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**Premier atelier
canadien sur la
logique floue et
ses applications
dans l'industrie**

Le jeudi 17 mars 1994

***First Canadian
Workshop on
Fuzzy Logic and
its Industrial
Applications***

Thursday, March 17, 1994

ATELIER / WORKSHOP

Organisé par / Organized by



**Centre de recherche
informatique de Montréal**

CRIM

Avec la collaboration de / In collaboration with

CITI

Centre d'innovation
en technologies de l'information
Centre for Information
Technologies Innovation



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Logique floue : historique et concepts de base

Dr Benoît Julien, CRIM

10 h 30 Fuzzy Control and Applications

13 h 45 Software Tools for Fuzzy Control

Prof. M. Stephen L. Chiu, Rockwell International Science Center

11 h 15 Impact of Fuzzy Theory on Science and Technology

13 h 00 Applications of Fuzzy Theory

Dr. I. Burhan Türksen, Université de Toronto

Fuzzy Logic: A New World Technology

MM. Stéphane Côté et George Keirys, Omron Canada Inc.

14 h 45 AutoFuzz: A System For Automatic Fuzzy Controller

Application Development -

Dr Talib Janabi, Mentalogic Systems Inc.

15 h 00 Overview of MSI Fuzzy Logic Technology Developments

Dr Labib Sultan, Mentalogic Systems Inc.

Exemple d'applications de la logique floue pour le choix des conditions de coupe en tournage

M. Marek Balazinski, École Polytechnique de Montréal

Systèmes de contrôle - logique floue

MM. Mario Deschênes et Jean-François Ouellet, AutoSoft



Centre de recherche
informatique de Montréal
1801, avenue McGill College
Bureau 800
Montréal (Québec)
H3A 2N4
Tél.: (514) 398-1234
Télec.: (514) 398-1244

Premier atelier canadien sur la logique floue et ses applications dans l'industrie

Liste des participants

Centre de recherche informatique de Montréal
17 mars 1994

M. Roger Adm

Conseiller en développement technologique
Soutien à la recherche et au développement
Min. Industrie, Commerce, Science et Technologie
770, rue Sherbrooke ouest, 6e étage
Montréal, Québec
H3A 1G1

Téléphone : (514) 982-3001

Télécopieur: (514) 873-1353

M. Aissa Aomari

Chargé de secteur
Technologies avancées de production
Industrie Canada
800, Place Victoria, bureau 3800
C.P. 247
Montréal, Québec
H4Z 1E8

Téléphone : (514) 283-7814

Télécopieur: (514) 283-3302

M. Luc Audette

Chercheur

IREQ
1800, Montée Ste-Julie
Varenes, Québec
J3X 1S1

Téléphone : (514) 652-8230

Télécopieur: (514) 652-8005

M. Daniel Authier

Chef de projets

S.M.I.S. Inc.
3330, rue King Ouest, bureau 212
Sherbrooke, Québec
J1L 1C9

Téléphone : (819) 829-5120

Télécopieur: (819) 829-1133

Dr. Marek Balazinski

École Polytechnique de Montréal
C.P. 6079, succ. centre-ville
Montréal, Québec
H3C 3A7

Téléphone : (514) 340-4015

Télécopieur: (514) 340-5867

M. Fred Bassal

Professeur agrégé
Génie industriel
École Polytechnique de Montréal
C.P. 6079, succ. centre-ville
Montréal, Québec
H3C 3A7

Téléphone : (514) 340-4868

Télécopieur: (514) 340-4173

M. Jean Bernier

Professeur

Cégep de Limoilon
445, Jean XXIII
Charlesbourg, Québec
G2N 1V4

Téléphone : (418) 647-6720

Télécopieur: (418) 647-6798

M. Claude Blais

Chargé projet-Transf. Partenariats tech.
Compétitivité et analyse économique (CAE)
Industrie Canada
800, Place Victoria, bureau 3800
Montréal, Québec
H4Z 1E8

Téléphone : (514) 283-7856

Télécopieur: (514) 283-3302

M. Marc Bourgault

Journaliste

"Aujourd'hui la science" - Information radio
Société Radio-Canada
1400, boul. René-Lévesque est
Montréal, Québec
H2L 2M2

Téléphone : (514) 597-5739

Télécopieur: (514) 597-5728

M. Jean-Marc Bourgeois

Chercheur

IREQ
1800, Montée Ste-Julie
Varenes, Québec
J3X 1S1

Téléphone : (514) 652-8477

Télécopieur: (514) 652-8435

M. Serge Bédard

Agent de développement industriel

Min. Industrie, Commerce, Science et Technologie
710, Place d'Youville, 5e étage
Québec, Québec
G1R 4Y4

Téléphone : (418) 691-5898
Télécopieur: (418) 643-6669

M. Bob Chafetz

Centre innovation technologies information (CITI)
1575, boul. Chomedey
Laval, Québec
H7V 2X2

Téléphone : (514) 270-7798
Télécopieur: (514) 973-5757

M. Jeannot Chapdelaine

Directeur associé

Informission Ltée
7811, Louis H. Lafontaine, bureau 200
Anjou, Québec
H1K 4E4

Téléphone : (514) 351-7755
Télécopieur: (514) 351-5845

M. Raynald Chassé

Écotoxicologue

Ministère de l'Environnement du Québec
360, rue Franquet
Bureau 40
Ste-Foy, Québec
G1P 4N3

Téléphone : (418) 528-0416
Télécopieur: (418) 528-1091

M. Stephen Chiu

Professor
Control and Signal Processing Dept.
Rockwell International Science Center
1049 Camino Dos Rios
P.O. Box 1085
Thousands Oaks, California
USA
91360
Téléphone : (805) 373-4408
Télécopieur: (805) 373-4383

M. Denis Choquette

Quebec Regional Manager

Mentalogic Systems Inc.
145 Renfrew Drive - Unit #210
Markham, Ontario
L3R 9R6

Téléphone : (905) 940-6756
Télécopieur: (905) 940-0321

M. Pierre Chouinard

Enseignant

Cégep de Limoilon
445, Jean XXIII
Charlesbourg, Québec
G2N 1V4

Téléphone : (418) 647-6758
Télécopieur: (418) 647-6798

M. Stéphane Côté

OMRON Electronics Inc.
1825, 32e Avenue
Lachine, Québec
H8T 3G1

Téléphone : (514) 636-6676
Télécopieur: (514) 636-2959

Mme Kim Dalkir

Responsable
Systèmes de soutien à la performance
Centre innovation technologies information (CITI)
1575, boul. Chomedey
Laval, Québec
H7V 2X2

Téléphone : (514) 973-5840
Télécopieur: (514) 973-5757

Dr. Renato De Mori

Director
School of Computer Science
Université McGill
3480, rue University
Bureau 318
Montréal, Québec
H3A 2A7

Téléphone : (514) 398-7072
Télécopieur: () -3883

M. Mario Deschênes

AutoSoft
5655, avenue Élie, bureau 404
St-Hubert, Québec
J3Y 6P3

Téléphone : (514) 656-2323
Télécopieur: (514) 656-1009

M. François Desjardins
Conseiller

Informission Ltée
7811, Louis H. Lafontaine
Bureau 200
Anjou, Québec
H1K 4E4

Téléphone : (514) 351-7755
Télécopieur: (514) 351-5845

M. Pierre Desjardins

Centre innovation technologies information (CITI)
1575, boul. Chomedey
Laval, Québec
H7V 2X2

Téléphone : (514) 973-5700
Télécopieur: (514) 973-5757

M. Richard Desjardins
Président

CSTEMS-EXPERT
872, montée Ste-Thérèse
Bellefeuille, Québec
J0R 1A0

Téléphone : (514) 431-2174
Télécopieur: (514) 431-1662

M. Alain Dionne
Programmeur

CSTEMS-EXPERT
872, montée Ste-Thérèse
Bellefeuille, Québec
J0R 1A0

Téléphone : (514) 431-2174
Télécopieur: (514) 431-1662

M. Camille Dubé
Staff Engineer

IBM Canada Ltée
23, boul. de l'Aéroport
Bromont, Québec
J0E 1L0

Téléphone : (514) 534-6187
Télécopieur: (514) 534-7100

M. Carl Duhamel
Ingénieur concepteur électrique

Bombardier Inc.
1110, rue Parent
St-Bruno, Québec
J3V 6E6

Téléphone : (514) 441-2020
Télécopieur: (514) 441-6417

Poste: 6771

Dr. Jennifer Farkas

Chercheure
Architecture de l'information
Centre innovation technologies information (CITI)
1575, boul. Chomedey
Laval, Québec
H7V 2X2

Téléphone : (514) 973-5825
Télécopieur: (514) 973-5757

M. Abel Ferreira

Directeur, Ingénierie et production

Alex Informatique Inc.
8055, route Transcanadienne
Saint-Laurent, Québec
H4S 1S4

Téléphone : (514) 956-5500
Télécopieur: (514) 956-5505

M. Marc Fortin
Ingénieur de projet

Digico
950, rue Bergar
Laval, Québec
H7L 5A1

Téléphone : (514) 967-7100
Télécopieur: (514) 967-7444

M. Paul Freedman

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Réal Frenette

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Gilles Gagnon

Chargé de secteur
Produits électroniques et informatiques
Industrie Canada
800, Place Victoria, bureau 3800
C.P. 247
Montréal, Québec
H4Z 1E8

Téléphone : (514) 283-7861
Télécopieur: (514) 283-3302

M. Pierre Gauthier

Technicien de recherche

IREQ
1800, Montée Ste-Julie
Varenes, Québec
J3X 1S1

Téléphone : (514) 652-8438
Télécopieur: (514) 652-8435

M. Pierre Gautreau

Expert- conseil en gestion de la technologie
Direction des technologies de l'information
Industrie Canada
235, Queen Street
Ottawa, Ontario
K1A 0H5

Téléphone : (613) 954-3467
Télécopieur: (613) 952-8419

M. Daniel Gauvin

Directeur, R-D

Groupe LGS Inc.
1253, avenue McGill College
7e étage
Montréal, Québec
H3B 2Y5

Téléphone : (514) 861-2673
Télécopieur: (514) 861-3832

M. Denis Gingras

Chercheur
Traitement de l'information
Institut national d'optique
369, rue Franquet
Sainte-Foy, Québec
G1P 4N8

Téléphone : (418) 657-7006
Télécopieur: (418) 657-7009

M. Yves Gonthier

Graduate Student
CIM
Université McGill
3480, University, Room 410
McConnell Building
Montréal, Québec
H3A 2A7

Téléphone : (514) 398-7472
Télécopieur: () -7348

M. Bertrand Grenier

Directeur Systèmes Procédés
Plastiques et Chimiques
Pétromont Inc.
10555, boul. Métropolitain est
Montréal-Est, Québec
H1B 1A1

Téléphone : (514) 640-6400
Télécopieur: (514) 645-4705

Poste: 1202

M. Dominik Hartman

Graduate Student
CIM
Université McGill
3480, University, Room 410
McConnell Building
Montréal, Québec
H3A 2A7

Téléphone : (514) 398-6319
Télécopieur: () -7348

Dr. Talib Janabi
Director of Technology

Mentalogic Systems Inc.
145 Renfrew Drive - Unit #210
Markham, Ontario
L3R 9R6

Téléphone : (905) 940-6756
Télécopieur: (905) 940-0321

M. Normand Janelle
Ingénieur, R-D

FRIGIDAIRE CANADA
802, boulevard l'Ange Gardien
L'Assomption, Québec
J0K 1G0

Téléphone : (514) 589-5701
Télécopieur: (514) 589-0601

M. Antoni Jedrzejowski

étudiant
Département de génie mécanique
École Polytechnique de Montréal
C.P. 6079, succ. centre-ville
Montréal, Québec
H3C 3A7

Téléphone : (514) 340-4015
Télécopieur: (514) 340-5867

Dr. Benoît Julien
Chercheur

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Aldo Kamponico

Equifax Canada Inc.
7171, rue Jean-Talon Est
Anjou, Québec
H1M 3N2

Téléphone : (514) 493-2472
Télécopieur: (514) 355-0731

M. George Keirys

OMRON Electronics Inc.
885 Milneraue
Scarborough, Ontario
M1B 5V8

Téléphone : (416) 286-6465

M. Réal L'Archevêque

Premier conseiller à la Haute direction

Agence spatiale canadienne
6767, route de l'Aéroport
St-Hubert, Québec
J3Y 8Y9

Téléphone : (514) 926-4329
Télécopieur: (514) 926-4315

M. Gérard Lachiver

Professeur
Département de génie électrique et informatique
Université de Sherbrooke
2500, boul. de l'Université
Sherbrooke, Québec
J1K 2R1

Téléphone : (819) 821-7141
Télécopieur: (819) 821-7937

M. Marc Lacroix

Ingénieur
Division Automatismes
Hydro-Québec
Complexe Desjardins, 11e étage
C.P. 10000
Montréal, Québec
H5B 1H7

Téléphone : (514) 289-3913
Télécopieur: (514) 289-4695

M. René Lacroix

Attaché de recherche
Département de génie agricole
Université McGill
21111 Lakeshore Road
Campus Macdonald
Ste-Anne-de-Bellevue, Québec
H9X 3V9

Téléphone : (514) 398-7530
Télécopieur: () -8387

M. Daniel Lanoix
Ingénieur concepteur électrique

Bombardier Inc.
1110, rue Parent
St-Bruno, Québec
J3V 6E6

Téléphone : (514) 441-2020 Poste: 6505
Télécopieur: (514) 441-6417

M. Yves Lapierre
Spécialiste, transfert de technologie

Téléport de Montréal
1205, Papineau, bureau 351
Montréal, Québec
H2K 4R2

Téléphone : (514) 599-5723
Télécopieur: (514) 599-5724

M. Jean-Pierre LeBoeuf
Consultant

Kéops Informatique Inc.
266, rue Notre-Dame Ouest
Bureau 201
Montréal, Québec
H2Y 1T6

Téléphone : (514) 845-6158
Télécopieur: (514) 845-7274

M. Sinh LeQuoc
Directeur
Direction de l'enseignement et de la recherche
Ecole de technologie supérieure
4750, avenue Henri-Julien
Montréal, Québec
H2T 2C8

Téléphone : (514) 289-8806
Télécopieur: (514) 289-8539

Mme Monique Lefebvre
Présidente-directrice générale

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Marc Legault
Chef de division

Hydro-Québec
Complexe Desjardins, 11e étage
C.P. 10000
Montréal, Québec
H5B 1H7

Téléphone : (514) 289-4482
Télécopieur: (514) 289-4695

M. Marc C. Lemieux
Directeur exécutif

Industrie Canada
800, Place Victoria, bureau 3800, C.P. 247
Montréal, Québec
H4Z 1E8

