of each year will be deducted from the gross premium of the following year. For each year, net savings will be the difference between the net premium on standard life and the premium (basic rate x face value + policy fee) on five-year renewable and convertible term insurance.

For every duration t, the rate of return r on net savings accumulated over years 1 to t will be the compound rate that equates those accumulated savings to the expected cash surrender value as of the end of year t. The problem is then to solve the following equation for r:

$$ECV_{t} = \sum_{i=1}^{L} \frac{NS_{i} (1+r)^{t}}{(1+r)^{i-1}} \qquad (t = 1, 2, ...,)$$

where:

ECVt

is the expected cash value at the end of year tand is equal to the quoted cash surrender value as of the end of t times the probability for the insured to survive to the end of year t.4

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NS.

is net savings or addition to accumulated savings at the beginning of year *i*.

The data used to solve the equation above are taken from *itone and Cox Life Insurance Tables* 1973 and survival rates are based on 1958 *CSO Mortality Table*. Table 5 shows our assessment of the rates of return on the savings component of three types of policies (nonparticipating standard life, participating standard life and twenty-year endowment policies<sup>5</sup> written for a man, at age 35, and issued by three major companies operating in Canada.<sup>6</sup> For each policy and for each duration (from 1 to 20), Table 5 shows the *expected cash value*, the annual *net wavings* and the *yield*. The last column of each table shows the average *yield* for each type of policy.

<sup>4</sup> Let us assume that a policy is issued on the day when the insured reaches age "a"; then,

 $ECV_{t} = \prod_{j=0}^{t-1} (1-d_{a+j}) CV_{t}$ 

where  $d_a$  is the mortality rate for ages between a and a+1.

<sup>5</sup> Participating and nonparticipating policies differ in that the former yields dividends while the latter does not. The main characteristic of endowment policies is that their cash surrender value reaches their face value at some predetermined date.

<sup>6</sup> The computer program was provided by Pierre MERCIER of the Economic Council of Canada.

Table 5-A

# YIELD ON SAVINGS THROUGH A \$10,000 NON-PARTICIPATING LIFE POLICY ISSUED AT AGE 35

		COMPANY A			COMPANY B			COMPANY C	-	0.0000000000000000000000000000000000000
Duration	ECV	NS	Yteid	ECV	SX	13 - 04 -	ECV	NS	11 14 24 24	- + - - (1)
-		2.9	.0000		38.3	0000	0.0	6.0	000	.0000
2	0.0	102.90	0000	0.0	08.3	CCCQ-		6.0	0000	0000
3	0.0	32.9	-1-00000	8.9	108.33	m	9.6	96.03		
4	0.0	32.9	0000*	1.0	(1) (0) (1)	0.1544	78.0	6.0	. 2847	503
2	14.0	2.9	0715	34.2	3	€ 56C*	05.6	6.0	.1468	1048
0	61.9	2	-0.02159	56.	2.5	.0391	44.	3.0	653	423
7		2.2	.0033	36.5	7.5	5010.		3.0	.0257	0108
2	53.6	2.2	65	55.6	7.5	.0055	17.2	3.0	.0035	0061
6	5	2 . 2	.023	03.1	7.5	\$\$10*	1.7	3.0	0092	157
10	139.1	2 . 2	0273	48.7	7.5	+610-	84.6	3.0	•C157	211
11	298.1	1 . 9	.0340	9.50	8.1	.5253	38.0	3.6	.0234	295
12	+ 24 ·	C6° 12	0.03783	460.5	·-1 • (0)	.0303	279.1	3.6	.C344	341
13	6.6	1.9	.0396	612.4	1.0	•0325	22.7	3.6	•C364	369
14	159.5	6.		4.15	8.1	.0335	563.6	3.6	1040.	0383
15	06.9	1.9	.0407	6.906	-	•0339	01.2	3.6	.0419	0388
16	2350.50	2.7		9.7.20	4.	.0358	350.2	0.5	4	406
17	9 . 8	-	.0421	5.40	8.4	.0369	995.0	0	-C45 8	416
1 00	324.4	2.7	•0421	346.2	ŝ	.0372	2.	0.5	.0455	419
19		5.		9.	3.	-037	270.3	0.5	-0	418
20	57	2.7	60%0*	613.0	4.	-0368	1.66	0.5	*0°	414

