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Predictive Analytics for the Royal Canadian Navy Fleet Maintenance Facilities

An application of data science to maintenance task completion times

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Abstract

In November 2016, Cdr Timothy Gibel, Directorate of Naval Strategic Management (DNSM) requested the Centre for Operations Research and Analysis's (CORA) assistance with creating a predictive model for actual work hours per task on Royal Canadian Navy (RCN) vessels at the Cape Scott and Cape Breton Fleet Maintenance Facilities (FMF). He also requested help in finding patterns in maintenance task completions at the vessel level. The FMF provided dataset contains information on 132,292 unique tasks separated into 43,731 order keys. Using regression trees with feature engineering for actual work hours, I find that a simple 14 terminal node tree explains 18% of the variance in the data. Gradient boosted stumps explain as much as 25% of the variance, but at the expense of an inter-pretatable structure for schedule validation. Hidden Markov Modelling of monthly order key completion time series data reveals coastal differences between the the RCN's two maintenance facilities, providing an objective motivation to discover the source.

Significance for defence and security

In November 2016, Cdr Timothy Gibel, Directorate of Naval Strategic Management (DNSM) requested DRDC CORA's assistance with creating a predictive model for Actual Work Hours on naval vessels at the Cape Scott and the Cape Breton Fleet Maintenance Facilities (FMF). The FMF provided Centre for Operational Research and Analysis (CORA) with two CSV (comma separated variable) files of 62 MB and 44 MB respectively, which contained maintenance data from 5 February 2004 to 6 July 2016. This paper shows the Royal Canadian Navy (RCN) the power of using data science on its operational and transactional data. Given the Royal Canadian Navy's (RCN) new SAP data environment, this work provides the timely demonstration of the data science possibilities that the RCN can now exploit.

Résumé

En novembre 2016, le cdr Timothy Gibel, de la Direction de la gestion stratégique de la marine (DNSM), a sollicité l'aide du Centre de recherche et d'analyse opérationnelles (CORA) pour créer un modèle prédictif des heures de travail réelles par tâche sur les navires de la Marine royale canadienne (MRC) des installations de maintenance de la flotte au Cap Scott et Cape Breton (FMF). Il a également demandé de l'aide pour trouver des tendances dans l'achèvement des tâches d'entretien au niveau des navires. L'ensemble de données fourni par FMF contient des informations sur 132 292 tâches uniques, séparées en 43 731 clés d'ordre. En utilisant des arbres de régression avec l'ingénierie des caractéristiques pour les heures de travail réelles, je trouve qu'un simple arbre de 14 nœuds terminaux explique 18% de la variance dans les données. Les *Gradient boosting stumps* expliquent jusqu'à 25% de la variance, mais aux dépens d'une structure inter-simulable pour la validation de la cédule. La modélisation de Markov cachée des données des séries chronologiques d'acheminements mensuels des principales commandes révèle les différences côtières entre les deux installations de maintenance de la MRC, fournissant ainsi une motivation objective à la recherche de la source.

Importance pour la défense et la sécurité

En novembre 2016, le Capf Timothy Gibel, de la Direction de la gestion stratégique de la marine (DNSM), a sollicité l'aide de RDDC CORA pour créer un modèle prédictif des heures de travail réelles des navires de la marine aux installations de maintenance de la flotte de Cape Scott et de Cape Breton. Le FMF a fourni au Centre de recherche opérationnelle et d'analyse (CORA) deux fichiers CSV (variables séparées par des virgules) de 62 et 44 Mo respectivement, contenant les données de maintenance du 5 février 2004 au 6 juillet 2016. Ce document présente la Marine royale canadienne (RCN) la puissance de l'utilisation de la science des données sur ses données opérationnelles et transactionnelles. Compte tenu du nouvel environnement de données SAP de la Marine royale canadienne (MRC), ce travail fournit une démonstration opportune des possibilités en science des données que la MRC peut maintenant exploiter.

1 Statement of results

I build a regression tree (see [1], [2]) with R [3] using packages [4], and [5], based on the log of actual work hours as the target. The key results are:

- The regression tree explains 20% of the variance in data;
- Feature engineering through unsupervised learning gives the regression tree an interpretable structure;
- The R scripts yield prediction quantiles of actual work hours based on task features. The client can include these scripts within the RCN's SAP Business Objects database tool.

Using time series analysis and Hidden Markov Models (HMM) (see [6], [7], and [8]) with R [3] (including package [9]) with monthly order key completion data by vessel data, the key results are:

- FMF Cape Scott show a downward trend on monthly order key completions from 2008 to 2016 while FMF Cape Breton does not show a trend over 2008 to 2013;
- Once accounting for trends, the monthly completion data on each coast shows one-month autocorrelation.
- A five-state HMM describes the data generating process;
- Clustering in the HMM rate space identifies each FMF, suggesting different challenges and business practices between the coasts.

The regression tree is a predictive model which helps FMF planners better understand the risk of schedule creep. Planners can use the model to validate technician built schedules by comparing planned hours to the information in the terminal nodes of the regression trees (e.g., in a 100 job task schedule, roughly 5 tasks should have planning time estimates that exceed the 95% quantile). The time series analysis demonstrates that the maintenance system has memory and that each FMF faces different challenges. Interpretation remains problematic—we do not know the reason for the coastal differences in order key completion rates. Order key completion records occur on the date at which the FMF closes a ticket and each FMF has its own close out policies. Given the downward trend in Figure 15 relative to Figure 16, there are differences between the two facilities. The time series analysis shows that we can identify each FMF by observing historical work patterns at the individual vessel level.

Acknowledgements

I would like to thank LCdr Andrew Sargeant and LCdr Jon Lee for their help in making this work possible. Both officers proved invaluable in helping me understand and interpret the Fleet Maintenance Facility datasets. Without their regular input and patience, this work would not have been possible.

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2 Introduction and Data Overview

Defence Resource Management Information System (DRMIS) unifies Department of National Defence (DND)'s financial information and materials management into a single Enterprise Resource Planning (ERP), replacing both Financial and Managerial Accounting System (FMAS) and Materiel Acquisition and Support Information System (MASIS). The system improves data visibility and transactional efficiency through a harmonized and expandable software system. DND uses a SAP¹ ERP solution which includes SAP's web intelligence and Business Objects.

Given the new visibility of the RCN's data, in November 2016, Cdr Timothy Gibel, Directorate of Naval Strategic Management (DNSM), requested Defence Research and Development Canada (DRDC) Centre for Operational Research and Analysis (CORA)'s assistance with creating a predictive model for actual work hours on naval vessels at the Cape Scott and Cape Breton Fleet Maintenance Facility (FMF). He also requested help in identifying the differences in maintenance activity between the two coasts. LCdr Jon Lee and LCdr Andrew Sargeant of FMF (Cape Scott) provided data on the maintenance tasks by using SAP Business Explorer (BEx) queries. The data consists of two Comma Separated Variable (CSV) files of 62 MB and 44 MB respectively. Together, the data files contain information on 132,292 individual ship specific maintenance tasks in 43,731 unique order

¹<https://www.sap.com/corporate/en/company.html>

keys over the date range 5 February 2004 to 6 July 2016. All tasks have both start and end dates—none of the tasks are time censored. Each task contains the following information (parenthetical values indicate the number of covariate levels):

- Order Key initiation time;
- Order Key close out time;
- Actual Hours;
- FMF (2;)
- Vessel name (21);
- PM activity (44);
- Materiel status (2);
- Work center (254) and;
- Functional location (1801).

Tasks belong to order keys and an order key can contain more than one task. Actual Hours record the amount of actual work time on the task while the lapsed order key time indicates the time between order key initiation and close out. In this study, I concentrate only on vessel maintenance activity, and the dataset contains information on 21 vessels (Halifax, Tribal, Protecteur, and Victoria Class). Each maintenance task belongs to a PM activity and a functional location on the vessel. Each task is routed to a work center with a materiel status indicating the presence of missing parts or materiel during the order key's life. The data contain some missing information in the Actual Hours covariate—approximately 30% of the tasks do not have a record for Actual Hours. I split the data analysis into two parts—a regression tree analysis (see [1] and references therein) that predicts of Actual Hours based categorical task covariates, and a time series analysis of monthly order key completions. In the regression tree analysis of Actual Hours, I use only the uncensored dataset, reducing the number of individual tasks to 91,482. In addition to the missing Actual Hours data, some of the covariates area associated with a small numbers of observations. Before beginning the regression tree analysis, I conduct high level feature engineering by coercing all levels within a covariate which has less than 30 observations into a single level called “OTHER”. These activities occur rarely and for the purpose of the regression analysis they belong to a single, rare class. The feature engineered dataset contains the following covariate and level information:

- Order Key initiation time;
- Order Key close out time;
- Actual Hours;
- FMF (2);
- Vessel name (21);
- PM activity (32);
- Materiel status (2);
- Work center (173) and;
- Functional location (573).

The final result is a single pruned regression tree with quantile informations for each of the tree's 14 terminal nodes. I grow the tree based on an unsupervised learning step in the covariate levels to reduce level complexity and I compare the result to gradient boosted methods.

In the second case, I analyze time series data on monthly order key completions through the lens of Hidden Markov Model (HMM) (see [7], and [8]). The monthly order keys do not have any missing data although the vessel time series do not all begin on the same date. Based on the analysis of pseudo-residuals and Akaike Information Criteria (AIC), I build a 5-state Poisson HMM for each vessel's monthly order key completion time series. The final result indicates a difference between the operations at the FMFs in that clustering analysis of the HMM rate vectors separates the vessels based on their coastal assignments.

3 Regression Models for Actual Hours

The covariates associated with the positive continuous Actual Hours target are all categorical. Regression trees are well suited for this type of data [1] which, based on a loss function, cut the target space into regions associated with the covariate information. In this study, I use CART (see [1] and references therein), and gradient boosting implemented in R with Rpart [4] and Gradient Boosted Model (GBM) [10].

Since Actual Hours span the range 0.25 to 11053, I log transform the data, resulting in the new target Log Actual Hours (LAH). The client requires more than a simple prediction of the mean LAH. To be useful for schedule risk assessment, the client needs distributional information on the subpopulations that reside inside the LAH target variable. In this circumstance, the client needs at least a partially interpretable model. I aid interpretation by reducing the covariate space through feature engineering in the mean-standard deviation within the each of the covariate levels.

To gauge the highest amount of variance we can hope to explain, consider Figure 1, which provides distributional comparisons of Actual Hours to the normal distribution. Notice that while we can reject the normal as a fit to the data (the Kolmogorov-Smirnov test confirms the rejection) we see that qualitatively, the data has normal-like properties. The structure in each tail suggests the possible presence of subpopulations but, given the approximate normal distribution description, we should not anticipate that regression techniques will explain most of the variance. The data is noisy. Table 1 summarizes the Actual Hours data.

Table 1: Empirical distributional information on Actual Hours across all tasks.

1st Quartile	Median	Mean	3rd quartile
8	19	39	48

We can detect the presence of subpopulations by using a Gaussian Mixture Model (GMM) (see [1] for details) on the LAH target. Figure 2 shows that the data supports between 8 and 15 Gaussian mixtures [5], which suggests internal structure that a suitable regression tree will discover.

To get a sense of how well regression trees might perform on the data, I fit a gradient boosted model (GBM) of stumps (see [1] for details) with LAH as the target using the covariates (number of levels in parentheses):

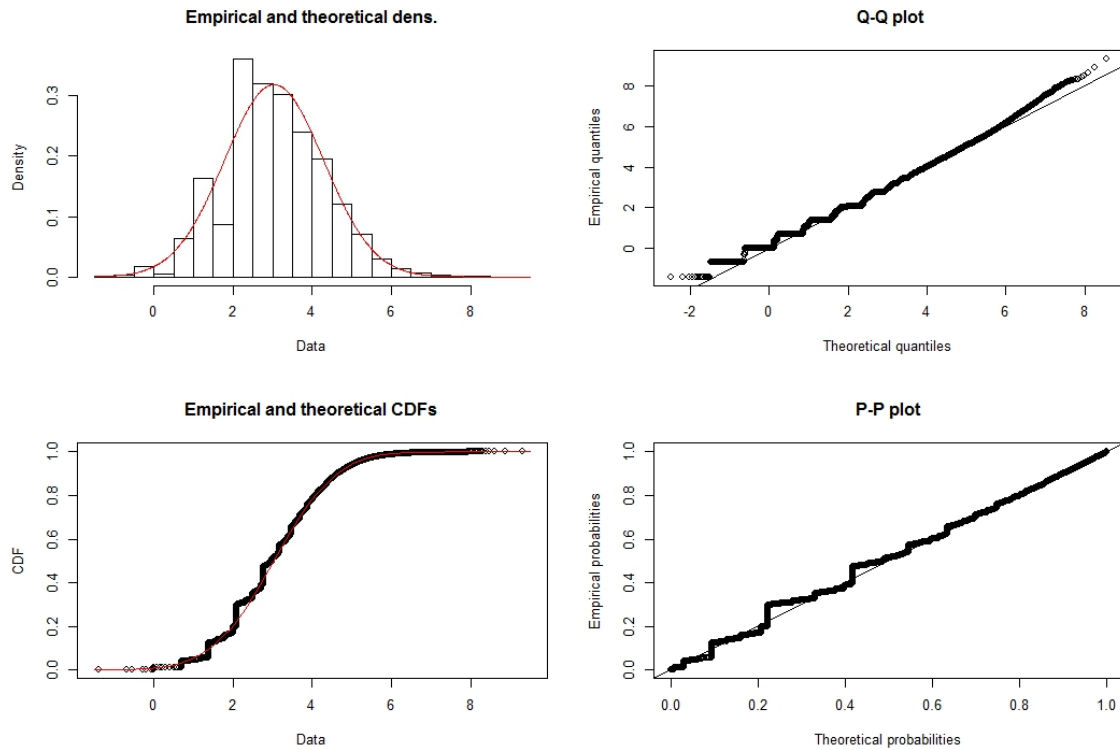


Figure 1: LAH comparisons to the normal distribution. The data are not explained by the normal distribution, but the approximate normal description implies that regression techniques will not explain most of the data's variance.

- Order Key initiation time;
- Order Key close out time;
- FMF (2);
- Vessel name (21);
- PM activity (32);
- Materiel status (2);
- Work center (173);
- Functional location (573).

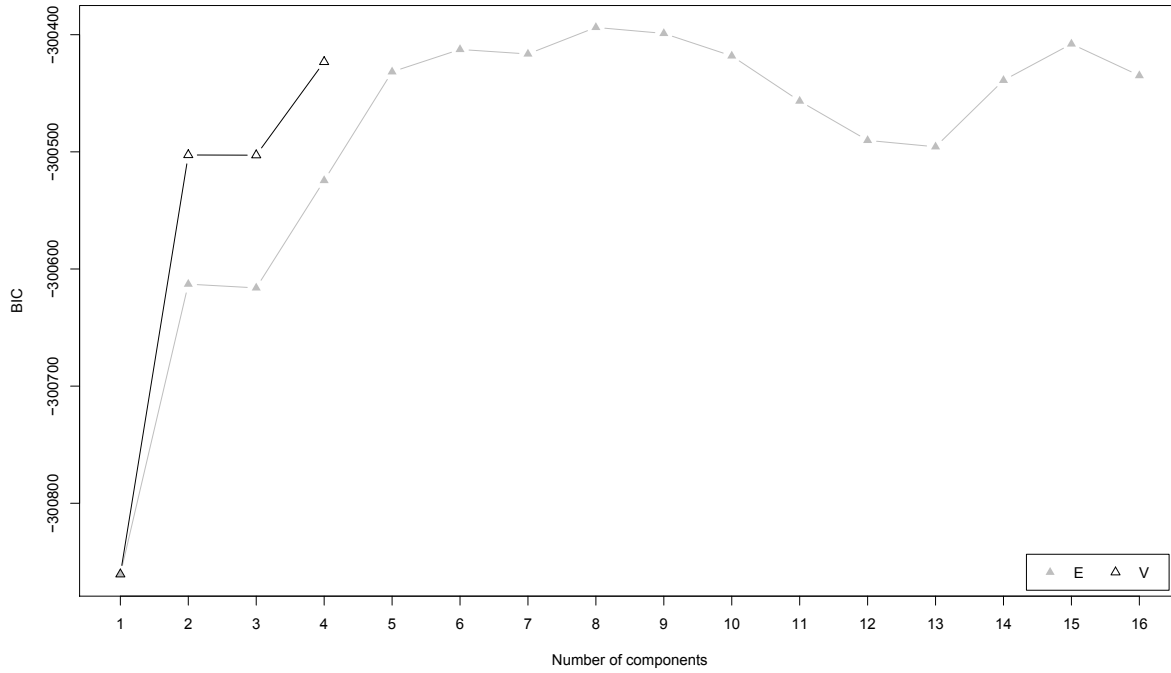


Figure 2: GMM applied to the LAH. Notice the presence of multiple subpopulations. The two curves label equal (E) and unequal (V) variance components.