Téléphone : (514) 283-1885
Télécopieur: (514) 283-3302

M. Robert Lessard
Designer

Autolog Inc.
1287, rue Bergar
Laval, Québec
H7L 4Z7

Téléphone : (514) 967-0766
Télécopieur: (514) 967-0769

M. Yves Lusignan
Président

Groupe conseil Sygertech Inc.
600, boul René-Lévesque ouest
11e étage
Montréal, Québec
H3B 1N4

Téléphone : (514) 861-7360
Télécopieur: (514) 861-8934

M. Félix Maltais
Journaliste

Agence Science-Pressé
3995, rue Ste-Catherine Est
Montréal, Québec
H1W 2G7

Téléphone : (514) 522-1304
Télécopieur: (514) 522-1761

M. Mircea Manolescu
Senior System Engineer

Mentalogic Systems Inc.
145 Renfrew Drive - Unit #210
Markham, Ontario
L3R 9R6

Téléphone : (905) 940-6756
Télécopieur: (905) 940-0321

M. Joseph Merheb-Herb

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Jean Millo
Président

Systèmes Intégrés A.B.D.M.F.
233, rue Dunbar, bureau 302
Montréal, Québec
H3P 2H4

Téléphone : (514) 737-4763
Télécopieur: (514) 737-9353

M. Bernard Morneau
Président

COGEXEL
8150, boul. Métropolitain Est
Bureau 200
Anjou, Québec
H1K 1A1

Téléphone : (514) 493-0663
Télécopieur: (514) 493-0980

M. Jean-François Ouellet

AutoSoft
5655, avenue Élie, bureau 404
St-Hubert, Québec
J3Y 6P3

Téléphone : (514) 656-2323
Télécopieur: (514) 656-1009

M. Louis Paquette

Professeur
Département Mathématiques et Informatique
Université du Québec à Trois-Rivières
C.P. 500
Trois-Rivières, Québec
G9A 5H7

Téléphone : (819) 376-5125
Télécopieur: (819) 376-5012

Mme Valérie Paquette

étudiante
Département d'animation culturelle
Université du Québec à Montréal
C.P. 8888, succ. A
Montréal, Québec
H3C 3P8

Téléphone : (514) 383-0404
Télécopieur: (514) 383-4971

Mme Annick Paraud

Conseillère en communications

Industrie Canada
800, Place Victoria, bureau 3800
C.P. 247
Montréal, Québec
H4Z 1E8

Téléphone : (514) 283-5142
Télécopieur: (514) 283-2269

M. David E. Paterson

Dir. gén. de l'ind. des technologies d'information
Industrie Canada
235, rue Queen, bureau 978 A
Ottawa, Ontario
K1A 0H5

Téléphone : (613) 954-3294
Télécopieur: (613) 952-8419

M. Michel Payment

FRIGIDAIRE CANADA
802, boulevard l'Ange Gardien
L'Assomption, Québec
J0K 1G0

Téléphone : (514) 589-5701
Télécopieur: (514) 589-0601

M. Jean Perron
Scientifique

Alcan Aluminium Ltée
1955, boul. Mellon
C.P. 1250
Jonquière, Québec
G7S 4K8

Téléphone : (418) 699-2339
Télécopieur: (418) 699-6378

M. Richard Pinsonneault

S.M.I.S. Inc.
3330, rue King Ouest, bureau 212
Sherbrooke, Québec
J1L 1C9

Téléphone : (819) 829-5120
Télécopieur: (819) 829-1133

M. Michel Rheault
Chargé de projet

Raymond, Chabot, Martin, Paré & Associés
600, rue de la Gauchetière ouest
Bureau 1900
Montréal, Québec
H3B 4L8

Téléphone : (514) 878-2691
Télécopieur: (514) 878-2127

M. Alain Ross
Agent de recherche

Centre de recherche industrielle du Québec (CRIQ)
8475, Christophe-Colomb
Montréal, Québec
H2M 2N9

Téléphone : (514) 383-1550 Poste: 553
Télécopieur: (514) 383-3229

M. Michel Ruel
Enseignant

Cégep Lévis-Lauzon
205, Mrg Bourget
Lévis, Québec
G6V 6Z9

Téléphone : (418) 833-5110
Télécopieur: (418) 833-7323

M. Carlos Saldanha
Chercheur principal

CRIM
1801, avenue McGill College
Bureau 800
Montréal, Québec
H3A 2N4

Téléphone : (514) 398-1234
Télécopieur: () -1244

M. Lofti Sansa

Département de génie mécanique
Université Concordia
1455, boul. de Maisonneuve ouest
Montréal, Québec
H3G 1M8

Téléphone : (514) 848-7930

M. Marc Alain Simard

Systèmes Paramax Canada Inc.
6111, avenue Royalmount
Montréal, Québec
H4P 1K6

Téléphone : (514) 340-8310
Télécopieur: (514) 340-8318

Dr. Labib Sultan
Director of R&D

Mentalogic Systems Inc.
145 Renfrew Drive - Unit #210
Markham, Ontario
L3R 9R6

Téléphone : (905) 940-6756
Télécopieur: (905) 940-0321

M. Gabriel Taraboulsi
Assistant gradué en recherche
CONCAVE {génie mécanique}
Université Concordia
1455, boul. de Maisonneuve ouest
Montréal, Québec
H3G 1M8

Téléphone : (514) 848-7939
Télécopieur: (514) 848-8635

M. Michel Teasdale
Chargé de secteur
Logiciel
Industrie Canada
800, Place Victoria, bureau 3800
C.P. 247
Montréal, Québec
H4Z 1E8

Téléphone : (514) 496-1388
Télécopieur: (514) 283-3302

M. Michel Thibault
Vice-président

Automation R.P. Inc.
593, Principale
St-Étienne-de-Lauzon, Québec
G6J 1E7

Téléphone : (418) 831-3344
Télécopieur: (418) 831-8200

M. Jean-Raymond Touchette
Professeur
Pavillon Ordinique
Collège Lionel-Groulx
150, rue Duquet
Ste-Thérèse, Québec
J7E 5B3

Téléphone : (514) 437-8088
Télécopieur: (514) 437-1102

M. Claude Tremblay
Conseiller en technologie industrielle (CTI)
CNRC
ACRGTO
435, Grande Allée Est
Québec, Québec
G1W 2A9

Téléphone : (418) 529-2949
Télécopieur: (418) 522-4105

M. Alexander Trica
Senior System Engineer

Mentalogic Systems Inc.
145 Renfrew Drive - Unit #210
Markham, Ontario
L3R 9R6

Téléphone : (905) 940-6756
Télécopieur: (905) 940-0321

M. E. Turcott
Research Associate

Université McGill
817, rue Sherbrooke Ouest
Montréal, Québec
H3A 2K6

Téléphone : (514) 398-4237
Télécopieur: () -7361

Dr. I. Burhan Turksen

Department of Industrial Engineering
University of Toronto
10, Kings College Road
Toronto, Ontario
M5S 1A4

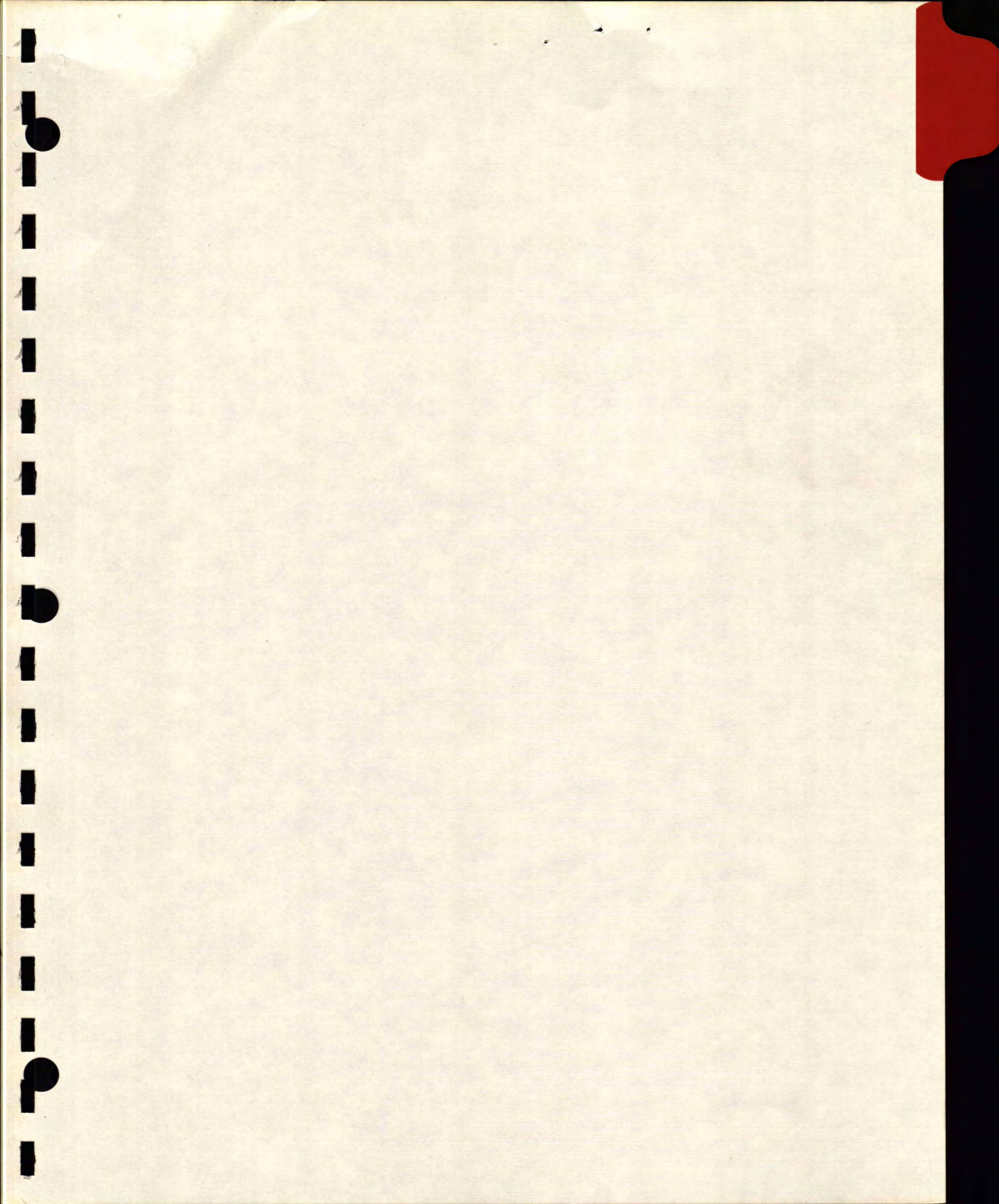
Téléphone : (416) 978-1278
Télécopieur: (416) 978-1280

M. Laurent Villeneuve
Professeur titulaire

École Polytechnique de Montréal
C.P. 6079, succ. centre-ville
Montréal, Québec
H3C 3A7

Téléphone : (514) 340-4911
Télécopieur: (514) 340-4173

Total de la liste: 88.



PROGRAMME

- 8 h 00** **Inscription tardive et petit déjeuner continental**
- 9 h 00** **Mots de bienvenue**
Mme Monique Lefebvre, Présidente et directrice générale du CRIM
M. Marc C. Lemieux, directeur exécutif, Industrie Canada
- 9 h 15** **Allocution d'ouverture**
Dr Renato De Mori, directeur du Département d'informatique de l'Université McGill
- 9 h 25** **Logique floue : historique et concepts de base**
Dr Benoît Julien, chercheur, groupe des systèmes à base de connaissances, CRIM
- 10 h 20** **Pause**
- 10 h 30** **Fuzzy Control and Applications**
M. Stephen L. Chiu, chercheur, Rockwell International Science Center
- 11 h 15** **Impact of Fuzzy Theory on Science and Technology**
Dr I. Burhan Türksen, professeur, Génie industriel, Université de Toronto
- 12 h 00** **Déjeuner**
- 13 h 00** **Applications of Fuzzy Theory**
Dr I. Burhan Türksen, professeur, Génie industriel, Université de Toronto
- 13 h 45** **Software Tools for Fuzzy Control**
M. Stephen L. Chiu, chercheur, Rockwell International Science Center
- Présentation de logiciels à logique floue**
- 14 h 30** **Fuzzy Logic: A New World Technology**
Stéphane Côté et George Keirys, OMRON Canada Inc.
- 14 h 45** **AutoFuzz: A System For Automatic Fuzzy Controller Applications Development**
Dr Talib Janabi, Mentalogic Systems Inc.
- 15 h 00** **Overview of MSI Fuzzy Logic Technology Developments**
Dr Labib Sultan, Mentalogic Systems Inc.
- 15 h 15** **Logique floue en fabrication**
M. Marek Balazinski, École Polytechnique de Montréal
- 15 h 30** **Systèmes de contrôle - logique floue**
M. Mario Deschênes et M. Jean-François Ouellet, AutoSoft
- 15 h 45** **Pause-café et démonstration de logiciels à logique floue**
- 16 h 30** **Table ronde**
Conférenciers et sociétés participantes
- 16 h 45** **Cocktail**

PROGRAM

- 8:00** Late registration et continental breakfast
- 9:00** Welcoming speeches
Mrs. Monique Lefebvre, P & CEO, CRIM
Mr. Marc Lemieux, Executive Regional Director, Industry Canada
- 9:15** Opening speech
Dr. Renato De Mori, Director of the Computer Science Department at McGill University
- 9:25** Logique floue : historique et concepts de base
Dr. Benoît Julien, Research Scientist, Knowledge-based systems, CRIM
- 10:20** Coffee break
- 10:30** Fuzzy Control and Applications
Mr. Stephen L. Chiu, Research Scientist, Rockwell International Science Center
- 11: 15** Impact of Fuzzy Theory on Science and Technology
Dr. I. Burhan Türksen, Professor, Industrial Engineering, University of Toronto
- 12:00** Lunch
- 13: 00** Applications of Fuzzy Theory
Dr. I. Burhan Türksen, Professor, Industrial Engineering, University of Toronto
- 13:45** Software Tools for Fuzzy Control
Mr. Stephen L. Chiu, Research Scientist, Rockwell International Science Center
Presentations of fuzzy logic software
- 14:30** Fuzzy Logic: A New World Technology
Mr. Stéphane Côté and Mr. George Keirys, OMRON Canada Inc.
- 14:45** AutoFuzz: A System For Automatic Fuzzy Controller Applications Development
Dr. Talib Janabi, Mentalogic Systems Inc.
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Mr. Mario Deschênes and Mr. Jean-François Ouellet, AutoSoft
- 15:45** Coffee break and demonstrations of fuzzy logic software
- 16:30** Panel
Guest speakers and participating companies
- 16:45** Cocktail



