# PIT SLOPE MANUAL 

## supplement 2-2

## DOMAIN ANALYSIS PROGRAMS

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1. Summary
2. Structural Geology
3. Mechanical Properties
4. Groundwater
5. Design
6. Mechanical Support
7. Perimeter Blasting
8. Monitoring
9. Waste Embankments
10. Environmental Planning

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## CONTENTS

SUMMARY
Page
INTRODUCTION ..... 1
FILE PREPARATION AND DEFINITION OF GROUPS ..... 2
Program DTFX ..... 2
Solution ..... 2
Capabilities ..... 4
Input ..... 4
Output ..... 4
Variables ..... 4
Storage requirements ..... 4
Program TRVL2 ..... 4
Input ..... 4
Output ..... 5
Run time ..... 5
Program INPT1 ..... 5
Solution ..... 6
Capabilities ..... 6
Input ..... 6
Output ..... 7
Variables ..... 7
Storage requirements ..... 7
Program MAP3 ..... 7
Solution ..... 7
Capabilities ..... 8
Program options ..... 8
Input ..... 8
Output ..... 9
Variables ..... 9
Storage requirements ..... 10
Sample Run - Stage 1 ..... 10
COMPUTATION OF GROUP MEANS AND DISPERSIONS ..... 14
Program WNST5 ..... 14
Solution ..... 15
Capabilities ..... 15
Input ..... 15
Output ..... 15
Subroutines ..... 15
Variables ..... 16
Storage Requirements ..... 16
Program GRPKI ..... 17
Solution ..... 17
Capabilities ..... 17
Input ..... 17
Output ..... 18
subroutines ..... 18
Variables ..... 18
Storage Requi rements ..... 18
Program INPK1 ..... 18
Solution ..... 19
Capabilities ..... 20
Input ..... 20
Output ..... 21
Subroutines ..... 21
Variables ..... 21
Storage requirements ..... 21
Program GRPS ..... 21
Solution ..... 22
Capabilities ..... 22
Input ..... 22
Output ..... 22
Subroutines ..... 22
Variables ..... 23
Storage requirements ..... 23
Sample Run - Stage 2 ..... 24
DISPLAY OF GROUP MEANS AND DISPERSIONS ..... 28
Program DSPD ..... 28
Solution ..... 28
Capabilities ..... 28
Options ..... 28
Input ..... 29
Output ..... 30
Subroutines ..... 30
Variables ..... 31
Storage requirements ..... 31
Program NPPL1 ..... 31
Solution ..... 31
Capabilities ..... 31
Input ..... 31
Output ..... 32
Variables ..... 32
Subroutines ..... 33
Storage requirements ..... 33
Program WNDPLT3 ..... 33
Solution ..... 34
Capabilities ..... 36
Options ..... 36
Input ..... 36
Output ..... 37
Variables ..... 37
Storage requirements ..... 37
Sample Run - Stage 3 ..... 37
DEFINITION OF DOMAINS AND CHARACTERIZATION OF DOMAIN SUBFABRICS ..... 49
Program HOMO ..... 50
Solution ..... 50
Capabilities ..... 50
Options ..... 50
Input ..... 53
Output ..... 53
Subroutines ..... 53
Variables ..... 54
Storage requirements ..... 54
Program DDKY ..... 54
Solution ..... 54
Capabilities ..... 54
Input ..... 54
Output ..... 55
Variables ..... 55
Storage requirements ..... 55
Sample Run - Stage 4 ..... 55
FIGURES
Page
1 Stage 1 - File preparation and definitions of groups ..... 3
2(a) Flow diagram for program DTFX - Part 1 ..... 3
2(b) Flow diagram for program DTFX - Part 2 ..... 3
3 Flow diagram for program TRVL2 ..... 5
4(a) Flow diagram for program INPT1 - Part 1 ..... 5
4(b) Flow diagram for program INPT1 - Part 2 ..... 6
5 Flow diagram for program MAP3 ..... 8
6 Input parameters for Stage 1 ..... 11
7 Traverses with numbers of observations (above) and traverse numbers (below) ..... 12
8 Stage 2 - Computation of group means and dispersions ..... 14
9 Flow diagram for program WNST5 ..... 15
10 Flow diagram for program GRPK1 ..... 17
11(a) Flow diagram for program INPKI - Part 1 ..... 19
11(b) Flow diagram for program INPK1 - Part 2 ..... 19
11(c) Flow diagram for program INPKI - Part 3 ..... 20
12 Flow diagram for program GRPS ..... 22
13 Input to Stage 2 ..... 26
14 Stage 3 - Display of group means and dispersions ..... 29
15 F1ow diagram for program DSPD ..... 29
16(a) Flow diagram for program NPPL1 - Part 1 ..... 32
16(b) Flow diagram for program NPPL1 - Part 2 ..... 32
17(a) Flow diagram for program WNDPLT3 - Part 1 ..... 34
17(b) Flow diagram for program WNDPLT3 - Part 2 ..... 34
17(c) Flow diagram for program WNDPLT3 - Part 3 ..... 35
18 Input to Stage 3 ..... 38
19 Plot of true orientation ..... 40
20 Plot with mean vector vertical ..... 41
21 Plot of groups in true orientation ..... 43
22 Plot of groups with mean vertical ..... 44
23 Point diagram of 297 observations ..... 45
24 Point diagram of 297 orientations with mean in vertical position ..... 46
25 Locations and orientations of observed discontinuities ..... 46
26 Point diagram of 32 group means ..... 47
27 Point diagram of 32 groups means with mean vertical ..... 47
28 Locations and orientations of deviations of group means from overall mean ..... 48
29 Stage 4 - Definition of domains and characterization of doma in subfabrics ..... 49
30(a) Flow diagram for program HOMO - Part 1 ..... 50
30(b) Flow diagram for program HOMO - Part 2 ..... 51
30(c) Flow diagram for program HOMO - Part 3 ..... 51
30(d) Flow diagram for program HOMO - Part 4 ..... 52
30(e) Flow diagram for program HOMO - Part 5 ..... 52
31 Flow diagram for program DDKY ..... 55
32 Coding form for INPTI and INPK1 ..... 58

## SUMMARY

This report documents a User's Manual for the domain analysis of structural data. Card decks are supplied separately. Documentation of the computer programs that comprise the system has been carried out to ASCE standards (ASCE Proceedings 99, SM3, 1973, pp 249-266).

Domain analysis proceeds in four stages and the computer programs documented are grouped in these four stages. In stage 1 , four programs -

DTFX, TRVL2, INPT1 and MAP3 - prepare files and define groups of observations. In stage 2, four further programs are introduced - WNST5, GRPK1, INPKI and GRPS - which assist in the computation of group means and dispersions. Stage 3 requires three programs - DSPD, NNPL1 and WNDPLT3 - for the display of group means and dispersions. Stage 4 uses two further programs - HOMO and DDKY.

## INTRODUCTION

1. This analysis defines the orientation domains of a particular discontinuity. The discontinuity type (fabric element) to be analyzed must first be identified and retrieved from the master data file before the domain-analysis procedure can begin. Observations of orientation of the discontinuity type within the study area are then divided into groups and each group is characterized by a mean and dispersion. Statistical tests are used to define the largest possible areas within which the means and dispersions of the groups are similar. These areas are subfabric
domains. Since the statistical tests are based on Fisher's model, the distribution of poles to the fabric element within each group should be unimodal and axially symmetric.
2. The procedure may be conveniently divided into four stages which are described as: File Preparation and Definition of Groups, Computation of Group Means and Dispersions, Display of Group Means and Dispersions, and Definition of Domains and Characterization of Domain Subfabrics.
3. The following four Sections describe each of these four stages in detail.

## FILE PREPARATION AND DEFINITION OF GROUPS

4. Stage 1 is illustrated by the flow diagram in Fig 1, and consists of four steps,
5. Stage la. The file containing data for the fabric element, shown as uncorrected data file in Fig 1, is processed by the program DTFX. This produces a new data file in which every observation is associated with a distance from the traverse origin and observations on each traverse appear in order of increasing distance. This makes it possible to split traverses in the definition of groups.
6. Stage 1b. One of the requirements of the statistical tests for homogeneity of group means and dispersions is that groups contain not less than five observations. To satisfy this requirement, a map is produced that shows traverses and the number of observations on each traverse. This in turn requires that program TRVL2 uses the master traverse file and the data file produced by DTFX to produce a new corresponding traverse file.
7. Stage 1c. Program INPT1 reads the new traverse file and stores the data for program MAP3, which produces the map.
8. Stage ld. The groups are outlined on the traverse map, and the group specifications tabu-
lated in terms of traverse and observation numbers on each traverse.
9. Note that in all subsequent stages, references to the data files are taken to mean the new or adjusted data file, and all references to the traverse file are taken to mean the new traverse file.

## PROGRAM DTFX

10. The program makes adjustments to a data file so that it is in a suitable form for areal analysis. The fabric data are examined one traverse at a time. Observations without corresponding distances are assumed to be uniformly distributed along the traverse. All observations on the traverse are then ordered by increasing distance. A flow diagram is given in Fig 2(a) and 2(b).

## Solution

11. The fabric data are examined one traverse at a time. Those observations that have no corresponding distances associated with them are distributed uniformly along the traverse. The algorithm for doing this is as follows:


Fig 1 - Stage 1 - File preparation and definitions of groups

$$
\begin{aligned}
1= & \text { length of traverse } \\
n= & \text { number of observations wi thout recorded } \\
& \text { distance } \\
x(i)= & \text { distance assigned to the } i-\text { th observa- } \\
& \text { tion without distance } \\
a= & 1 / n \\
b= & a / 2 \\
x(i)= & (i * a)-b: i=1,2, \ldots n
\end{aligned}
$$

All observations on the traverse are then ordered by increasing distance, and all the data for that traverse are written on the output file. The next traverse is then read from the input file and the process repeated. The first observation with zero distance following at least one observation with-zero distance is taken as the first observation for which distance is not recorded. This observation and all those that follow it in the traverse are assumed to have no distance recorded.


Fig 2(a) - Flow diagram for program DTFX - Part 1


Fig 2(b) - Flow diagram for program DTFX - Part 2

## Capabilities

12. Maximum number of observations in one traverse is 100. Those observations without distance must follow those with distance in each traverse.

## Input

13. Unit I - tape or disk - input data file. Record length is 112 bytes. The records must all have the same length and format. Twenty-eight variables are read in each record with the format (A4, I4, 3A4, 2I3, I4, A4, AI, I4, 2I6, 15, 14A4). This file is created by CONVRT.

Variable no. Columns Specifications

| 2 | $005-008$ integer, traverse number <br> $021-023$  <br> integer, trend of  <br> traverse  |  |
| :--- | :--- | :--- |
| 7 | $024-026$ | integer, plunge of <br> traverse |
| 8 | $027-030$ | integer, length of <br> traverse |
| 11 | $036-039$ | integer, distance along <br> traverse |
| 12 | $040-045$ | integer, easting <br> integer, northing <br> 13 |
| 14 | $046-051$ | integer, elevation |

Output
14. Unit 6-printer - statistics. Record length is 37 bytes. Prints number of traverses processed and the number of observations that were without distance.
Unit 2 - tape or disk - output data file. Record length is 112 bytes. Same as input data file (TAPE 1).

## Variables

```
END end-of-traverse flag
FLAG flag to indicate non-zero distance has been found
K array to contain input lines
TITLE array to contain title
DTR degrees-to-radians conversion factor
NTOT counter of observations in file without
        distance
```

NTRAV
I index J index
N0 number of observations on traverse
TR trend of traverse
PL plunge of traverse
CP cosine of plunge of traverse
DNORTH first direction cosine of traverse
DEAST second direction cosine of traverse
DELEV third direction cosine of traverse
NFIRST number of first observations on traverse without distance
NZ number of observations on traverse without distance
A see "method"
B see "method"
X see "method"
$L \quad$ index
MIN smallest distance
M index

External References: FORTRAN functions SIN, COS, FLOAT.

## Storage Requirements

15. Input and output file formats described elsewhere.

| Code | bytes | words |
| :---: | :---: | :---: |
| DTFX | $\frac{5724}{}$ | $302 B$ |
|  | $\underline{10205}$ (buffers) | $\underline{4229}$ |
|  |  | 7257 |

## PROGRAM TRVL2

16. The program reads traverse data from a traverse file. By simultaneously reading the data file, the program obtains the range of line numbers in the data file that corresponds to observations on each traverse. A new traverse file is produced containing this information. A flow diagram is presented in Fig 3.

## Input

17. Unit 1 - tape or disk - traverse identification from data file. Record length 808 bytes


Fig 3 - Flow diagram for program TRVL2
unformatted. This is usually the output of INPTl or INPKT.

Unit 4 - tape or disk - traverse list. Record length defined by format. Identical records, one for each traverse. Records are composed of:
a. double-word variable containing one to eight character identification of the traverse followed by
b. single word variables that may contain other information about the traverse
Unit 5 - card reader - formats for reading and writing the traverse data files. There are two records, one format on each (one for reading, one for writing). The formats are in columns 3-102. See Sample input.