I train the GBM on 90% of the data, holding back 10% for validation. Using Out-of-bag (OOB) sampling, the GBM contains 7425 stumps and the application of the GBM on the validation set explains 24.8% of the variance in the data. Table 2 shows the variable importance² of the GBM.

Table 2: GBM variable importance (24.8% variance explained).

Work center	Functional location	PM Activity	Materiel Status	Customer	FMF
66.8%	30.3%	1.5%	1.4%	0.0%	0.0%

The GBM provides predictions of mean LAH based on covariate information but the client requires a distributional understanding of subpopulations. The client cannot understand

²The model determines variable importance from the variable's strength in improving the loss function at each stump and how often the variable appears across all stumps. See [10] for details.

schedule risk from a point prediction. Given the large amount of unexplained variance, we need a model that captures subpopulation information even if the method sacrifices some of the explained variance. The GBM does not allow us to make a clean interpretation of LAH subpopulations, but it does provide us with an upper bound on how much variance we can expect to explain.

Single regression trees, using Classification and Regression Tree (CART), offer a more interpretable structure in that the terminal nodes of the tree reveal information on the data's subpopulations. Notice that the number of levels vary widely across the covariates even after the level reduction that results from pooling the small number observation levels. To simplify the levels, I feature engineer by using GMM in the mean-standard deviation LAH space of each covariate's levels. In Figures 3, 4, 5, and 6 we see that the unsupervised learning approach finds, by maximizing the Bayesian Information Criteria (BIC), a small number of clusters in the levels associated with each covariate:

- Vessel name (2);
- PM activity (3);
- Work center (2);
- Functional location (2).

Thus, instead of using hundreds of levels in an unbalanced setting, we can collapse the covariate levels down to a handful—assigning the covariate's levels according to its associated cluster. The reduced feature space balances the levels, which helps with variable importance identification. While Bayesian Information Criteria (BIC) favours a low number of levels, I consider three different feature engineered scenarios by expanding out to four Gaussian mixtures in each covariate's mean-standard deviation level space³. Figures 3—6 show that BIC disfavors a large number of clusters, but that including up to four does not lead to a large drop in BIC.

In the first scenario, I use the number of levels implied by BIC, and in the second and third scenarios I force the GMM to find exactly three and four clusters in the levels of each covariate respectively. The three different scenarios allow us to build three different regression trees. Table 3 show the results where again I hold back 10% of the data for validation. I have included random forests and GBMs on each featured engineered scenario for comparison.

³In the large cluster number limit, we return to the original GBM model—a tree structure without any feature engineering.

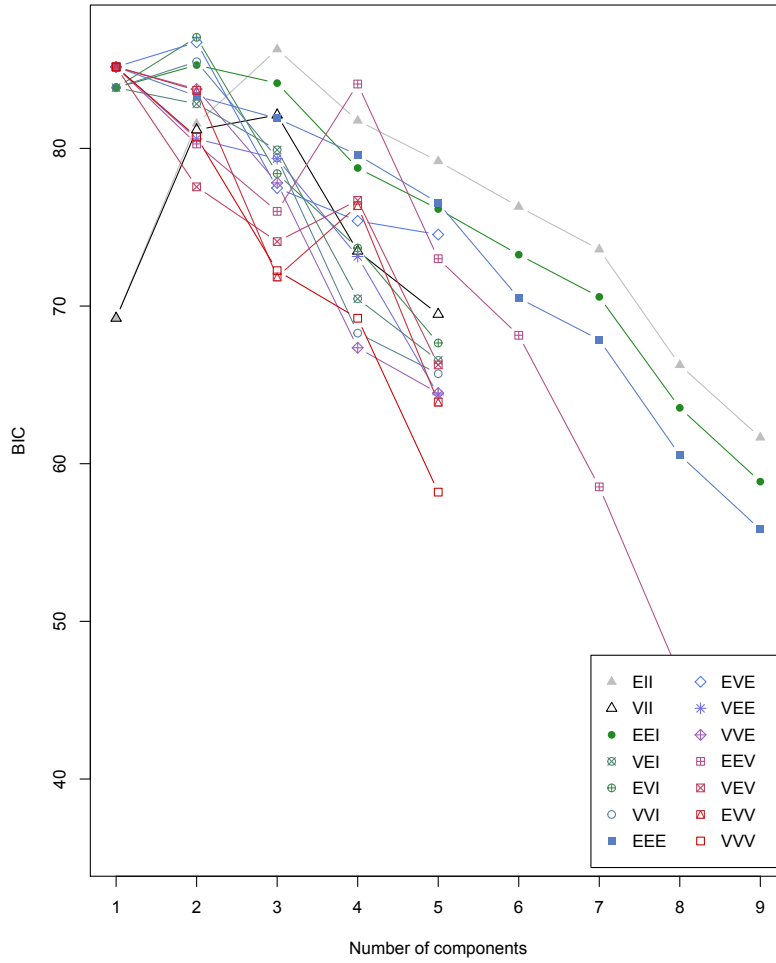


Figure 3: GMM BIC analysis of clusters in mean-standard deviation LAH by vessel name. The different curves label different parameterizations of the GMM covariance matrix. See [5] for details.

Notice that the four cluster model explains 18.6% of the variance while the GBM applied to the unengineered feature space (Table 2) explains 24.8%. The dramatic reduction of in the complexity of the feature space only sacrifices 6.2% of the explained variance, but leaves us with a more interpretable structure. For the rest of this paper, I will focus the analysis on the four cluster model with CART.

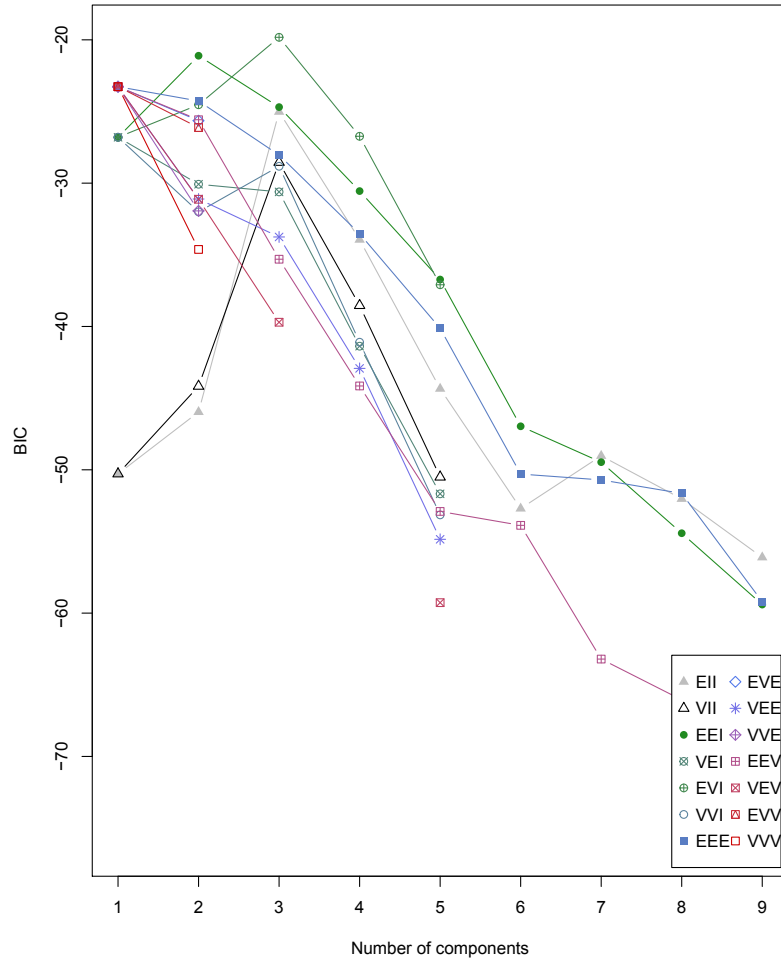


Figure 4: GMM BIC analysis of clusters in mean-standard deviation LAH by PM Activity. The different curves label different parameterizations of the GMM covariance matrix. See [5] for details.

In figures 7, 8, 9, and 10 we see the four clusters in the mean-variance space of each covariate's levels determined by the GMM. Tables 5, 6, 7, and 8 show the cluster membership of the levels. I build the regression tree to a depth of 70 trees (which overfits the data) and then prune back based on Rpart's complexity parameter. Rpart uses 10-fold cross validation to determine the relative error at a fixed complexity parameter values. As a function

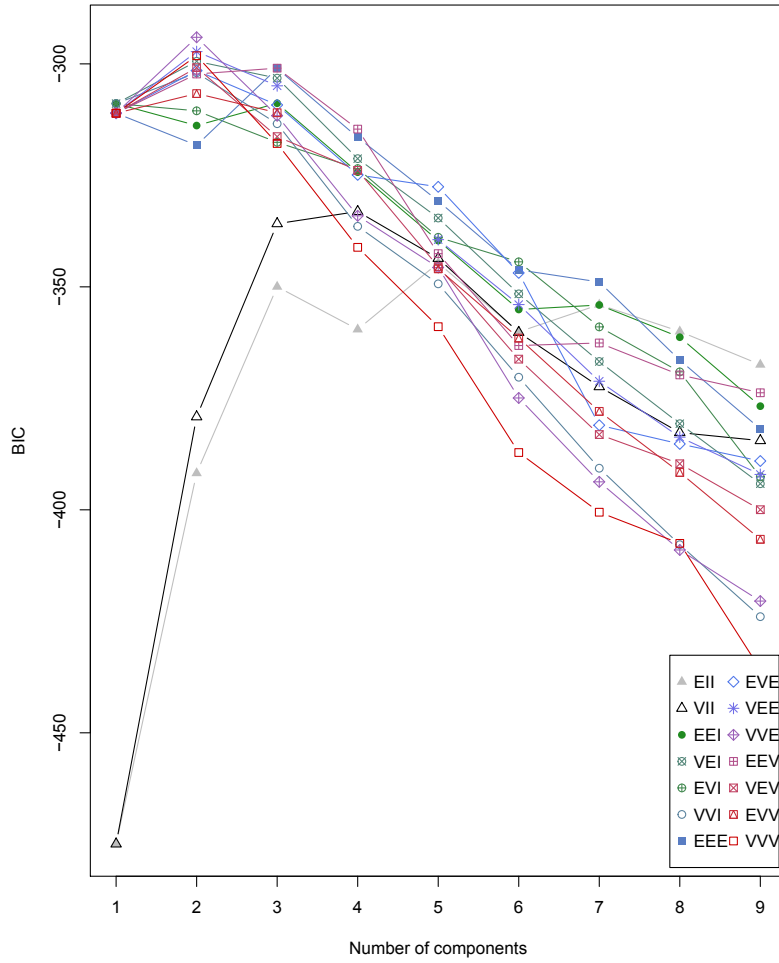


Figure 5: GMM BIC analysis of clusters in mean-standard deviation LAH by work center. The different curves label different parameterizations of the GMM covariance matrix. See [5] for details.

of tree depth, the relative error eventually reaches a plateau which allows us to prune the tree to an optimal depth. I locate the optimal tree by finding the tree depth which has the bottom of its 10 fold cross validation error bar touching the top of the last error bar in the plateau that arises from the overfit. Figure 11 shows the pruning method. Using this technique, I find the optimal tree has 14 terminal nodes, which concurs with the approx-

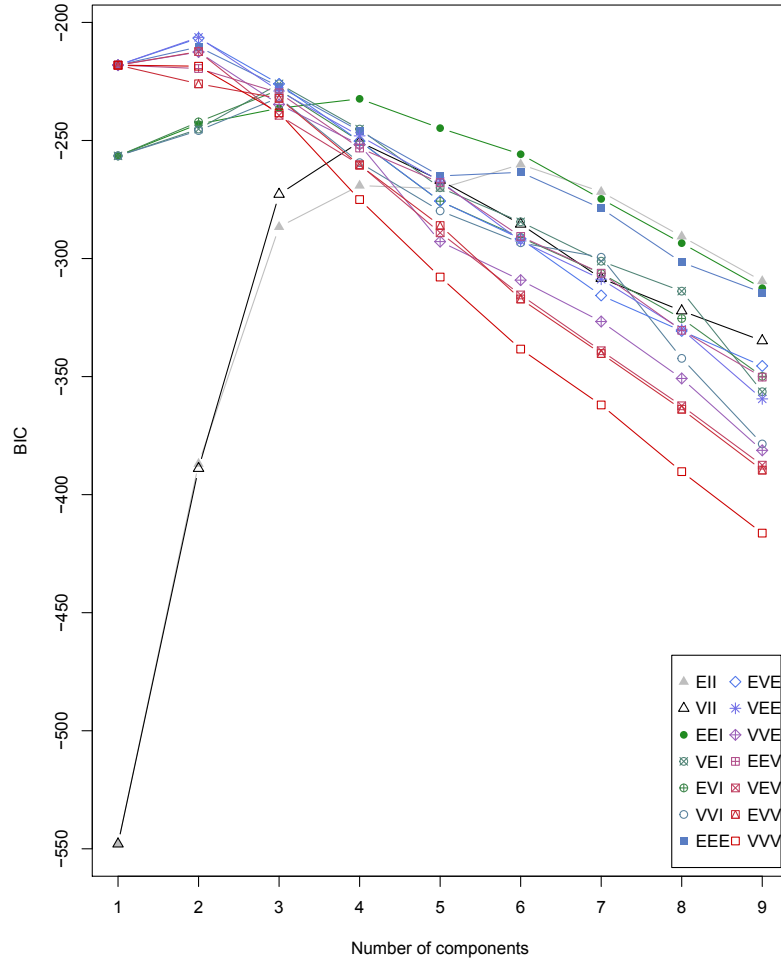


Figure 6: GMM BIC analysis of clusters in mean-standard deviation LAH by functional location. The different curves label different parameterizations of the GMM covariance matrix. See [5] for details.

imate number of subpopulations indicated by the GMM in Figure 2. Table 4 shows the variable importance of the four cluster feature space regression tree which compares well with the unengineered GBM variable importance of table 2. As compared to the GBM, the feature engineering of the four cluster model shares the relative variable importance of the functional location with the PM Activity. Notice that even though we have radically

Table 3: Scenario explained variance (out of sample validation)

Scenario	Regression method		
	Random Forest (300 trees)	GBM (OOB)	CART (pruned)
BIC cluster	13.1%	13.4%	13.8%
Three cluster	15.8%	17.0%	16.7%
Four cluster	18.2%	18.9%	18.6%

reduced the covariate levels as compared to the GBM with the unengineered feature space, the order of the variable importance remains the same.

Table 4: Four cluster scenario variable importance (18.6% variance explained).

Work center	Functional location	PM Activity	Materiel Status	Customer	FMF
69.3%	15.1%	10.8%	3.4%	0.9%	0.6%

The 14 terminal node tree allows us to build Actual Hour quantiles for each node, which can help the client understand potential variability and risk within planned schedules. Figure 12 shows the regression tree with the primary nodes⁴. Notice that the Work center forms the first split and continues as a splitting variable throughout the tree. The Work center has the highest relative importance among the covariates. Figure 13 shows the distributional information associated with each of the 14 terminal nodes, including node quantile information.

⁴Rpart builds the regression tree with both primary and surrogate nodes. The tree uses surrogate node information in the absence of primary node information and Rpart incorporates surrogate node strength in determining variable importance (see [4] for details).