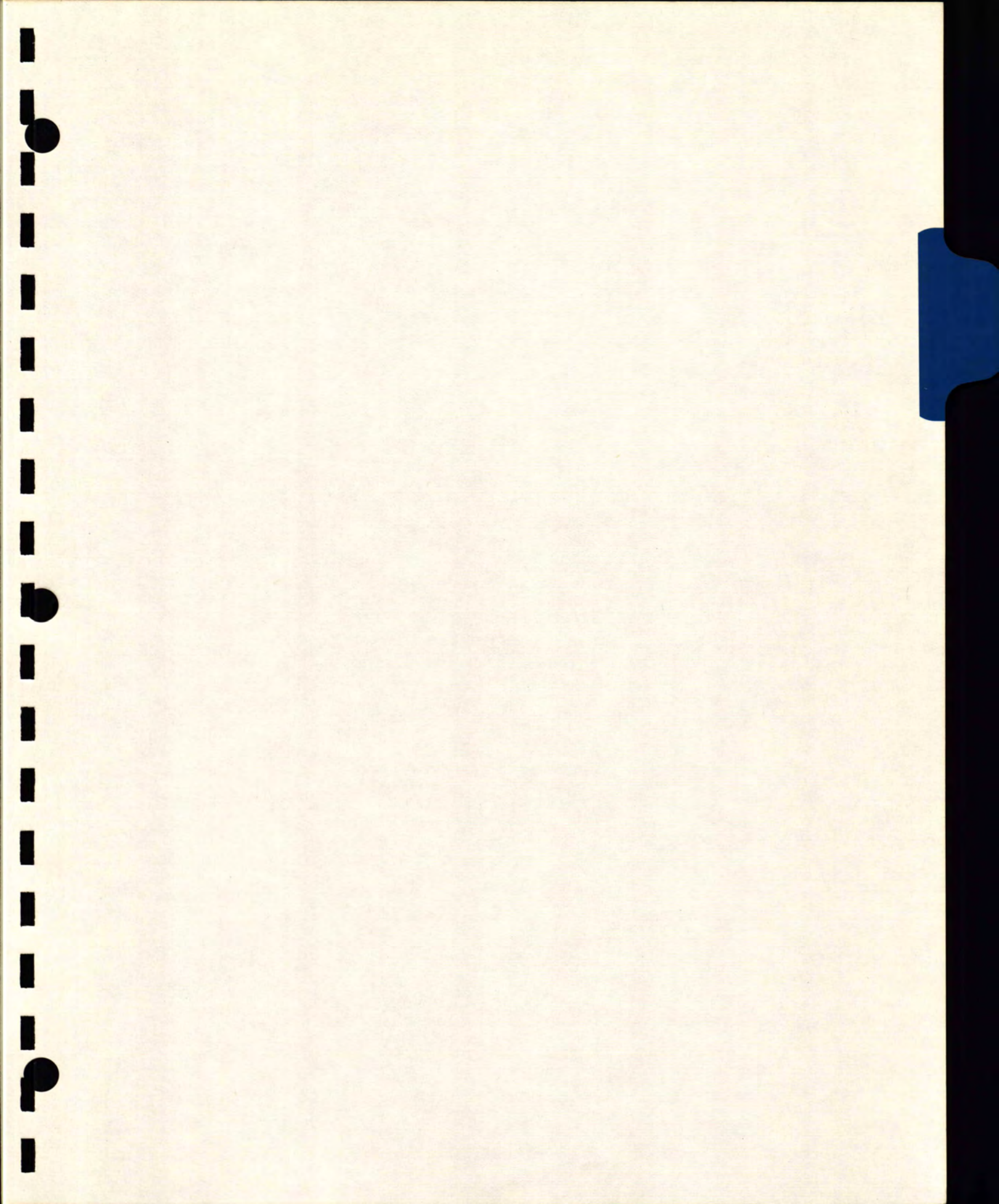
LISTE DES COMMANDITAIRES

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informatique de Montréal

Premier atelier canadien sur la logique floue et ses applications dans l'industrie

Logique floue : historique et concepts de base

Présenté par

Benoît Julien, Ph.D., ing.

Chercheur

Groupe des systèmes à base de connaissances

Mars 1994

Introduction

Chapitres:



Introduction

- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*

Points abordés:

- *Motivations*
- *Applications*
- *Bref historique*
- *Définitions générales*

Introduction

Motivations

Plus un système devient complexe, plus la formulation d'énoncés précis et pertinents sur son comportement est difficile.

Le précision et la pertinence peuvent même devenir mutuellement exclusives.

Plutôt que de chercher à éliminer l'imprécision associée aux comportements de systèmes complexes, les approches "floues" visent à représenter et manipuler cette imprécision.

Introduction

Applications

● **Systèmes de contrôle**

En 1991, le Japon possède approximativement 80 % des parts du marché de la logique floue avec des revenus d'environ 200 millions de dollars canadiens.

Il existe plus de 2 000 brevets reliés à la logique floue au Japon.

Produits développés

- Métro de Sendai (accélération plus graduelle et arrêt avec trois fois la précision du contrôle manuel),
- Machines à laver (contrôle flou implanté sur 70% des machines de Matsushita Electric),
- Caméras-vidéos (optimise le focus de certaines caméras-vidéos de Sanyo avec moins de mémoire),
- Climatiseurs (économie de 20% en électricité pour le produit de Mitsubishi),
- Ordinateurs et microprocesseurs,
- Transmissions d'automobile, etc.

● **Systèmes d'aide à la décision**

- Ingénierie (ex : gestion de réservoirs),
- Environnement,
- Gestion et sélection de projets (ex : gestion de portefeuilles)

Introduction

Bref historique

- 1965 Le Professeur Lotfi A. Zadeh introduit la notion d'ensemble flou.
- 1970 Première application par Bellman et Zadeh de la théorie des ensembles flous à des problèmes de décision.
- 1974 Premier développement d'un système à contrôle flou par Mamdani.
- 1975 Premier développement de la logique floue et du raisonnement approximatif par Zadeh.
- 1977 Introduction du concept de mesure floue par Sugeno.
- 1978 Développement de la théorie des possibilités.
- 1985 Première implantation sur microprocesseur (Togai et Watanabe).

Introduction

Définitions générales

Théorie des ensembles flous

Cadre mathématique pour le traitement de problèmes dans lesquels l'incertitude provient de l'imprécision plutôt que de l'aléatoire.

- **Énoncé précis**

La température est à 27°C.

- **Énoncé imprécis**

La température est élevée.

Introduction

Définitions générales

Logique floue

Logique à valeurs multiples permettant le raisonnement approximatif à partir d'informations imprécises.

- Règle précise

Si température $> 17^{\circ}\text{C}$
alors fermer la valve de 2 unités.

- Règle imprécise

Si température élevée
alors fermer la valve légèrement.

Contexte

Chapitres:



- *Introduction*
- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*

Points abordés:

- *Caractéristiques de l'information*

Contexte

Caractéristiques de l'information

- **Information inexacte**

Exprime la différence entre une croyance et la réalité.

Exemple : Jean a 25 ans. (En fait Jean a 22 ans).

- **Information incomplète**

Impossibilité de formuler certaines affirmations à partir d'énoncés connus.

- **Information incertaine**

Degré de croyance dans un énoncé.

Expressions possibles de l'incertitude

- **Probabiliste**

Exemple : Jean a 22 ans (probabilité de 80 %).

- **Imprécision**

Exemple : Jean a environ 22 ans.

- **Possibiliste**

Exemple : Jean a 22 ans (possibilité de 100 %).

Contexte

Caractéristiques de l'information

- **L'imprécis et l'aléatoire**

- 1) Le coût du projet est environ 70 millions de dollars.
- 2) Le coût du projet est 70 millions de dollars avec une probabilité de 80 %.

- **L'imprécis et le précis**

- 1) Le niveau de nitrate est bas.
- 2) Le niveau de nitrate est inférieur à 10 mg/l.

Théorie des ensembles flous

Chapitres:



- *Introduction*
- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*

Points abordés:

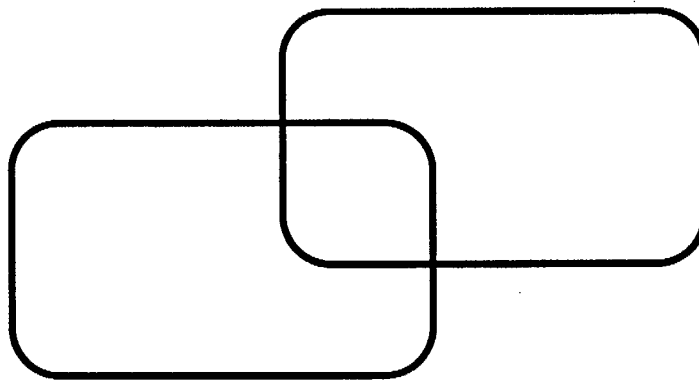
- *Ensembles classiques*
- *Objectif*
- *Définition d'un ensemble flou*
- *Ensembles flous et classiques*
- *Nombre flou*
- *Représentation discrète*
- *Acquisition*
- *Opérateurs de base*
- *Principe d'extension*

Théorie des ensembles flous Ensembles classiques

$A \cap B$:

$A \cup B$:

Personnes moins de 25 ans



Hommes

Jean est un homme de moins de 25 ans.

$Jean \in (A \cap B)$

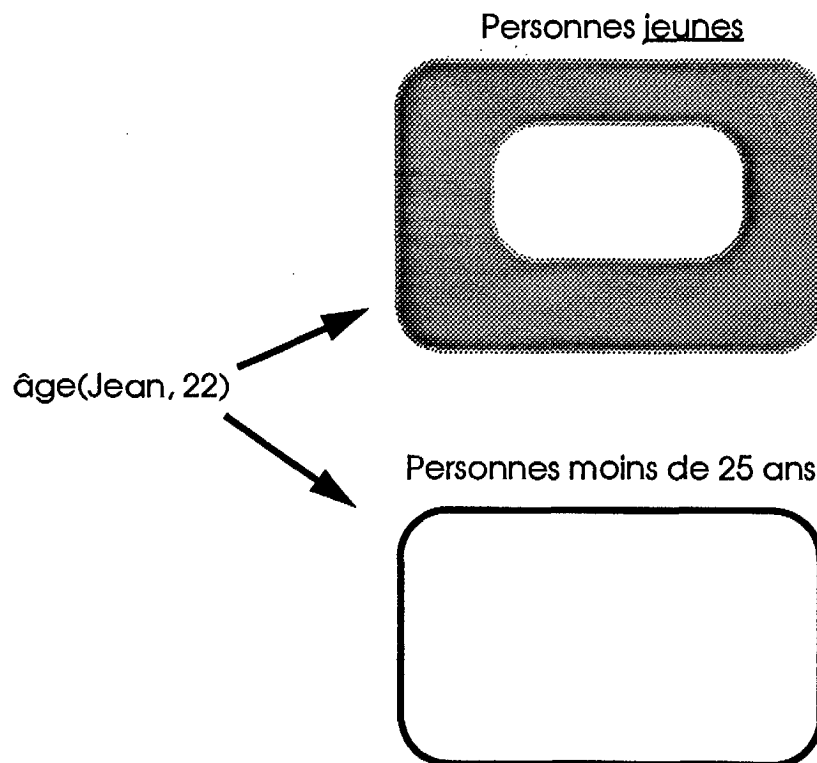
Théorie des ensembles flous

Objectif

Fournir un cadre mathématique pour la représentation et le traitement de l'incertitude attribuable à l'imprécision.

L'imprécision est définie par l'absence d'une démarcation nette entre l'appartenance et la non-appartenance à une classe.

La théorie des ensembles flous représente le degré d'appartenance d'éléments à des ensembles possédant des frontières imprécises.

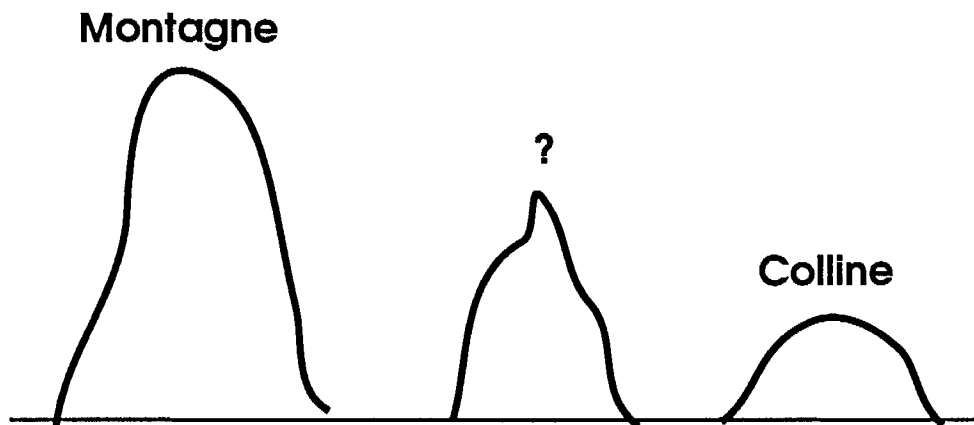


Théorie des ensembles flous

Ensembles flous et classiques

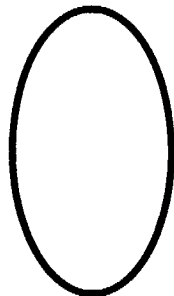
Exemples

- À partir de quelle hauteur un relief est-il une colline ou une montagne?

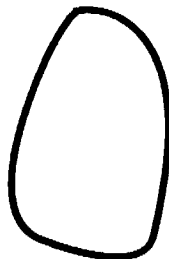


- Ovale flou ou parfait?

Ovale parfait



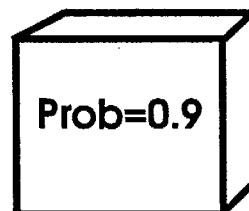
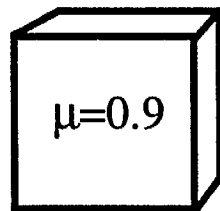
?