Table 5-B

# YIELD ON SAVINGS THROUGH A \$10,000 FARTICIPATING LIFE POLICY ISSUED AT AGE 35

		COMPANY &			COMPANY	(2)		COMPANY C		123
1010	ECV	SN	Yleid	EC :	NS	Ytela.	ECV	NS	Yield	11
0	0.0	67.1	1.000		37.6	0000		34.2	C000*	000
79	5	5.3	.619.	0.0	124.63	-0000-		1.0	.0000	.8730
23	5.12	37.4	.2825	26.	23.5	.4488	9.2	17.4	.5193	169
00 (*1	-	9.6	.1472	76.	19.4	.2217	47.2	14.0	-2457	.2052
54		21.3	• 0 8 C C	23.	4 . B	0.1207	94.3	10.5	.1311	.1106
0		102.50	351	579.21	08.96	-0.05938		63	-0.06065	05
86		8 .8	1010*	33.9	6.1	.0250	28 5	9.3	.0225	.0192
102		5.0	6300*	86.8	· • C	0+17+	63.4	4.6	5000-	000
117	7.73	2.	-0143	038.	6.9	.0079	016.6	9.8	.0135	119
133		7.4	+020*	187.3	2.1	.0154	168.0	4.9	.0225	197
151	2.	3.1	.0293	350.0	7.0	.0260	330.8	9-0	•0333	295
169	5	0.6	•0351	51C.1	2.2	.0325	491.0	5.4	\$C\$0°	360
185		4.9	•0383	667.4	7.5	.0369	648.5	0.3	.0452	404
203	3	0.9	-0415	821.6	1.	.0399	602.8	5.1	.0484	0433
220	¢.04	6.8	5 O.+	1972.35	0.0	.0419	3.6	0-0	.0505	452
235	• · ·	3.6	·0452	130.2	••	.0451	8.101	-8.23	.0531	478
252	•		•0499	283.5	2		261	-12.58	.0553	498
268		0	•0475	431.7	6.0	.049	408 -0	6.9	.0565	.05101
282			0483	574.3	00	498		-21.34	.0573	517
307	0.76	5	.0505	2798.79	-15.60	.0526	843.2	5.7	.0515	549