Qutput
Unit 6,8 - tape, disk or card punch - printed out-
put. Record length defined by format. Title of the traverse. New traverse file. Same variables as read on input unit 4, preceded by 4 full word integer variables containing:
a. sequence number of traverse in input file 4.
b. data file line number of first observation of this traverse
c. data file line number of last observation on this traverse
d. number of observations of this traverse.

## Run Time

18. The program required 1.3 seconds of CPU time to process a data file containing 297 observations on 43 traverses.

## PROGRAM INPTI

19. The program reads specified variables from an input file and writes the data in a convenient form for use by other programs in the areal analysis package. A flow diagram is shown in Fig 4(a) and 4(b).


Fig 4(a) - Flow diagram for program INPT1 - Part 1


Fig 4(b) - Flow diagram for program INPT1 - Part 2
20. INPT1 accepts as parameters the number of variables to be read from each record of the input file and the format for reading those variables. The first field in the format specification must refer to a line-type character and must be specified as Al. The given number of variables must include the line-type character. Since the data array is declared as integer, and some FORTRAN input routines will not allow data to be read into an integer variable with an $F$ format code, ie, as a real number, all input data must be in integer form and all fields must be specified with an I format code. If it is desired to convert integers to real numbers before they are placed in the output file, an additional set of
parameters may be added to the parameter card containing the input format. These parameters specifiy which input variables are to be converted to real numbers and how many decimal places each should have.
21. At each data record in the input file, the program reads the specified number of one-word variables using the specified format. The data are written unformatted onto the output file as a header record followed by data records. Each output data record except the last always contains the data from 100 input records.

## Solution

22. The output data records are first written onto a scratch file. After all the input records have been read, the title record is written onto the output file, and the output data records are then copied from the scratch file to the output file.
23. After each set of input records, terminated by a delimiter record, has been processed, the program attempts to read another title record. If an end-of-file condition results, the program terminates normally. If another title record is read, the program continues as before. If the next record is not a title record, the program stops after writing an error message.

## Capabilities

24. Maximum length of the given format is 60 characters. Maximum number of variables read from each input record is 10 .

## Input

Unit 1 - tape or disk - input data file. Record length defined by format. The file contains one or several sets of data records. Each set must be preceded by a title record and followed by a delimiter record. The title record must contain the letter $T$ in column 1 (this is called the line type character).
Unit 5 - card reader - a single record up to 102 bytes long. Record length: 102 bytes formatted.
Col 1-2 contains the number of variables to be read, right-justified.
3-62 FORTRAN format for reading input data from
unit 1.
63-102 up to 20 2-digit numbers. These numbers are interpreted in pairs: the first number of each pair is the number of a variable to be converted to a real number; the second number of the pair is the number of decimal places.
Example: '43' asks for the fourth variable (do not count the line-type character) to be divided by $10^{3}$. The result is placed in the output record as a real number.

Unit 7 - scratch tape or disk - scratch file. Record length: $8+400 \times N V$ bytes unformatted. Output data records are stored in this file until they are copied to the output file.

## Output

Unit 6-printer messages - record length: 35 bytes unformatted. The program writes the number of output records. Error messages are selfexplanatory.
Unit 8 - tape or disk - output file. Record length: $8+400 \times N V$ unformatted. Output is written unformatted on this file as a header record followed by data records. Each header record contains four full word integers followed by the 120 -byte title. The four integers are:
a. the total number of words in this set of data
b. the number, NV, of variables read from each input record
c. the total number of input records read in this set of data
d. the number of output data records following the header record.
Each data record contains 2 full word integers followed by the data from up to 100 input records. The integers contain:
a. the number, $N$, of input records in this output record ( $100 \max$ )
b. the number of words of data in this output record $=N \times N V$
The data are the variables from the input records in the order in which they were read.

Variables

| NVAR | number of variables |
| :--- | :--- |
| FMT | format |
| IC | conversion factors |
| LINTYP | line-type character |
| NTOT | total number of data records read |
| NPHR | number of output data records (after title <br> record) |
| N number of data records in batch |  |
| DATA | array to contain the data |
| IV number of variable to be converted to real |  |
| RDATA | array to contain real values - same loca- <br> tion as DATA |
| IE | number of data words in data record |
| NN number of data words in entire sample |  |

25. The arrays DATA and RDATA occupy the same storage.

| Code | bytes | words |
| :---: | :---: | :---: |
| INPTT | 2400 | 1280 |
|  | $\frac{12246(\text { buffers })}{14646}$ | $\frac{5286}{6566}$ |

## PROGRAM MAP3

26. The program draws a map with coordinate grid lines showing either (1) survey traverses, (2) strikes of discontinuities, or (3) threedimensional orientations of discontinuities. Three-dimensional orientations are represented by a line whose azimuth and length are those of a line drawn on an equal-area projection from the centre of the projection to the point representing the given orientation. A flow diagram is given in Fig 5.

## Solution

27. MAP3 determines the maximum and minimum $X$ and $Y$ values from the data. It then determines the position of the first grid line above the maximum $X$ value, and the position of the first grid line below the minimum $X$ value, using the given interval between grid lines. This is repeated for the $Y$ values. The four grid lines so


Fig 5 - Flow diagram for program MAP3
determined become the borders of the map. This border is drawn, as well as all intermediate grid lines, and a title is written below the lower border. The data points are then plotted. Optimization of plotting is achieved in the following way: Using the extreme $X, Y$ values corresponding to the borders of the map, the program subdivides
the whole rectangular region into a 60 by 60 grid, determines the number of observations within each grid square, and sets up pointers to locate all observations within each grid square. This enables the program to do a scan on the 60 by 60 matrix to optimize plotting.
28. The scale of the map is determined by a scale factor read from the parameter card. This scale factor specifies the number of data units that are to correspond to one inch on the map.
29. Beside each data point the program writes one number and one character string of up to four characters. If the number is zero, it is not plotted. From each data point a line is drawn with azimuth $A$ and length, $L$. $A$ and $L$ are determined from the data items NUM1 and NUM2 associated with the data point, in a way determined by the parameter MODE.

## Capabilities

30. Maximum number of data points in one map is 1500 .

## Program Options

31. If $M O D E=1$ (traverses) $A=N U M 1$ and $L=N U M 2 /$ SCALE (same scale as coordinates). If MODE $=2$ (strikes) $A=N U M 1$ and $L=0.5$. If MODE=3 (threedimensional directions) $A=$ NUMT and $L=$ PROJARD (NUM2, DPI), where PROJARD(NUM2, DPI) is the distance on a Lambert equal-area projection with radius DPI from the centre of the projection to a point representing a plunge of NUM2 degrees. DPI is read from the parameter card.
32. Optional printout of the input and certain derived data are controlled by the LIST parameter.

## Input

Unit 1-tape or disk - data unformatted, as written by program INPTI, INPKI or DSPD. Record length: 2408 bytes, unformatted.

Unit 5 - card reader - record 1 ength: 50 bytes formatted. One record containing:
Column Content


The values are for variables: NUMI, NUM2, TREND, PLUNGE,PROJX,PROJY (PROJEX and PROJY are the $X$ and $Y$ increments from the beginning to the end of the plotted line segment).

Output
Unit 6 - line printer. Record length: 112 bytes, formatted. Parameter list and messages. Input parameters.

Unit 7 - line printer. Record length: 120 bytes, formatted. Data listings. These listings are controlled by LIST parameter on I/0 unit 5 parameter card.
Unspecified Plotter or plotter output tape. Record length: defined by plotting routines. This unit is selected by the plot routines which are not part of these programs.

## Variables

KEY control code
INTGR grid interval (data units)
SCALE scale (data units per inch)
DPI radius of projection for plotting orientations
LIST printout parameter
XSTART $x$-coordinate of left-hand side of map
NN number of data words in sample
NV number of variables in input
NO number of observations in input
NPHR number of data records following title record
TITLE array to contain title
$N \quad$ number of observations in data record
IE number of data words in record
IX,IY $\quad x$ and $y$ coordinates
IZ number to be written beside data point
LABEL character string to be written beside data point
NUMT azimuth
NUM2 see "options"
External References: The following subroutines
from the Calcomp plotting library:
$\operatorname{PLOT}(X, Y, J)$
Moves the pen from its current position to the point ( $X, Y$ ) with pen up $(J=3)$ or down ( $J=2$ ). Plot origin is reset to $(X, Y)$ if $J<0$.
WHERE (X,Y,F)
Returns in $X, Y$ the current pen position, and in $F$ the current scaling factor.
PLOTS
Initializes the plotting routines.
XLIMIT(X)
Resets the default limit of plotting in the

X-direction to $X$ in.
NUMBER $(X, Y, H, R, T, N)$
Writes the real number, $R$, with $N$ decimal places at the location $X, Y$ with a character height of $H$, making an angle of $T$ degrees with the positive $x$ axis (counter-clockwise).
$\operatorname{LINE}(X, Y, N, I, J, K$,
Given $N$ data points whose coordinates are in every $i$-th word of the vectors $X$ and $Y$, either draws a line through the points ( $J=0$ ), or draws the symbol number $K$ at each point $(J<0)$ or both ( $\mathrm{J}>0$ ).
SYMBOL (X,Y,H,IC,T,N)
Starting at the point $X, Y$ and using a symbol height of $H$ in., either draws $N$ characters stored in EBCDIC in the array IC ( $N>0$ ) or draws symbol under IC ( $\mathrm{N}=1$ ) or draws symbol under IC with a line from the current pen position ( $N=-2$ ). The symbols make an angle of T degrees with the positive $x$ axis (counterclockwise).

## Storage Requirements:

| Code | bytes |  | words |
| :---: | :---: | :---: | ---: |
| MAP3 | 008144 | 2547 | 1383 |
|  |  | 10205 (buffers) | 4229 |
| PGRID | 001072 | 454 | 300 |
| PPTS2 | 001928 | 247 | 167 |
| TPXYEQ | 000928 | 117 | 79 |
| PPTS | 002112 | 353 | 235 |
| RJUST8 | 000560 | 47 | 33 |
| PPL0T | 008680 | 43441 | 18209 |
| LEN1 | 000512 | 24 | 20 |
| PPTS3 | 002120 | 401 | 257 |
| LIMT |  | 10 | 8 |
| Labe1led COMM0N |  |  | 9003 |
| MAP1 | 042016 | 21453 | 9208 |
| areas- |  |  |  |
| MAP2 | 018416 | 21990 | 55131 |

## SAMPLE RUN - STAGE 1

| Input Files |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Uncorrected Data File |  |  |  |  |  |  |  |  |  |  |  |  |
| Unit 1 input to DTFX |  |  |  |  |  |  |  |  |  |  |  |  |
| TTEST DATA |  |  |  |  |  |  |  |  |  |  |  |  |
| D2DM0051 | 3 | 126967 | 259-5 | 217150 3 | 538053989391 D069687BG | 66 | 23-1589-3570 | 9205 | 33L | 0 | 0 | OMDSR2 |
| D2DM0051 | 3 | 126967 | 259-5 | 2171505 | 89805363939D936969DBG | 83 | 27 -553-45D6 | 8910 | 27 L | 20 | 0 | Orisk 3 |
| D2D ${ }^{\text {do051 }}$ | 3 | 126967 | 259-5 | 2171506 | 92805360939D9369690BG | 83 | 27-553-4506 | 8910 | 27L | 20 | 0 | DCMSR1 |
| D2D\%0051 | 3 | 126967 | 259-5 | 21715010 | 17680527893907769697BG | 62 | 26-2058-3871 | 8988 | 291 | 10 | 0 | OMDSR3 |
| 220140051 | 3 | 126967 | 259-5 | 21715014 | $0805450939110696 \mathrm{B2BG}$ | 46 | 17-2031-2103 | 9563 | 628 | 0 | D | OMISR2 |
| 020M0051 | 3 | 126967 | 259-5 | 21715015 | D20545D939110696828G | 83 | 27-553-4506 | 8910 | 27 日 | 0 | 0 | OCMSR1 |
| 02DH0052 | 3 | 126967 | 2625 | 2802201 | 080479093BB5069692BG | 96 | $15 \quad 271-2574$ | 9659 | 3017 | 2172FD-9255 | 3587 | 12151/DSR3 |
| ... | - | .... | -• | ... | ... | . | - . . | , . | - . | . . | . | - . |
| 12\%HMDD89 | 3 | 116700 | 241-28 | 14023023 | 0805360941610673488 G | 61 | 18-1498-2703 | 9511 | 58 F | 0 | 0 | OCOLS4 |