Pas un ovale



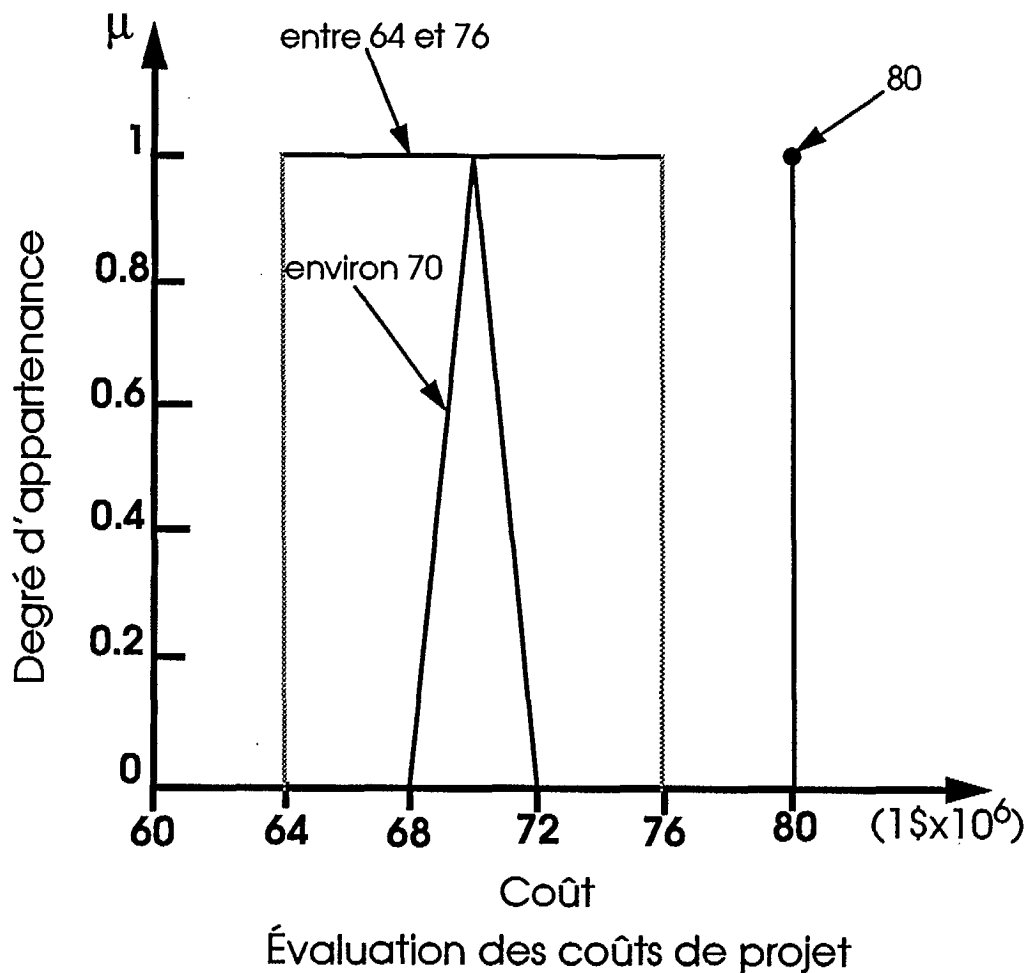
- Liquide potable ou non potable?



Théorie des ensembles flous

Définition d'un ensemble flou

Une collection d'éléments pour lesquels il n'existe pas de brusque transition entre l'appartenance ($\mu = 1$) et la non-appartenance ($\mu = 0$).



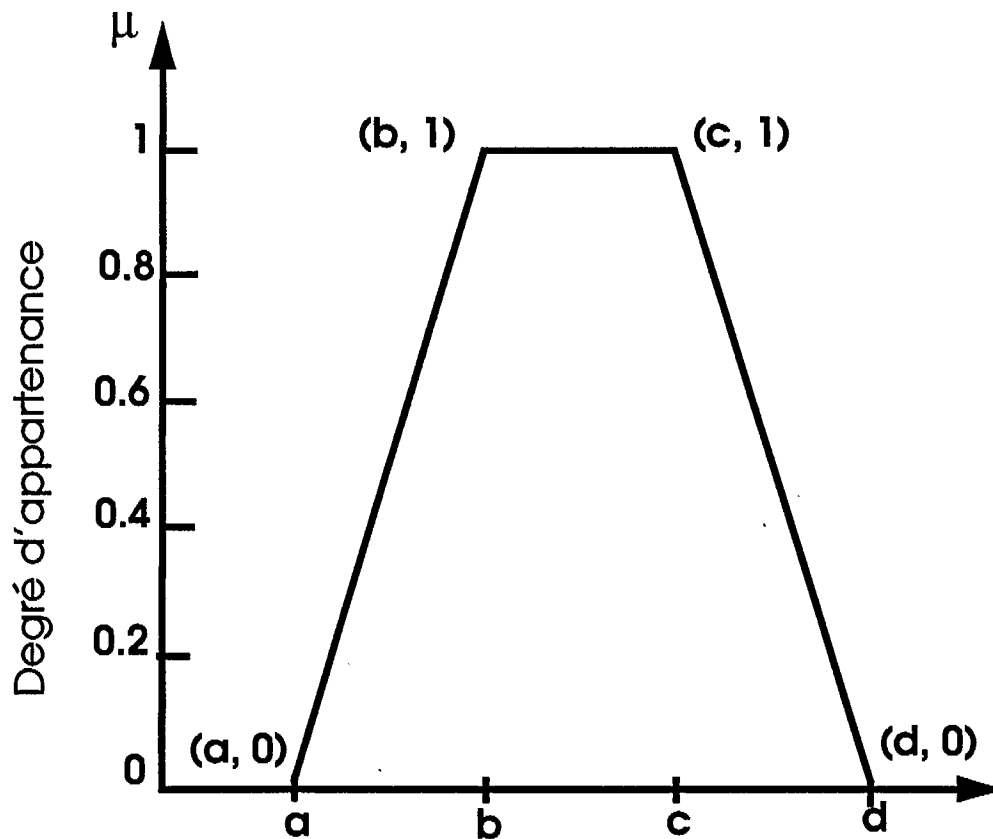
Théorie des ensembles flous Nombre flou

Représentation simplifiée : (a, b, c, d)

Si $b = c$, fonction d'appartenance triangulaire.

Si $a=b=c=d$, nombre précis.

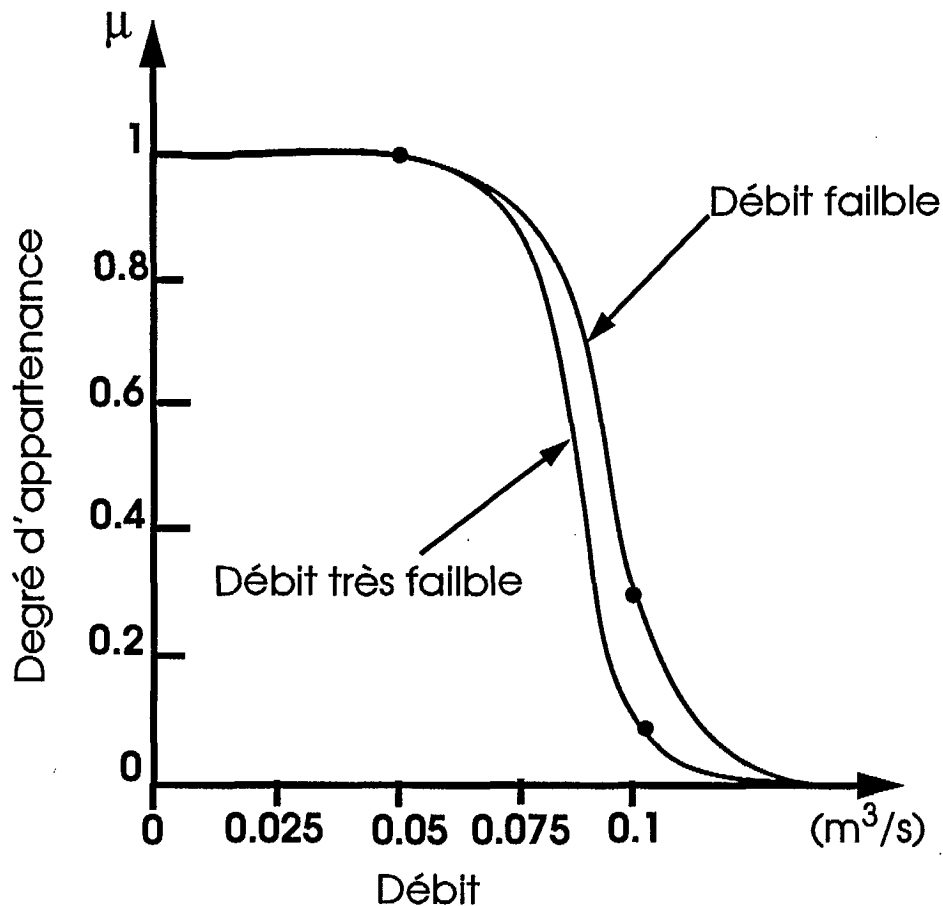
Si $a=b, c=d$, ensemble (intervalle).



Théorie des ensembles flous Représentation discrète

Débit faible (m^3/s) = $\mu_{\text{DF}}(x)$
 $\mu_{\text{DF}}(x) = \{1/0.05, 0.3/0.1\}$

Débit très faible (m^3/s) = $\mu_{\text{DTF}}(x) = (\mu_{\text{DF}}(x))^2$
 $\mu_{\text{DTF}}(x) = \{1/0.05, 0.09/0.1\}$

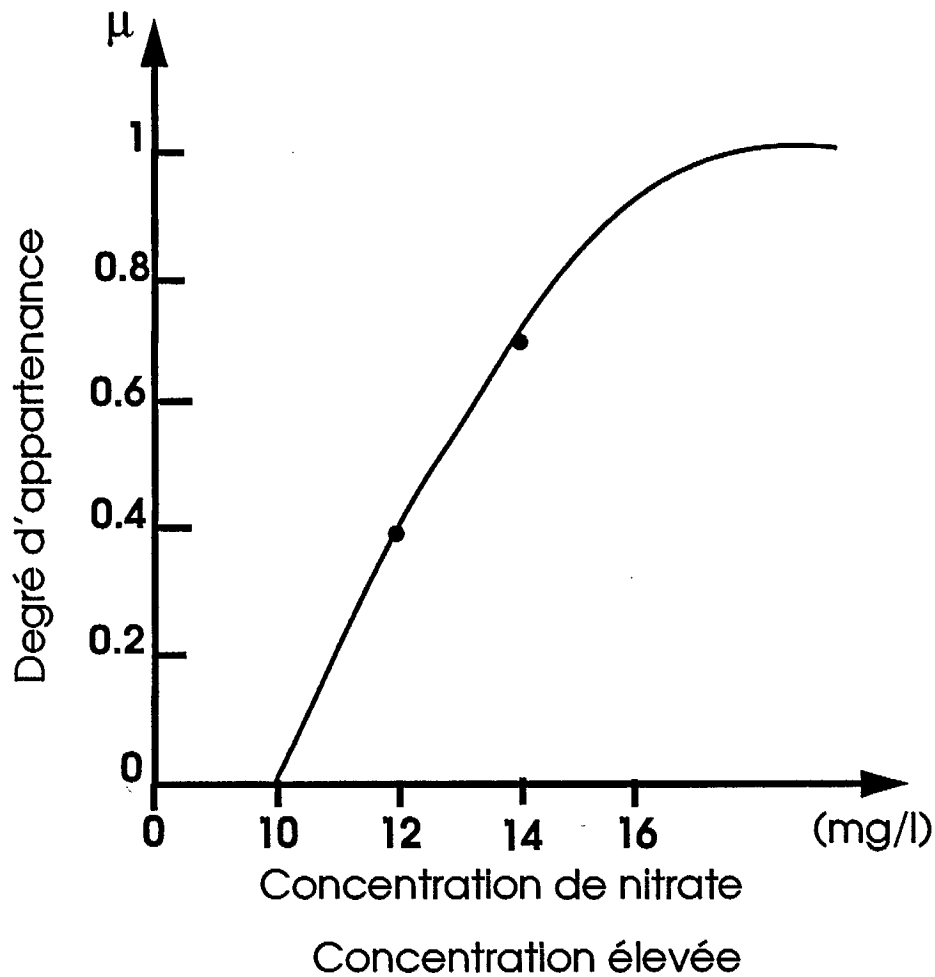


Théorie des ensembles flous Représentation discrète

Concentration élevée de nitrate (mg/l) = $\mu_{CE}(Y)$

$\mu_{CE}(Y) = \{0.4/12, 0.7/14\}$

Valeur linguistique : concentration élevée



Théorie des ensembles flous

Acquisition

Les degrés d'appartenance sont généralement subjectifs et dépendent du contexte de l'évaluation.

Des études (Turksen 1991, Norwich et Turksen 1984) ont démontré que les degrés d'appartenance peuvent au mieux être mesurés sur une échelle ordinale ou intervalle.

Des méthodes empiriques ont été proposées pour la détermination des fonctions d'appartenance. Ces méthodes requièrent la définition d'expériences sur des populations tests afin de mesurer les perceptions subjectives des degrés d'appartenance.

Méthodes par apprentissage.

Théorie des ensembles flous

Opérateurs de base

Exemple

Débit faible = $\mu_{DF}(x) = \{1/0.05, 0.3/0.1\}$

Concentration élevée = $\mu_{CE}(y) = \{0.4/12, 0.7/14\}$

(Débit faible) et (Concentration élevée de nitrate) = ?

Union

$$\forall (x, y) \in X \times Y : \mu_{A \cup B}(x, y) = \max(\mu_A(x), \mu_B(y))$$

Intersection

$$\forall (x, y) \in X \times Y : \mu_{A \cap B}(x, y) = \min(\mu_A(x), \mu_B(y))$$

Complément

$$\forall x \in X : \mu_{\neg A}(x) = 1 - \mu_A(x)$$

Avantages

- Les opérateurs max et min respectent la plupart des propriétés de l'union et l'intersection classiques.
- Ces deux opérateurs sont non interactifs et limitent donc la propagation des erreurs de mesure.