Table 5-C

# YIELD ON SAVINCS THROUGH A \$10,000, 20-YEAR ENDOWMENT INSURANCE POLICY ISSUED AT AGE 35

ECV    NS    Yield    ECV    NS    Yield    ECV    NS    Yield		COMPANY A			COMPANY B		CON	COMPANY C		Average
0.0    0.0 <th>Duration ECV</th> <th>NS</th> <th>6</th> <th>ECV</th> <th>SN</th> <th>1-4</th> <th></th> <th>NS</th> <th>Yielč</th> <th>Yteld</th>	Duration ECV	NS	6	ECV	SN	1-4		NS	Yielč	Yteld
2  467.58  397.10  -0.31787  358.15  362.00  -0.39627  0.0  363.99  -1.00000  -1.57    3  1879.97  367.59  375.30  -0.17659  1155.20  355.30  -0.17659  357.30  -0.17659  357.30  -0.17659  357.30  -0.017695  1155.01  355.30  -0.017695  1155.20  -0.07685  1155.20  -0.07685  1156.20  -0.07695  -0.017697  -0.017697  -0.017697  -0.017697  -0.011601  -0.0169747  -0.0169747  -0.01601  -0.01607  <	.0	422.7	0000 1		3.0	0000.1		32.8	0000-1	1.0
8 179.97  383.84  -0.14637  751.00  353.90  -0.17639  714.29  356.90  -0.19913  - 17    1 1 286.77  370.77  -0.04199  1165.71  345.30  -0.016952  1152.61  345.50  -0.016951  -0.04657  -0.016453  -0.016652  1152.65  -0.016652  1152.65  -0.016652  1152.65  -0.016652  1152.65  -0.016652  1152.65  -0.016652  -0.016652  1162.2.61  345.50  -0.016615  -0.01661  -0.016615  -0.01661  -0.01661  -0.01661  -0.01661  -0.01661  -0.01661  -0.01661  -0.01661  -0.016615  -0.016615  -0.016615  -0.016616  -0.01661  -0.01661	\$67.5	8 397.1	0.3178	58.	2.0	0.3962		63.9	1.0000	.5713
6  1286.79  370.77  -0.07685  1165.71  345.37  -0.08256  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.09747  -0.01435  -0.01435  -0.016010  -0.016010  -0.016010<	879.9	7 383.8	0.1463	51.	53.9	0.1763	14.2	54.9	1991.0	.1739
5  1695.70  357.33  -0.0(4199)  1528.10  336.30  -0.0(4575 00    7  2599.21  322.80  0.01013  243.60  316.30  -0.01633  1972.66  316.30  -0.01693  1972.66  0.00056 00    7  5599.21  322.80  0.010102  2849.55  296.60  0.001563  219.20  0.01663 00564  0.00266 00    3594.465  312.60  0.01603  3280.95  286.40  0.01148  2457.09  278.30  0.01267 01    3594.465  312.60  0.01603  3280.95  286.40  0.011168  286.709  20.0264  0.01267 02    16468.70  259.93  0.01963  3776.60  0.011168  286.709  0.02643 013    14468.70  259.93  0.003459  278.30  0.02195  3735.90  2036472 02    14468.70  259.91.30  0.033564  278.35  0.013472  278.39  0.023472 03    14468.70  259.91.30  0.023564  278.544  0.012565  278.379 <td>1286.7</td> <td>8 370.7</td> <td>0.0768</td> <td>165.</td> <td>45.3</td> <td>0.0825</td> <td>122.6</td> <td>45.6</td> <td>4260-0</td> <td>.0856</td>	1286.7	8 370.7	0.0768	165.	45.3	0.0825	122.6	45.6	4260-0	.0856
6  2149.47  332.70  -0.01633  -0.01693  1978.53  313.10  -0.01601  -0.01601    7  2599.21  322.80  0.001029  2425.02  301.60  2425.00  000266  0.00106    8  304.40  0.01102  2847.00  0.01169  286.70  0.01169  286.70  0.01169  286.70  0.01166  200.00	1695.7	0 357.3	0.0419	528.	36.3	0.0495	543.6	36.0	0.0467	.04
7  2599.21  322.83  0.00111  2413.27  3306.60  0.001367  200.00    8  304.45  312.60  0.01160  3280.95  296.70  0.01148  2455.02  331.60  0.00268  0.01367  0.01367    9  344.45  312.60  0.01600  3280.95  286.50  0.01367  200  0.02043  0.01367  0.01367  0.01367  0.01367  0.01367  0.01367  0.01367  0.02349  0.01361  0.02349  0.02349  0.023413  0.02471  0.02471  0.02413  0.023413  0.02413  0.02413  0.023413  0.023413  0.023413  0.023413  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.03414  0.04144  0.04444	2149.4	7 332.7	0.0143	972.6	16.3	6910.0	78.5	13.1	0.0160	.0157