## Master traverse file

Unit 4 input to TRVL2

| *0101/2DM | 2/59421/01/0R4/5920/ | /78383 /9 | /222/-02/1001/ /68/312/ |
| :---: | :---: | :---: | :---: |
| *0101/2DM | 3/59538/01/0R4/5920/ | /78314 /96363 | 7/ 0/ 211/ /20./317/ |
| *0101/2DM | 4/59425/01/OR4/5920/ | /78237 /96226 | /201/-02/ 998/ /41/291/ |
| *0101/2DM | 5/58837/01/OR4/5870/ | /78202 /96299 | /184/-03/ 289/ /12/274/ |
| *0101/2DM | 6/58808/01/OR4/5870/ | /78186 /96242 | /200/-02/ 898/ /42/290/ |
| *0101/2DM | 7/58881/01/0R4/5870/ | /78147/9607 | /201/+02/ 278/ /29/291/ |
| *0101/2DM | 8/58880/01/0R4/5870/ | /78118/95961 | /191/-01/ 185/ /11/281/ |
|  |  |  |  |
| *0101/2HM | 90/64088/ 2/ 4/. / | /79118/94566 | /162/-04/ 330/ / 4/172/ |

Output files

Data file
Unit 2 output from DTFX
Unit 1 input to INPTl

TTEST DATA

| D2DM | 51 | 3 | 126967 | 259 | -5 | 2171503 | 5380539893910069687 BG 66 | 66 | 23-1589-3570 | 9205 | 33L | 1 | 0 | D | OMOSR2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| D20M | 51 | 3 | 126967 | 259 | -5 | 21715014 | 5480539793910069687BG 4 | 461 | 17-2031-2103 | 9563 | 62 B |  | 0 | 0 | OMDSR2 |
| 020M | 51 | 3 | 126967 | 259 | -5 | 2171505 | 8980536393909369690BG 8 | 83 | $27-553-4506$ | B910 | 27L | 2 | 0 | 0 | OMDSR3 |
| 02DM | 51 | 3 | 126967 | 259 | -5 | 2171506 | 9280536093909369690BG 8 | 832 | $27-553-4506$ | B910 | 27L | 2 | 0 | 0 | OCMSR1 |
| D20M | 51 | 3 | 126967 | 259 | -5 | 27715015 | 163B0529193907969696BG 8 | 832 | 27-553-4506 | 8910 | 27 B |  | 0 | 0 | OCMSR1 |
| 020M | 51 | 3 | 126967 | 259 | -5 | 21715010 | 17680527893907769697BG 6 | 62 | 26-2058-3871 | 8988 | 29L | 1 | 0 | 0 | OMDSR3 |
| 020M | 52 | 3 | 126967 | 262 | 5 | 2802201 | 080479093885069692BG 9 | 961 | 15 271-2574 | 9659 | 30L Z |  |  | 87 | 15MDSR2 |

Traverse file
Unit 8 output from TRVL2
Unit 1 input to INPT1

| TTEST | DATA |  |  |  |  |  | TRAVERSES |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 1 | 6 | 62DM | 5169682 | 3 | 126967 | 80545 | 93911 | 259-05 | 217 |
| 51 | 7 | 13 | 72DM | 5269692 | 3 | 126967 | 80479 | 93885 | 262 | 5280 |
| 52 | 14 | 21 | 82DM | 5469142 | 3 | 126900 | 80569 | 93962 | 258 | 472 |
| 53 | 22 | 49 | 282DM | 5569047 | 3 | 126900 | 80410 | 93953 | 252-02 | 294 |
| 54 | 50 | 59 | 102DM | 5668502 | 3 | 126833 | 80592 | 94086 | 247+01 | 133 |
| 55 | 60 | 90 | 312DM | 5768452 | 3 | 126833 | 80535 | 94062 | 228-14 | 435 |
| 63 | 91 | 96 | 62DM | 6568482 | 3 | 116833 | 80331 | 93992 | 2597 | 7375 |
| 64 | 97 |  | 420M | 6767817 | 3 | 116767 | 80705 | 94157 | 246+01 | 311 |
|  |  |  |  |  | . |  | . .... |  |  |  |
| 163 | 291 | 297 | 72HM | 8967348 | 3 | 116700 | 80536 | 94161 | 241-28 | 140 |

Input parameters (Unit 5 , see Fig 6)


Fig 6 - Input parameters for Stage 1

```
Printed Output:
Unit 6 output from DTFX:
PROGRAM "PFIX" STATISTICS
NUMBER OF TRAVERSES: 43
OBSERVATIONS WITHOUT DISTANCE: 123
Unit 6 output from INPT1:
    3 VARIABLES
FORMAT=(Al,A4,A3)
TEST DATA
    2 9 7 \text { DATA POINTS 3 PHYSICAL RECORDS}
Unit 6 output from TRVL2:
TTEST DATA TRAVERSES
Unit 6 output from INPTl:
    7 VARIABLES
FORMAT=(A1, 39X ,216,T14,14,T2,A4,4BX , 13,4X,13)
TEST DATA TRAVERSES
    4 3 \text { DATA POINTS 1 PHYSICAL RECORDS}
Unit 6 output from MAP3:
    MODE=1 DATA UNITS BETWEEN GRID LINES= 5000
DATA UNITS PER INCH= 500.0000 PROJECTION RADIUS= 3.937
INCHES PER DATA UNIT= 0.002000 PROJECTION RADIUS= 3,937
1
2
3
```



Fig 7 - Traverses with numbers of observations (above) and traverse numbers (below)

## COMPUTATION OF GROUP MEANS AND DISPERSIONS

33. Stage 2 of domain analysis, is illustrated by the flow diagram in Fig 8 and consists of three steps.
34. Stage 2a. Program INPT1 reads the data file and stores the data required by program WNST5 which computes statistics for the whole data file. The eigenvectors for the whole data file are stored for use in Stage 2c and in Stage 3a.
35. Stage 2 b . Using the group specifications and the traverse file, program GRPKI computes the group keys, ie, the line-numbers in the data file corresponding to each group of observations outlined on the map.
36. Stage 2c. Program INPK1 reads the data file under control of the group keys and stores the data required by program GRPS, which computes the mean and dispersions of each group.

## PROGRAM WNST5

37. The program computes axis statistics and vector statistics for weighted points on the hemisphere. A flow diagram is presented in Fig 9.
38. WNST5 calls the subroutines DCPM1 to compute the data cross-product matrix, then subroutine ESTAT1 to estimate population parameters using Bingham's model. This subroutine also tests


Fig 8 - Stage 2 - Computation of group means and dispersions


Fig 9 - Flow diagram for program WNST5
the hypotheses of uniformity and axial symmetry using the eigenvalues of the data cross-product matrix. Depending on the results of these tests, the program performs a more sensitive test for axial symmetry, using Kuiper's statistic, by calling the subroutine CIRCT.
39. Fisher statistics are obtained by calling subroutine SCOM1 to compute sums of components, subroutine PSTATI to estimate population parameters using Fisher's modet, and subroutine

CIRCI to test for axial symmetry about the Fisher mean.

## Solution

See subroutine documentation in source listing.

## Capabilities

Maximum number of data points in one sample is 2000.

## Input

Unit 1 - tape or disk - record length: 1600 bytes unformatted. Input data. Unformatted records containing direction cosines and weights for up to 100 points. The sequence direction cosines, weight (four full word real numbers) is repeated for each data point. This file is written by program INPT1 or INPKI.

## Output

Unit 6 - printer - record length: 76 bytes formatted. Statistics. All computed statistics are written on this I/0 unit, with printer carriage control.
Unit 7 - disk or card punch - record length: 30 bytes formatted. Eigenvectors. The eigenvectors of the data cross-product matrix are written on this unit for later use by other programs. Three formatted records are written, each containing the direction cosines of one eigenvector in the normal sequence (north, east, down). The sequence of eigenvectors is such that the associated eigenvalues are in ascending order.

## Subroutines

FSTAT1 Given the sums of components of a set of vectors, computes the length, direction cosines and angular co-ordinates of the resultant vector. FSTATI also computes the concentration parameter and confidence radius of the mean assuming Fisher's distribution. FSTAT1 calls RTSP and XKF. RTST computes the angular co-ordinates of the resultant, and XKF estimates the concentration parameter of the population. Calling sequence: CALL FSTAT1(TITLE,N,SW, U, E,S,T,XK,CR, IPRINT) TITLE $=120$-byte title
$\mathrm{N} \quad=$ number of data points
SW = sum of weights of the data points
$\mathrm{U}=$ vector of sums of components
$\mathrm{E}=$ vector of direction cosines returned
$\mathrm{S} \quad=$ vector of angular co-ordinates returned. It contains trend and plunge, followed by dip direction and dip, of the perpendicular plane.
$T \quad=a$ rector returned containing 1. length of the resultant vector, and 2. Tength of the resultant divided by SW.
XK = estimated concentration parameter returned.
$C R \quad=$ confidence radij of mean returned.
IPRINT = print out parameter provided by calling routine IPRINT is less than zero if there is to be no print out. IPRINT is greater than or equal to zero for a printout, and the value of IPINT is the I/0 unit.
KUIP2 See source
XK1 Function, See source
ROTMAT See CONVRT
XK3 Function, See source
BSTATC See source
RSTP See DSPD
ANDC Converts from spherical to rectangular coordinates for points on the unit sphere.
Calling sequence: $\operatorname{CALL} \operatorname{ANDC}(T, P, J, A, B, C$, J3, N)
$T=$ vector of horizontal angles
$P=$ vector of vertical angles
$\mathrm{Jl}=$ first input code of spacing of input, in words, of vectors $T$ and $P$.
Jl is greater than zero if the input units are in degrees. It is less than zero if the input units are radians.
$\mathrm{J} 2=$ second input code.
$=1$ if input type is trend and plunge of line
$=2$ if input type is dip direction and dip of plane.
$=3$ if input type is strike and dip of plane.
In cases 2 and 3 the pole is the unit hemisphere and J 2 is greater than zero if the domain of input is the unit sphere; J 2 is less than zero if the domain of inputs is the unit hemisphere.
$A=$ vector of first direction cosines returned
$B=$ vector of second direction cosines
$C=$ vector of third direction cosines
J3 = output code of spacing, in words, of vectors $A, B$, and $C$
$N=$ number of data points input.

## Variables

WEIGHT weighting code
NN number of data words in sampie
NV number of variables
NO number of observations
NPHR number of data records following title record
TITLE array to contain title
N
NE
DC direction cosines
W weights
SW sum of weights of observations
External references:
Standard Fortran IV built-in functions.

Storage Requirements

| Code |  | bytes | words |
| :--- | :---: | :---: | :---: |
| WNST5 | 58456 | 34052 | 14378 |
|  |  | 10205 (buffers) | 4229 |
| BSTATC | 01768 | 326 | 214 |
| KUIP2 | 00848 | 114 | 76 |
| ANDC | 01008 | 131 | 89 |
| SYMM | 01968 | 300 | 192 |
| XKF | 01344 | 332 | 218 |
| EIGEN | 02792 | 432 | 282 |
| DCPM1 | 00656 | 103 | 67 |
| TAB1 | 00704 | 43 | 35 |
| FSTAT1 | 01848 | 304 | 196 |


| RTSP | 01496 | 206 | 134 |
| :--- | :--- | ---: | ---: |
| GMPRD | 00680 | 103 | 67 |
| XK1 | 00904 | 223 | 147 |
| GTPRD | 00672 | 100 | 64 |
| CIRC1 | 02424 | 713 | 459 |
| ESTAT1 | 02144 | 445 | 293 |
| BSTATG | 01752 | 321 | 209 |
| SCOM1 | 01032 | 142 | 98 |
| VRM1 | 00880 | 71 | 57 |
| ROTMAT1 | 00848 | 131 | 89 |
| XK3 | $\underline{00944}$ | $\underline{203}$ | $\underline{131}$ |
| TOTAL | 85168 | bytes | 49000 |

## PROGRAM GRPK1

40. Using a list of the traverses in each domain and a list of the observations in each traverse, this program generates keys containing the numbers of the observations in each domain. A flow diagram is shown in Fig 10.

## Solution

41. The program reads from the traverse file the range of data-file line numbers for each traverse. It then reads group definitions, one at a time. Each group is defined by traverse numbers and observation numbers on each traverse. Traverses specified for a group are processed in order of increasing traverse number, so that line numbers in the key will be in sequence. This traverse number is not the field traverse number, but one assigned by TRVL2 to place traverses sequentially in the data file. If the entire traverse is not to be included, the range of line numbers to be included in the key is computed. The line numbers in this range are added to the key.
42. The number of the traverse just processed is replaced by 10000 and the group definition again searched for the smallest traverse number. When all the traverses included in the group have been processed, the key is written out and the next group definition is read.

## Capabilities

43. Maximum number of traverses in the traverse file is 999. Maximum number of traverses in one group is 10 . Maximum number of line numbers


Fig 10 - Flow diagram for program GRPK1
in key is 20.