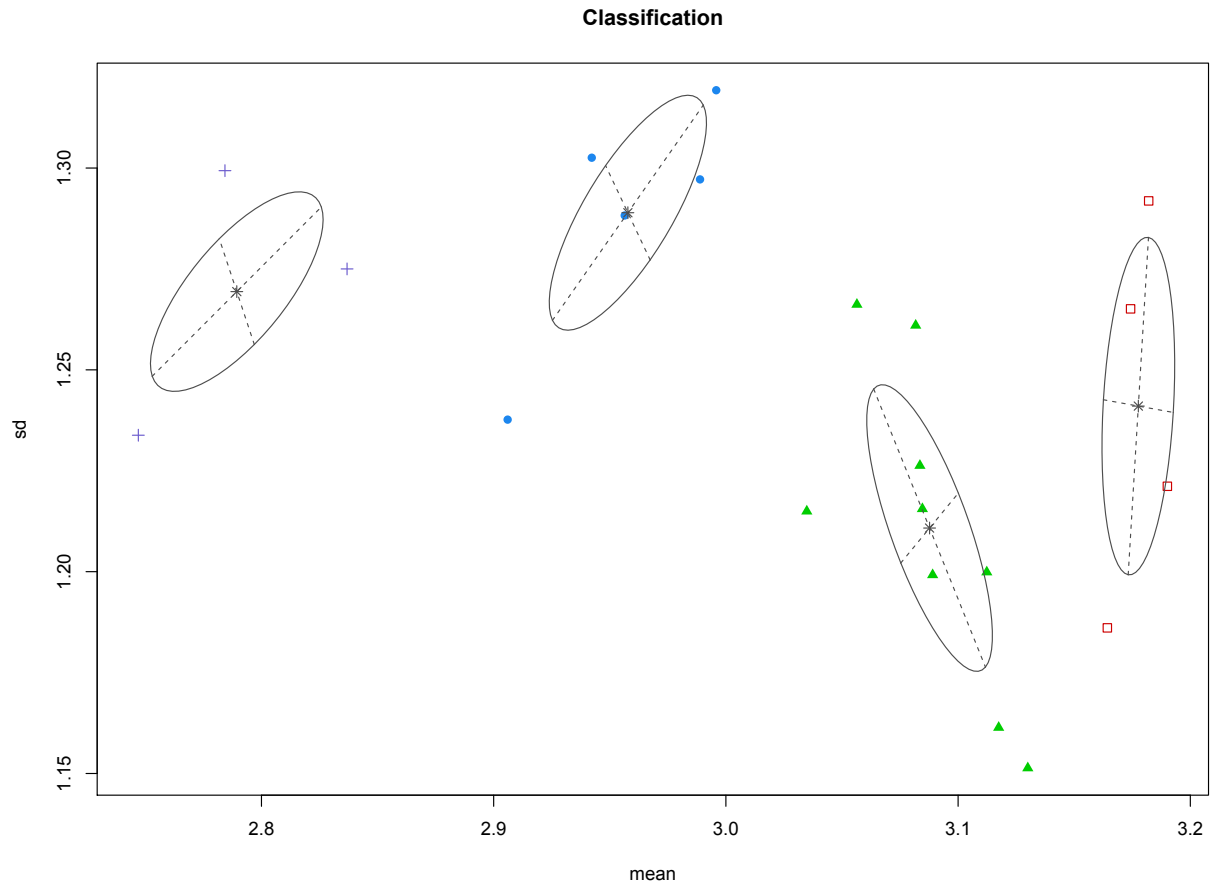


Figure 7: Four cluster GMM applied to vessel name in the LAH mean-standard deviation space. Standard error ellipsoid indicated.

The four cluster model provides the client with distributional results that a straightforward application of boosted models do not. Since the client is interested in understanding the distributional relationships of subpopulations which live in the data, the pruned regression tree offers the client insight that a point prediction from a boost model cannot. The greater interpretability of the regression tree—which has only 14 terminal nodes—relative to the GBM makes up for small sacrifice in explained variance. We see that regardless of the model, the data remains noisy.

To test the model’s strength in the face of the noisy data I compute the Naive Bayes Clas-

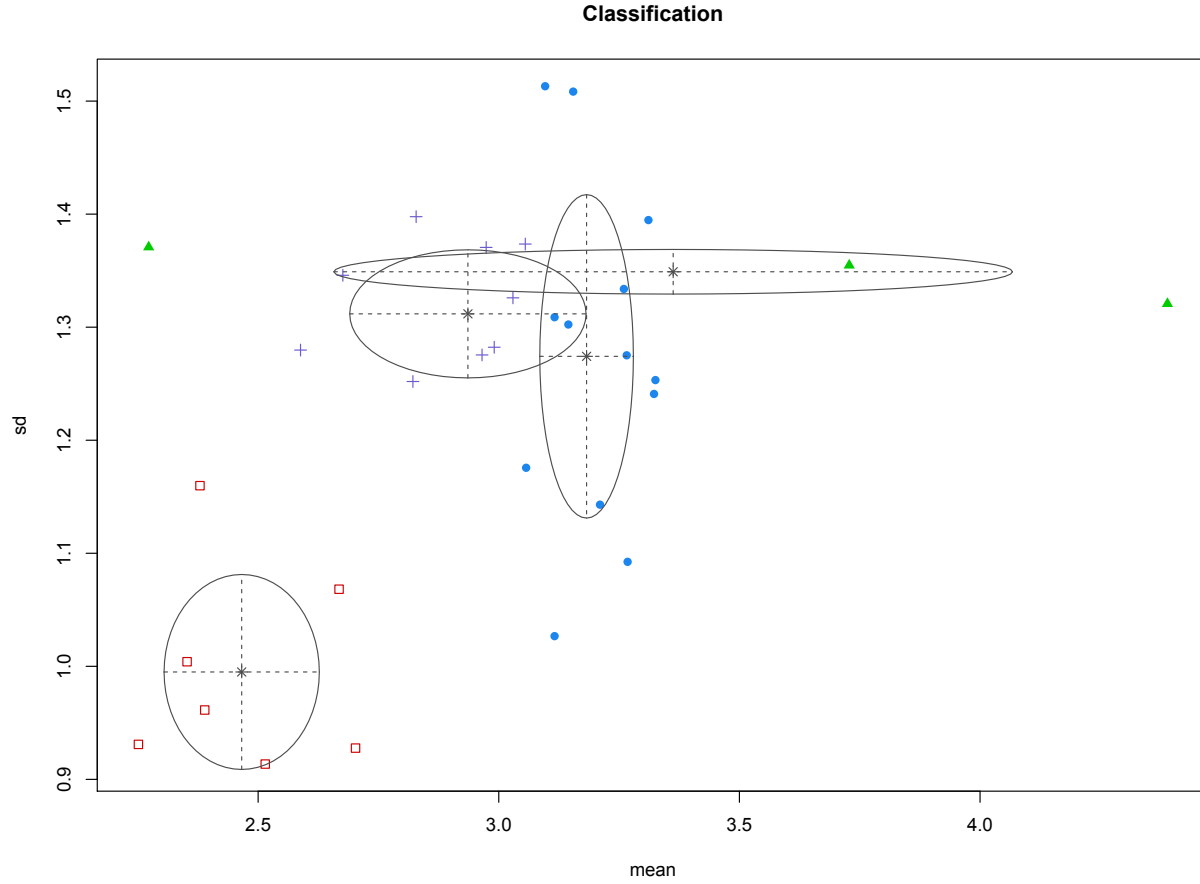


Figure 8: Four cluster GMM applied to PM activity in the LAH mean-standard deviation space. Standard error ellipsoid indicated.

sifier (see [1] for details) of each terminal node as a function of LAH, displayed in Figure 14. The figure shows the probability of reaching a terminal node conditioned on the LAH value. Figure 12 labels the terminal nodes by their respective mean LAH. We see the trend that high values of LAH lead to high probabilities of ending up in terminal nodes with large means. We can also see the effect of the noise in the data—LAH values larger than 5 only imply a probability of less than one chance in three of belonging to the terminal node with the highest mean.

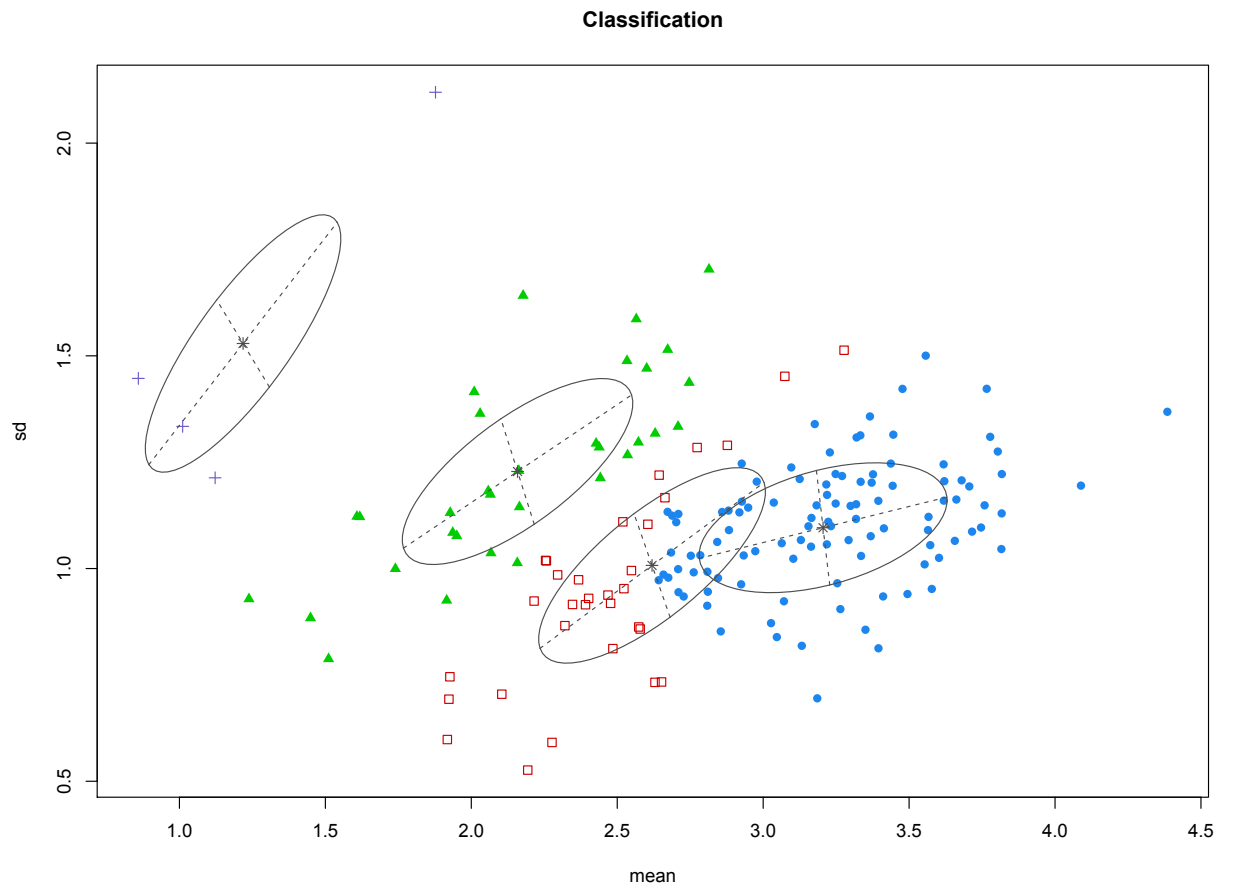


Figure 9: Four cluster GMM applied to work centers in the LAH mean-standard deviation space. Standard error ellipsoid indicated.

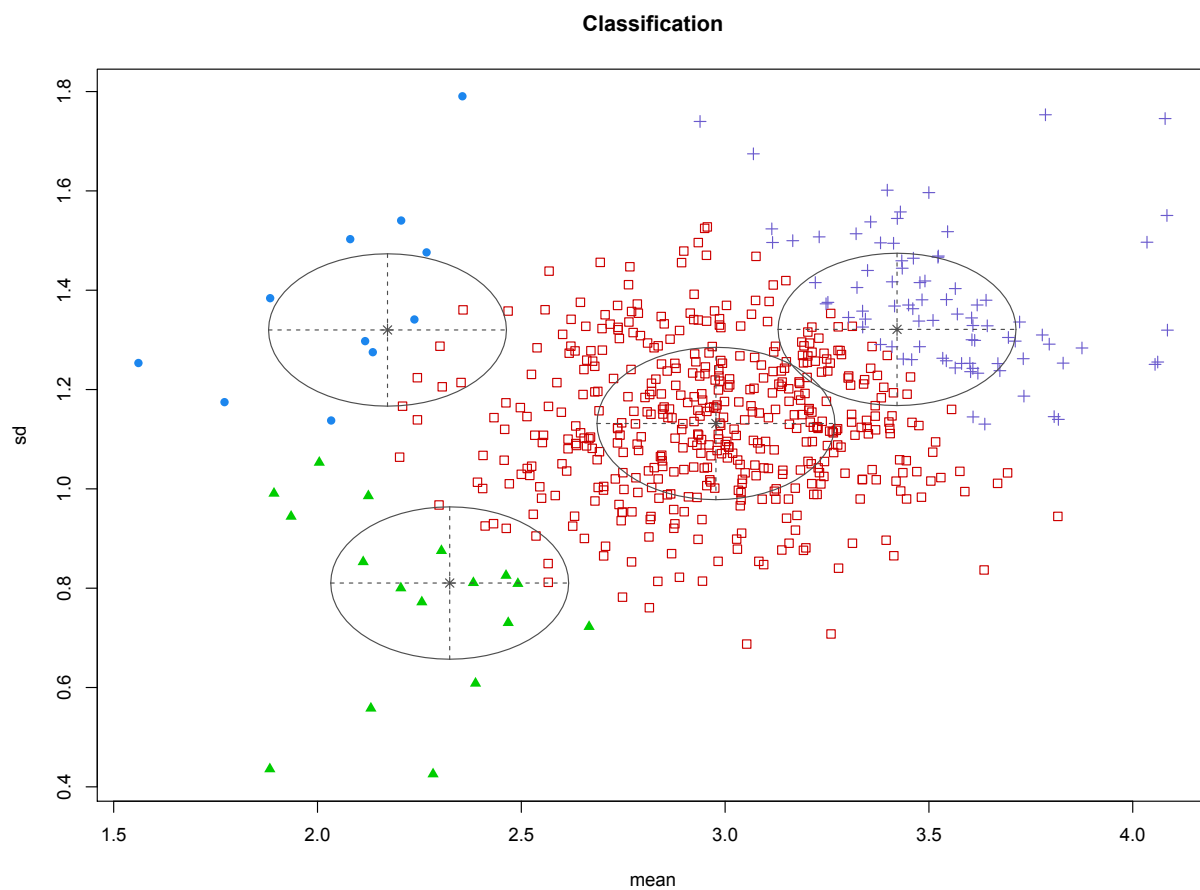


Figure 10: Four cluster GMM applied to functional locations in the LAH mean-standard deviation space. Standard error ellipsoid indicated.

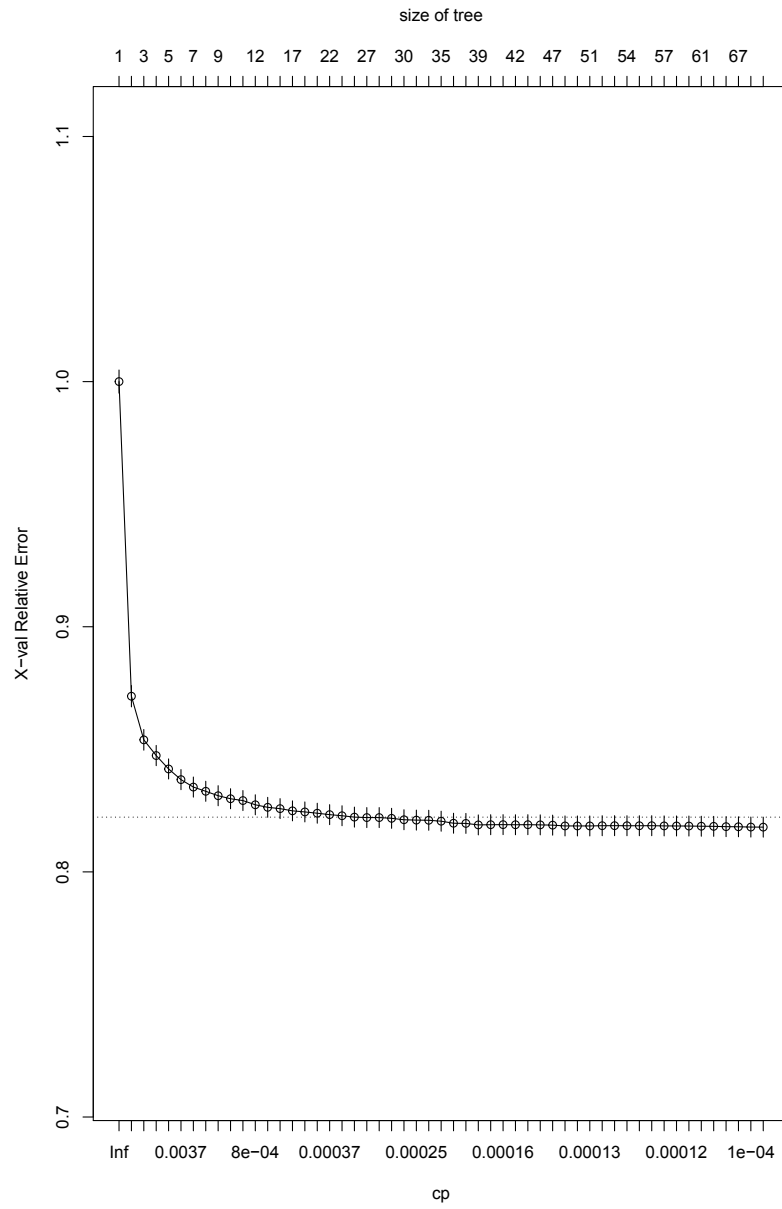


Figure 11: Complexity parameter relative error by 10-fold cross validation. The method selects 14 terminal nodes.