Théorie des ensembles flous Opérateurs de base

Exemple

(Débit faible) et (Concentration élevée) = $\mu_{DF \cap CE}(x, y)$

| | | min | y | |
|------|---------------|---------------|-----|-----|
| x | $\mu_{DF}(x)$ | $\mu_{CE}(y)$ | 12 | 14 |
| 0.05 | 1 | | 0.4 | 0.7 |
| 0.1 | 0.3 | | 0.3 | 0.3 |

$$\mu_{DF \cap CE}(x, y) = \{0.4/(0.05, 12), 0.7/(0.05, 14), \\ 0.3/(0.1, 12), 0.3/(0.1, 14)\}$$

Théorie des ensembles flous Opérateurs de base

Les lois classiques de contradiction et d'exclusion des ensembles ne sont plus valides dans la théorie des ensembles flous. Elles sont remplacées par :

$$\begin{aligned}A \cap (\neg A) &\neq \emptyset \\ A \cup (\neg A) &\neq X\end{aligned}$$

Exemple

$$\mu_A(x) = \{1/x_1, 0.3/x_2\}$$

$$\mu_{\neg A}(x) = 1 - \mu_A(x) = \{0/x_1, 0.7/x_2\}$$

$$\mu_{\neg A \cap A}(x) = \min(\mu_A(x), \mu_{\neg A}(x)) = \{0/x_1, 0.3/x_2\} \neq \{0/x_1, 0/x_2\}$$

$$\mu_{\neg A \cup A}(x) = \max(\mu_A(x), \mu_{\neg A}(x)) = \{1/x_1, 0.7/x_2\} \neq \{1/x_1, 1/x_2\}$$

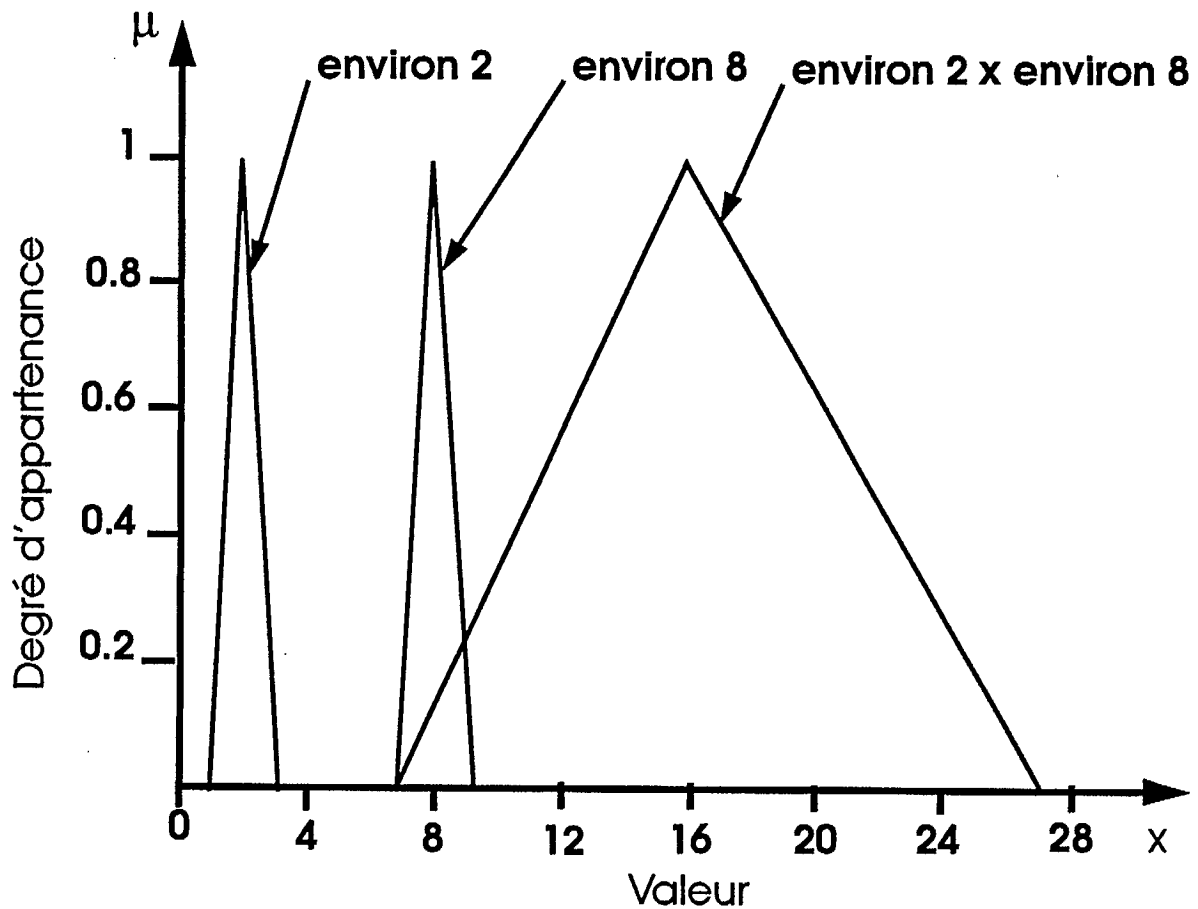
Théorie des ensembles flous . Principe d'extension

Exemple

$$\alpha = 0 : (1, 3) \times (7, 9) = (7, 27)$$

$$\alpha = 0.5 : (1.5, 2.5) \times (7.5, 8.5) = (11.25, 21.25)$$

$$\alpha = 1 : (2, 2) \times (8, 8) = (16, 16)$$



environ 2 multiplié par environ 8

Théorie des ensembles flous

Principe d'extension

Le principe d'extension permet d'étendre l'applicabilité d'un opérateur mathématique conventionnel afin de traiter des quantités floues.

$$\mu_B(z) = \bigvee_{x \in A, y \in B, y = f(x, y)} \{ \wedge (\mu_A(x), \mu_B(y)) \}$$

$$\mu_B(z) = \max_{x \in A, y \in B, y = f(x, y)} \{ \min (\mu_A(x), \mu_B(y)) \}$$

Solution approximative

- Ensemble niveau α

$$A_\alpha = \{x \in X \mid \mu_A(x) \geq \alpha\}$$

- Calcul par intervalle

$$(a, b) + (c, d) = ((a+c), (b+d))$$

$$(a, b) - (c, d) = ((a-d), (b-c))$$

$$(a, b) \times (c, d) = (\min(ac, ad, bc, bd), \max(ac, ad, bc, bd))$$

$$(a, b) \div (c, d) = (a, b) \times (1/c, 1/d) \text{ si } c \neq 0 \text{ et } d \neq 0$$

- Mise en garde

$$(a, b) \div (a, b) \neq 1$$

Théorie des possibilités

Chapitres:



- *Introduction*
- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*

Points abordés:

- *Interprétation*
- *Principe de cohérence*

Théorie des possibilités Interprétation

Grâce aux opérateurs max et min d'union et d'intersection, la théorie des ensembles flous peut être reliée à celle des possibilités.

La théorie des possibilités interprète la fonction d'appartenance comme une distribution de possibilités exprimant une restriction floue sur les valeurs qui peuvent être assignées à une variable.

Exemple

- **Théorie des ensembles flous**

âge 22, $\mu_{\text{jeune}}(0.7)$

Degré de compatibilité de 0,7 de l'âge 22 ans avec le concept imprécis de jeune.

- **Théorie des possibilités**

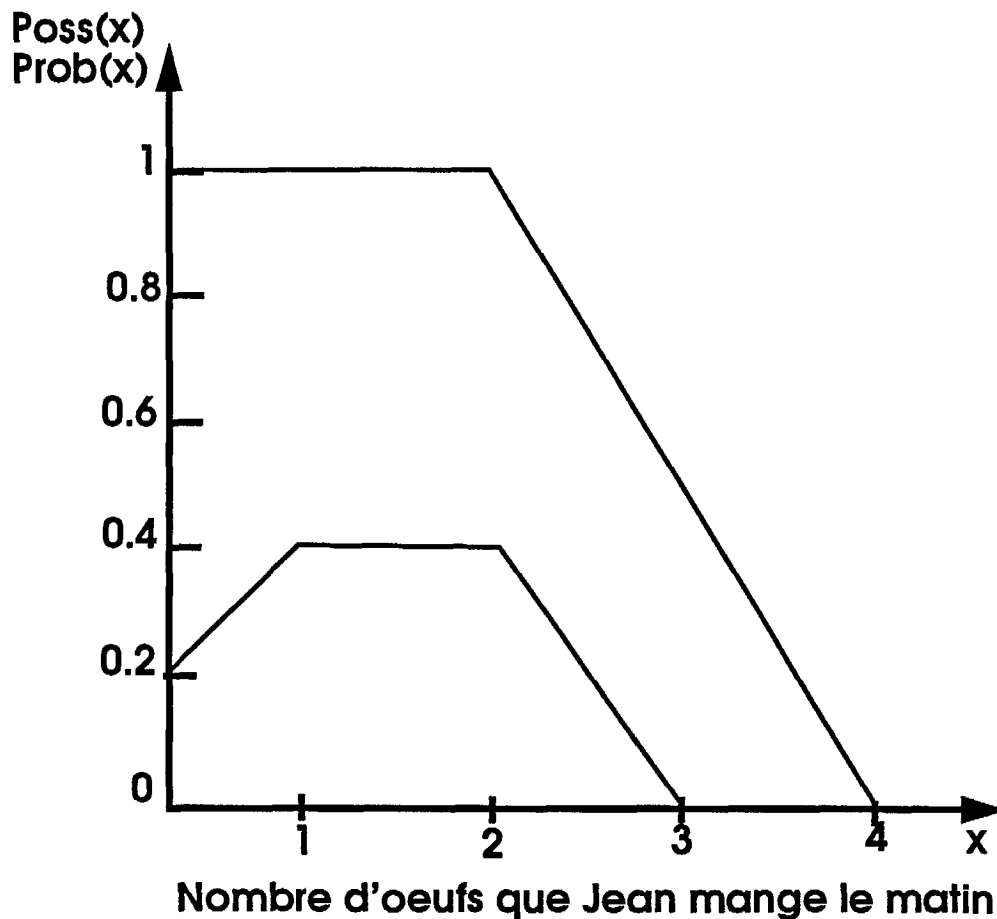
Jean est jeune.

Si Jean est jeune le degré de possibilité qu'il ait 22 ans est de 0,7.

Théorie des possibilités Principe de cohérence

Une distribution de possibilités peut être interprétée comme une enveloppe sous laquelle doit se retrouver la fonction de probabilité.

Exemple



Théorie des possibilités Principe de cohérence

Plutôt que d'être possibles (1) ou impossibles (0), des événements sont possibles à différents degrés entre 0 et 1.

Le principe de cohérence stipule qu'un événement x doit d'abord être possible avant d'être probable.

$$\text{Poss}(x) \geq \text{Prob}(x)$$

$$(\text{Poss}(x) = 0) \rightarrow (\text{Prob}(x) = 0)$$

Logique floue

Chapitres:

- *Introduction*
- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*



Points abordés:

- *Objectif*
- *Implication floue*

Logique floue Objectif

Afin de raisonner avec des informations imprécises, il nous faut assouplir les structures logiques classiques.

Il faut éviter l'exactitude de la logique classique en permettant à la vérité d'être imprécise.

Grâce à la théorie des ensembles flous, la distinction nette entre le vrai et le faux peut être éliminée.

Les degrés d'appartenance deviennent des degrés de vérité associés à des énoncés.

Exemples

1. L'eau est polluée de nitrates.
2. Le niveau de pollution en nitrate est élevé.

Logique floue Implication floue

Exemple

Si température $> 17^{\circ}\text{C}$ (a)
alors fermer la valve de 2 unités (b).

La logique floue est une logique à valeurs multiples entre 0 et 1.

La logique du premier ordre utilise l'opérateur d'implication booléen suivant :

| $a \rightarrow b$ CNF: $(\neg a \cup b)$ | | b | |
|---|---|---|---|
| | | 0 | 1 |
| a | 0 | 1 | 1 |
| | 1 | 0 | 1 |

Logique floue

Implication floue

Différents opérateurs d'implication à valeurs multiples ont été suggérés :

| Opérateur | Nom | Définition de $a \rightarrow b$ |
|--------------------|------------------------------|---|
| \rightarrow_1 | standard sharp | 1 si $a \neq 1$ ou $b = 1$ 0 autrement |
| \rightarrow_2 | standard strict | 1 si $a \leq b$ 0 autrement |
| \rightarrow_3 | standard star | 1 si $a \leq b$ b autrement |
| \rightarrow_4 | Gaines | 1 si $a = 0$ $\min(1, b/a)$ autrement |
| \rightarrow_5 | Gaines modifié | 1 si $a = 0$ ou $b = 1$ $\min(1, b/a, (1-a)/(1-b))$ autrement |
| \rightarrow_6 | Lukasiewicz | $\min(1, 1 - a + b)$ |
| \rightarrow_7 | Kleene-Dienes Lukasiewicz | $1 - a + ab$ |
| \rightarrow_8 | Kleene-Dienes | $\max((1-a), b)$ |
| \rightarrow_9 | early Zadeh | $\max(a \rightarrow_8 b, a, (1-a))$ |
| \rightarrow_{10} | Willmott | $\min(a \rightarrow_9 b, \max(b, (1-b)))$ |

Logique floue Implication floue

L'opérateur d'implication à valeurs multiples établit une relation entre la prémisse et la conclusion d'une règle lorsque ces deux composantes sont imprécises.

L'implication floue permet donc de générer un ensemble flou représentant une règle.

Exemple

Si température élevée (A)
et pression forte (B)
alors fermer la valve légèrement (C).

$$\begin{array}{l} \text{Si } (A \text{ et } B) \rightarrow C \\ \quad \boxed{\phantom{\mu_{A \cap B}(x,y)}} \\ \mu_{A \cap B}(x,y) \\ \quad \boxed{\phantom{\mu_{((A \cap B) \rightarrow C)}(x,y,z)}} \\ \mu_{((A \cap B) \rightarrow C)}(x,y,z) \end{array}$$

Conclusion

Chapitres:

- *Introduction*
- *Contexte*
- *Théorie des ensembles flous*
- *Théorie des possibilités*
- *Logique floue*
- *Conclusion*



Points abordés:

- *Avantages*
- *Limites*
- *Controverse*
- *Mot de la fin*

Conclusion

Avantages

Théorie des ensembles flous

- **La théorie des ensembles flous offre une représentation mathématique rigoureuse de l'incertitude attribuée à l'imprécision.**
- **L'interprétation possibiliste permet de relier la théorie des ensembles flous à celle des probabilités.**
- **La théorie classique des ensembles devient un cas spécial de la théorie des ensembles flous.**

Conclusion

Avantages

Logique floue

- **La logique floue permet le raisonnement approximatif à partir d'informations imprécises.**
- **La disponibilité de divers opérateurs d'implication et de mesure de similarité permet d'adapter le mode de raisonnement pour chaque application.**
- **La logique du premier ordre devient un cas spécial de la logique floue.**

Conclusion

Limites

- **Définition et signification des fonctions d'appartenance**
- **Sélection et validité des opérations affectant les fonctions d'appartenance**
- **Validation et vérification des systèmes flous**

Conclusion

La controverse

● Opposants

“... we should keep the vagueness of the scale localised into it, rather than letting it infect the whole inferential system”

Patrick J. Hayes, 1974

“It is so difficult to quantify a belief or preference as a single number, why is it easier to quantify it as a complete set membership function?”