Input
Unit 1 - tape or disk - record length: 121 bytes, formatted. Traverse numbers and line number ranges. One record for each traverse containing:

Column Contents

| $2-5$ | traverse number |
| :---: | :--- |
| $13-16$ | starting line number for traverse |
| $17-20$ | ending line number for traverse |

These data created by TRVL2.
Unit 2 - card reader - record length: 120 bytes formatted. Group definitions. One record for each group. Each record contains 120 characters, or 30 in each \%, 4 character fields.
A group may have up to 10 traverses. Each traverse has 3,4 character fields:
field 1 is the traverse number
field 2 is the number of the first observation to be included. If this field is blank or zero, the first observation of the traverse is assumed.
field 3 is the number of the last observation to be included. If this field is blank or zero, the last observation of the traverse is assumed.
Each field is right justified.

Output
Unit 6 - printer - record Tength: 121 bytes formatted. Error messages. If the number of observations indicated for inclusion in a traverse is greater than the number of observations taken for that traverse, an error message is produced. The program stops immediately.
Unit 7 -disk or card punch - record length: 80 bytes formatted. Key. Writes a single key for each group of traverses. These keys are used as input to the program INPK1.

## Subroutines

WRITEK Writes a set of half-work integers in a special format: All records are 80 bytes long, sequenced in positions 78-80 Record 1: 1-72 = first 72 bytes of title Record 2: 1-48 = last 48 bytes of title 53-56 $=$ LENFIL 61-64 = LENKEY
0ther records: 1-72 keys; usually 18 Calling sequence: CALL WRITEK (IOU,TITLE, LENFIL, LENKEY, KEY)
IOU = I/O Unit to be written on
TITLE $=120$ bytes title
LENFIL $=$ size of universe to which the set of data belongs.
LENKEY = size of set of the data
KEY = set of key data

## Variables

| FMT | format for reading traverse file |
| :--- | :--- |
| TITLE | title |
| M | number of first observation on traverse |
| N | number of last observation on traverse |
| LENFIL | number of observations in survey |
| IGROUP | counter for domains |
| LENKEY | number of observations in domain |
| L | array of traverse numbers in domain |
| NT | number of traverses in domain |
| MIN | smallest traverse number in domain |
| KEY | array of observation numbers in domain |

Storage Requirements

| Code | bytes | words |  |
| :--- | :--- | :--- | :---: |
|  |  |  |  |
| GRPK1 | 6016 | 5075 | 2621 |
|  |  | 10205 (buffers) | 4229 |
| WRITEK | $\underline{0904}$ | $\frac{100}{15380}$ | $\frac{64}{6914}$ |
| TOTAL | 6920 |  |  |

## PROGRAM INPKI

44. The program reads specified variables from an input file using a key and writes the data in a convenient form for use by other programs in the areal-analysis package. A flow diagram given in Fig $I T(a)$ to (c).
45. INPKT accepts as parameters the number of variables to be read from each record of the input file and the format for reading those variables. The first field in the format specification must refer to a line-type character and must be specified as A1. The specified number of variables must include this field. Because the data array is declared as integer, and some FORTRAN input routines will not allow data to be read into an integer variable with an $F$ format code, ie, as a real number, all input data must be in integer. form and all fields must be specified with an I format code. If it is desired to convert integers to real numbers before they are placed in the output file, an additional set of parameters may be added to the parameter card containing the input format. These parameters specify which input variables are to be converted to real


Fig 11(a) - Flow diagram for program INPK - Part 1
numbers and how many decimal places each should have.
46. Which records of the input file are read is determined by a key of record numbers. At each record of the input file whose number appears in the key, the program reads the specified number of full word variables using the specified format. The data are written unformatted into the output file as a header record followed by data records. Each output data record except the last always contains the data from 100 input records.


Fig 11(b) - Flow diagram for program INPK - Part 2

Solution
47. The output data records the first written onto a scratch file. After all the input records have been read, the header record is written onto the output file, and the output data records are then copied from the scratch file to the output file.
48. If the first byte of the first input record contains the letter $T$, this record is assumed to be a title record and counting of input records begins with record 2; otherwise counting


Fig 11(c) - Flow diagram for program INPK - Part 3
of the input records begins with record 1. Since only those input records are read whose numbers appear in the key, an end-of-file condition resulting from an attempt to read the inpui file always indicates an error, and the program stops after printing a message. After processing the input records as directed by a key, the program attempts to read another key. If an end-of-file conditions results, the program stops normally. If another key is read, the input file is rewound and the process repeated using the new key. In
this way, any number of sets of data may be extracted from the input file and written sequentially on the output file.

## Capabilities

49. Maximum length of the given format is 60 characters. Maximum number of variables read from each input record is 10 . Maximum number of variables read from each input record is 10. Maximum number of input record numbers in one key is 5000 .

## Input

Unit 1 - tape or disk - record length: determined by format from unit 5. output from DTFX. Input data file. All records have the same format unless the first record is a title record, in which case the first record contains the letter $T$ in column 1 (This is the line type character) and a title in column 2-121.
Unit 2 - card reader - record length: 80 bytes formatted. Keys. This is the output file from GRPKT, unit 7.
Unit 5 - card reader - record length: 102 bytes, formatted. Parameters. One record containing:

## Columns

Contents


Output
Unit 6-line printer - record length: 35 bytes, formatted. Messages. The program writes the number of output data records. Error messages are self-explanatory.
Unit 7 - tape or disk - record length: $8+400 \times$ NV unformatted. Scratch file. Output data records are stored in this file until they are copied to the output file.
Unit 8 - tape or disk - record length $8+400 \mathrm{x}$ NV, unformatted. NV = number of variables. Output file. Output is written unformatted on this file as a header record followed by data records. Each header record contains four full word integers followed by the 120 byte title. The four integers contain:
(1) total number of words in this set of data
(2) number, NV, of variables read from each input record
(3) total number of input records read in this set of data
(4) number of output data records following the header record.

Each data record contains two full word integers followed by the data from up to 100 input records.

## Subroutines

READK reads a set of integers formatted by the subroutine WRITEK.
Calling sequence: CALL READK (IOU,TITLE, LENFIL, LENKEY, KEY)
IOU $=\mathrm{I} / 0$ unit to be read
TITLE $=$ title of the set of data to be read
LENFIL = size of the universe to which the set belongs
LENKEY = size of set
KEY = the set of data
double return from this routine
return 1 return taken if end-of-file is encountered at the first record
return 2 return is taken if end-of-file is encountered after the first record (set is not complete) of records is out of sequence.

Variables
NVAR number of variables
FMT format
IC conversion factors
LINTYP line-type character
TITLE array to contain title
TITL flag to indicate title present
NFILE number of records in data file
LENK number of records to be read
KEY array of record numbers
NTOT total number of data records read
NPHR number of output data records (after title record)
$N$ number of data records in batch
DATA array to contain the data
IV number of variable to be converted to real
RDATA array to contain real values - same locations as DATA
IE number of data words in data record
NN number of data words in entire sample

Storage Requirements
The arrays DATA and RDATA occupy the same storage.

Code bytes words

| INPK1 | 16512 | 14313 | 6347 |
| :--- | :--- | :--- | ---: |
|  |  | 12246 (buffers) | 5286 |
| READK | 00952 | $\frac{120}{17464}$ | 26679 |

## PROGRAM GRPS

50. This program computes statistics for each domain for areal analysis. A flow diagram is given in Fig 12.
51. GRPS accepts as parameters the format of the output and the pole of the hemisphere to be used for computing statistics. The data are read from a file written by program INPK. As the data for each group are read, statistics are computed by calling subroutines SCOM1 and FSTAT1. Since these are vector statistics, the pole read from the parameter card is used for assigning sense to the axes.


Fig 12 - Flow diagram for program GRPS

## Solution

52. See subroutine documentation in source listing.

## Capabilities

53. Maximum number of observations in any group is 100 .

Input
Unjt 1 - tape or disk - record length: 2408 bytes, unformatted. Input data file as written by INPKI. Unit 3 - card reader - record length: 30 bytes, formatted. Pole of hemisphere. Three records containing in the usual sequence, direction cosines of pole, one direction cosine per record in columns 21-30 with decimal point.
Unit 5-card reader - output format. Columns 3102. See below.

Output
Unit 8 - tape or disk - record length: determined by format. Output data file. Format determined by given format specification on unit 5. Variables written are:
(1) number of group
(2) mean coordinate of group
(3) mean $Y$ coordinate of group
(4) number of observations in group
(5) sum of weights times 10
(6) three sums of components in the usual sequence times 10
(7) three direction cosines of mean direction, in the usual sequence, times $10^{6}$
(8) length of resultant divided by sum of weights times $10^{6}$
(9) trend and plunge of mean direction as integers
(10) concentration parameter as integer.

Subroutines for GRPS
SCOM1:
Computes the sums of the components of a set of vectors. This subroutine calls ANDC.
Calling sequence:
CALL SCOMT (DC, W,N,V,JM,U)
$D C=3 * N$ matrix of direction cosines
$W=$ vector of weights
$N=$ number of data points
$V=$ vector of length 2 or 3 - see JM
$J M=0$ if directions used are given
$=1$ if directions are to be adjusted and $V$ contains trend and plunge of center of hemisphere in degrees.

```
        = 2 if directions are to be adjusted and V
        contains trend and plunge of centre of
        hemisphere in radians.
        = 3 if directions are to be adjusted and V
        contains direction cosines of centre of
        hemisphere.
    U = vector of length 3 that returns the sums
        of the components.
SRF:
    Converts real numbers to integers, multiplying
    by a given power of }10\mathrm{ and rounding: Each real
    number is multiplied by 10**IF and then round-
    ed. If the resulting integer is greater than
    MAX, it is set to MAX, if it is less than -MAX,
    it is set to MAX.
    Calling sequence:
    CALL SRF(RL,IN,N,IF,MAX)
    RL = vector of real numbers. They may be in
                same location as IN, and may be positive
        or negative.
    IN = vector of returned integers.
    N = number of numbers to be processed.
    IF = power of 10 by which the numbers are to
        be multiplied.
    MAX = the maximum value to which resulting
        integers are truncated.
    Function:
TAB1
    Looks up and interpolates a one-dimensional
    table. If X is beyond the range of the table,
    the returned value is the extreme value of B in
    the table.
    Calling sequence:
    Y = TAB1 (X,A,B,N)
    X = given value with which to enter table
    A = vector containing the column of the
        table in which X is to be found
    B = vector containing the column of the
        table from which the returned value
        (TABT) is to be obtained.
    N = number of rows or entries in the table.
TABT = the value of the function is the value
    obtained from the table.
```

XKF See HOMO
RISP See DSPD
FSTAT1 See WNST5
ANDC See WNST5

Variables
IGRP counter of domains
$V$ direction cosines of pole of hemisphere
ISX sum of $x$-coordinates
ISY sum of $y$-coordinates
SW sum of weights
NN number of numbers in input records
NV number of variables in input records
NO number of observations in input records
NPHR number of input records following title record
TITLE title
$N$ number of observations in data record
KE number of numbers in data record
IX $x$-coordinate
IY $\quad y$-coordinate
DC direction cosines
W weight
U vector of sums of components
E vector of direction cosines of resultant
$S \quad$ vector of angular coordinates of resultant
$T$ length and fractional length of resultant
XK estimated concentration parameter of population
R confidence radii on mean: $95 \%$ and $99 \%$
ITR trend of resultant
IPL plunge of resultant
IXAVG average $x$-coordinate
IYAVG average $y$-coordinate

External References: Standard Fortran IV built-in functions.