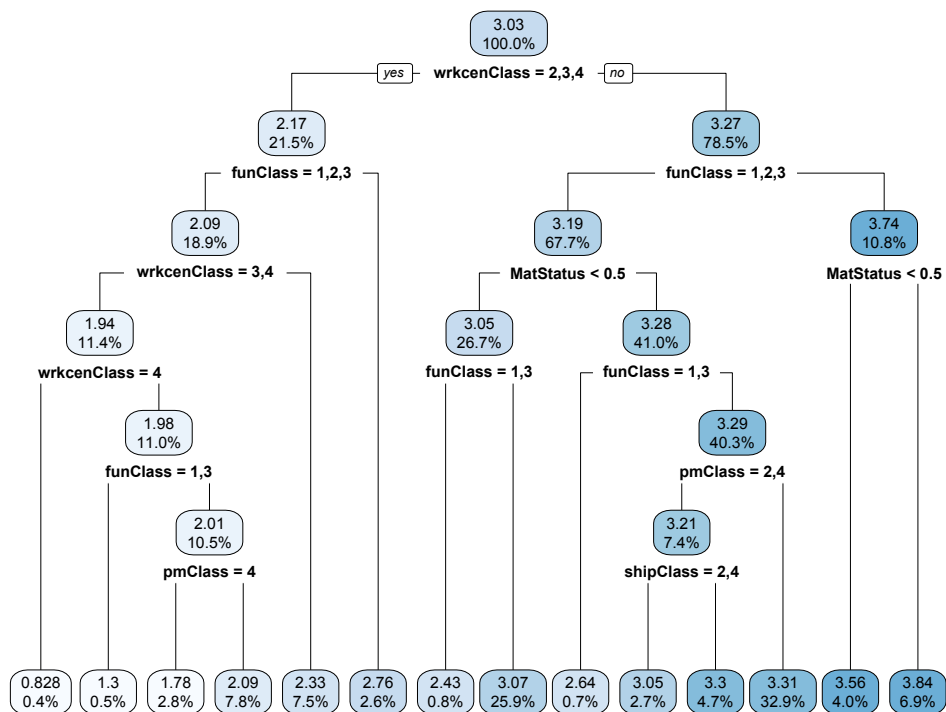


Figure 12: Pruned regression tree built from the four cluster model. The primary nodes are labelled by the LAH mean along with the percentage of the data contained within the nodes.

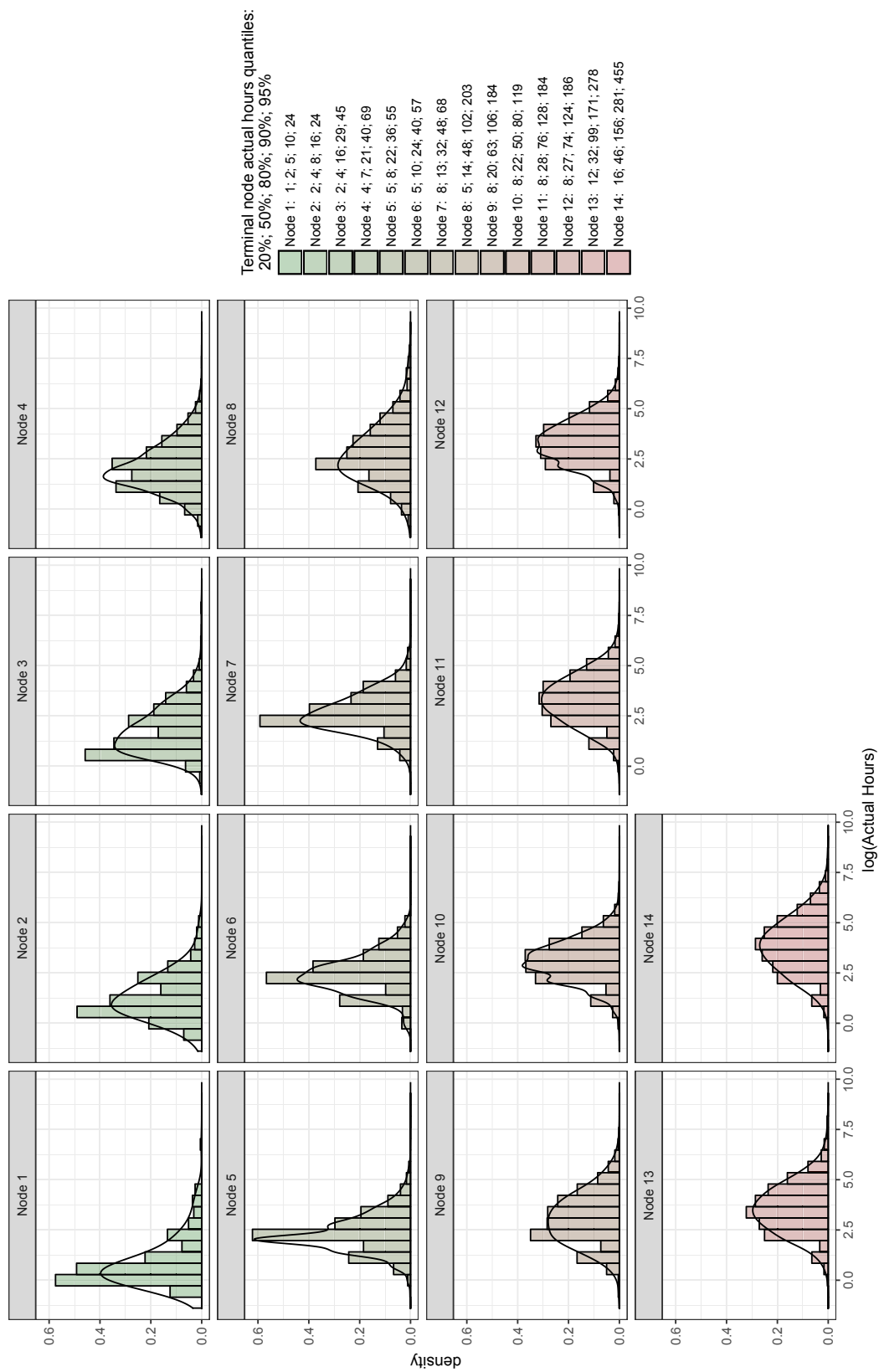


Figure 13: LAH terminal node distributional information.

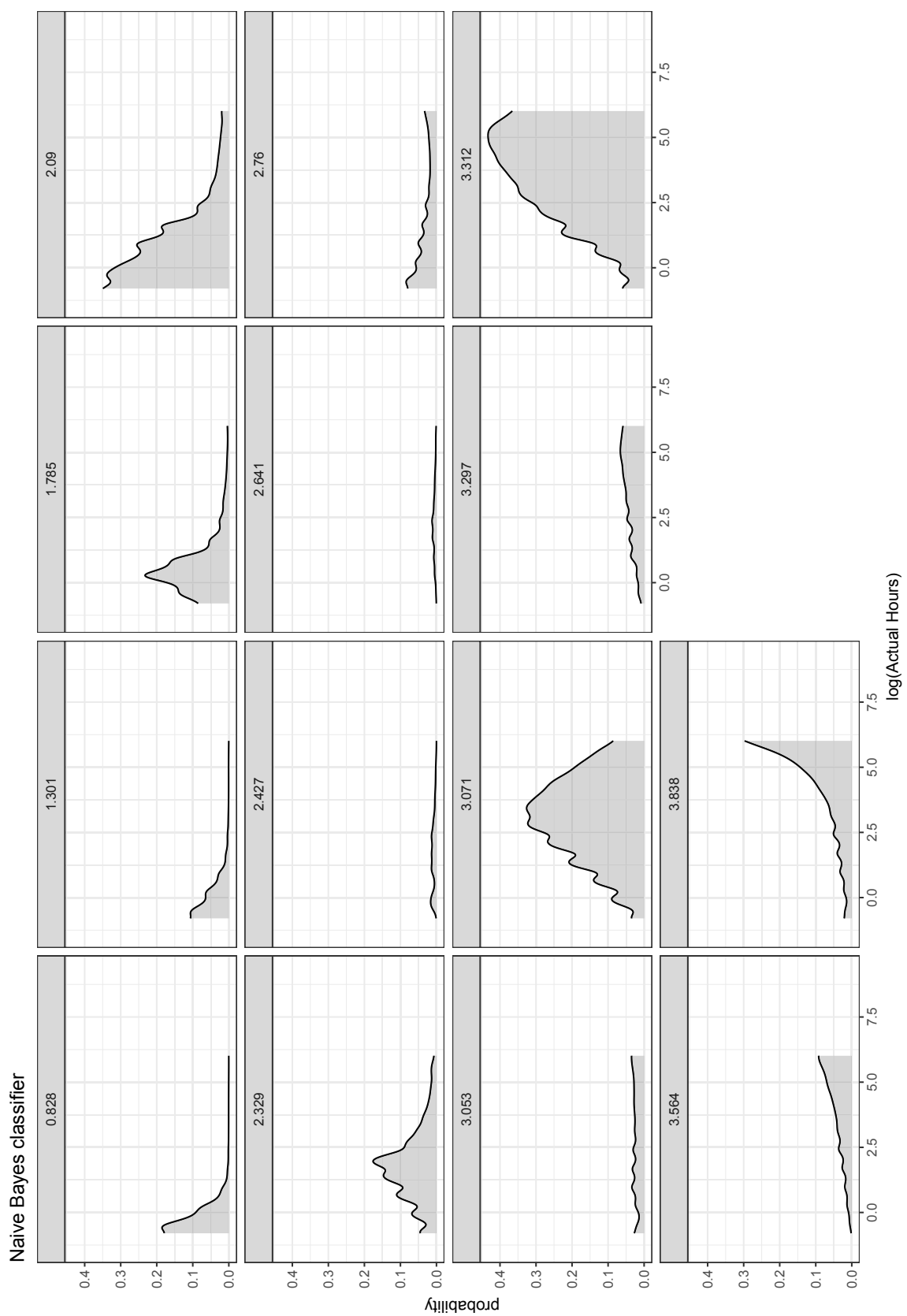


Figure 14: Naive Bayesian Classifier of terminal nodes based on LAH.

Table 5: Vessel features: GMM classification assignments with four clusters.

Blue (1)	Red (2)	Green (3)	Purple (4)
HMCS Algonquin	HMCS Athabaskan	HMCS Charlottetown	HMCS Chicoutimi
HMCS Calgary	HMCS Iroquois	HMCS Cornerbrook	HMCS Vancouver
HMCS Ottawa	HMCS Protecteur	HMCS Fredericton	HMCS Victoria
HMCS Regina	HMCS Windsor	HMCS Halifax	
HMCS Winnipeg		HMCS Montreal	
		HMCS Preserver	
		HMCS St. John's	
		HMCS Toronto	
		HMCS Ville de Quebec	

Table 6: PM Activity features: GMM classification assignments with four clusters.

Blue (1)	Red (2)	Green (3)	Purple (4)
Capital EVAL	Certifications	Costed	NP Canavmod
Capital Major	Condition Based Assessment	NP Major	NP Minor
Capital Minor	Inspections	Trials	Other Capital
Corrective	MRS Particularization		Other Work
Growth Work	Safety		PM Arising
Manufacturing	Surveys/Audits		Preventive RF
NP EVAL	Technical Assistance		Preventive SS
Other Non Capital Work			Temporary (M/F)
PMRS			Warranty
Re-Work			
Repair & Overhaul 3rd Line			
Services			
Supplemental			

Table 7: Work center features: GMM classification assignments with four clusters.

Class	Work Centers			
Blue (1)	*****DELETED***** - USE 12148 250 BARGE ABOVE WATER WEAPONS ANTENNA MFWC ATS AUXILIARIES 2 AWSE -Inspection Naval Ordnance BATTERY BELOW WATER WEAPONS BOILERMAKERS CABLE CABLING CCS ENGINEERING COATINGS COMM / NAV ENG COMM Ship COMMUNICATION COMMUNICATIONS CONTROL SYSTEMS CONTROL SYSTEMS Electronics CONTROL SYSTEMS ENGINEERING CONTROL SYSTEMS Mechanical CREW - CCS/Radar/Electronic Warfare DI/EHM/TRIALSTION DIESEL TECHS DIESELS DRAWING OFFICE	ELECTRICAL ELECTRICAL SYSTEMS EC'S & PROJECTS ELECTRICAL TEST EW / CCS / Nav Aids FIRE CONTROL SHOP FOUNDRY GAS TURBINE GAS TURBINES GENSETS & FIRE PUMPS (SURFACE) GOVERNOR SHOP GUN WEAPONS SYSTEMS GUNS AND MISSILES - ELECTRICAL GUNS AND MISSILES - ELECTRONIC GUNS AND MISSILES - MECHANICAL HEAVY ELECTRICAL HULL SURVEYORS HYDRAULICS IMCS LAGGERS LAGGING MACHINE SHOP MACHINING SERVICES MAIN PROP & AUX (SURFACE) MARINE ELECTRICAL ENGINEERING MARINE MACHINERY MARINE MACHINERY (NAT INV) MARINE MACHINERY SUB-SURFACE	MARINE MACHINERY SURFACE MECHANICAL FITTERS MOTOR MULTOTS NAV AIDS SUPPORT NAV AIDS SUPPORT METER SECTION NAV AIDS SUPPORT SHOP NAV ARC AND MATERIAL ENGINEERING (NA/ME) NESTRA Optics PIPE FABRICATION PIPEFITTERS PLANT MAINTENANCE PLATE RADAR / FIRE CONTROL FITTERS RADAR / IFF / TACAN / IR REFRIGERATION & AIR CONDITIONING RIGGERS RIGGING RIGGING LOFT SAIL/LIFE RAFT/CANVAS SCALERS & CLEANERS SENSORS - ELECTRONICS SENSORS - MECHANICAL SYSTEMS SHEET METAL SHEETMETAL SHIPS SYSTEM ENGINEERING	SHIPWRIGHT SHIPWRIGHTS SHIPWRIGHTS & STAGING SONAR SONAR CANTASS SONAR ELECTRONIC SONAR MECH SUB PIPE FABRICATION SUB ELECTRICAL SUB PLATE SUB SHEET METAL SUB SONAR *****DELETED***** SUB WELDING TEMPORARY LIGHT TILE PREPARATION TILING UNDERWATER RANGE UNDERWATER WEAPONS - ELECTRICAL UNDERWATER WEAPONS - ELECTRONICS UNDERWATER WEAPONS - MECHANICAL SYSTEMS UNDERWATER WEAPONS -MECHANICAL VCS FC / SONAR TECHNOLOGISTS WELDERS WELDING
Red (2)	AUXILIARIES 1 COMM CONO - PAINT & TILE CONO - FIRE SENTRY CONTROLS SYSTEMS ELECTRICAL POWER SYSTEMS ELECTROPLATORS FIRE CONTROL	GUIDED WEAPONS INO LIFTING APPLIANCE CERTIFICATION MAIN PROP TECHS MECHANICAL PROCESS ENGINEERING NON-DESTRUCTIVE TESTING OPTICS PAINTERS	PNEUMATICS POWER SYSTEMS PRESSURE VESSELS RADAR/EW TECHNOLOGISTS Ranges Manager SHIP INSPECTION SIGN & GRAPHICS SUBMARINE COMMUNICATIONS	SUBMARINE ELECTRICAL SUBMARINE HULL SURVEYOR SUBMARINE MECHANICAL SURFACE SONAR / NAV AIDS TECHS TEMPORARY VENT VCS / SURFACE UW WEAPONS TECHNOLOGISTS VIBRATION ANALYSIS WELDING INSPECTION
Green (3)	ABOVE WATER SYSTEMS ENGINEERING AWSE - ELEC AWSE - MECH C4I CANTASS CHEMICAL CLEANING COMBAT MANAGEMENT SYSTEMS TECHNOLOGISTS COMBAT SYSTEMS ENGINEERING OFFICER	CONO - O & M CRANE OPERATORS DIESEL INSPECTION CELL ENGRAVING SHOP HULL INSPECTORS HULL SYSTEMS HULL SYSTEMS ENGINEER HULL SYSTEMS TECH	LIFTING APPLIANCE MAIN MACHINERY ENGINEERING NACE INSPECTORS NAV NDT/NACE INSPECTORS NET-C Other Center PETROLEUM, OILS & LUBRICANTS	PLANT MAINTENANCE ELECTRICAL QAR Windsor EDWP QUALITY CONTROL INSPECTORS SAIL/CANVASS & MARINE SURVIVAL SYSTEMS SURVEIL / ELEC. WARFARE ENG. SURVEILLANCE SYSTEMS SENIOR ENGINEER UW ENG ELEC UW ENG MECH
Purple (4)	MECHANICAL AUXILIARIES SAWS TRIALS CPO UWW SENIOR ENGINEER			

Table 8: Functional location features: GMM classification assignments with four clusters.