Simon French, 1984

● Partisans

“In fact, it is the ability to reason in qualitative, imprecise terms that distinguishes human intelligence from machine intelligence.”

Lotfi A. Zadeh, 1979

“... In the decision process certain forms of imprecision occur that are intrinsic to the problem and for which the probability calculus is inadequate.”

Gaines et al., 1984

Conclusion

Mot de la fin

Si nous acceptons l'imprécision dans le seul but d'excuser notre propre ignorance, alors il est possible que nous ne fassions jamais l'effort de discerner certains phénomènes précis.

Si, par contre, nous refusons de reconnaître que certains concepts sont fondamentalement imprécis alors il se peut que nous produisions une multitude d'alternatives plus précises mais moins utiles.

La théorie des ensembles flous est en elle-même neutre, car elle permet la représentation de concepts précis aussi bien qu'imprécis. Les seuls avantages et dangers résident dans la façon de l'utiliser.

Traduit de Gaines, 1976



Bibliographie

Livres

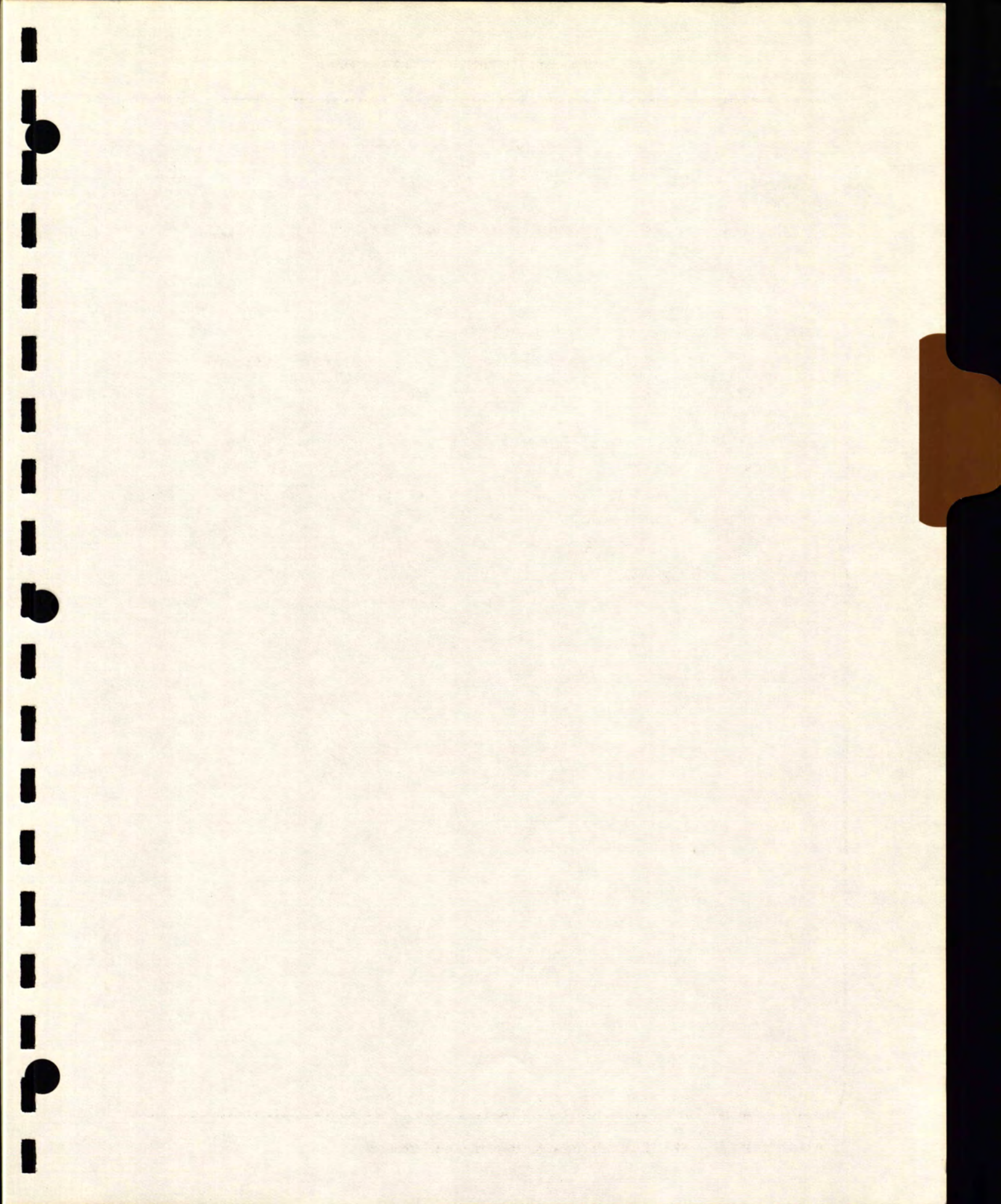
- [DUBO80] Dubois, Didier et Prade, Henri. *Fuzzy Sets and Systems: Theory and Applications*, Academic Press, New York, 1980.
- [DUBO88] Dubois, Didier et Prade, Henri. *Possibility Theory, An Approach to Computerized Processing of Uncertainty*, Plenum Press, New York, 1988.
- [DUBO92] Dubois, Didier, Prade, Henri et Yager Ronald R., éditeurs. *Readings in Fuzzy Systems*. Morgan Kaufmann Publishers, 1992.
- [GUPTA82] Gupta, M. M. et Sanchez, E., éditeurs. *Approximate Reasoning in Decision Analysis*. Elsevier North-Holland, 1982.
- [GUPTA85] Gupta, M. M., Kandel, A., Bandler, W. et Kiszka, J. B., éditeurs. *Approximate Reasoning in Expert Systems*. North Holland, 1985.
- [KANA86] Kanal, L. N. et Lemmer J. F., éditeurs. *Uncertainty in AI*. Elsevier Science Publishers, 1986.
- [KAND86] Kandel, A. *Fuzzy Mathematical Techniques with Applications*. Addison-Wesley Publishing Company, 1986.
- [KLIR88] Klir, G. J. et Folger, T. A. *Fuzzy Sets Uncertainty and Information*. Prentice Hall, 1988.
- [KOSK92] Kosko, B. *Neural Networks and Fuzzy Systems*. Prentice Hall, Englewood Cliffs, New Jersey, 1992.
- [SUGE90] Sugeno, M. *Industrial Applications of Fuzzy Control*. North Holland, 1990.
- [WANG91] Wang, Z. et Klir G. J. *Fuzzy Measure Theory*. Plenum Press, New York, 1991.
- [YAGE87] Yager, R. R. et al. *Fuzzy Sets and Applications: Selected Papers by L.A. Zadeh*. John Wiley & Sons, New York, 1987.
- [YAGE91] Yager, R. R. et Zadeh, L.A. *An Introduction to Fuzzy Logic Applications in Intelligent Systems*. Kluwer Academic Publishers, 1991.
- [ZIMM85] Zimmermann, H.-J. *Fuzzy Set Theory and its Applications*. Kluwer-Nijhoff Publishers, 1985.
- [ZIMM87] Zimmermann, H.-J. *Fuzzy Sets, Decision Making, and Expert Systems*. Kluwer Academic Publisher, 1987.



Bibliographie

Articles généraux

- [CONN93] Conner, D. «Special report: designing a fuzzy logic control systems requires a new way of thinking». *EDN*, 1993 (Mars).
- [COX93] Cox, E. «Adaptative fuzzy systems». *IEEE Spectrum*, 1993 (Février).
- [KOS93] Kosko, B et Isaka, S. «La logique floue». *Pour la Science*, 1993 (Septembre).
- [ROGE90] Rogers, M. et Hoshiai, Y. «The future looks fuzzy». *Newsweek*, 1990 (Mai).
- [SCHW92] Schwartz, D. G. «Fuzzy logic flowers in Japan». *IEEE Spectrum*, 1992 (Juillet).
- [SELF90] Self, K. «Designing with fuzzy logic». *IEEE Spectrum*, 1990 (Novembre).
- [SIBI92] Sibigtroth, J. M. «Implementing fuzzy expert rules in hardware». *AI Expert*, 1992 (Avril).





Fuzzy Control and Applications

**First Canadian Workshop on Fuzzy Logic & Industrial Applications
March 17, 1994**

Stephen L. Chiu

**Rockwell International Science Center
1049 Camino Dos Rios
Thousand Oaks, CA 91360
Email: slc@risc.rockwell.com**

Outline

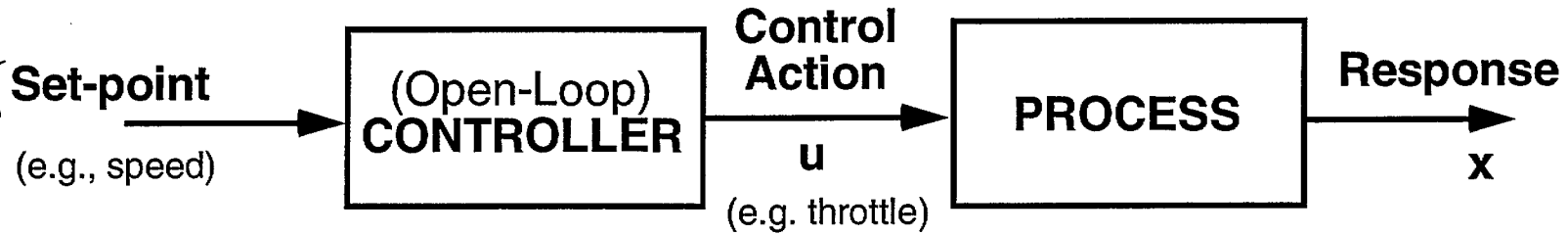
1. What is fuzzy control?
2. What are its advantages & disadvantages?
3. How can I use fuzzy control?

Examples

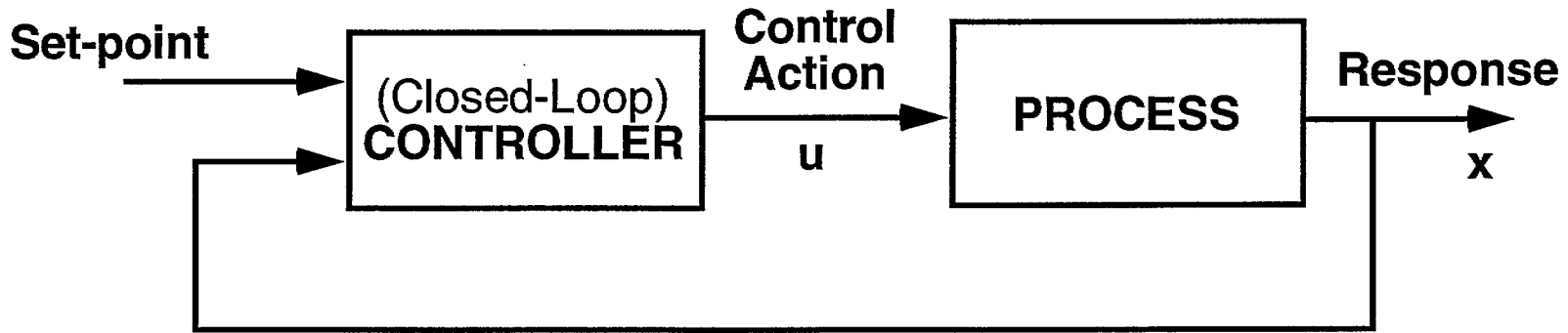
- Temperature control
- PID supervisory control
- Automatic transmission
- Subway train operation
- Consumer products

Set-Point Control: Make Response Follow Command

When knowledge of process is good



Weak/poor process model



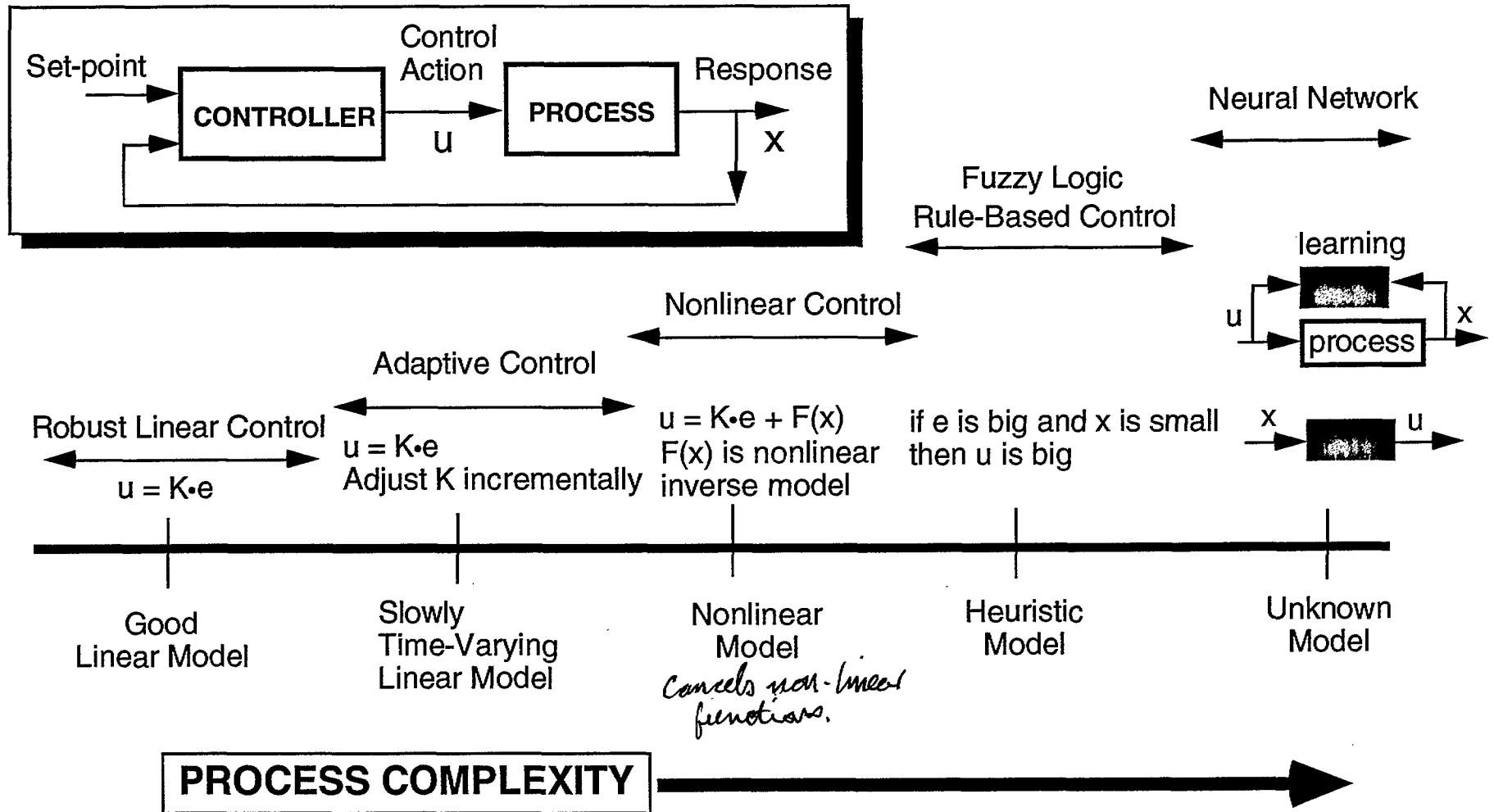
Controller is based on Inverse Model

Process Model: If u is applied, what will x be?