Storage Requirements

| Code | bytes | words |  |
| :--- | :---: | :---: | :---: |
| GRPS | 04632 | 1703 | 963 |
|  |  | 10205 (buffers) | 4229 |
| FSTAT1 | $0184 B$ | 304 | 196 |
| SCOM1 | 01032 | 142 | 98 |


| TAB1 | 00704 | 43 | 35 |
| :--- | ---: | ---: | ---: |
| RTSP | 01496 | 206 | 134 |
| ANDC | 01008 | 132 | 90 |
| XKF | $\underline{00640}$ | $\frac{41}{12704}$ | 13108 |
| Total |  | $\boxed{33}$ |  |

SAMPLE RUN - STAGE 2

Input Files

Data File:
Unit 1 input to INPT1
Unit 1 input to INPK]
See TTEST DATA (STAGE 1)

## Traverse File.

Unit 1 input to GRPK1.

| TTEST DATA |  |  |  |  |  |  | TRAVERSES |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 50 | 1 | 6 | 62 DM | 516982 | 3 | 126967 | B0545 | 93911 | 259-05 | 217 |
| 51 | 7 | 13 | 72 DM | 5269692 | 3 | 126967 | B0479 | 93B85 | 2625 | 280 |
| 52 | 14 | 21 | 82 DM | 5469142 | 3 | 126900 | 80569 | 93962 | 2580 | 472 |
| 53 | 22 | 49 | 282DM | 5569047 | 3 | 126900 | B0410 | 93953 | 252-02 | 294 |
| 54 | 50 | 59 | 102DM | 5668502 | 3 | 126833 | B0592 | 94086 | 247+01 | 333 |
| 55 | 60 | 90 | 312 DM | 5768452 | 3 | 126833 | B0535 | 94062 | 228-14 | 435 |
| 63 | 91 | 96 | 62 DM | 6568482 | 3 | 116833 | 80331 | 93992 | 2597 | 375 |
| 64 | 97 | 100 | 42DM | 6767817 | 3 | 116767 | 80705 | 94157 | 246+01 | 311 |
| 65 | 101 | 106 | 62 DM | 6867832 | 3 | 116767 | 80558 | 94114 | 250-02 | 400 |
| 66 | 107 | 111 | 52DM | 6967857 | 3 | 116767 | 80492 | 94082 | 227-14 | 268 |
| . | -•• | . . | ..... | . . . . . . | - | . . . . . | . .... | . . . | ... | . $\cdot$ |
| 163 | 297 | 297 | 72 HM | 8967348 | 3 | 116700 | 80536 | 94161 | 241-2B | 140 |

Group Specifications.
Unit 2 input to GRPK1.

| 159 |  |  | 73 | 74 | 161 | 0 | 0 | 55 | 21 | 29 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 75 |  |  |  |  |  |  |  | 55 | 30 | 37 | 13B |  |  | 145 |
| 162 |  |  | 163 |  |  |  |  | 63 |  |  | 147 |  |  |  |
| 64 |  |  | 149 | 150 |  |  |  | 135 |  |  |  |  |  |  |
| 65 |  |  | 151 |  |  |  |  | 53 | 1 | 10 |  |  |  |  |
| 66 |  |  | 152 | 67 |  |  |  | 53 | 11 | 19 |  |  |  |  |
| 153 |  |  |  |  |  |  |  | 53 | 20 | 28 |  |  |  |  |
| 68 |  |  |  |  |  |  |  | 52 |  | . |  |  |  |  |
| 154 |  |  |  |  |  |  |  | 158 |  |  | 72 |  |  |  |
| 69 |  |  |  |  |  |  |  | 50 |  |  | 132 | 1 |  |  |
| 155 |  |  |  |  |  |  |  | 132 | 6 | 10 | 51 | 1 |  |  |
| 70 |  |  |  |  |  |  |  | 51 | 6 | 7 | 133 |  |  | 134 |
| 136 |  |  | 54 |  |  |  |  | 156 |  |  |  |  |  |  |
| 137 |  |  |  |  |  |  |  | 71 |  |  |  |  |  |  |
| 55 | 1 | 10 |  |  |  |  |  | 157 |  |  |  |  |  |  |
| 55 | 11 | 20 |  |  |  |  |  | 148 |  |  |  |  |  |  |

Output files

Group keys.
Unit 7 output from GRPKI.
Unit 2 input to INPKI.


Eigenvectors.
Unit 7 output from WNST5.
Unit 3 input to GRPS.

| -0.569916 | 0.817640 | -0.081612 |
| ---: | ---: | ---: |
| 0.801487 | 0.531250 | -0.274574 |
| 0.181146 | 0.221895 | 0.958096 |

Group Data
Unit 8 output from GRPS.

| GROUPS |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1806565941979 | 8 | 771 | -117001 | -103741 | 746239 | -153454 | -136064 | 978744 | 988907 | 222 | 78 | 68 |
| 2805748941650 | 8 | 326 | - 63014 | - 40096 | 316908 | -193537 | -123150 | 973333 | 998744 | 212 | 7 | 597 |
| 3805336941579 | 10 | 724 | - 49212 | -202889 | 682455 | - 68956 | -284288 | 956256 | 985738 | 256 | 73 | 56 |
| 4806601941425 | 7 | 284 | - 40332 | - 60184 | 273266 | -142663 | -212684 | 966606 | 995448 | 236 | 75 | 157 |
| 5805301941031 | 9 | 603 | 54374 | -108352 | 560983 | 94740 | -188788 | 977437 | 951797 | 297 | 78 | 6 |
| 680451594064510 | 10 | 644 | -142256 | -15561 | 606118 | -221672 | -242483 | 9444 | 996492 | 228 | 1 | 22 |
| 7803860940368 | 11 | 229 | - 37460 | - 73441 | 21326 | -163838 | -321205 | 932730 | 998439 | 243 | 69 | 52 |
| 8803612940354 | 15 | 451 | 62815 | -161007 | 413149 | 140262 | -359507 | 922541 | 992991 | 29 | 67 | 12 |
| 9803430940339 | 8 | 210 | 3960 | - 75036 | 195880 | 18876 | -357660 | 933661 | 999037 | 273 | 69 | 779 |
| 10803224940174 | 6 | 369 | - 43438 | - 95381 | 352669 | -118066 | -259248 | 958567 | 997054 | 246 | 73 | 226 |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| 31799914938586 | 8 | 712 | - 43871 | -253532 | 662314 | - 61744 | -356818 | 932131 | 997946 | 260 | 69 | 365 |
| 3280080793880611 | 11 | 420 | - 41477 | -119483 | 394625 | -100091 | -288329 | 952286 | 986663 | 251 | 72 | 61 |

## Input parameters" (Unit 5, see Fig 13)



Fig 13 - Input to Stage 2

Printed Output:

Unit 6 output from program INPT1:

## 5VARIABLES

FORMAT $=(A 1,63 X, 315,13)$
TEST DATA
297 DATA POINTS
3 PHYSICAL RECORDS

Unit 9 output from program WNST5:
297 TEST DATA
Unit 6 output from program INPK1:

| 8 TEST DATA | GROUP | 1 |
| :--- | :--- | :--- |
| 1 PHYSICAL DATA RECDRDS |  |  |
| B TEST DATA | GROUP | 2 |
| 1 PHYSICAL DATA RECORDS |  |  |
| 10 TEST DATA | GROUP | 3 |

1 PHYSICAL DATA RECORDS

7 TEST DATA 9 TEST DATA GROUP 5

1 PHYSICAL DATA RECORDS 10 TEST DATA GROUP

GROUP 6
1 PHYSICAL DATA RECORDS
11 TEST DATA
1 PHYSICAL DATA RECORDS
15 TEST DATA
1 PHYSICAL DATA RECORDS
8 TEST DATA
GROUP
9
1 PHYSICAL DATA RECORDS
6 TEST DATA
GROUP 10
1 PHYSICAL DATA RECORDS

11 TEST DATA
11 TEST DATA GROUP 32
GROUP 4

GROUP 7

GROUP 8

1 PHYSICAL DATA RECORDS

```
Statistics for Data File.
    Unit 6 output from UNST5.
TEST DATA
    297 POINTS WITH TOTAL WEIGHT OF 1568.1
"BINGHAM" STATISTICS
EIGENVAL EVAL/SN DIRECTION COSINES TR PL DD DP
    20.23 0.01290
    24.10
1523.75 0.97173 -0.08161 -0.27457 0.95870
TEST OF HYPOTHESIS K1-K2-K3: TEST STATISTIC- 5243.8984 5% POINT=17.0705
TEST OF HYPOTHESIS K2-K3: TEST STATISTIC= 1702.3879 5% POINT-5.99147
TEST OF HYPTTHESIS Kl-K2; TEST STATISTIC= 3.0383 5% POINT=5.99147
HYPOTHESIS K1=K2 ACCEPTED
\begin{tabular}{lcccc} 
K FOR & CONFIDENCE RADII & \\
CLUSTER & \(95 \%\) & \multicolumn{2}{l}{} & \(99 \%\) \\
\\
35.377 & 8.4 & 8.4 & 10.5 & \(\mathbf{1 0 . 5}\)
\end{tabular}
test df umiformity about eigenvector 3
KUIPER'S STATISTIC = 2.479 95% POINT = 1.747
TEST DATA
    297 POINTS WITH TOTAL WEIGHT OF 1568.1
"FISHER" STATISTICS
\begin{tabular}{cccccccc} 
R & R/SN & DIRECTION & COSINES & TR & PL & DD & DP \\
1545.26 & 0.98546 & -0.08043 & -0.27388 & 0.95839 & 253.6 & 73.4 & 73.6 \\
& & & 16.6 \\
FISHER & CONFIDENCE & RADII & & & & & \\
K & \(95 \%\) & \(99 \%\) & & & & & \\
68.327 & 1.0 & 1.2 & & & & &
\end{tabular}
```

test of uni fopmity about fisher mean KUIPER'S STATISTIC $=2.516 \quad 95 \%$ POINT $=1.747$

## DISPLAY OF GROUP MEANS AND DISPERSIONS

54. Generation of displays in the observations and/or the group means and dispersions, both on maps and as point diagrams and density diagrams, constitutes Stage 3 of the procedures as shown in Fig 14, Display of the group data is illustrated; if the group data file is replaced by the data file and the format on the parameter card changed appropriately, the flow diagram will illustrate display of the individual observations.
55. Stage 3a. Program INPTI reads the group data file and stores the information required by program DSPD. This program prepares data for the display programs, including rotation of the data so that the overall mean is vertical using the eigenvectors for the whole data file produced in Stage 2a.
56. Stage 3b. Program NPPLT produces point diagrams on the plotter, program WNDPLT3 produces density diagrams on the printer, and program MAP3 produces a plotted map. Each data point on this map is shown as a line that begins at the point of observation, ie, the centre of the group in the case of group means, whose azimuth is the trend of the pole of discontinuity, and whose length is the distance from the centre of an equal-area projection to the projected pole.

## PROGRAM DSPD

57. To read a data file written by program INPTl or INPKI and output four data files suitable for input to programs WNDP3, NPPLT and MAP3. A flow diagram is presented in Fig 15.
58. DSPD reads a rotation matrix and two parameters. Each block of data read from the input file is written onto output files 10D and IMA. The data is then rotated using the rotation matrix, and the rotated data written onto output files 100 R and IMAR. Files 100 and 100 R are suitable for input to programs WNDP3 and NPPLT; files IMA and IMAR are suitable for input to program MAP3.

## Solution

See options.

## Capabilities

No restrictions.

## Options

59. If the input parameter has a value of 1 , the input data are assumed to contain the direction cosines of lines and the trends and plunges of the lines. The data are output as read. If


Fig 14 - Stage 3 - Display of group means and dispersions
the input parameter has a value of 2 , the input data are assumed to contain the direction cosines of the poles to planes and the dip directions and dips of the planes. The dip directions and dips are replaced by the trends and plunges of the poles to the planes before the data are written. After rotation, new trends and plunges are computed from the direction cosines. If the output parameter is not zero, all the numbers for display on the map are replaced by zeros. If the output parameter is neither zero nor 1 , all the labels to be plotted on the map are replaced by blanks.


Fig 15 - Flow diagram for program DSPD

Input
Unit 2 - card reader - record length: 30 bytes, formatted. Rotation matrix. Three records, each containing the corresponding column (1, 2, or 3) of the matrix as three real numbers:

Card column
Contents
row 1, column (1, 2 or 3 )
row 2, column (1, 2 or 3)
row 3, column (1, 2 or 3)

Unit 5 - card reader - record length: 3 bytes, formatted. Parameters. One containing:

Column
Contents

| 1 | input parameter |
| :---: | :---: |
|  | 1-input is direction cosines of lines and the trends and plunges of the lines. |
|  | 2-input is direction cosines of the poles to planes and the dip directions and dips of the planes. for more information see program options. |
| 3 | output parameters. |
|  | $\neq 0$ all numbers on the map are replaced by zeroes. |
|  | $\neq 0$ and $\neq$ all the labels to be plotted are replaced by blanks. |

See program options.

Unit 7 - tape or disk - record length: 4008, unformatted. Input data file. This file is created by INPT1 and INPKI. Variables for each observation are:
(1) three direction cosines
(2) weight
(3) easting
(4) northing
(5) number to appear on map
(6) label to appear on map
(7) trend or dip direction (depending on input parameter)
(8) plunge or dip (depending on input parameter)

## Qutput

Unit 6-1ine printer - record length: 62 bytes, formatted. Messages. If the number of variables in the input data file is not 10, an error message is written and the program stops immediately.
Unit 3 - tape or disk - record length: 1608 bytes, unformatted. Data file for orientation diagrams. Variables for each observation are: three direction cosines, weight.

Unit 4 - tape or disk - data file for orientation diagrams rotated. Same as unit 3 output except rotated direction cosines are used.

Unit 8 .- tape or disk - record length: 2408, unformatted. Data file for map. Variables for each observation are: easting, northing, number to appear on map, label to appear on map, trend, plunge.
Unit 9 - tape or disk - data for map, rotated. Same as unit 8 output, except rotated trend and plunge are used.