Class	Functional Locations			
Blue (1)	AUTOMATIC IDENTIFICATION SYSTEM (AIDS). AUXILIARY VENT & BLOW SYSTEM BOOMS & LIFTING APPLIANCES	COMMUNICATION SYSTEM, MISCELLANEOUS FAN SYSTEM, VANEAXIAL, SF-12, 13, 14, 15 FIRE FIGHTING (HALON GAS)	LIFERAFT, INFLATABLE, 20 MAN MAIN CABLING PUMP SYSTEM, CENTRIFUGAL (CHILLED WATER)	SHAFT SEAL COOLING & LUBN SOUNDING SET, SONAR
Red (2)	1 DECK (WEATHER) 140KW MOTOR GEN & ASSOC. EQUIP (FWD/AFT) 15 TON DECK CRANES 2 DECK 2D SEARCH AND SURVEILLANCE RADAR, AN/SPS 3 DECK 4 DECK 440/60 HZ DIST & MAIN AC SWITCHBOARD 5004 SATELLITE TELEVISION SYSTEM 5KHZ/25KHZ UHF SATCOM DAMA TERMINAL ACCOMMODATION SPACES (GENERIC) ADVANCED HARPOON WEAPONS CONTROL SYSTEM AIR CONDITIONING & VENTILATION SYSTEM AIR CONDITIONING HYDRONIC SYSTEM AIR CONDITIONING SYSTEM (PIELSTICK ENG) AIR DISTRIBUTION SYSTEM AIR PURIFICATION & LIFE SUPPORT AIR SUPPLY SYSTEM AIRCRAFT FUELLING SYSTEM AIRCRAFT SUPPORT EQUIPMENT GROUP AN/SRD-504 RADIO DIRECTION FINDING SET AN/ULR-502 (SUB ESM) AN/USC-69(V)3 X AND KU BAND SATELLITE CO ANCHOR AND ASSOCIATED EQUIPMENT ANCHORING, MOORING & TOWING GEAR ANTENNA AS-5196/U ANTENNA GROUP OE-5034/SR ANTENNA GROUP OE-5036/SR ANTENNA GROUP, OE-273A(V)/URN ANTENNA GROUP, OE-5023/SLQ-501 ANTENNA GROUP, OE-5039/SPS-505 ANTENNA GROUP, OE-82C/WSC-1(V) ANTENNA GROUP, OE-82D/WSC ANTENNA, AS-3263/SPS-49(V) ANTENNA, AS-5169/SRC ARMAMENT, COMMAN'T & CONTROL FOUNDATIONS AUTOMATIC CONTROL (PIELSTICK ENGINE) AUTOMATIC LUBRICATION SYSTEM AUXILIARY SEAWATER CIRCULATING SYSTEM AV & B REDUCING STATIONS AWNINGS, AWNINGS STANCHIONS & MISC COVERS BALLAST PUMPS & COMPENSATING UNITS BATTERY COOLING SYSTEM BATTERY SWITCHBOARD BATTERY VENTILATION BILGE PUMPS & COMPENSATING UNITS BINOCULAR SYSTEM, MK 3, MOD 5 (BIG EYE). BLACK & GREY WATER COLLECTION SYSTEM BLACK & GREY WATER SEWAGE TREATMENT PLNT BLACK AND GREY WATER COLLECTION SYSTEM (BLANKER-VIDEO MIXER SET AN/SLA-10B BOAT DAVIT SYS (RIGID INFLATABLE BOAT) BOAT, INFLATABLE MAT, SEA RESCUE, 10 MAN BOATS HANDLING & STOWAGE BOILER, AUXILIARY BOTTLE ASSEMBLIES	DECKS DECKS (GENERIC) DECKS (SUPER STRUCTURE) DEGAUSSING SYSTEM (GENERIC) DETECTING RANGING SET SONAR DIDSBURY TORPEDO HANDLING SYSTEM DIESEL EXHAUST SYSTEM DIESEL GENERATOR SET, 850 KW DIESEL GENERATORS & CONTROL EQUIPMENT DIRECTION FINDER SET DIRECTION FINDER SET, AN/SRD-504A DISTRIBUTION SYSTEM, AC, 450V, 3 PH DOMESTIC HOT & COLD FRESH WATER DOOR SPECIAL PURPOSE (HANGER) DOORS & FRAMES DOORS, HANGAR, VERTICAL ROLLING DOORS, HATCHES AND MANHOLES DOORS, HATCHES, MANHOLES & SCUTTLES DOPPLER SPEED LOG SYSTEM DRAINS, SANITARY SYSTEM DRIER, AIR-GAS DESICCANT DRYER, AIR-GAS DESICCANT HP EBS, BIBS, HIS, SBSS ECHO SOUNDER TYPE 778JJ ELECTRONIC SUPPORT MEASURES AN/SLQ-501 ELECTRONIC SUPPORT MEASURES SET ELECTRONIC WARFARE EQUIPMENT GROUP ELEVATOR AMMUNITION EMERGENCY BREATHING SYSTEM ENGINE DIESEL ENGINE DIESEL, PORT ENGINE DIESEL, STBD ENGINE GROUP, GAS TURBINE ENGINE, DIESEL (850KW GENERATOR SET) ENGINE, DIESEL (SEAWATER SERVICE SYSTEM) ENGINE, GAS TURBINE EXHAUST & IR SUPPRESSION EXHAUST DUCTING EXHAUST SYSTEM EXHAUST SYSTEM (PIELSTICK ENGINE) EXT HYD POWER PLANT ANC EQUIPMENT EXTERNAL COMMUNICATIONS EQUIPMENT EXTERNAL HYDRAULIC POWER PLANT EXTERNAL HYDRAULIC SYSTEM EXTERNAL WEATHER DECKS & PLATFORMS FAN SYSTEM, VANEAXIAL, MUC-1 & MCU-2 FAN SYSTEM, VANEAXIAL, EF-9, EF-11, EF-13 FILTRATION UNIT 1-1A, 4-4A FILTRATION UNIT 2-3 FILTRATION UNITS, NBC FINE WATER SPRAY SYSTEM (FIRE SUPPRESSIO FIRE AND PREWET PUMP UNIT FIRE FIGHTING EQUIPMENT, PORTABLE FIRE MAIN SYSTEM FIREMAIN SYSTEM FIXED EXTINGUISHING SYSTEMS	HYDRAULIC STEERING SYSTEM BROWN BROTHERS HYDRAULIC SYSTEM TUBE 2 (WDS) HYDROGEN DETECTION ASSEMBLY HYDRONIC SYSTEM HYDROPLANES & STEERING HYDRAULIC SYSTEM HYDROPLANES STEERING GEAR HYD PP ANC HYDROPLANES STEERING OPERATING GEAR IFF SYSTEM GROUP, MK 12 (TRL, PTR, FSE, INDICATOR BUOY RELEASE MECHANISM GENERIC INERTIAL NAVIGATION GROUP INSTRUMENTS & SAFETY SYS (PIELSTIC ENG) INSULATION, PAINT, DECK & HULL COVERINGS INTERIOR COMMUNICATIONS & ALARM INTERIOR COMMUNICATIONS & ALARM SIGNAL INTERNAL COMMUNICATION SYSTEM (SHINCOM) INTERROGATOR-TRANSPONDER SET LADDER, ACCOMMODATION, ARTICULATED LADDERS & GRATINGS LADDERS, BOOMS AND STAFFS LADDERS, GANGWAYS, RAILS, STAFFS & GRATI LAUNCHING SYSTEM LAUNDRY EQUIPMENT GROUP LIFE SAVING EQUIPMENT LIFTING & LOAD HANDLING LINK 16 LOBBYS AND PASSAGEWAYS (GENERIC) LOCKER (DAMAGE CONTROL) LONG RANGE SURVEILLANCE RADAR SYSTEM LONGITUDINAL STRUCTURAL BULKHEADS LP BLOW & VENTILATION EXHAUST SYSTEM LP COMPRESSED AIR SYSTEM LUBE OIL PURIFIER LUBE OIL SYSTEM MACHINERY CONTROL CONSOLE MACHINERY SPACE VENTILTN/SNORT INDUC SYS MACHINERY SPACES, MARINE SYSTEMS MAIN GEAR TRANSMISSION ASSEMBLY MAIN ENGINE, GEARING & SHAFTING SYSTEM MAIN GUN SYSTEM, 57 MM MAIN GUN SYSTEM, 57 MM, MK III MAIN HYD POWER PLANT ANCILLARY EQUIPMENT MAIN HYDRAULIC SYSTEM MAIN LUBRICATING OIL SYSTEM MAIN NON-STRUCTURAL TANKS MAIN PROPULSION EQUIPMENT MAIN PROPULSION MOTOR COOLING MAIN PROPULSION SYSTEM (GENERIC) MAIN REFRIGERATION SYSTEM MAIN SEAWATER CIRCULATING SYSTEM MAIN SHAFTING SYSTEM (GENERIC) MAIN STRUCTURE GENERAL MARINE ENGINEERING AUX EQUIP GROUP (GEN) MARINE ENGINEERING AUXILIARY EQUIP GROUP MARINE SANITATION DEVICE MARINE SYSTEMS MASTS (GENERIC)	REPLENISHMENT-AT-SEA EQUIPMENT GROUP REPLENISHMENT AT SEA EQUIPMENT RETRACTABLE POST REVERSE OSMOSIS PLANT REVERSE OSMOSIS UNIT, SKID MOUNTED RIGGING & CANVASS SACRIFICIAL ANODES SALT WATER SANITARY SYSTEM SANITARY SYSTEM SATELLITE COMMUNICATION GROUP SATELLITE TELEVISION SYSTEM SCUPPERS & DRAINS SEA WATER SYSTEM SEARCHLIGHT, 2.5 KW XENON SEARCHLIGHT, SIGNALLING TYPE SEASEARCH SYSTEM SEAWATER CIRC PUMP SYS, SEAWATER CIRCULATING SYSTEM SEAWATER SERVICE SYSTEM, FIREMAIN SEPARATOR, OILY WATER, HYDROMEM SERVICE STEAM & DRAIN SYSTEM SHELL PLATING (GENERIC) SHELL, HULL (GENERIC) SHINCOM 2128 SWITCH SYSTEM (DUAL CENTRAL SHIP'S SERV 120V 60 HZ LTG & PWR DIST SY SHIPBOARD ELECTRIC CLOCK SYSTEM SHIPBOARD ELECTRO-OPTIC SURVEILLANCE SYS SHIPBOARD INTEGRATED NAVIGATION/DISPLAY SHIPBOARD LAN (SHIPLAN) SHIPBOARD LAN (SHIPLAN) (GENERIC) SHIPS FRESH WATER COOLING SYSTEM SHIPS LOG OUTFIT SSL AGILOG SHIPS SEAWATER COOLING SYSTEM SHORE CONNECTION BOXES SHORE SUPPLY EQUIPMENT GROUP SICK BAY EQUIPMENT GROUP SIRIUS - LONG RANGE SEARCH/TRACK SYSTEM SLIDING TROLLEY BLOCK ASSEMBLY SLOW SPEED PROPULSION SNORT INDUCTION MAST SONAR SONAR 2041 SONAR 2071 ADA SUB ACOUSTIC AUGMENTOR SONAR DOME ASSEMBLY, 163 INCH DOME SONAR HULL OUTFIT C5 SYSTEM SONAR SET 2007AE SONAR SET 2040AA SONOBUOY PROCESSING SYSTEM SOUND PROOF CASING (PIELSTICK ENGINE) SPEED LOG DOPPLER SONAR SYSTEM SSE SYSTEM AFT MK 9 SSE SYSTEM FWD MK 9 STABILIZED HORIZON REF SYS, AN/SJN-5-501 STEAM GENERATOR STEERING GEAR AND CONTROL SYSTEMS STOWAGE-HANDLING TOWED ARRAY OK-410 (V)1

Green (3)

BOUYANT WIRE AERIAL SYSTEM
 BUILT-IN BREATHING SYSTEM
 BULKHEADS
 BUS ACCESS MODULE LOOPS
 CAMERA SET, TELEVISION, AN/WXY-501
 CANSOT SHF SATCOM
 CAPSTAN AFTER (MOORING TOWING ASSEMBLY)
 CAPSTAN SYSTEM, AFT
 CAPSTAN WINDLASS ASSY
 CAPSTAN, WINDLASS SYSTEM
 CASUALTY POWER SYSTEM (GENERIC)
 CATHODIC PROTECTION SYSTEM (GENERIC)
 CDN REC AND ASST SEC & TRAV SYSTEM
 CENTERING SYSTEM
 CHILLED WATER SYSTEM
 CHILLER SET, 85 TON
 CIWS MK 15 MOD 21 BLOCK 1B
 CLOSE-IN WEAPON SYSTEM BLOCK 1B
 CLOSE IN WEAPON SYSTEM MK15 MOD 21 BLOCK
 CLOSED CIRCUIT TELEVISION SURVEILLANCE
 CLOSURES, WATERTIGHT/GASTIGHT/OILTIGHT
 COLD FRESH WATER SYSTEM
 COMBAT SYSTEMS
 COMMAND & CONTROL EQUIPMENT GROUP
 COMMAND AND COMBAT SYSTEM EQUIP SPACES
 COMMAND AND COMBAT SYSTEM EQUIPMENT SPAC
 COMMAND AND CONTROL MISC EQUIP GROUP
 COMMUNICATION SET, SONAR, AN/WQC-501(V)
 COMMUNICATIONS CONTROL & MONITORING SYS
 COMMUNICATIONS GROUP (EXTERNAL)
 COMMUNICATIONS GROUP, EXTERNAL
 COMMUNICATIONS SYSTEM, AN/SSC-510
 COMPRESSED AIR SYSTEM, HIGH PRESSURE
 COMPRESSED AIR SYSTEM, HP (GENERIC)
 COMPRESSOR ASSEMBLY TYPE 5436N
 COMPRESSOR UNIT, RECIPROCATING
 COMPRESSOR UNIT, RECIPROCATING (HP AIR)
 COMPRESSOR UNIT, ROTARY (LP AIR)
 CONTINUOUS WAVE ILLUMINATOR SYSTEM
 CONTROLLABLE PITCH PROPELLERS AND PROPEL
 COOLER, FLUID, INDUSTRIAL, OA-5181/SP
 COUNTERMEASURES SET, AN/SLQ-502
 COUNTERMEASURES SET, AN/SLQ-502A
 COUNTERMEASURES SET, AN/SLQ-503
 CROSS CONNECT GEARING AND PLATFORM
 CRUISE ENG ENCL COOLING AIR INTKE & EXHS
 DAMAGE CONTROL SYSTEM
 DATA / VIDEO / AUDIO COLLECTION
 DATA LINK PROCESSING SYSTEM (DLPS)
 DATA TERMINAL SET, P/O AN/USQ-125(V)
 DAVIT, BOAT BOOM, RIGID INFLATABLE BOAT
 DE-ICING SYSTEM
 DECK & HULL EQUIPMENT GROUP
 DECK AND HULL FITTINGS
 DECK COVERING TREADMATS TREADSTRIPS ETC
 DECK CRANE ASSEMBLY
 DECK CRANE GENERAL PURPOSE (HIAB 61)
 DECK, THREE (GENERIC)
 DECK, TWO (GENERIC)