8  3044.45  312.60  0.01029  2869.55  296.70  0.01191  3304.24  290.20  0.01367  .01    9  3484.68  302.10  0.01600  3280.95  286.40  0.01791  3304.24  278.30  0.02643  .01    1  4466.70  259.90  0.01560  3280.95  286.40  0.012195  3735.90  2566.00  0.02643  .00    1  4466.70  259.90  0.003165  4719.47  275.80  0.01356  3735.90  2566.00  0.032473  .02    1  4466.70  2591.30  0.01365  575.19  1.266.70  0.03345  278.50  0.03346  .03    2  55671.39  0.03556  577.23  20.3556  0.03738  5732.54  181.78  0.03418  .03    5  55671.39  211.10  0.03857  5732.54  181.78  0.05457  .03    5  55671.39  1567.28  5732.54  181.78  0.064518  195.96  0.044578  .03    5  55671.39  1567.35  1957.85  15	2599.2	322.8	.6011	413.2	36.6	-000a	25.0	8-IC	.0026	0015
9  3484.68  302.00  0.01600  3280.95  286.45  0.01791  3304.24  278.35  0.02643  .001    1  4466.70  259.93  0.01963  3715.80  0.00195  3715.90  0.03172  .002    1  4466.70  259.93  0.001963  475.83  0.002693  4719.47  232.91  3705.90  0.003172  .003    2  5541.22  239.57  0.003656  0.003565  0.003565  0.003318  .0033172  .003    3  5541.22  235.50  0.003565  5213.06  0.003565  0.003318  .003357  .003356  0.005195  .003    5  5541.22  235.50  0.03565  5213.06  252.53.33  0.063318  .003    5  5541.22  235.51  0.03565  520.55  0.033565  55478.16  .003    5  5541.25  157.25  157.25  157.25  157.25  .003  .006157  .0266.83  .0266.83  .0266.84  .0266.84  .0266.84  .0266.84  .0266.85  .0266.86  .0266.86  .0266.86 <td>3344.4</td> <td>5 312.6</td> <td>.0102</td> <td>2849.5</td> <td>96.7</td> <td>\$110-</td> <td>867.0</td> <td>90.2</td> <td>.013</td> <td>0118</td>	3344.4	5 312.6	.0102	2849.5	96.7	\$110-	867.0	90.2	.013	0118
0  3919.32  291.33  0.01963  3736.94  275.80  0.02195  3735.90  266.00  0.02471  .02    1  4466.70  259.93  0.02693  4217.13  245.43  0.022195  3735.90  256.00  0.03172  .03    2  559.93  0.02365  0.032691  4751.93  223.93  0.033172  .03    3  5541.22  235.50  0.033659  5213.04  223.93  0.033918  .03    4  6571.22  235.50  0.033556  0.033738  5732.54  0.033918  .03    5  5541.22  235.55  0.033738  0.033738  5732.56  0.033918  .03    5  5541.23  223.33  0.03877  566.00  0.04106  6778.13  195.82  .03    5  5541.23  169.77  0.03373  6206.83  164778  .03    5  5541.25  235.56  195.06  0.06416  7333.64  181.77  .03    5  5541.35  156.6.07  0.04116  10.04416  7878.13  114.09	3484.6	8 302.1	.0160	3280.9	86.4	9119	304.2	78.3	.0204	01
1  4466.70  259.90  0.02693  4217.13  245.40  0.02862  4751.93  223.90  0.03172  .03    2  5009.67  247.70  0.03165  4719.47  232.98  0.03291  4751.93  229.85  0.03655  .03    3  5541.22  235.50  0.03756  0.03756  5747.18  195.82  0.033918  .03    4  6505.222  235.50  0.03756  5247.18  195.82  0.033918  .03    5  5541.22  223.330  0.03738  5732.56  0.033618  .033918  .03    5  5541.22  223.330  0.03738  5732.56  0.034579  .03    5  5541.22  223.330  0.03773  0.03738  5732.56  181.778  .03    5  5571.39  211.10  0.03773  5746.716  1957.72  0.04106  .03    7  7567.35  156.73  0.04116  1733.64  181.778  0.046478  .04    7  7567.35  156.35  0.04691  0.046416  7811.71  99.00	3919.3	291.3	.0196	206.9	75.8	.0213	735.9	66.0	.0247	0221
2  5009.67  247.70  0.03165  4719.47  232.98  0.03291  4751.93  209.85  0.03625  .03    3  5541.22  235.50  0.03469  5213.04  220.55  0.03556  55247.18  195.82  0.03918  .03    4  6506.222  223.33  0.03469  5213.04  220.55  0.03738  5732.54  181.79  0.03410  .03    5  6571.39  211.10  0.03877  6169.47  195.72  0.038399  6206.83  181.79  0.04104  .03    5  5573.55  153.60  0.03877  6169.47  195.72  0.03878  0.04215  .03    7  7567.35  159.70  0.04116  157.356  130.60  0.04577  .04    7  7567.35  156.25  0.04416  7871.11  146.87  .04  .04    8  155.26  0.03393  0.04416  123.06  0.044979  .04    8  156.36  0.033956  138.325  107.82  0.04691  91.46  .04    8  160.0469	4466.7	0 259.9	.0269	217.1	45.4	.0285	247.8	23.9	71E0.	0364