## Subroutines

RTSP
Converts from rectangular to spherical co-ordinates.
Calling sequence:
$\operatorname{CALL} \operatorname{TRSP}(A, B, G, \mathrm{~J}, \mathrm{~T}, \mathrm{P}, \mathrm{R}, \mathrm{J} 2, \mathrm{~J} 3, \mathrm{~N})$
$A=$ vector of $X$ components.
$B=$ vector of $Y$ components .
$G=$ vector of $Z$ components.
$\mathrm{J1}=$ input description parameter of the spacing in words of components. in vectors $A, B$ and $G$.
$T=$ vector of horizontal angles.
$P=$ vector of vertical angles.
$R=$ vector of distances from origin.
$\mathrm{J} 2=$ first output description parameter of spacing of output words in vectors $T$ and P. J2 is greater than zero if the output units are to be in degrees. J2 is less than zero if the output units are to be in radians.
$J 3=$ second output description parameter.
$=1$ if output type is to be trend and plunge.
$=2$ if output type is to be dip direction and dip.
$=3$ if output type is to be strike and dip. $J 3$ will be greater than zero if the domain is the sphere, and less than zero if the domain is the hemisphere.
$N=$ number of data points.
SRF See GRPS.
GMPRD See CONVRT.

Variables

| RM | rotation matrix |
| :---: | :---: |
| KK | first input parameter |
| KL | second input paraneter |
| NN | number of numbers in input record |
| NV | number of variables in input |
| NO | number of observations in input |
| NPHR | number of input records following title record |
| TITLE | array to contain title |
| NTOT | total number of points in sample |
| NVOD | number of variables in output for orientation diagrams |
| NNOD | number of numbers in output for orientation diagrams |
| NVMA | number of variables in output for maps |
| NNMA | number of numbers in output for maps |
| NR | number of variables in record |
| IE | number of numbers in record |
| DC | direction cosines |
| W | weights |
| DATA | other variables |
| T | trends |
| P | plunges |
| DCR | rotated direction cosines |

External References: Standard Fortran IV built-in functions.

| Storage Requirements |  |  |  |
| :---: | :---: | :---: | :---: |
| Code |  | bytes | words |
| DSPD | 10480 | 3665 | 1973 |
|  |  | 16350(buffers) | 7400 |
| RTSP | 01496 | 205 | 133 |
| SRF | 00640 | 41 | 33 |
| GMPRD | 00680 | 103 | 67 |
| TOTAL | 13296 | 53364 | 9606 |

## PROGRAM NPPLI

60. The program generates commands for a digital incremental plotter to produce a point diagram on non-polar orientations on Lambert's equal-area projection. A flow diagram is shown in Fig 16(a) and (b).

Solution
61. The orientations must be given as direction cosines. These are converted into $X, Y$ coordinates on the projection by the subroutine RTXYEQ. The projection is horizontal unless defined otherwise by a parameter card. If a non-horizontal projection is requested, the data are rotated before the subroutine RTXYEQ is called.

Capabilities
62. Maximum number of points in any plot is 1000.

Input
Unit 1 - tape or disk - record length: 1608 bytes, unformatted. Data. As written by programs INPTI, INPK or DSPD. As many samples as desired may follow sequentially. One plot will be produced for each sample.
Unit 4 - card reader - record length: determined by format from unit 5. Normal to projection plane. Used only if a $P$ or Q parameter card is supplied with a non-position number in the fourth numeric field of parameter unit 5 .
Format given on parameter card.
formatted. Parameters. One or more cards of format:



Fig 16(a) - Flow diagram for program NPPL1 - Part 1
column 1, two plots will be produced, one using the horizontal projection plane and one the specified projection plane.

## Output

Unit 6-printer - record length: 81 bytes, formatted. Error messages.
other - plotter or plot tapes - output from plot-


Fig 16(b) - Flow diagram for program NPPL1 - Part 2
ting subroutines. Unit number and device requirements depending on the plotting subroutines.

## Variables

A parameter code
X parameters
ALPHA alphanumeric parameter
BOTH flag to indicate two plots required
ROTAT flag to indicate rotation required

RM rotation matrix
IPLOT counter of plots
NN number of data words in sample
NV number of variables in output
NO number of observations in sample
TITLE array to contain title
DC direction cosines of data points
$W \quad$ weights of data points
$N$ number of observations in sample
XP,YP coordinates of center of projection
DCR rotated direction cosines
External References: The following subroutines from the plot library:
$\operatorname{PLOT}(X, Y, J)$.
Moves the pen from its current position to the point $(X, Y)$ with pen up $(J=3)$ or down $(J=2)$. Plot origin is reset to $(X, Y)$ if $J<0$.
$\operatorname{NUMBER}(X, Y, H, R, T, N)$.
Writes the real number $R$ with $N$ decimal places at the location $X, Y$ with a character height $H$ making an angle of $T$ degrees with the positive $x$ axis (counter-clockwise).
$\operatorname{SYMBOL}(X, Y, H, I C, T, N)$.
Starting at the point $X, Y$ and using a symbol height, $H$ in., either draws $N$ characters stored in EBDIC in the array IC ( $N>0$ ) or draws symbol number IC ( $N=-1$ ) or draws symbol number IC with a line from the current pen position $(N=-2)$. The symbols make an angle of $T$ degrees with the positive $x$ axis (counter-clockwise).
$\operatorname{CIRCLE}(X, Y, A, B, C, D, E)$.
Draws a circular or spiral arc (solid if $E=$ 0.0 , dashed if $E=0.5$ ) starting at the point ( $X, Y$ ). $A$ and $B$ are the angles measured counter-clockwise from the positive $x$ axis to the radius at the start of the arc and the radius at the end of the arc respectively. $C$ and $D$ are the corresponding radii in inches.

## Subroutines

ROTMAT
See CONVRT.
RTXYEQ
See source listing.
VRMI
Returns the rotation matrix that will rotate a
given direction to the vertical. The trend and plunge of the axis of rotation and the angle of rotation are computed, and the subroutines ROTMAT and RTSP are called.
Calling sequence: $\operatorname{CALL} \operatorname{VRM1}(V, M, J)$
$V=$ vector of length 2 or 3 . See $J$.
$M=$ returns rotation matrix
$J=1$ if $V(1), V(2)$ contain trend and plunge in degrees
$=2$ if $V(1), V(2)$ contain trend and plunge in radians
$=3$ if $V(1), V(2), V(3)$ contain direction cosines
GMPRD
See CONVRT.

Storage Requirements
Code bytes words

| NPPLI | 30160 | 20265 | 8373 |
| :--- | :---: | :---: | ---: |
|  |  | 10205 (buffers) | 4229 |
| RTXYEQ | 00992 | 132 | 90 |
| GMPRD | 00680 | 103 | 67 |
| RTSP | 01496 | 206 | 134 |
| CC1 | 09968 | 4447 | 2343 |
| VRMI | 00880 | 73 | 59 |
| GRPRD | 00672 | 100 | 64 |
| ROTMAT | 00848 | 131 | 89 |
| CIRCLE | $\underline{13024}$ | $\underline{32}$ | $\underline{266}$ |
| TOTAL | 58720 | 35694 | 15474 |

## PROGRAM WNDPLT3

63. For weighted, non-directed orientations, the program produces on the line printer equalarea projections of point density having a high density of counting locations. A flow diagram is presented in Fig 17(a) to (c).
64. The plane of the projection is horizontal, unless a parameter card is given redefining the projection plane. In this case the directions are rotated before being plotted. The program uses by default a 1 per cent counting circle, a contour


Fig 17(a) - Flow diagram for program WNDPLT3 Part 1
interval of 1 per cent, and the following characters to represent successive contour intervals 0-1 per cent, 1-2 per cent, and so on: "1234567890abc defghijklmnopqrstuvwxyz****". Any of these defaults may be overridden by appropriate parameter cards.
65. The input data must include weights. Unless otherwise directed, the program uses these weights in the computations. A parameter card may be used to indicate that the weights are to be truncated at some specified upper limit, or that the weights are to be set equal to 1 .


Fig 17(b) - Flow diagram for program WNDPLT3 Part 2

## Solution

66. To map the density of points on the sphere, a density estimate is computed at each of a number of pre-determined counting locations. For unweighted points, the density estimate at a particular location would be obtained by counting the points falling inside a pre-determined area, the counting circle, surrounding the location. The density estimate is usually obtained by expressing this count as a percentage of the total number of points. This program obtains a density estimate for weighted points by summing the


Fig 17(c) - Flow diagram for program WNDPLT3 Part 3
weights of the points falling inside the area and expressing this sum as a percentage of the total of the weights of all the data points. The density estimates are printed in the form of an equal-area projection.
67. This program employs a print matrix consisting of 3713 print positions: 47 lines with 79 print positions on each. Printed six lines to the
inch, the matrix is approximately eight inches square. The equal-area projection is a circle with a 10 cm radius centred on the print matrix. Every print position whose centre lies within the circle represents a counting location of which there are 2933. The counting locations are defined by direction cosines, which are read in by the program at the start of each run.
68. With such a large number of counting locations it is inefficient to compare every counting location with every data point in the counting process. The number of comparisons is thus reduced. For a particular data point, those counting locations that are to be incremented lie within a circle on the sphere whose projection approximates an ellipse that has its greatest size when the data point lies in the plane of projection. Before beginning the counting procedure, the program computes the maximum dimension, $m$, for the ellipse in this case. For each data point, the program computes $X P, Y P$, the $x$ and $y$ coordinates on the print matrix of the projection of the data point, then determines the submatrix of the print matrix that lies inside the square bounded by $X=X P+M, \quad X=X P-M, \quad Y=Y P+M, \quad Y=Y P-M$. This square wholly contains the projection of the counting circle centred on the data point. Each counting location represented in this submatrix is then tested by computing its angular distance from the data point and comparing this with the radius of the counting circle. This process is repeated in a slightly different form if the data point is close enough to the horizontal to affect counting locations on the diametrically opposite part of the projection.
69. After the counting procedure is completed, the program constructs the plot, line by line, by expressing each count as a percentage of the total weight and then placing the appropriate character in the corresponding print position. A contour interval and a string of characters are supplied to the program on parameter cards. As an enhancement to the visual impact of the plot, characters representing higher densities are overprinted, the number of overprintings increasing with the density value.


## Co 1

Contents

4180
e. Weighting procedure. Default: weights are used as read. Card format:

Co 1
Contents

| 1 | "W" |
| :---: | :---: |
| 2-11 | value |
| Action: |  |
| If value $=0$ | all weights will be set to 1.0 before data is processed. |
| If value > 0 | weights greater than value will be set equal to value. <br> Weights less than or equal to value will not be changed. |
| If value < 0 | the default action will remain in effect. |

f. Printout. Default: overprinting and list of character values. Card format:

Col
Contents

## 1 "0"

Action: Overprinting and list of character values suppressed.

Input
Unit 1 - tape or disk - record length: 1608 bytes, unformatted. Data. As written by program INPTI, INPK1, or DSPD, as many samples as desired. One plot will be produced for each sample.
Unit 3 - tape or disk - record length: 80 bytes, formatted. Direction cosines of counting locations. A file of direction cosines is supplied with this set of programs, filename: DIRECTIONCOSINE.
Unit 4 - card reader - record length: determined by format. Normal to projection plane. The contents and format of the single record are described under "p" option under program options.
Unit 5 - card reader - record length: 80 formatted. Parameters. All parameter cards are optional because all parameters have default values. The reading of parameter cards is determined by a
blank card or an end-of-file (7/8/9). One parameter record must be supplied for each parameter for which a value is to be specified. See Program Options.

## Output

Unit 6 - printer - record length: 42 bytes, formatted. Messages. Error messages are selfexplanatory.
Unit B - printer - record length: B4 bytes, formatted. Plot. Preceding the plot, there are five records.
(1) first 80 characters of the title
(2) remainder of the title
(3) number of data points and total weight
(4) size of counting circle
(5) contour interval and characters.

The plot consists of 49 lines, each having 82 characters of which the first is carriage control. Unit 9 - Iine printer - record length: 127 bytes, formatted. Title of each sample. On this unit the program writes the number of data points and the title for each sample as it is read.

## Variables

ICODE1 overprinting flag
CHAR array to contain plot characters
SIZE percent size of counting circle
CONTI contour interval
WEIGHT weighting code
A parameter code
$X$ array to contain parameters
ALPHA array to contain new plot characters
BOTH flag for unrotated plot when ROTAT=. true.
ROTAT flag for rotation of data
CRC cosine of radius of counting circle
CRCC test value
RC radius of counting circle (radians)

MPLRC maximum projected length of RC
NN number of data words in sample
NV number of variables in input
NO number of observations in sample
NPHR number of data records following title record
TITLE array to contain title
NB number of observations in record
NWD number of data words in record
DC direction cosines of data points
$W \quad$ weights of data points
DCR array to contain rotated direction cosines
RM rotation matrix
External References: None.