Inverse Model: If we want x , what should u be?



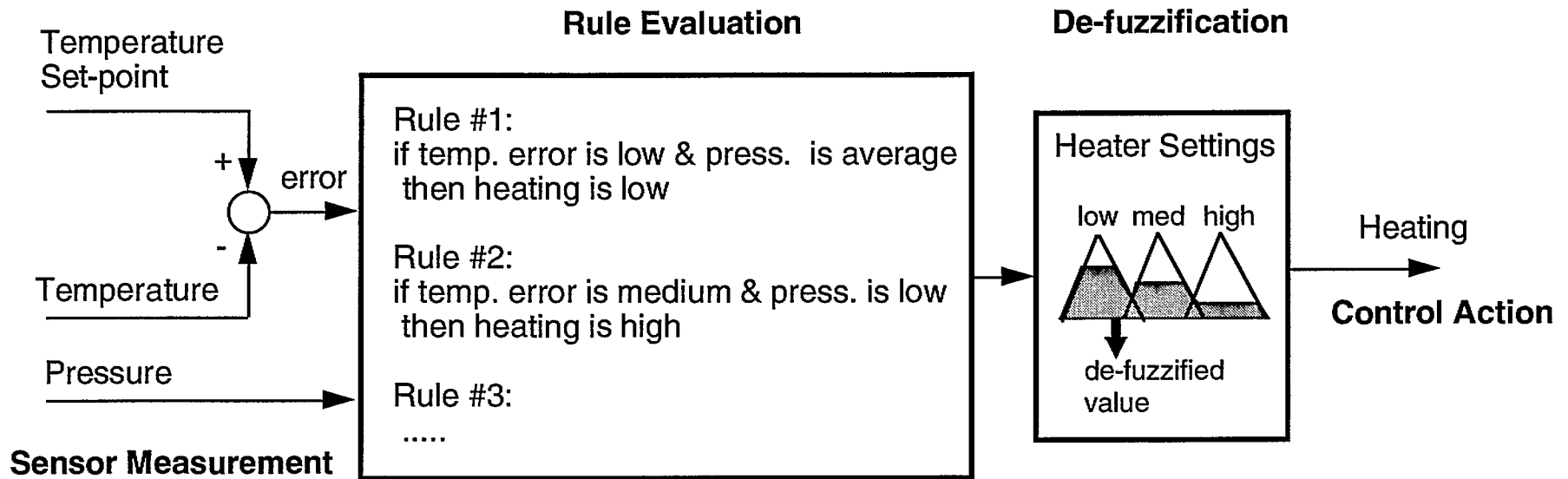
Applicability of Control Methods



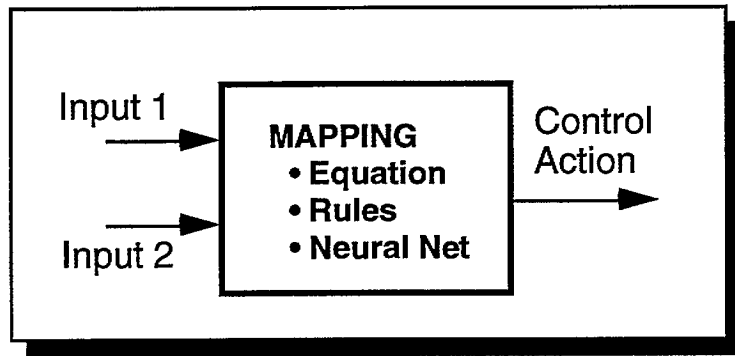
Fuzzy Controller

A controller that uses fuzzy rules to determine control action

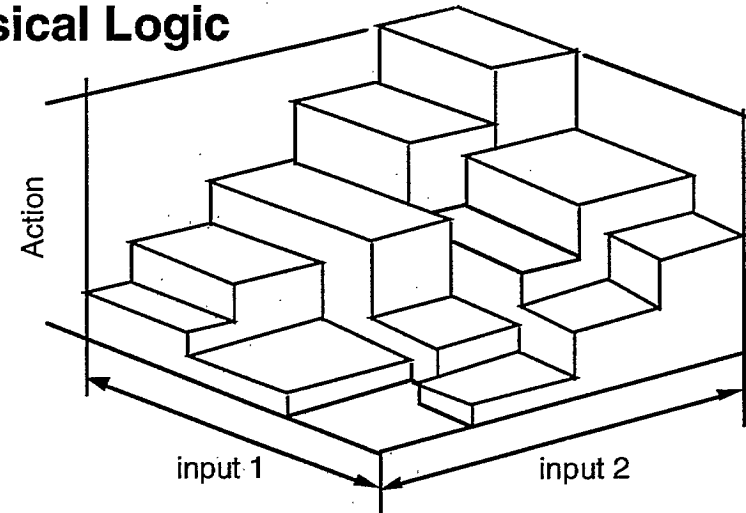
- "If" part of rule is a process state
- "Then" part of rule is a control action



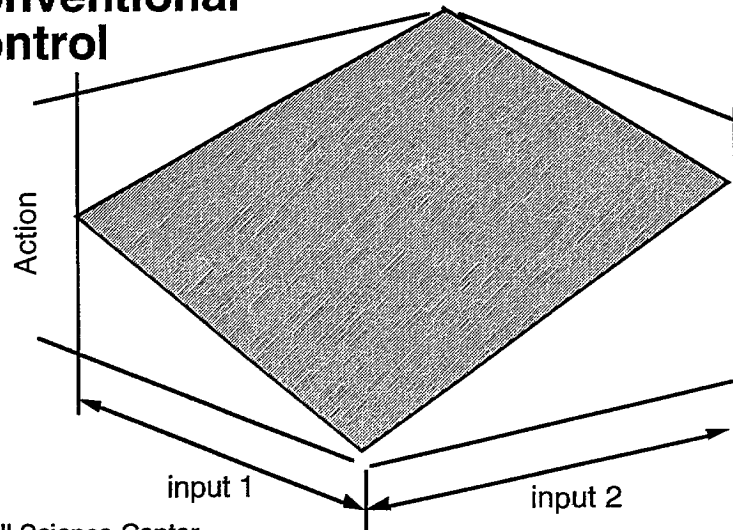
Fuzzy Control = Interpolative Rule-Based Control



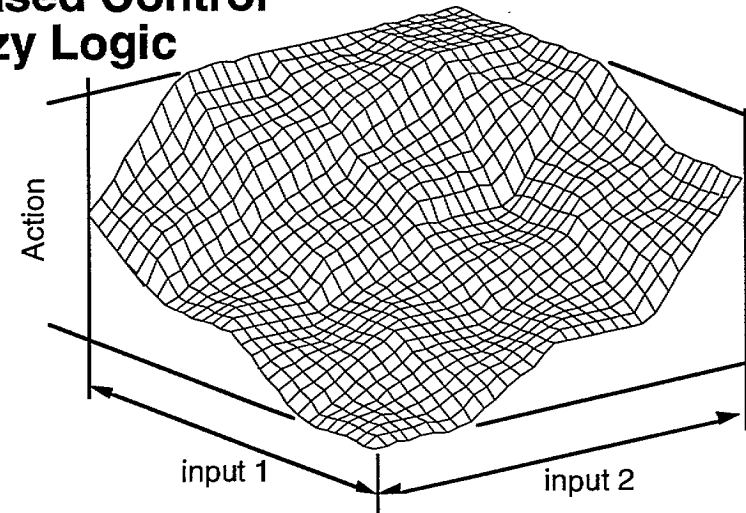
Rule-Based Control via Classical Logic



Conventional Control



Rule-Based Control via Fuzzy Logic



Why Fuzzy Control?

Difficulties in applying conventional control

- **Requires accurate mathematical model of process**
 - expensive to obtain
- **Process is often highly nonlinear**
 - requires many different linear controller designs
- **Control objective limited to a linear quadratic form**
- **Loss of physical insight in large problems**
- **Not applicable to high-level, task-oriented control**

Advantages of fuzzy control

- **Does not require mathematical model of process**
 - A qualitative inverse plant model is implicitly provided by the human expert
- **Control law can be highly nonlinear to exploit process nonlinearity**
- **Complex objective is easily incorporated in control rules**
- **Easy to understand & apply (fast time-to-market)**
- **Easy to maintain & extend**
- **High speed hardware available (> 200,000 rules/sec)**

Why NOT Fuzzy Control?

Disadvantages of Fuzzy Control

- 1. Ad-hoc design methodology**
 - automated design methods exist only for very simple systems
- 2. Lacks well-developed stability & robustness analysis techniques**
 - validate by extensive simulation & prototype testing
- 3. Increased computation**

#1 and #2 apply only to set-point oriented fuzzy control

Essence of Fuzzy Control:

IT LETS YOU EXPRESS WHAT'S IN YOUR MIND

Commercial-Refrigeration/Incubation Module (C-RIM) (Space Industries, Texas)

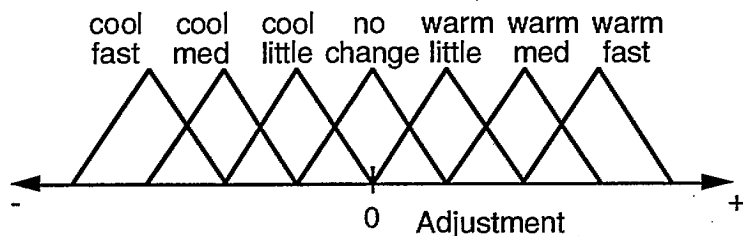
- Controls temperature in chamber for crystal growth experiments
- Flown on Space Shuttle in April 1992



Why fuzzy control?

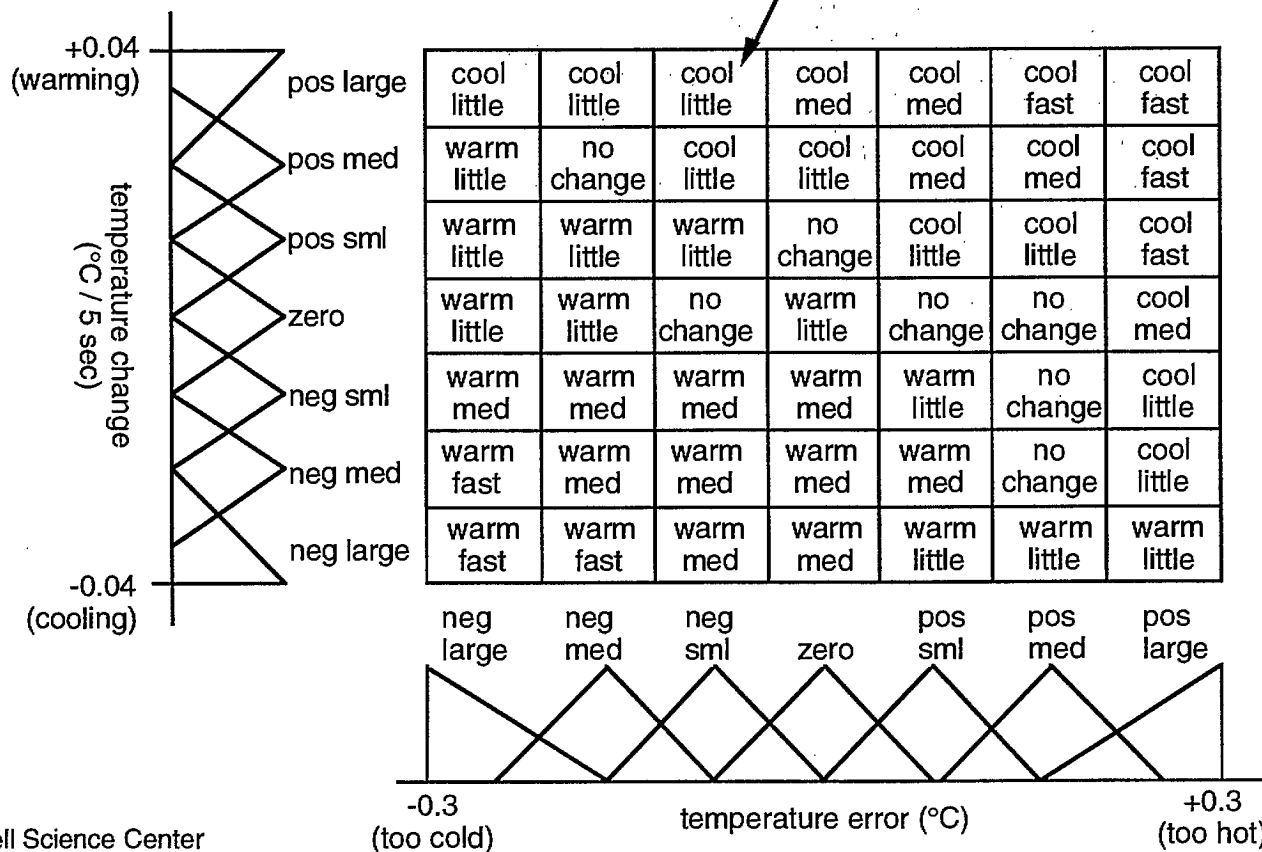
1. **Traditional control techniques did not achieve desired accuracy** (need to control temp. to $\pm 0.5^{\circ}\text{C}$; previous unit can only maintain $\pm 2^{\circ}\text{C}$)
2. **Widely variable thermal load** (no accurate process model)
3. **Had only 10 months development time**