3  5541.22  235.50  0.03469  5213.04  220.55  0.03556  5547.18  195.82  0.0318  .03    4  6362.22  223.33  0.03559  5696.75  238.14  0.03738  5732.54  181.78  0.04104  .03    5  6571.39  211.10  0.03877  6159.44  195.72  0.038399  6206.83  167.74  0.04215  .03    6  735.15  169.70  0.03877  6748.47  153.60  0.06416  6778.13  130.60  0.04579  .04    7  7548.58  155.26  0.05434  0.04416  7333.66  114.80  0.04539  .04    8  155.26  0.03934  753.65  0.04416  7333.66  114.80  0.04539  .04    8  8313.57  140.82  0.03954  138.325  137.82  0.04416  7871.71  99.00  0.04539  .04    8  8313.57  140.82  0.04691  9.04691  9124.58  67.49  0.04539  .04    9  9124.26  9126.50  92.06 <t< td=""><td>5009.6</td><td>7 247.7</td><td>.0316</td><td>719.4</td><td>32.9</td><td>.0329</td><td>751.9</td><td>39-8</td><td><b>•0362</b></td><td>0336</td></t<>	5009.6	7 247.7	.0316	719.4	32.9	.0329	751.9	39-8	<b>•0362</b>	0336
6571.39  211.10  0.03559  5696.75  208.14  0.03738  5732.54  181.78  0.064104  .03    6571.39  211.10  0.03773  6169.47  195.72  0.03839  6206.83  167.74  0.04215  .03    7567.35  159.70  0.03877  6748.47  153.60  0.04116  6778.13  130.60  0.04572  .04    7548.58  155.26  0.03934  7311.59  138.34  0.04299  7333.64  114.60  0.04539  .04    8013.57  140.82  0.03934  7311.59  138.34  0.04414  7871.11  99.00  0.04539  .04    813.3.57  140.82  0.03956  8383.25  107.82  0.04479  8390.44  93.20  0.04577  .04    8460.60  126.39  0.04479  8390.45  9106.50  92.56  0.04691  9124.28  57.40  0.05012  .04    9123.339  111.94  9124.28  5124.28  5124.20  0.04124  9124.28  5124.20  0.04797  .04	5541.2	2 235.5	.0346	213.0	20.5	.0355	247.1	95.8	.0391	0351
6571.39  211.10  0.03773  6169.44  195.72  0.03839  6206.83  167.74  0.04215  .03    7067.35  169.70  0.03877  6748.47  153.60  0.04116  6778.13  130.60  0.04727  .04    7548.58  155.26  0.03934  7311.59  138.34  0.04299  7333.65  0.04539  .04    8013.57  160.82  0.03934  7311.59  138.34  0.04299  7333.66  114.60  0.046539  .04    8013.57  160.82  0.03958  7857.16  123.09  0.04414  7871.11  99.00  0.04579  .04    8460.60  126.39  0.04479  8383.25  107.82  0.04479  8390.44  93.20  0.04577  .04    9123.39  111.94  0.04491  9124.28  67.40  0.05312  .04	6362.2	2 223.3	•0365	696.7	1.80	.0373	732.5	81.7	-0410	038
6  70.67.35  169.70  0.03877  6748.47  153.60  0.06416  6778.13  130.60  0.06472  .04    7  7548.58  155.26  0.03934  7311.59  138.34  0.04299  7333.64  114.80  0.05639  .04    8  8013.57  140.82  0.03954  7657.16  123.09  0.06414  7871.71  99.00  0.064741  .04    9  80.13.57  140.82  0.03954  7657.16  123.09  0.06414  7871.71  99.00  0.064741  .04    9  8460.60  126.39  0.03956  8383.25  107.82  0.06479  8390.44  83.20  0.064797  .04    9  9123.39  111.94  0.064136  92.56  0.064691  9124.28  0.065012  .04	6571.3	9 211.1	.0377	169.4	95.7	.0383	206.8	57.7	.0421	0394
75 48.58  155.26  0.03934  7311.59  138.34  0.04299  7333.64  114.80  0.054539  .04    8013.57  140.82  0.03958  7657.16  123.03  0.04414  7871.71  99.00  0.064741  .04    8460.60  126.33  0.03956  8383.25  107.82  0.04479  8390.44  93.20  0.04777  .04    9123.39  111.94  0.04479  9124.28  9126.50  92.56  0.04691  9124.28  67.40  0.05012  .04	7067.3	5 159.7	.0387	748.4	53.6	1140-	778.1	30.6	-0447	0415
8  8013.57  140.82  0.03958  7857.16  123.09  0.04414  7871.71  99.00  0.04791  .04    9  8460.60  126.39  0.03956  8383.25  107.82  0.04479  8390.44  83.20  0.04777  .04    0  9123.39  111.94  0.04136  9126.50  92.56  0.04691  9124.28  57.40  0.05312  .04	7 7548.5	8 155.2	.0393	311.5	38.3	.0429	333.	14.8	-0463	042
9 8460.60 126.39 0.03956 8383.25 107.82 0.04479 8390.44 83.20 0.04797 .04 0 9123.39 111.94 0.04136 9126.50 92.56 0.04691 9124.28 57.40 0.05312 .04	8 8313.5	140.8	.0395	657.1	23.0	1490*	71.	0-6	+1+0-	437
0 9123.39 111.94 0.04136 9106.50 92.56 0.04691 9124.28 67.40 0.05312 .04	9 8460-6	0 126.3	-0395	383.2	8.7C	-0447	390.	3.2	61 +0-	0441
	0 9123.3	9 111 -9	.0413	106.5	92.5	.0469	124.2	7.4	1020-	461