FLIGHT DECK LIGHTING SYSTEM (GENERIC)
 FLT DECK CCTV
 FOAM SYSTEM, AQUEOUS FILM FORMING
 FORWARD MOORING/TOWING WINDLASS
 FOUNDATIONS/SEATINGS (GENERIC)
 FRESH WATER SYSTEM
 FUEL FILLING AND COMPENSATING SYSTEM
 FUEL OIL CENTRIFUGE
 FUEL OIL FILLING & TRANSFER SYSTEM
 FUEL OIL SERVICE SYSTEM
 FUEL SYSTEM (PIELSTICK ENGINE)
 FWD/AFT CAPSTAN & EQUIPMENT
 FWSS SUPPRESSION SYSTEM
 GALLEY & SERVERY EQUIPMENT GROUP
 GARBAGE EJECTOR ASSEMBLY
 GENERATOR AC
 GENERATOR GROUP, 750 KW
 GENERATOR TEST, TERMINAL BOXES
 GENERATOR, AC (850 KW)
 GLOBAL COMMAND AND CONTROL SYS MARITME
 GOVERNOR (PIELSTICK ENGINE)
 GUARD RAILS & STANCHIONS
 GUN ASSEMBLY
 HANDLING SYSTEM, TORPEDO
 HANDLING SYSTEM, TORPEDO, SHIPBOARD
 HATCHES, DOORS, MANHOLES
 HEAVY MACHINE GUN SYSTEM, .50 CALIBRE.
 HIGH SPEED DATA CONNECTIVITY (HSDC)
 HMCS ATHABASKAN
 HMCS CHARLOTTETOWN
 HMCS CORNERBROOK
 HMCS FREDERICTON
 HMCS HALIFAX
 HMCS IROQUOIS
 HMCS MONTREAL
 HMCS PRESERVER
 HMCS REGINA
 HMCS ST. JOHN'S
 HMCS TORONTO
 HMCS VANCOUVER
 HMCS VILLE DE QUEBEC
 HORIZON BAR SYSTEM, STABILIZED (GENERIC)
 HP AIR REDUCING STATIONS
 HP AIR SYSTEM
 HP AIR VALVES & FITTINGS
 HP COMPRESSED AIR SYSTEM
 HP DIRECT BLOW SYSTEM
 HPAC ARRANGEMENT
 HPB VALVES
 HULL INSULATION
 HULL NON-PENETRATING MAST
 HULL NON-PENETRATING MASTS
 HULL PENETRATING MASTS, WEAPONS
 HULL STRUCTURE
 HULL STRUCTURE (GENERIC)
 HULL SYSTEMS
 HULL SYSTEMS & FITTINGS
 HULL VALVES
 HVAC SYSTEM
 HYDRAULIC OIL FILLING & TRANSFER SYSTEM

MBT VENTING ARRANGEMENTS
 MESSAGE HANDLING & DISTRIBUTION SYSTEM
 METEOROLOGICAL SYSTEM
 MF/HF ANTENNA SYSTEM AJU
 MOISTURE SEPARATOR SYSTEM
 MOTOR PROPULSION
 MOTOR, ELECTRIC, 60/30 H.P.
 NAVAL AEHF SYSTEM
 NAVAL EXTERNAL COMMUNICATIONS SYSTEM
 NAVAL FIREFIGHTING HOSES, NOZZLES
 NAVAL INFORMATION SYSTEMS (NAVIS)
 NAVAL INFORMATION SYSTEMS (NAVIS).
 NAVIGATION DISTRIBUTION SYSTEM
 NAVIGATION SET,TACAN (AN/URN-25)
 NAVIGATION SYSTEM EQUIPMENT GROUP
 NAVIGATION SYSTEM GROUP
 NAVIGATION SYSTEM, RING LASER GYRO NAVIG
 NAVIGATION SYSTEMS GROUP
 NAVIGATIONAL LIGHTING
 NERA SATURN BM MARINE MK2 INMARSAT
 NON-STRUCTURAL BULKHEADS & CLOSURES
 Not assigned
 NULKA ACTIVE MISSILE DECOY SYSTEM
 OFFICE SPACES (GENERIC)
 OIL POLLUTION ABATEMENT AND BILGE STRIP
 Other Location
 PADEYE INSTALLATION
 PLASTIC WASTE PROCESSOR
 PORTLIGHTS & WINDOWS
 POWER SYSTEM, AFTER CAPSTAN
 PRIMARY AIR CONDITIONING PLANTS NO.1 & 2
 PRIMARY ELEC POWER GENERATION & DIST SYS
 PRIMARY SWITCH GEAR (GENERIC)
 PRIMING SYSTEM
 PROPULSION SYSTEM, MAIN
 PUBLIC ADDRESS SET, AN/UIC-502
 PUMP SYSTEM (MAIN LUBE OIL)
 PUMP UNIT, CENTRIFUGAL (COLD FRESH WTR)
 PUMP UNIT, CENTRIFUGAL (DIES FIRE PUMP)
 PUMP UNIT, CENTRIFUGAL (FIRE PUMP).
 PUMP UNIT, CENTRIFUGAL (JOCKEY, FIRE)
 PUMP UNIT, F-401 (DFO)
 RADAR SET AN/SPG-503
 RADAR SET GROUP (LTWT RDR-ASSOP DIR SYS)
 RADAR SET, AN/SPG-501
 RADAR SET, AN/SPS-49A(V)5
 RADAR SET, AN/SPS-502
 RADAR SET, AN/SPS-505
 RADAR SET, AN/SPS-506
 RADAR SET, NAVIGATION, KH 1007
 RADIO SET, AN/SRC-513
 RADIO SET, AN/SRC-515
 RADIO SET, HF AN/URC-507
 RADIO SET, MARINE, GMDSS DSC CLASS D VHF
 RAILS, STANCHIONS & LIFELINES
 RAPID SECURING DEVICE
 RATIONALISED INTERNAL COMMUNICATIONS
 RECEIVER, RADIO, R-5095B/G.
 REFRIGERATION SYSTEM FOOD
 REPLENISHMENT-AT-SEA DECK MACHINERY

STRUCTURAL BULKHEADS (GENERIC)
 STRUCTURAL TANKS & ENCLOSURES
 SUB ESCAPE & RESCUE, LIFE SAVING SUPPORT
 SUBMARINE CONTROL CONSOLE
 SUBMARINE ESCAPE EQUIPMENT
 SUBMARINE PRESSURE HULL
 SUBMERGED SIGNAL EJECTOR MK9 SYSTEMS SSE
 SUPERCHARGING (PIELSTICK ENGINE)
 SUPERSTRUCTURE
 SUPPLY TO MAIN MOTOR AIR COOLERS
 SURFACE & AIR WEAPONS SYSTEM
 SWITCHBOARD PROPULSION
 SWITCHBOARD, MAIN & ASSOCIATED EQUIPMENT
 SWITCHBOARDS, FORWARD & AFTER
 SYS, 24V DC DISTRIBUTION
 SYSTEM VALVES AND FITTINGS
 SYSTEM, ATTACK PERISCOPE
 SYSTEM, SEARCH PERISCOPE
 TEMP EC - COMMAND & CONTROL EQUIPMENT
 TEMP EC - COMMUNICATIONS GROUP
 TEMP EC - COMMUNICATIONS GROUP, EXTERNAL
 TEMP EC - HULL SYSTEMS
 TEMP EC - NAVAL EXTERNAL COMMUNICATIONS
 TEMP EC - NAVAL INFORMATION SYSTEM NAVIS
 TEMP EC - UNDERWATER COMBAT SYSTEM
 TORPEDO HANDLING & STOWAGE SYSTEM
 TORPEDO LAUNCHING SYSTEM
 TORPEDO SETTING PANEL SYSTEM
 TORPEDO TUBE ASSEMBLY, MK 32, MOD 9
 TOWED ARRAY SYSTEMS
 TOWED ARRAY, SHIPBOARD SESS2-1
 TOWER ESCAPE ONE MAN FWD & AFT (STRUCT)
 TPS-250 PORTABLE VHF/AM TRANSCIEVER SYS
 TRANSMITTER GROUP MK 73 MOD 3
 TRANSMITTING SET, COUNTERMEASURES
 TRANSMITTING SET, RADIO AN/SRT-504
 TRIM SYSTEM
 TRIM SYSTEM VALVES
 TRIM, BILGE, BALLAST PRIMING SYSTEMS
 TURBINE, STEAM(FOR 1000 KW TURBINE GNRT)
 UNDERWATER COMBAT SYSTEM
 UNDERWATER DETECTION SYSTEM
 VALVES & FITTINGS NITROGEN CHARGING SYST
 VENT OVERFLOW AND SOUNDING SYSTEM
 VENTILATION SYSTEM
 VERTICAL CAPSTAN - LINE HANDLING WINCH
 VERTICAL STORES CONVEYOR
 VHF/UHF AM/FM RADIO SYSTEM AN/PRC-117F
 VPDC DISTRIBUTION
 WASHPLACES AND SHOWERS
 WATER CIRCUIT (PIELSTICK ENGINE)
 WATER PURIFICATION UNIT SKID MOUNTED
 WEAPONS DISCHARGE SYSTEMS (WDS)
 WEAPONS GROUP MK 16 MOD 3
 WEATHER DECK ARRANGEMENTS
 WEATHER DECK STOWAGES & LOCKERS
 WINCH, LINE HANDLING
 WIPER ASSEMBLY,WINDOW

BOAT, RIGID INFLATABLE, ALUMINUM HULL
 BOAT, RIGID, INFLATABLE, 24FT.
 COOLER UNITS, AIR (KU 3000) (GENERIC)
 COOLER UNITS, AIR (TYPE KU) (GENERIC)
 DETECTOR, WIND DIRECTION AND SPEED

DRIER, AIR-GAS, DESICCANT, HD-5029/SRC
 FAN COIL UNITS (GENERIC)
 FAN SYSTEM, VANEAXIAL, SF-10 & SF-11
 FUEL OIL CENTRIFUGE ASSEMBLY
 RADAR SET

SUBMARINE INDICATOR BUOY (SARSAT)
 WHISTLE SYSTEM, ELECTRIC (PORT & STBD)

AIR START SYSTEM
 ANTENNA AS-5171/SRC
 ANTENNA GROUP OE-5035/SR
 BATHYTHERMOGRAPH SYSTEM, AN/WQQ-502 (V)
 BEACON, RADIO, EMERGENCY POSITION INDICA

Purple (4)

ACCOMODATION SPACES AIR CONTROL SYSTEM (LOW PRESSURE) ANTENNA COUPLER GROUP BOILER, HIGH PRESSURE, AUXILIARY BOILER, MAIN STEAM, HP BREATHING APPARATUS, OXYGEN GENERATING, BRIDGE FIN, CASING & EXTERNAL STRUCTURES CENTRAL SURVEILLANCE SYSTEM COMPUTER SYSTEM, INTEGRATED SHIPBOARD CONTROL, SERVO CONTROLLABLE PITCH PROP DAMAGE CONTROL MONITORING & ALARM SYS DECK, ONE (GENERIC) ELECTRICAL PROPULSION MACHINERY ELECTRONIC STEERING CONTROL SYSTEM ENGINE DIESEL, (850 KW GENERATOR SET) ENGINE, DIESEL ENGINE, GAS TURBINE, MAIN AND CRUISE ENGINE, GAS TURBINE, MODEL 570 KF EVAPORATION & DISTILLATION PLANT FUTURE EXPANSION GALLEYS, SERVERYS AND DINING AREAS	GALLEYS, SERVERYS AND DINING AREAS (GEN) GENERATOR SET, DIESEL ENGINE (1000 KW) GUN MOUNT, SUPER RAPID, 76/62 MILLIMETRE GYRO COMPASS SYSTEM HALON FIRE SUPPRESSION SYSTEM HELICOPTER HAULDOWN SYSTEM HMCS ALGONQUIN HMCS CALGARY HMCS CHICOUTIMI HMCS OTTAWA HMCS PROTECTEUR HMCS WINDSOR HMCS WINNIPEG HULL INTEGRATED PLATFORM MANAGEMENT SYSTEM LAUNCHER SYSTEM GUIDED MISSILE VERTICAL LAUNCHING SYSTEM, GUIDED MISSILE LIGHTING GENERAL LM2500 GAS TURBINE ASSEMBLY LOBBIES AND PASSAGEWAYS LOCKERS, AMMUNITIONS	LUBE OIL SYSTEM (PIELSTICK ENGINE) MAIN BATTERY SYSTEM MASS (MULTI-AMMUNITION SOFTKILL SYSTEM) MEDIUM RANGE RADAR, AN/SPQ-501 MINOR STRUCTURE (GENERIC) MODEM COMMUNICATIONS MD-5077(V)3/U NAVIGATION SYSTEMS EQUIPMENT GROUP PASSIVE RANGING SONAR RADIO SET, AN/SRC-514 RADIO SET, AN/SRC-516 RADIO SET, TACAN, AN/URN-20A(V) RECEIVING SET, RADIO AN/SRR-505 RECOVERY ASSIST SECURE TRAVERSE SYSTEM (REPLENISHMENT-AT-SEA SYSTEMS SCBA SYSTEM SCUTTLES, WINDOWS & ASSOCIATED EQUIPT SECONDARY ELEC POWER GENERTN & DIST SYS SECURE LAN (SECLAN) SHAFT AND PROPELLER SHINCOM 3100 SHIP ARRANGEMENTS	SHIPS FURNITURE, NON-STANDARD SOLID WASTE SYSTEM SONAR TYPE 2008 UWT, VARIANT NG STOWAGE & HANDLING SPACE, AMMUNITION STOWAGES AND LOCKERS SUBMARINE FIRE CONTROL SYSTEM (SFCS) SUBMARINES, HMCS VICTORIA SUPERSTRUCTURE (GENERIC) TEMP EC - AIRCRAFT SUPPORT EQUIPMENT TEMP EC - DECK & HULL EQUIPMENT GROUP THERMAL INSULATION & ACOUSTIC DAMPING (V TORPEDO WARSHOT, MK48, MOD 4 TOWED ARRAY GROUP, SONAR, 0A-9056 (V)2 TUBE CONTROL & INDICATOR TURBINE, GAS UNDERWATER DETECTION EQUIPMENT UNDERWATER WEAPONS EQUIPMENT GROUP VERTICAL LAUNCHING SYSTEM, MK 41 MOD C WATER CHILLER UNIT, 125 TON CAPACITY WEAPONS HANDLING SYSTEM (WHS)
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4 Hidden Markov Models for Monthly Order Key Completions

The FMF creates task assignments based on unique order keys. Each order key can have subtasks and the FMF records an order key as complete once all its subtasks are finished. The elapsed time does not reflect the actual work hours committed to the task. Order keys have priority rankings during maintenance activities which can result in a long order key lifetime even though the task may require only a small amount of time to complete. An order key appears complete in the system only once the FMF closes the ticket—the actual work may finish well before the close date, depending on the filing practice of the FMF. Thus, order key completion records depend on the actual time need to complete the task(s), the priority of the work, and the business close out procedure. The lifetime of an order key does not simply reflect the required work effort.

The client needs an understanding of patterns in the order key completions by vessel and by FMF. The data contain 43,731 uncensored order key completions on Royal Canadian Navy (RCN)’s vessels (see Table 5) with start dates ranging from 14 November 2003 to 6 July 2016. The dataset contains work from both the Cape Scott and Cape Breton fleet maintenance facilities. From the raw data, I count the number of order key completions per month at each FMF. Figures 15 and 16 shows the monthly completed time series data. Notice that Figure 15 shows a downward, approximately linear, trend while Figure 16 does not. In Figures 17 and 18 we see the evidence of autocorrelation with a one month time lag—shocks to the system have a memory of one month.⁵ Approximating the job count data as continuous leads to an autoregressive time series model [6] with one lag (an Autoregressive (AR)(1) model). While in principle the AR(1) models provide a predictive framework for monthly job completions at each FMF, the downward linear trend in the Cape Scott data will eventually end. The nature of the stochastic process may change at the inflection point. If the FMF planners are confident that the trend will continue, the time series model can help predict the monthly job completions. Interpretation remains a difficult problem.

At the individual ship level, we can no longer ignore the discrete nature of the order key completion counts. Simple continuous time series modelling will not work with the count data. To account for the autocorrelation in the data while respecting the discreteness of the

⁵I computed the Cape Scott Autocorrelation function (ACF) by using the residuals after removing the linear trend. The ACF shows some evidence of autocorrelation at 12, 16, and 19 month lags but in building time series models the AIC prefers a one lag model.

count data, I model each ship as a Poisson HMM [7]. Examination of the AIC and pseudo-residuals, shown in Figures 19 and 20, points to a five hidden Poisson rates associated with each ship. The pseudo-residuals concord with their theoretical quantiles while exhibiting no autocorrelation. The five dimensional rate vectors point in the positive orthant above the 45-degree hyperplane (the rate vectors form order tuples). K-means clustering (see [1] for details) of the rate vectors find three clusters and Figure 21 shows the best two dimensional representation (based on rank reduced linear discriminant analysis, see [1] for details) of the five dimensional clusters. We see that the HMM finds the coast to which each vessel belongs. Each FMF completes order keys differently but the HMCS Victoria sits alone in her own cluster. Given the teething problems with the Victoria Class, it is not surprising that one of the RCN's submarines has an entirely different work flow pattern compared to the rest of the RCN's vessels. Figure 22 shows the monthly completion job counts for each ship with cluster colour and rate membership indicated.

The time series analysis demonstrates that the maintenance system has memory and that each FMF faces different challenges. Interpretation remains problematic—we do not know the reason for the coastal differences in order key completion rates. Order key completion records occur on the date at which the FMF closes a ticket. It might be the case that each FMF closes tickets based on different policies. It might also be the case that each FMF faces different challenges associated with each vessel or with its workforce. Given the downward trend in Figure 15 relative to Figure 16, there are differences between the two facilities. The time series analysis shows that we can identify each FMF by observing historical work patterns at the individual vessel level.