Storage Requirements

| Code |  | bytes | words |
| :--- | :---: | :---: | ---: |
| WNDPLT3 | 05336 | 2152 | 1130 |
|  |  | 10205 (buffers) | 4229 |
| PLOTIA | 00360 | 13 | 11 |
| PLOT1B | 07440 | 224 | 148 |
| GRID10 | 00496 | 61 | 49 |
| PLOTIC | 02224 | 721 | 465 |
| BLNK | $004 B B$ | 30 | 24 |
| RANGEX | 00912 | 76 | 62 |
| VRMT | 00880 | 73 | 59 |
| R0TMAT | 00848 | 131 | 89 |
| GRMPRD | 00680 | 103 | 67 |
| GTPRD | 00672 | 100 | 64 |
| RTSP | 01496 | 206 | 134 |
| Labe11ed |  |  |  |
| ONE | 15000 | 9503 | 3779 |
| TW0 | $\underline{22312}$ | $\underline{25612}$ | $\underline{11146}$ |
| TOTAL | 53912 | 49210 | 21456 |

SAMPLE RUN - STAGE 3

## Input Files

Data File.
Unit I input to INPT1


| Eigenvectors |  |  |
| :--- | :--- | ---: |
| Unit 2 input to DSPD   <br> $-D .569916$ 0.817640 -0.081612 <br> 0.801487 $0.53125 D$ -0.274574 <br> 0.181146 0.228195 0.958096. |  |  |

## Group data file

Unit 1 input to INPTI
(see Unit 8 output from GRPS Stage 2)
Input parameters (Unit 5, see Fig 18)


Fig 18 - Input to Stage 3

## Printed outputs

Unit 6 output from INPT1

## 11 VARIABLES

FORMAT $=(A 1,63 X, 3 I 5, I 3, T 40,2 I 6, I 5, A 2,2 I 3)$
TEST DATA
297 DATA POINTS 3 PHYSICAL RECORDS

Unit 6 output from DSPD:

TEST DATA
3 PHYSICAL RECORDS: 10 VARIABLES, 297 OBSERVATIONS

Unit 8 output from WNDPLT3:

CONTOUR VALUES AND CHARACTERS FOR THIS RUN ARE

| $>$ | 0.0\% | K > 20.0\% |
| :---: | :---: | :---: |
| $1>$ | 1.0\% | $L>21.0 \%$ |
| $2>$ | 2.0\% | $M>22.0 \%$ |
| $3>$ | 3.0\% | $N>23.0 \%$ |
| $4>$ | 4.0\% | $0>24.0 \%$ |
| $5>$ | 5.0\% | P > 25.0\% |
| 6 | 6.0\% | Q > 26.0\% |
| 7 | 7.0\% | $R>27.0 \%$ |
| $8>$ | 8.0\% | S > 28.0\% |
| $9>$ | 9.0\% | T > 29.0\% |
| A > | 10.0\% | U > $30.0 \%$ |
| B > | 11.0\% | $V>31.0 \%$ |
| C | 12.0\% | W > 32.0\% |
| D $>$ | 13.0\% | $x>33.0 \%$ |
| E > | 14.0\% | $Y>34.0 \%$ |
| F > | 15.0\% | Z > 35.0\% |
| $G>$ | 16.0\% | * > $36.0 \%$ |
| $H>$ | 17.0\% | * > $37.0 \%$ |
| I > | 18.0\% | * > 38.0\% |
| J > | 19.0\% | * > $39.0 \%$ |

297 OBS边VATIONS HITH TOTAL NEIGHT OF 1568.1
PEACEil O F LOTAL HEIGHT IN 1.0 PERCENT OF AREA


11111111
11123333332
12347A9876521
1476ADRDB98741111
248EGLQLOLHDSS1 1111



1238GO03*****OIA641111111

11133589 В вЕвв632
111223443321
1112211
1

1

Fig 19 - Plot of true orientation

297 OOSELVATIONS NITH TOTHL WEIGHT OF 1568.1 PEHCENT OF TOTAL $\forall E I G H T$ IN 1.0 PERCENT OF AREA


111
1177221
111222221
12332222222222
3358 ABD 9854322211
$11245 \mathrm{CGwAXIGD552} 1111$
1246BQ2****RH984111


1136 B ה $* *$ * $\ddagger$ ***
11149 FCH ****すPEDA86311
1122498 DKEKHFA 89633117
11125668987541121
1221111211

1

Fig 20 - Plot with mean vector vertical

Unit 6 output from MAP3:

MODE $=3 \quad$ DATA UNITS BETWEEN GRID LINES $=5000$

| DATA UNITS PER INCH $=500.0000$ | PROJECTION RADIUS $=$ | 3.937 |
| :--- | :--- | :--- |
| INCHES PER DATA UNIT $=0.002000$ | PROJECTION RADIUS $=$ | 3.937 |
| TTEST DATA |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| TTUE ORIENTATION |  |  |
| 1 |  |  |
| 2 |  |  |

Unit 6 output from INPTI:

11 VARIABLES

```
FORMAT=(AT,T54,3I7,T23,I7,T8,2I6,T4,I4,T89,A4,T82,I4,I3)
TEST DATA
GROUPS
    32 DATA POINTS I PHYSICAL RECORDS
```

Unit 6 output from DSPD:

## TEST DATA

GROUPS
1 PHYSICAL RECORDS; 10 VARIABLES, 32 OBSERVATIONS

Unit 8 output from WNDPLT3:

CONTOUR VALUES AND CHARACTERS FOR THIS RUN ARE

| $>$ | 0.0\% | A $>$ | 10.0\% | $K>20.0 \%$ | $U>30.0 \%$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $1>$ | 1.0\% | B > | 11.0\% | L > 21.0\% | $V>31.0 \%$ |
| $2>$ | 2.0\% | $C>$ | 12.0\% | M > 22.0\% | W > 32.0\% |
| 3 | 3.0\% | D $>$ | 13.0\% | $N>23.0 \%$ | $X>33.0 \%$ |
| 4 | 4.0\% | E > | 14.0\% | $0>24.0 \%$ | $Y>34.0 \%$ |
| 5 | 5.0\% | $F>$ | 15.0\% | $P>25.0 \%$ | $Z>35.0 \%$ |
| 6 | 6.0\% | $G>$ | 16.0\% | Q > 26.0\% | * > 36.0\% |
| 7 | 7.0\% | H $>$ | 17.0\% | R > 27.0\% | * > 37.0\% |
| 8 | 8.0\% | I > | 18.0\% | S > 28.0\% | * $>38.0 \%$ |
| $9>$ | 9.0\% | J > | 19.0\% | T> 29.0\% | * > 39.0\% |

## Printed Output (see SR-7 and SR-8)

```
TEST DATA GFOUPS TRUE OPTEITATION
32 OBSERVATIONS HYTH TOTAL HEIGHT OF 1568.1
PERCENT OF TOTAL WEIGHT IN 1.0 PFRCENT OF AREA CONTOUR INTERVAL 1.0 CHARACTEF SEQUESCE 123456789 AGCDEFGHIJKLTMOPQRSTUVAXYZ****
```

22222
2222213B8888
22444EPRBEB88
4ACHZTOBCBD51111
28 月****** पีD11 +111 $4 \mathrm{Ft} * *=3 A * * 0 \mathrm{E} 861111$


277PR*2RアPD662
5554666222
44

Fig 21 - Plot of groups in true orientation


2222211111 6B9998811111 446FFGGCEB61111 457V平半＊

7P＊まれチャ＊＊
 2．8LY本＊＊＊$=$ InEB88 449 CCEC 448772 2344442222 222222

Fig 22 －Plot of groups with mean vertical

Unit 6 output from MAP3:
$M O D E=3$
DATA UNITS BETWEEN GRID LINES= 5000

DATA UNITS PER INCH $=500.0000 \quad$ PROJECTION RADIUS $=3.937$

| INCHES PER DATA UNIT $=0.002000$ | PROJECTION RADIUS $=$ | 3.937 |
| :--- | :--- | :--- |
| TTEST DATA | GROUPS | TRUE ORIENTATION |
| 1 |  |  |
| 2 |  |  |
| 3 | GROUPS | MEAN VERTICAL |
| TTEST DATA |  |  |
| 1 |  |  |
| 2 |  |  |

Plotted Output (see Fig 23 to 28)


TEST DATA
TRUE ORIENTATION

Fig 23 - Point diagram of 297 observations


Fig 24 - Point diagram of 297 orientations with mean in vertical position


Fig 25 - Locations and orientations of observed discontinuities


TEST DATA
GROUPS TRUE ORIENTATION

Fig 26 - Point diagram of 32 group means


Fig 27 - Point diagram of 32 group means with mean vertical


Fig 28 - Locations and orientations of deviations of group means from overa 11 mean

## DEFINITION OF DOMAINS AND CHARACTERIZATION

## OF DOMAIN SUBFABRICS

72. In the final stage, the geologist uses the map displays produced in Stage 3 to combine groups into tentative doma ins (Fig 29).
73. Stage 4a. The information in the group data file is read by program INPTI and stored for input to program HOMO. This program may be instructed to perform tests for homogeneity of means and dispersions on any given set of adjacent groups. If the hypothesis of homogeneity is not rejected, the area is increased in size by including neighbouring groups and the tests repeated. The area is thus expanded to the point at which the inclusion of any more groups result in the rejection of homogeneity in either dispersions or means. The program is then instructed to output the numbers of the groups within the area, which is at this point a subfabric domain. The procedure is then repeated to define other domains.
74. Stage 4b. Program DDKY1 merges the datafile keys for the groups within each domain into a single key for the domain. This key is in turn used by program INPK1 to retrieve from the data file the observations in the domain. Program WNST5 characterizes the domain subfabric for the fabric element being analyzed.
75. If displays of the data within each domain are required, they can be produced by repeating


Fig 29 - Stage 4 - Defintion of domains and characterization of domain subfabrics

Stage 3 with the following changes. In Stage 3a (Fig 29) program INPTI is replaced by program INPK1 and the eigenvectors for the whole data file are replaced by the eigenvectors for the domain produced by program WNST5 in Stage 4b. Then using the group data file with the group numbers in the domain as written by program HOMO, it will produce displays of the group means within the domain. Alternatively, using the data file and domain key created by program DDKY will produce displays of the individual observations with in the domain.

## PROGRAM HOMO

76. This is an interactive program for testing grouped orientation data for homogeneity of concentration parameters and group means. The program first reads the group data, then accepts commands from the input device attached to I/0 unit 5, normally an interactive terminal but possibly a card reader. In response to these commands, the program will add groups to or delete groups from the set of currently included groups and test for homogeneity of concentration parameters or for homogeneity of mean directions among the currently included groups. A flow diagram is shown in Fig 30(a) to (e).

## Solution

77. The tests for homogeneity of concentration parameters and homogeneity of group mean directions are taken from Mardia, K.V., 1972, Statistics of Directional Data, London \& New York, Academic Press, pp 267-271, with the following change: The number of degrees of freedom for the Chi-square statistics used for testing the concentration parameters has been taken as $n-1$, where $n$ is the number of groups tested, instead of $2 n-2$ as given by Mardia. Checks performed using data generated artificially from a Fisher distribution with $k=50$ indicate that the correct number of degrees of freedom is approximately $n-1$.

## Capabilities

78. Maximum number of groups is 100 .

## Options

79. Details of the commands and their effects
follow. These commands are entered on cards as unit 5 input.
Name: Delete.
Form: "D" followed by optional list of group numbers.
Effect: If group numbers are given, those group numbers are deleted from the list of currently included groups. If no group numbers are given, all groups are deleted from the list.
Name: Restore.
Form: "R" followed by optional list of group numbers.
Effect: If group numbers are given, those group numbers are added to the list of currently


Fig 30(a) - Flow diagram for program HOMO - Part 1


Fig 30(b) - Flow diagram for program HOMO - Part 2


Fig $30(\mathrm{c})$ - Flow diagram for program HOMO - Part 3


Fig 30(d) - Flow diagram for program HOMO - Part 4
included groups. If no group numbers are given, all groups are added to the list.

## Name: List.

Form: "L".
Effect: Those group numbers in the list of currently included groups are printed. Those group numbers not in the list are printed separately.
Name: Concentration Parameter Test.
Form: "K".


Fig 30(e) - Flow diagram for program HOMO - Part 5

Effect: Concentration parameters of currently included groups are tested for homogeneity by the subroutine TCPF and the results of the test are printed.
Name: Mean Direction Test.
Form: "M".
Effect: Mean direction of currently included groups are tested for homogeneity by the subroutine TMDF and the results of the test are printed.

Name: Automatic Deletion of Groups until Means are Homogeneous.
Form: "A"
Effect: The group whose mean direction is farthest away from the overall mean direction is deleted from the list of currently included groups. The mean directions of the groups then remaining in the list are tested for homogeneity. If the test indicates that the means are homogeneous, a message to that effect is printed and the command list is executed before returning to command mode. If the test indicates that the means are not homogeneous, the procedure is repeated, a new overall mean direction being computed first. This iteration is continued until either the means become homogeneous or only two groups remain.
Name: Stop.
Form: "S".
Effect: The program requests and reads a name for the set of currently included groups. This set of group numbers is then written on I/0 unit 7 and the group stops.