Our results show rates of return which are only slightly higher than those found in previous studies (see Tables 1 to 4). This can be explained by the fact that we assume constant insurance protection to be purchased under term contract. Let us recall that other students of the problem, whether they use one-year or five-year term insurance as part of an alternative to standard life insurance, all assume that the protection purchased decreases over the years.

Earlier in this paper, we criticized the use of one-year term premiums and we suggested that premiums on five-year term insurance be used. Cameron has done so but his approach was formulated in terms not at all practical since, in his assessment of the cost of protection, premiums on five-year term insurance are multiplied by an amount of protection which decreases every year. In so doing, his approach falls only partly out of the range of our criticism of all the methods. By underestimating what we think to be the relevant cost of protection, we feel that all methods provide overestimated streams of annual savings. In the face of a given pattern of cash surrender value accumulation, it is no surprise that these approaches lead to relatively low rates of return.

As in previous studies, standard life participating policies rank first in terms of average yield when a twenty-year

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holding period is assumed. Twenty-year endowment policies rank second and nonparticipating policies rank third. The minimum holding period for the yield to become positive is 7 years, the negative yields over the early years resulting from heavy front-end loading.

Starting from those results, one has to be cautious when inferring about the whole population of standard life insurance policies. Those yields should merely be viewed as an indication of the returns available. They do, however, show an important feature of such rates which is their dependence on the length of the assumed holding period. Coupled with probable heavy withdrawal rates in the early periods of the contracts, this last point would lead to very low effective yields.

# Concluding Remarks

When a comparison is to be made between these yields and yields on other financial assets, a number of differences have to be stressed;namely, differences in *tax status*, *liquidity* and risk.<sup>7</sup> In a competitive world, these differences would account for the observed differences in nominal rates of return. We shall conclude with some comments on these three issues.

7 This last section draws heavily on CAMERON, pp. 15-20.

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There are some tax advantages to saving through life insurance. For example, the policy holder pays no income tax on the amounts which his savings earn while in the life policy. Moreover, at the end of the holding period, only part of the cash surrender value becomes taxable; more precisely, the taxable amount is then the terminal value less the total of net premiums paid (that is, both the savings elements and the protection elements). In this way, the cost of protection can be deducted. When the savings element is small, relative to the protection element, this feature may remove the entire tax liability.

On the *liquidity* side, the insured can borrow up to 90 or 95 per cent of accumulated cash value at an interest rate which used to be guaranteed in the contract at time of issue. However, in the early years, only part of the net level premium reserve held for the policy holder is made available through cash surrender value so that the advantage of realization applies to only a part of the policy holder's investment in his policy.

As for *risk*, one can think of various sources of uncertainty that cause investment in life insurance to be a risky investment. The first source applies only to participating policies, the return on which is contingent upon profits and dividends.<sup>8</sup>

<sup>&#</sup>x27; In our calculations, we used the dividends projected by the companies themselves which were based on past experience.

The second source of uncertainty is related to the probability of termination because of death. This aspect has already been discussed in relation to its effect on expected returns. At any time, however, termination of the contract because of death will cause the effective return to be zero, whereas, in the case of voluntary withdrawal, the effective return for the same duration will be larger than that shown in Table 5. A third source of uncertainty has been revealed by recent studies in the field which have suggested that a probability can also be assigned to voluntary withdrawal. Consideration of this probability in our calculations would reduce the expected returns and would add to uncertainty.

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