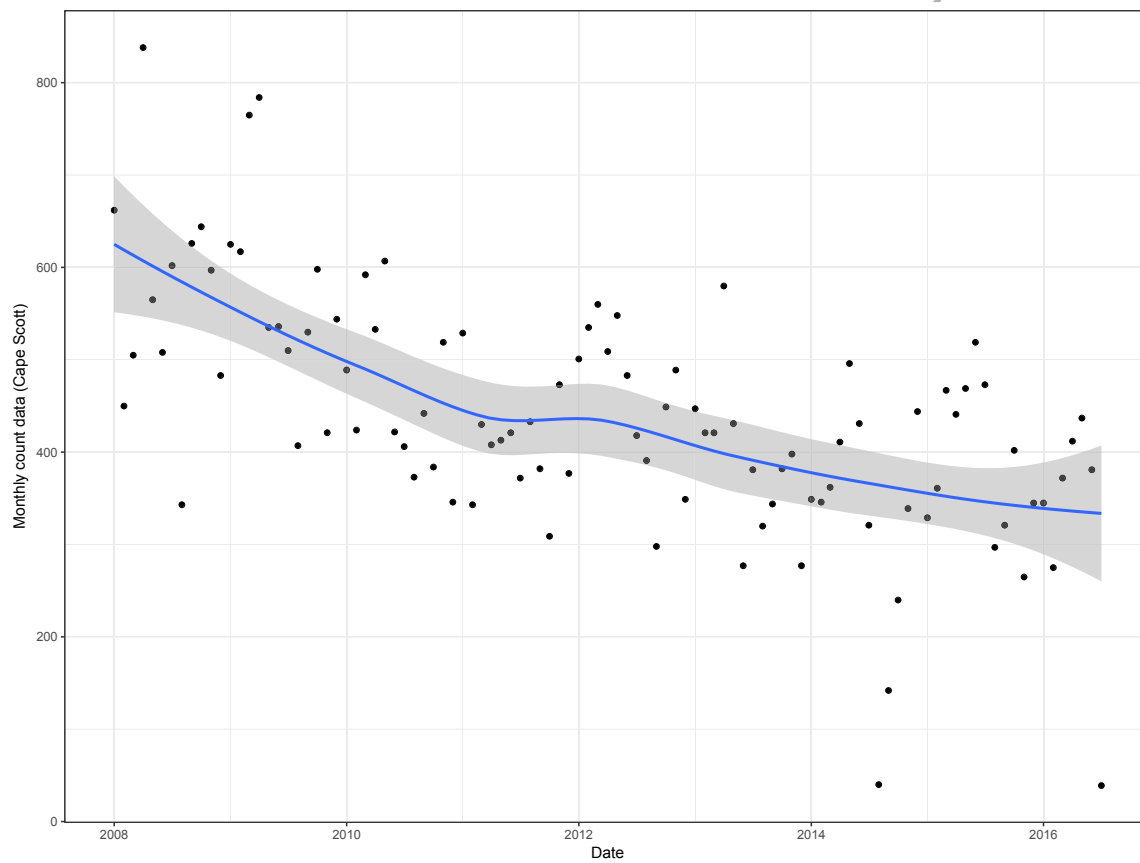


Figure 15: Cape Scott monthly completion time series with smoothing spline and error bar. Notice the presence of an approximately linear trend.

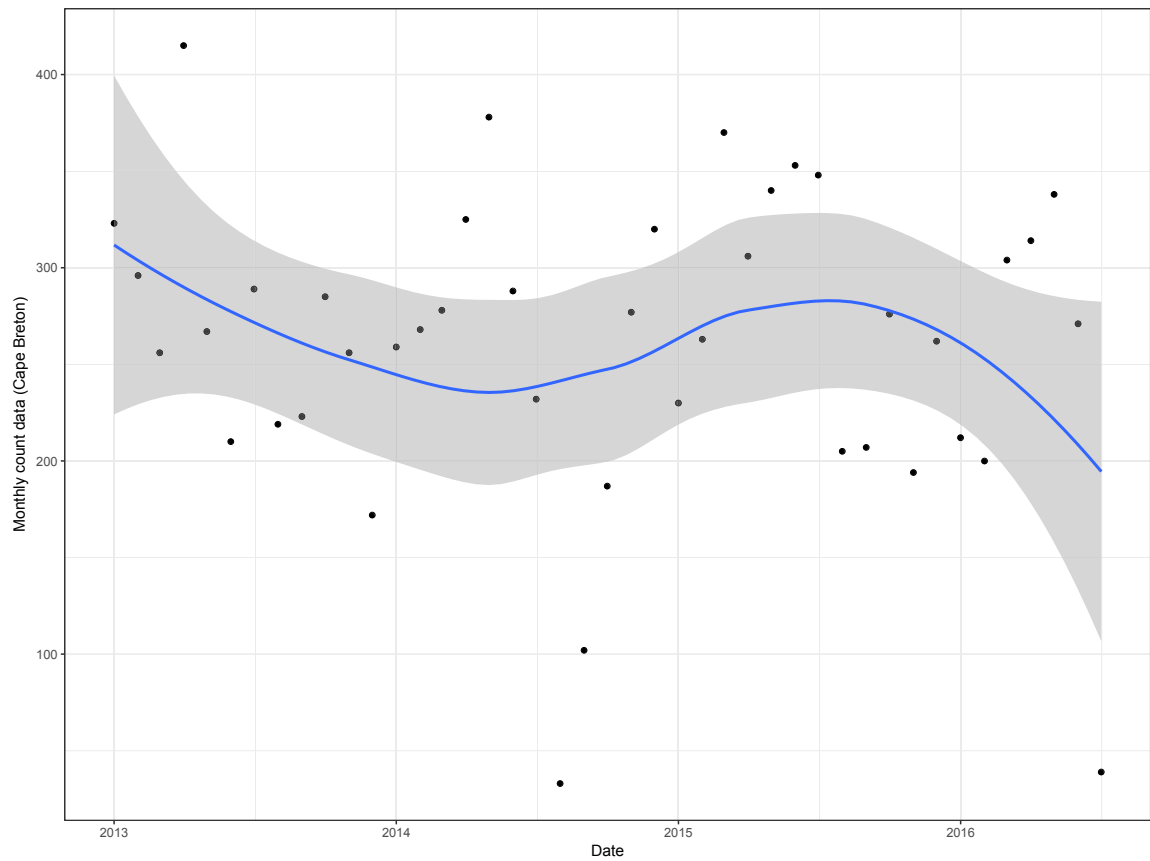


Figure 16: Cape Breton monthly completion time series with smoothing spline and error bar. Notice the absence of any trend.

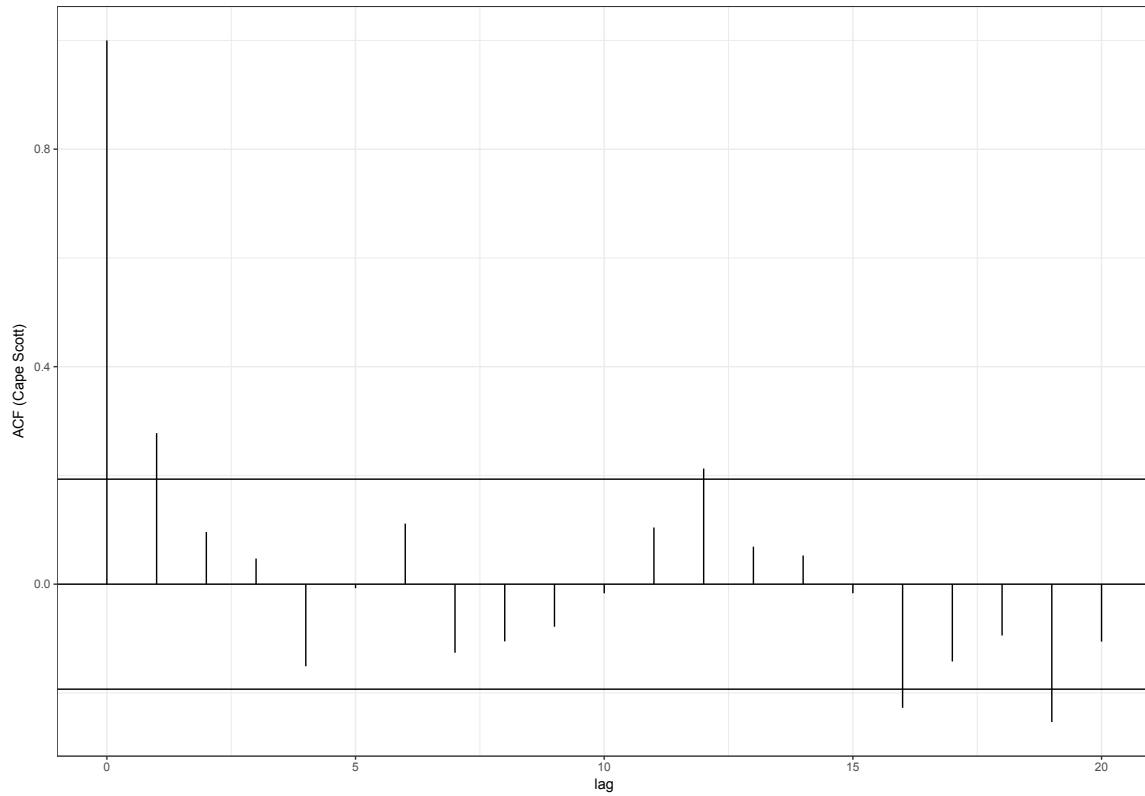


Figure 17: Cape Scott autocorrelation of monthly completions. The horizontal lines indicate the 95% confidence limits.

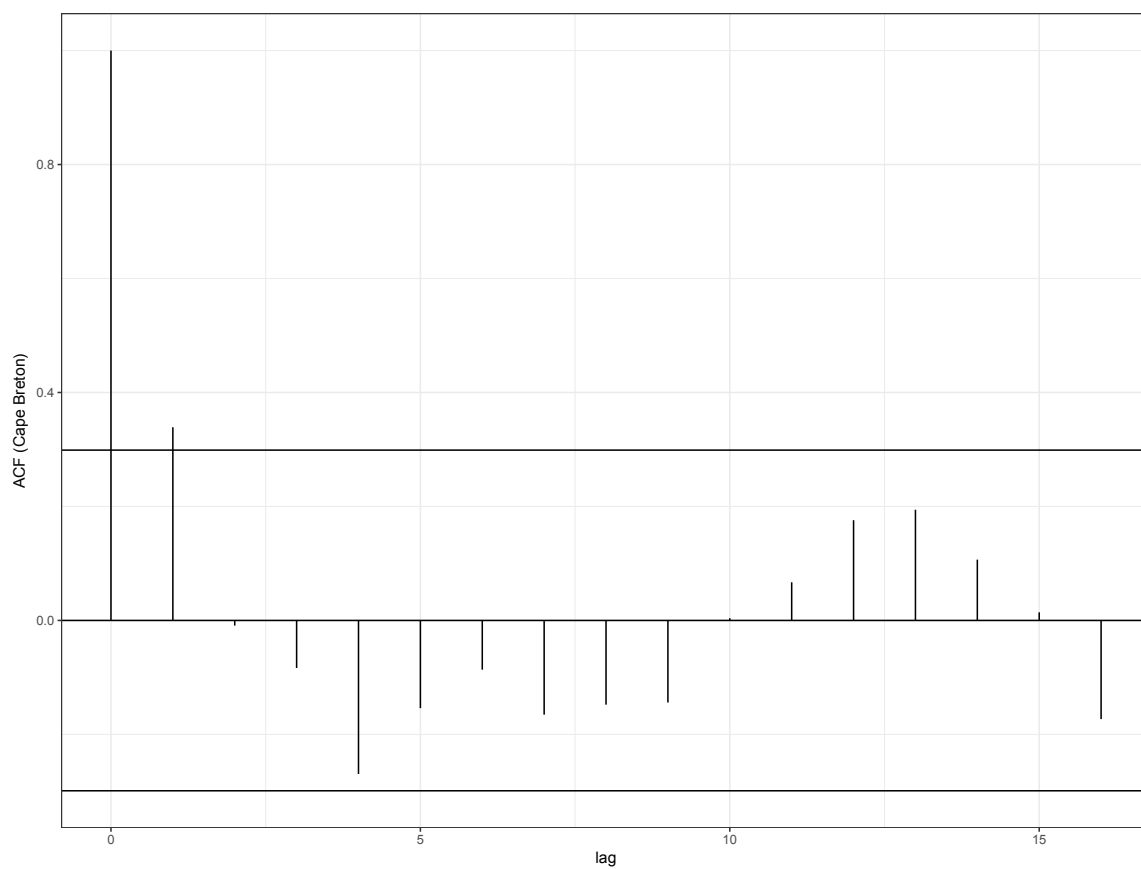


Figure 18: Cape Breton autocorrelation of monthly completions. The horizontal lines indicate the 95% confidence limits.

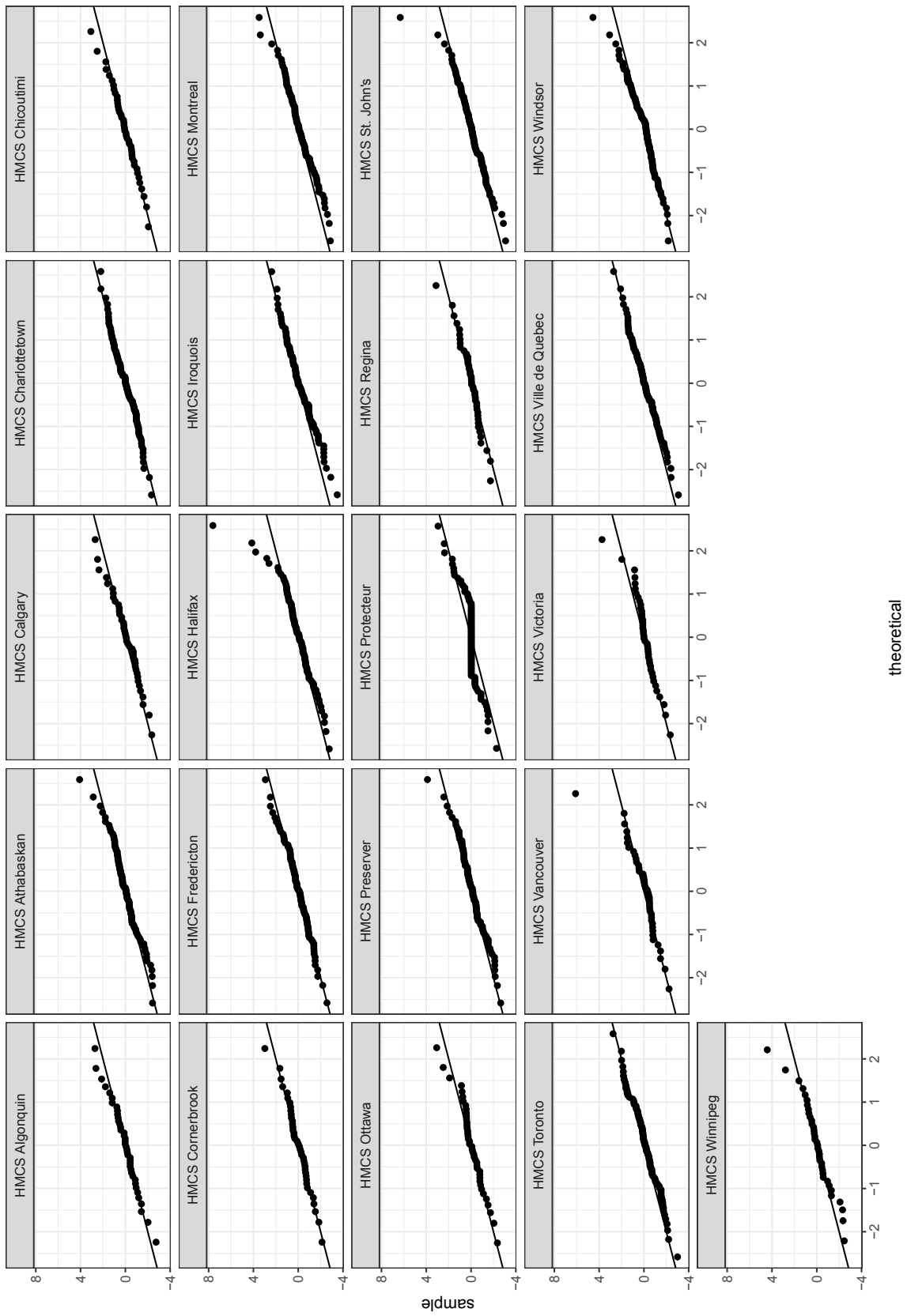


Figure 19: Pseudo-residual quantile analysis of the HMM estimation with 5 hidden states.