## Input

Unit 1 - tape or disk - record length: 3608 bytes, unformatted. Group data. As written by program INPT1 or INPK1.
Unit 2 - card reader - record length: 80 bytes, formatted. Predefined set of group numbers (optional). If this input is supplied, the format must be written by GRPS. The group number is the first variable of the GRPS output. See GRPS. If this is not supplied, an end-of-file (7/8/9) should be placed in the file.
Unit 5 - card reader - record length: 61 bytes, formatted. Commands. The commands are described under program options. The general format of the commands is:

Columns
Contents

| 1 | code letter |
| :--- | :--- |
| $2-5$ | first group number |
| $6-9$ | second group number |

```
78-81 twentieth group number
```


## Output

Unit 6 - printer - record length: 121 bytes, formatted. Messages and test results. These should be self-explanatory.
Unit 7 - card punch or disk - record length, 80 bytes, formatted. Final set of group numbers. Used as input by DDKY. These are in the same format as those produced by GRPS.

Subroutines
XKF
estimates the concentration parameter for Fisher's distribution, given as $R=Q / S$, where $Q=$ length of the resultant of a set of vectors, and $S=$ the sume of the lengths of the vectors. The table given by MARDIA (1972, p322) is used to obtain $A K$ if $R$ is less than 0.9 . Otherwise the estimate $(1-2 / N)(1-R)$ is used, The function TAB1 is used.
Calling sequence: CALL $\operatorname{XRF}(R, N, A K, I E)$
$R=$ proportional length resultant $=Q / S$
$N=$ number of vectors in the data
$A K=$ estimated concentration parameter returned by this routine
$I E=$ error code returned.
$=0$ if there is no error
$=1$ if $R$ is the outside range of 0 to 1 . AK is set to 0.0 .

TAB1
See GRPS
MDCH
See source listing
MGAMMA
See source listing
MDFD
See source listing
MERF
See source listing
UERTST
See HIST2V
WRITEK

| See GRPK1 |  |
| :---: | :---: |
| READK |  |
| See INPK1 |  |
| HOMNS |  |
| See source listing |  |
| TMDF |  |
| See source listing |  |
| TCPF |  |
| See source 1 isting |  |
| Variables |  |
| NN | number of numbers in input data |
| NV | number of variables in input data |
| NO | number of observations in input data |
| NPHR | number of data records following the title record |
| TITLE | title of input data |
| IE | number of numbers in input data record |
| N | array of numbers of observations in group |
| T | sums of weights for groups |
| $X, Y, Z$ | mean coordinates of groups |
| A, B, C | direction cosines of group means |
| R | lengths of resultants for groups |
| LENFIL | total number of groups |
| LENK | number of groups in predefined combination |
| KEY | numbers of groups in previously defined combination |
| IS | array of flags for 'included' groups |
| L | command code letter |
| IG | group numbers in command |
| U | test statistic |
| NDF | number of degrees of freedom |
| P | probability of test statistic $<=U$ |
| F | test statistic |
| ND1 | degrees of freedom |
| ND2 | degrees of freedom |
| External References: Standard FORTRAN built-in functions. |  |


| Storage Requirements  <br> Code  <br>   <br>  bytes | words |  |  |
| :--- | :---: | :---: | ---: |
| HOMO | 07592 | 2205 | 7152 |
|  |  | 10205 (buffers) | 422.9 |
| TCPF | 01784 | 251 | 169 |


| TMDF | 01328 | 164 | 116 |
| :--- | ---: | ---: | ---: |
| HOMNS | 01536 | 063 | 179 |
| READK | 00952 | 125 | 85 |
| WRITEK | 00904 | 100 | 64 |
| TABT | 00704 | 43 | 35 |
| XKF | 01344 | 332 | 218 |
| MDCH | 01736 | 371 | 249 |
| UERTST | 00776 | 104 | 68 |
| MDFD | 02960 | 320 | 208 |
| MGMMA |  | 400 | 256 |
| MERF | 254 | 176 |  |
| Labelled common: | $\underline{02808}$ | $\underline{1275}$ |  |
| HOMO |  | 16412 | 701 |
| TOTAL |  |  | 7910 |

## PROGRAM DDKY

80. The program reads sets of integers and constructs a new one containing all the integers in all sets read. Not all the sets in the input file are used. Which are used is determined by sequence numbers read from another $\mathrm{I} / 0$ unit. A flow diagram is given in Fig 31.

## Solution

81: The integers in the input sets are copied sequentially into the output set as they are read. After all the input sets have been copied, the integers in the output set are ordered by calling the subroutine ORDERH. The program does not check for duplicates. An integer will appear in the output set as many times as it appears in all of the input sets.

## Capabilities

82. Maximum number of input sets to be included is 100. Maximum size of each input set is 20 integers. Maximum size of the output set is 1000 integers.

Input
Unit 1 - tape or disk or card reader - record length: 80 bytes, formatted. Input sets. This is the output from HOMO.
Unit 2 - card reader - record length: 80 bytes, formatted. Numbers of those input sets to be used. Same format as for unit 1 , see format for


Fig 31 - Flow diagram for program DDKY

HOMO and GRPS.

Qutput
Unit 7 - tape, disk or card punch - record length:

80 bytes, formatted. Output set; used as input to INPK1. These output records are in the same format as the input.

## Variables

KEY list of numbers of sets to be merged
MKEY array to contain output set
IGN array to contain list of set numbers
TITLE array to contain title
OV array of blanks
TITLE2 array to contain title of output set
LEN counter for size of output set
NG number of sets to be merged
NGD number of sets in the output file
I index
IG counter of sets to be read
IGF counter of sets merged
LENFIL size of set of which all input sets are subsets
LENK size of input set
J index
Storage Requirements

| Code |  | bytes | words |
| :--- | :---: | :---: | :---: |
| DDKY | 3312 | 2375 | 1277 |
|  |  | 6144 (buffers) | 3172 |
| ORDERH | 536 | 40 | 32 |
| READK | 952 | 125 | 85 |
| WRITEK | $\underline{904}$ | $\underline{100}$ | $\underline{64}$ |
| Total | 5704 | 8784 | 4630 |

SAMPLE RUN - STAGE 4

| Group data file. <br> Unit 1 input to INPTI. |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| TTEST DATA |  |  |  | GROUPS |  |  |  |  |  |  |  |  |
| 1806565941979 | 8 | 771 | -117001 | -103741 | 746239 | -153454 | -136064 | 978744 | 988907 | 222 | 78 | 68 |
| 2805718941650 | 8 | 326 | - 63014 | - 40096 | 316908 | -193537 | -123150 | 973333 | 998744 | 212 | 77 | 597 |
| 3805336941579 | 10 | 724 | - 49212 | -202889 | 682455 | - 68956 | -284288 | 956256 | 985738 | 256 | 73 | 56 |
| 4806601941425 | 7 | 284 | - 40332 | - 60184 | 273266 | -142663 | -212884 | 966606 | 995448 | 236 | 75 | 157 |
| 5805301941031 | 9 | 603 | 54374 | -108352 | 560983 | 94740 | -188788 | 977437 | 951797 | 297 | 78 | 16 |
| 6804515940645 | 10 | 644 | -142256 | -155611 | 606118 | -221672 | -242483 | 944491 | 996492 | 228 | 71 | 228 |
| 7803860940368 | 11 | 229 | - 37460 | - 73441 | 213281 | -163838 | -321205 | 932730 | 998439 | 243 | 69 | 524 |
| 8803612940354 | 15 | 451 | 62815 | -161001 | 413149 | 140262 | -359507 | 922541 | 992991 | 291 | 67 | 124 |
| 9803430940339 | 8 | 210 | 3960 | - 75036 | 195880 | 18876 | -357660 | 933661 | 999037 | 273 | 60 | 779 |
| 10803224940174 | 6 | 369 | -43438 | - 95381 | 352669 | -118066 | -259248 | 958567 | 997054 | 246 | 73 | 226 |
| ............. | 11 | 420 | $\ldots \ldots$ | -119483 | … 394625 | -100091 | -288329 | 952286 | 986663 | 251 | 72 | 61 |

Group keys.
Unit 1 input to DDKY.


## Data file

Unit 1 input to INPK1

TTEST DATA


Qutput files

Group numbers in domain
Unit 7 output from HOMO
Unit 2 input DDKY


Data file key for domain
Unit 7 output from DDKY
Unit 2 input to INPK1

| TEST: DATA | 100 | 101 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 97 | 98 | 99 | 100 | 101 | 102 | 103 | 104 | 105 | 106 | 107 | 108 | 109 | 110 | 111 | 112 | 113 | 114 | 3 |
| 115 | 116 | 117 | 118 | 119 | 120 | 121 | 122 | 123 | 124 | 125 | 126 | 127 | 128 | 129 | 130 | 131 | 132 | 4 |
| 133 | 134 | 135 | 136 | 137 | 138 | 139 | 140 | 141 | 142 | 226 | 227 | 228 | 229 | 230 | 237 | 232 | 233 | 5 |
| 234 | 235 | 236 | 237 | 238 | 239 | 240 | 241 | 242 | 243 | 244 | 245 | 246 | 247 | 248 | 249 | 250 | 251 | 6 |
| 252 | 253 | 254 | 255 | 256 | 257 | 258 | 259 | 260 | 261 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 7 |

Eigenvectors for domain.
Unit 7 output from WNST5.
$0.199667 \quad 0.977697-0.065149$
$0.943174-0.209783-0.257709$
$0.265628 \quad 0.0099930 .964024$

Input parameters (Unit 5, see Fig 32)


```
    Printed output
    Unit 6 output from INPTT:
    10 VARIABLES
FORMAT=(A1,T20,13,17,318,317,17)
TEST DATA GROUPS
    3 2 \text { DATA POINTS 1 PHYSICAL RECORDS}
    Unit 5 input and unit 6 output for HOMO
    (> indicates input):
TEST DATA GROUPS
TEST FOR HOMOGENEITY OF FABRIC
ENTER
    D TO DELETE GROUPS
    R TO RESTORE GROUPS
    L TO LIST GROUPS INCLUDED AND DELETED
    K TO TEST CONCETNRATION PARAMETERS
    M TO TEST MEAN DIRECTIONS
    A FOR AUTOMATIC DELETION OF GROUPS UNTIL MEANS ARE HOMOGENEOUS
    S TO STOP
? d
* ? r 01 02 03 04 05 0607 08 09 10 11 12
-> ? k
    CHI-SQUARE = 114.27 DF= 11
    TAIL PROBABILITY = 0.0
-> ? m
    F STATISTIC= 11.78 DF= 22, 192
    TAIL PROBABILITY = 0.0
-> ? d 01 02 03
-> ? k
    CHI-SQUARE = 96.78 DF=8
    TAIL PROBABILITY = 0.000
* ? m
    F STATISTIC= 14.66 DF= 16,146
    TAIL PROBABILITY = 0.0
* ? s
    ENTER NAME OF DOMAIN
-> ? domainl
```


## Unit 6 output from INPTI:

## 82 TEST DATA

DOMAIN1
1 PHYSICAL DATA RECORDS

Unit 9 output from WNST5:

82 TEST DATA
DOMAIN1

Unit 6 output from WNST5:

1
TEST DATA DOMAIN7
82 POINTS WITH TOTAL WEIGHT OF 330.5
"BINGHAM" STATISTICS

| EIGENVAL | EVAL/SW | DIRECTION COSINES |  | TR | PL | DD | DP |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| 4.14 | 0.01251 | 0.19966 | 0.94317 | 0.26563 | 78.0 | 15.4 | 258.0 | 74.6 |
| 10.60 | 0.03207 | 0.97770 | -0.20978 | 0.00999 | 347.9 | 0.6 | 167.9 | 89.4 |
| 315.77 | 0.95542 | -0.06515 | -0.25771 | 0.96402 | 255.8 | 74.6 | 75.8 | 15.4 |

TEST OF HYPOTHESIS $K 1=K 2=K 3$ : TEST STATISTIC $=1186.5664 \quad 5 \%$ POINT $=11.0705$
TEST OF HYPOTHESIS K2=K3: TEST STATISTIC $=314.9097 \quad 5 \%$ POINT $=5.99147$
TEST OF HYPOTHESIS K1=K2: TEST STATISTIC $=24.2093 \quad 5 \%$ POINT $=5.99147$
ALL HYPOTHESES REJECTED

TEST DATA
DOMAIN1
82 POINTS WITH TOTAL WEIGHT OF 330.5
"FISHER" STATISTICS

| R | R/SW | DIRECTION | COSINES | TR | PL | DD | DP |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 322.85 | 0.97687 | -0.06154 | -0.25837 | 0.96408 | 256.6 | 74.6 | 76.6 |
|  |  | 15.4 |  |  |  |  |  |

FISHER CONFIDENCE RADII
K 95\% 99\%
$42.186 \quad 2.4 \quad 3.0$

TEST OF UNIFORMITY ABOUT FISHER MEAN
KUIPER'S STATISTIC $=2.310 \quad 95 \%$ POINT $=1.747$