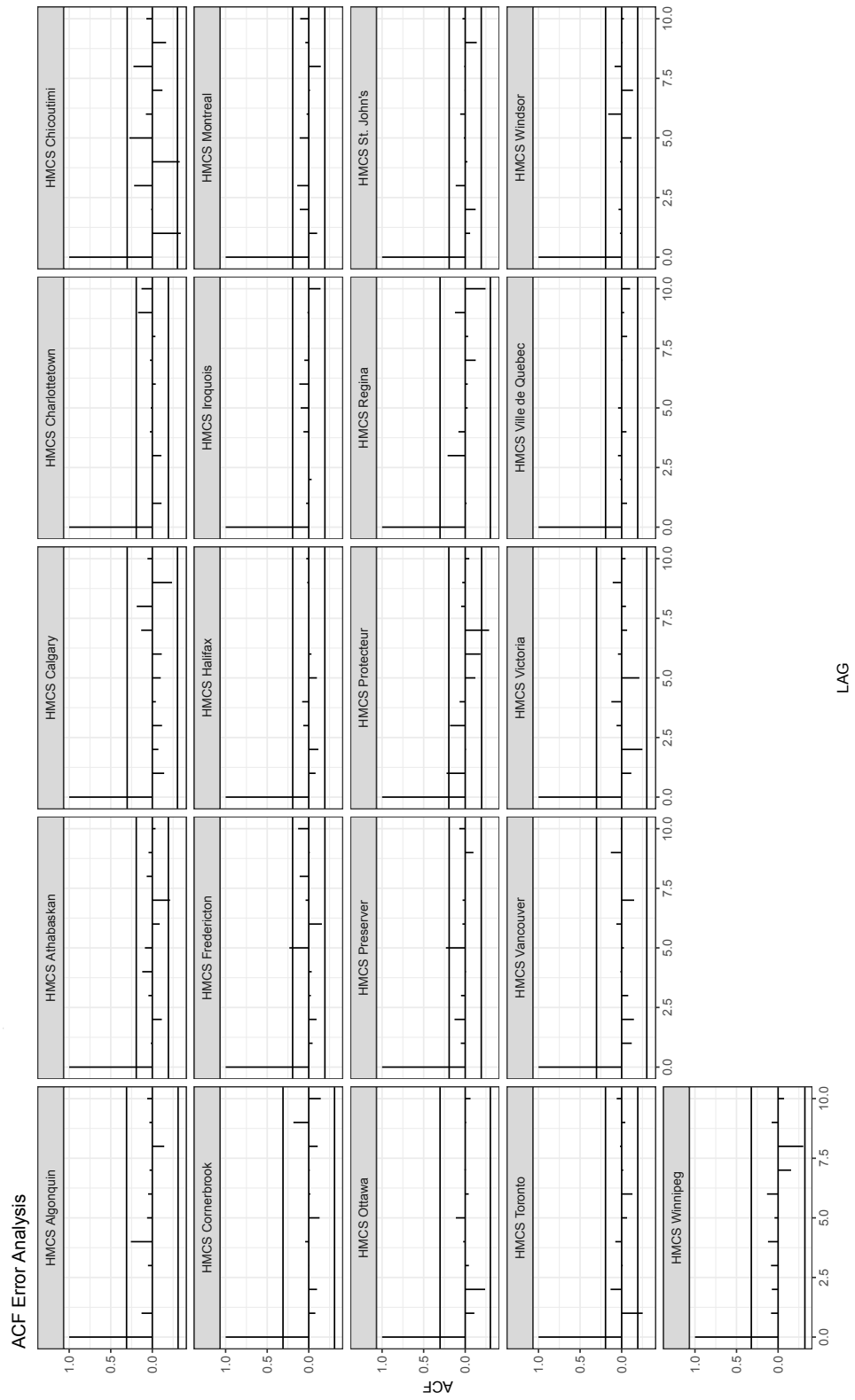


Figure 20: Pseudo-residual autocorrelation analysis of the HMM estimation with 5 hidden states.
No evidence of serial correlation in the pseudo-residuals.

Rate Clustering of 5-State Poisson Hidden Markov Model for Monthly Order Key Completions
Rank Reduced Linear Discriminant Analysis

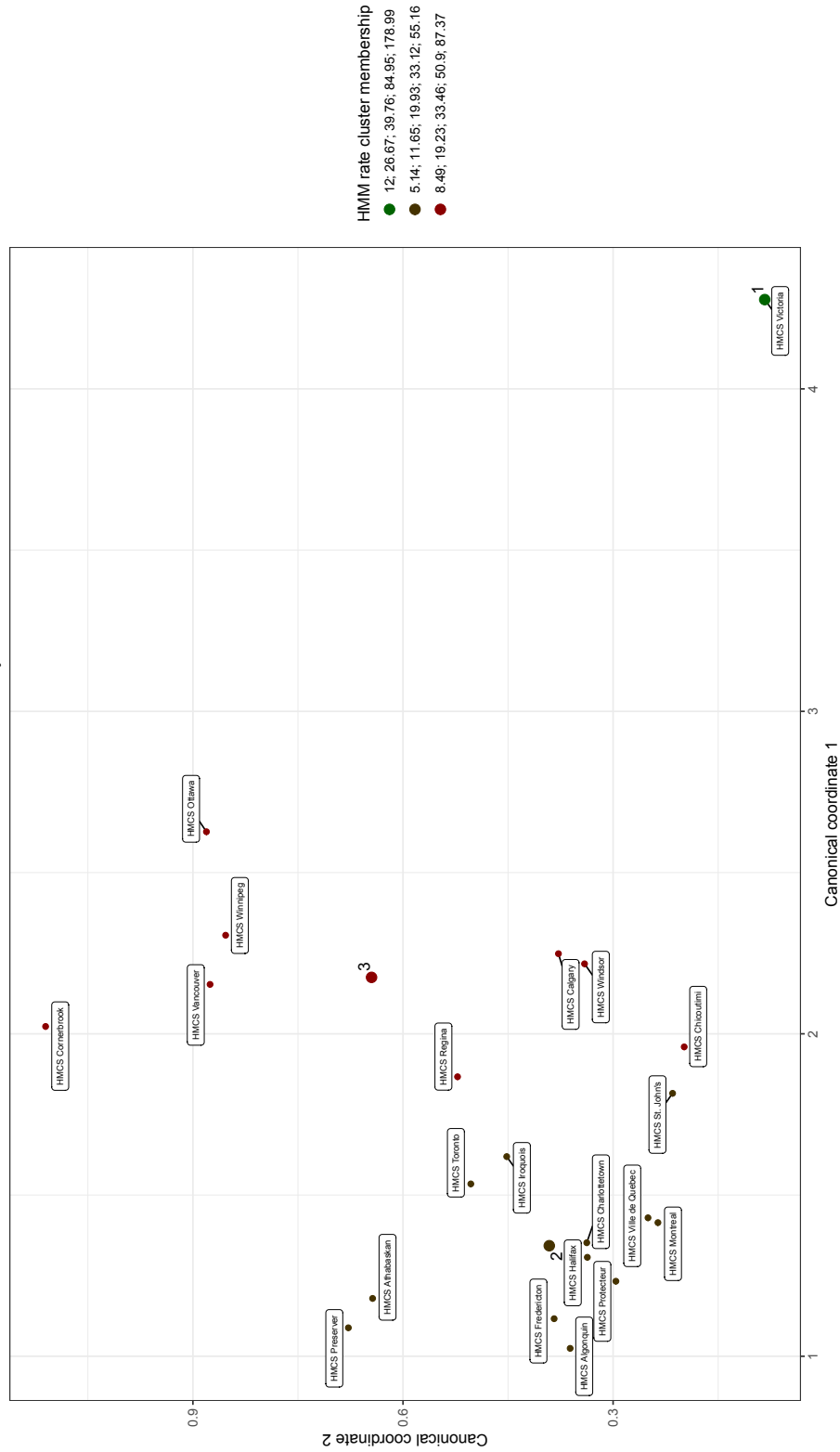


Figure 21: Clustering of the five dimensional rate vectors projected into the best two dimension plane by rank reduction. Cluster center rates are given in the legend.

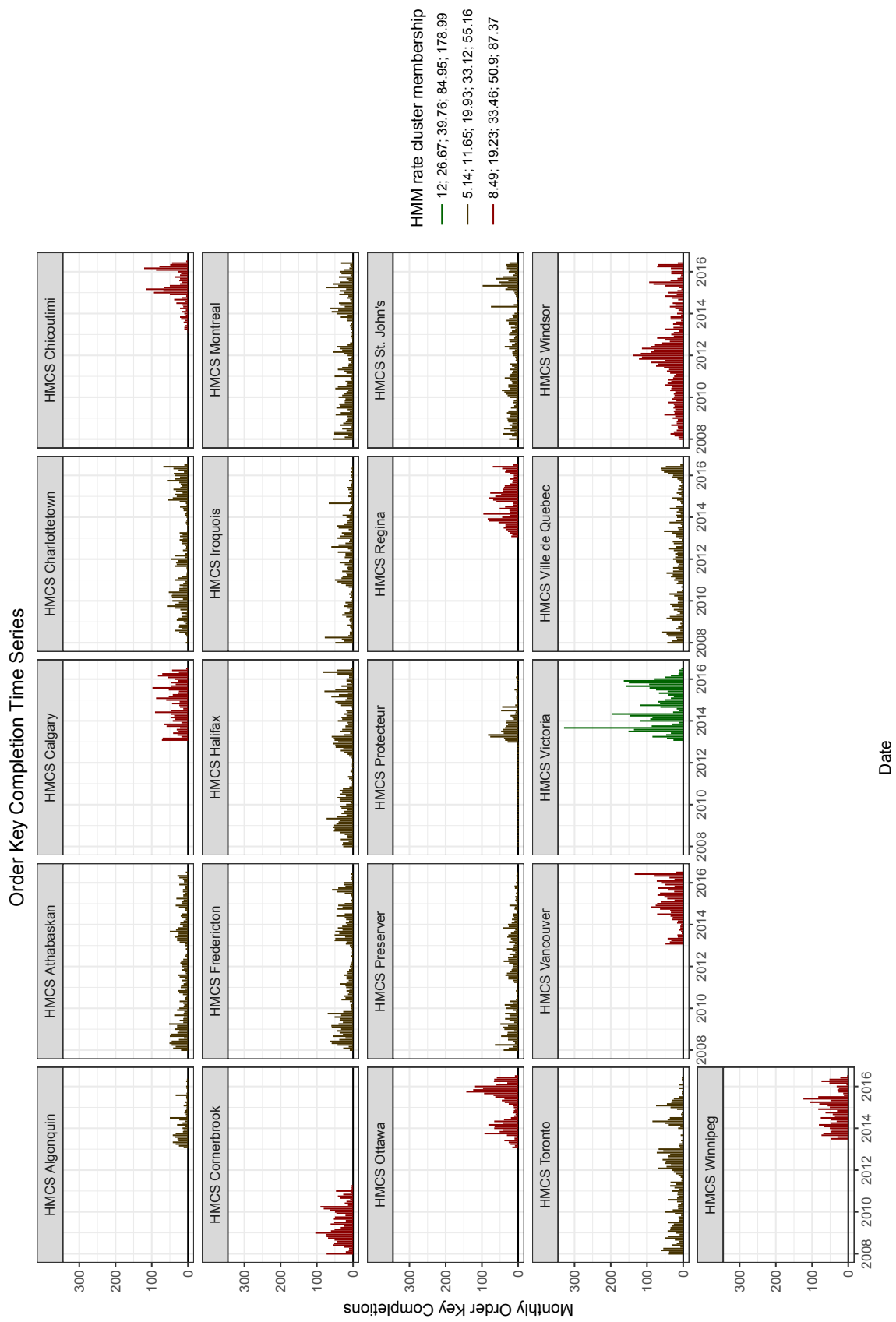


Figure 22: Time series counts by vessel with clustering.

5 Discussion

The regression tree provides the client with a predictive model. Given a task with covariate features, the model assigns the task to a terminal node. Using the quantile information within each terminal node, the planner can better understand the risk of schedule creep. The planner can also use the model to validate technician built schedules by comparing planned hours to the terminal node quantiles (e.g., in a 100 job task schedule, roughly 5 tasks should have planning time estimates that exceed the 95% quantile.)

The client can easily incorporate this tree model as an R script in the RCN's SAP Business Object framework. The full implementation to date includes three trees based on three different feature clustering assignments and all the trees can be used together to predict actual hour quantiles through a convex sum. The regression analysis places work centers at the top of the feature importance list.

The time series analysis demonstrates that the maintenance system has memory and that each FMF faces different challenges. Interpretation remains problematic—we do not know the reason for the coastal differences in order key completion rates. Order key completion records occur on the date at which the FMF closes a ticket. It might be the case that each FMF closes tickets based on different policies. It might also be the case that each FMF faces different challenges associated with each vessel or with its workforce. Given the downward trend in the Cape Scott monthly completion data relative to Cape Breton, there are differences between the two facilities. The time series analysis shows that we can identify each FMF by observing historical work patterns at the individual vessel level through an HMM construction.

This paper shows the RCN the power that data science can bring to operational data. The RCN is uniquely positioned to take advantage of statistical learning techniques in its new SAP environment. The demonstration of these methods in this paper is more important than any single result displayed. The RCN needs far more than one off results generated by CORA on task request basis. To bear fruit, the RCN requires a dedicated data science team that works in conjunction with SAP data maintainers. We have an enormous opportunity to fully exploit the SAP ERP capability, which will lead to operational treasure in the RCN's datasets. We are at the beginning of a journey of marrying data science and operational defence data, not just within the RCN but across all of DND.

Abbreviations and Acronyms

ACF	Autocorrelation function
AIC	Akaike Information Criteria
AIS	Automatic Identification System
AR	Autoregressive
BEx	Business Explorer
BIC	Bayesian Information Criteria
CART	Classification and Regression Tree
CSV	Comma Separated Variable
CORA	Centre for Operational Research and Analysis
DNSM	Directorate of Naval Strategic Management
DRMIS	Defence Resource Management Information System
DND	Department of National Defence
DRDC	Defence Research and Development Canada
ERP	Enterprise Resource Planning
FMAS	Financial and Managerial Accounting System
FMF	Fleet Maintenance Facility
GBM	Gradient Boosted Model
GMM	Gaussian Mixture Model
HMM	Hidden Markov Model
LAH	Log Actual Hours
MASIS	Materiel Acquisition and Support Information System
OOB	Out-of-bag
RCN	Royal Canadian Navy

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In November 2016, Cdr Timothy Gibel, Directorate of Naval Strategic Management (DNSM) requested the Centre for Operations Research and Analysis's (CORA) assistance with creating a predictive model for actual work hours per task on Royal Canadian Navy (RCN) vessels at the Cape Scott and Cape Breton Fleet Maintenance Facilities (FMF). He also requested help in finding patterns in maintenance task completions at the vessel level. The FMF provided dataset contains information on 132,292 unique tasks separated into 43,731 order keys. Using regression trees with feature engineering for actual work hours, I find that a simple 14 terminal node tree explains 18% of the variance in the data. Gradient boosted stumps explain as much as 25% of the variance, but at the expense of an interpretable structure for schedule validation. Hidden Markov Modelling of monthly order key completion time series data reveals coastal differences between the CN's two maintenance facilities, providing an objective motivation to discover the source.

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En novembre 2016, le cdr Timothy Gibel, de la Direction de la gestion stratégique de la marine (DNSM), a sollicité l'aide du Centre de recherche et d'analyse opérationnelles (CORA) pour créer un modèle prédictif des heures de travail réelles par tâche sur les navires de la Marine royale canadienne (MRC) des installations de maintenance de la flotte au Cap Scott et Cape Breton (FMF). Il a également demandé de l'aide pour trouver des tendances dans l'achèvement des tâches d'entretien au niveau des navires. L'ensemble de données fourni par FMF contient des informations sur 132 292 tâches uniques, séparées en 43 731 clés d'ordre. En utilisant des arbres de régression avec l'ingénierie des caractéristiques pour les heures de travail réelles, je trouve qu'un simple arbre de 14 nœuds terminaux explique 18% de la variance dans les données. Les *Gradient boosting stumps* expliquent jusqu'à 25% de la variance, mais aux dépens d'une structure inter-simulable pour la validation de la cédule. La modélisation de Markov cachée des données des séries chronologiques d'acheminements mensuels des principales commandes révèle les différences côtières entre les deux installations de maintenance de la MRC, fournissant ainsi une motivation objective à la recherche de la source.