C-RIM Temperature Control Rules



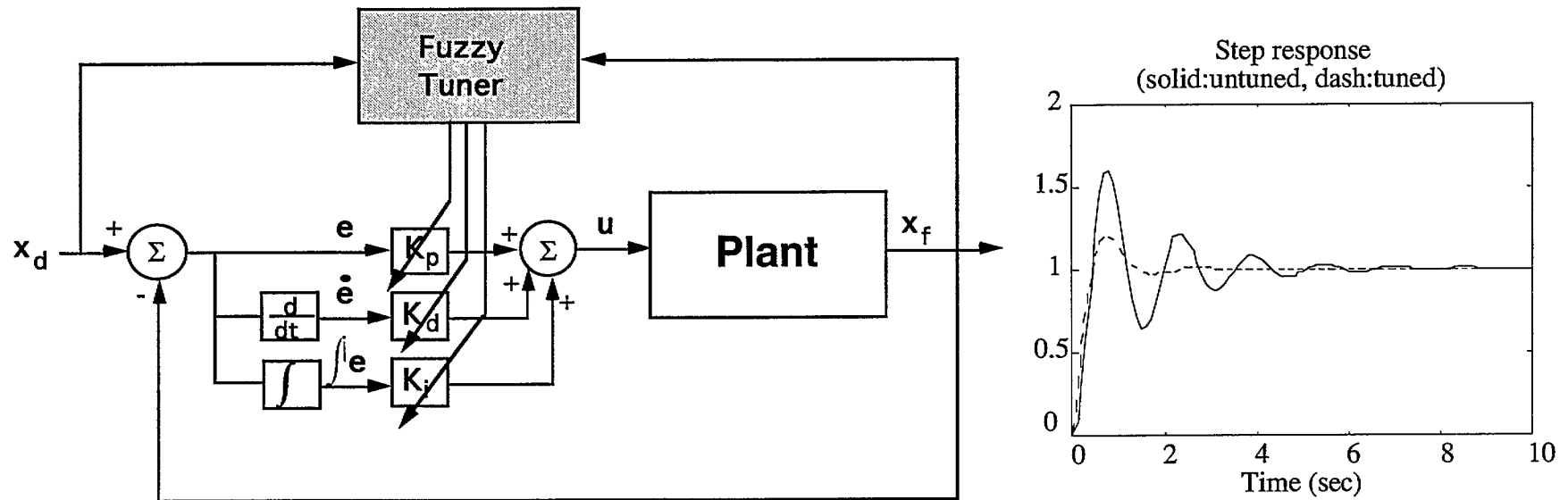
heat pump current = previous current + adjustment
(polarity of current determines heating or cooling)

if error is "neg.sml" & temp change is "pos large"
then adjustment is "cool little"



Supervisory Control: Self-Tuning PID Controller (Rockwell International)

On-line continuous adjustment of PID gains to compensate for changes in plant dynamics



- **23 rules encapsulate PID tuning expertise**
e.g., If damping is low then reduce K_p & increase K_d
- **Self-monitoring algorithm safeguards tuning**

PID Tuning Rules

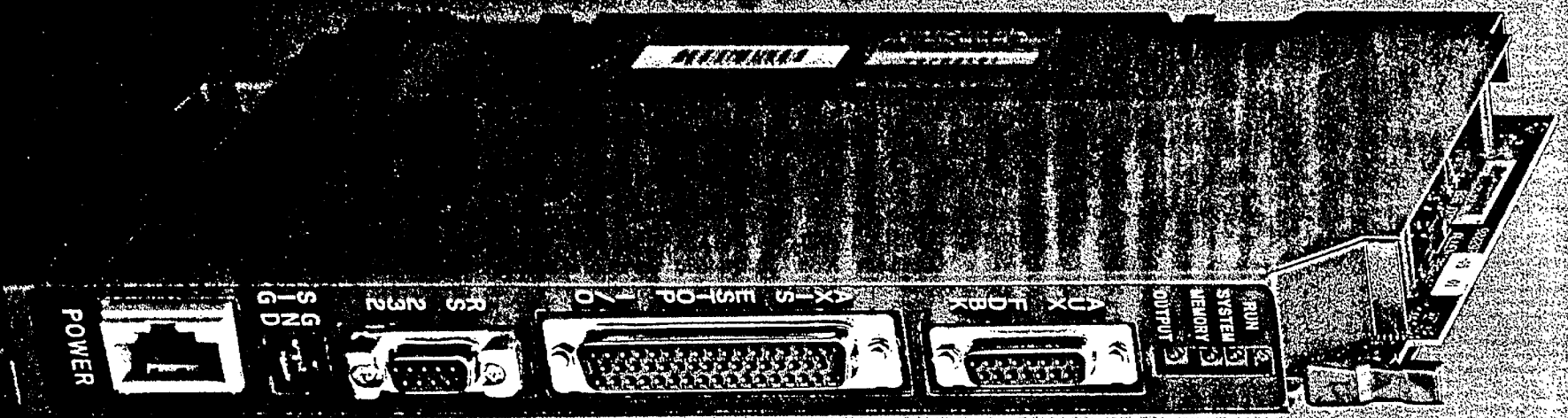
Basic Tuning Rules

if damping is very low then ΔK_p is neg. big & ΔK_d is pos. big
if damping is very high then ΔK_p is pos. big & ΔK_d is neg. big
:
if s.s. error is big then ΔK_i is pos. big
if freq is high then ΔK_p is neg. big & ΔK_i is neg. big

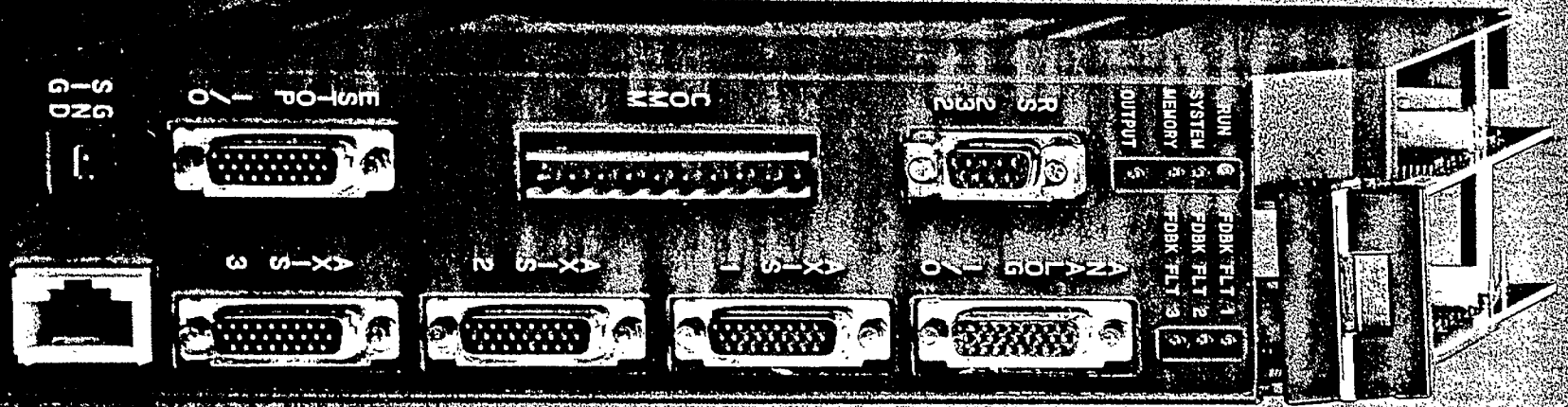
Self-Monitoring Rules

if consistency is high & effectiveness is high then reward factor is high
if consistency is med & effectiveness is medium then reward factor is med
if consistency is low or effectiveness is low then reward factor is low

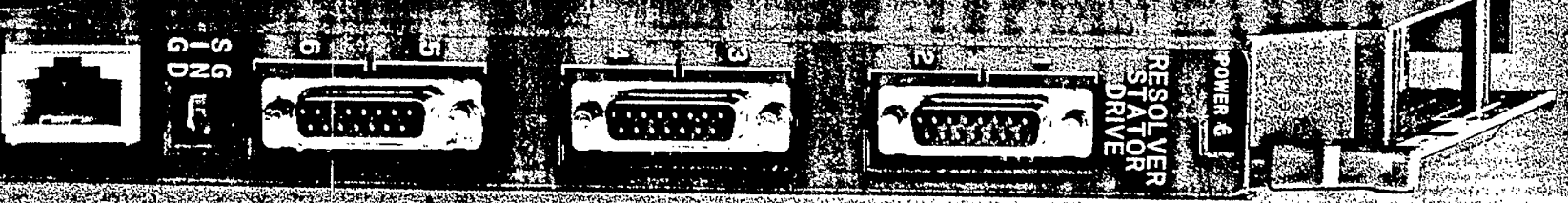
$$\Delta K_{\text{actual}} = \Delta K * RF$$



123



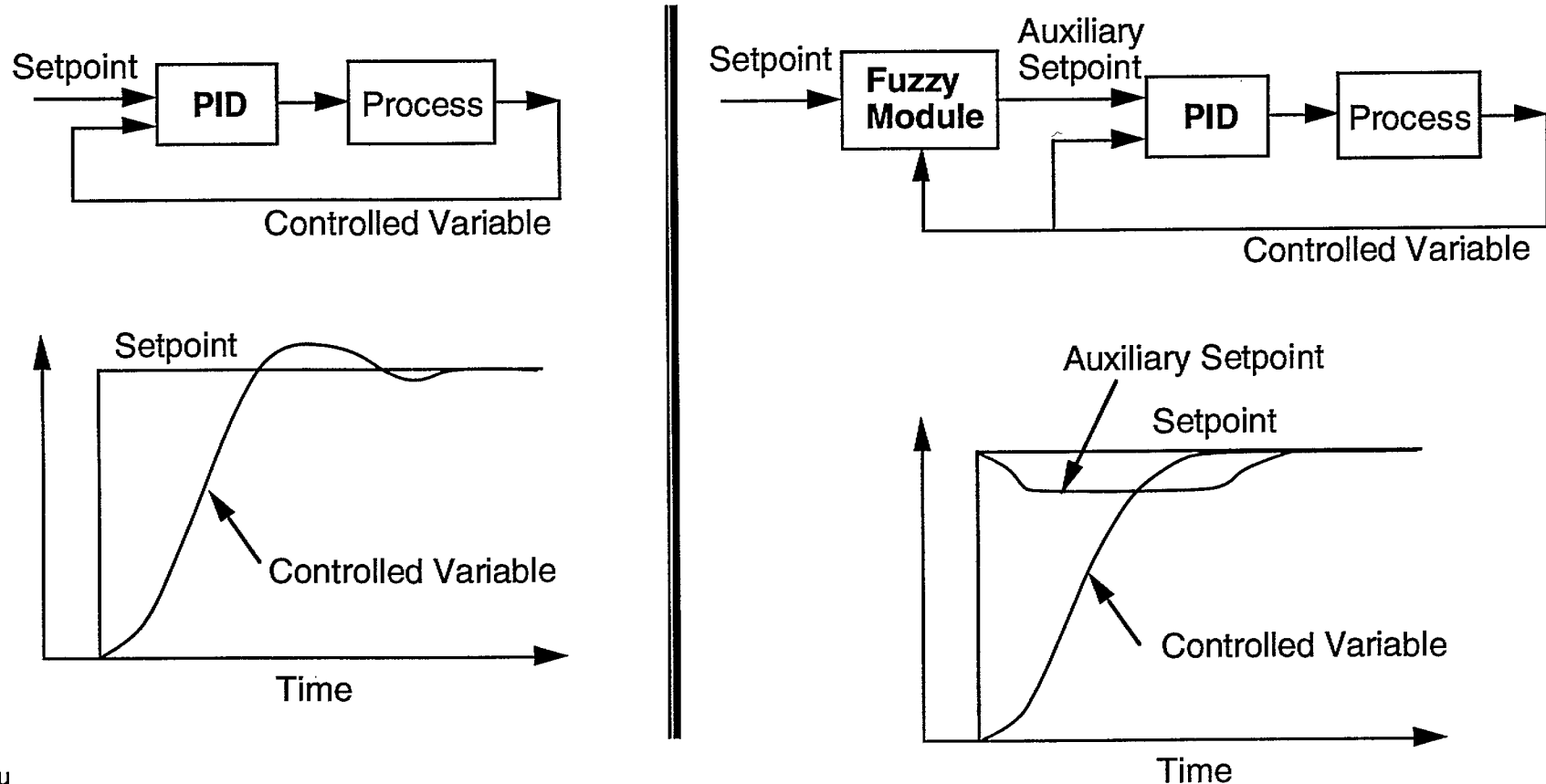
POWER



Fuzzy-Assisted PID Control (Yokogawa Electric)

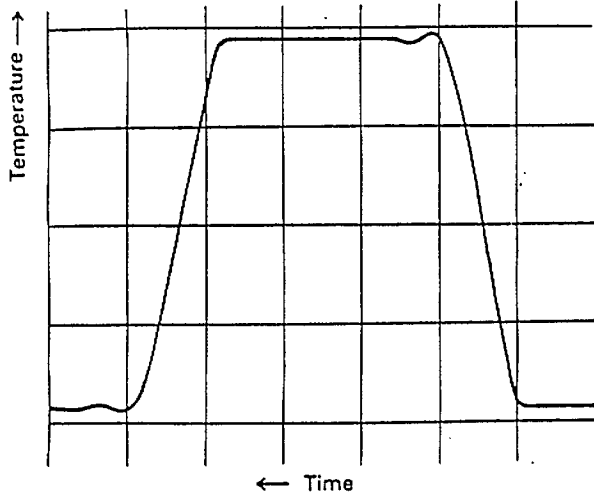
Emulate human operator strategy for suppressing overshoot

1. Sense impending overshoot
2. Change setpoint to "slightly lower" value
3. Monitor deviation & return setpoint "little by little" to desired value

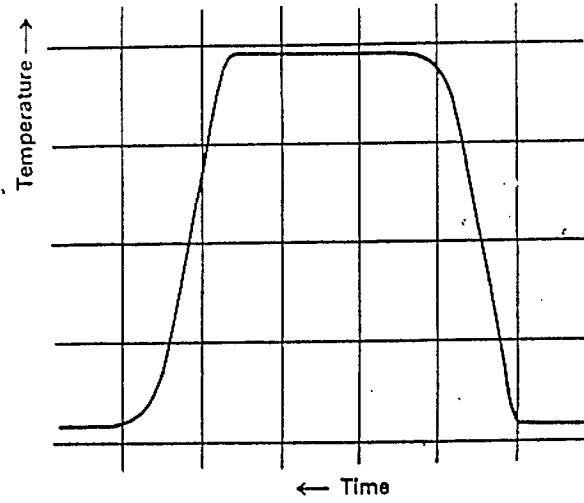


Response to an abrupt change in the setpoint

With "super" OFF

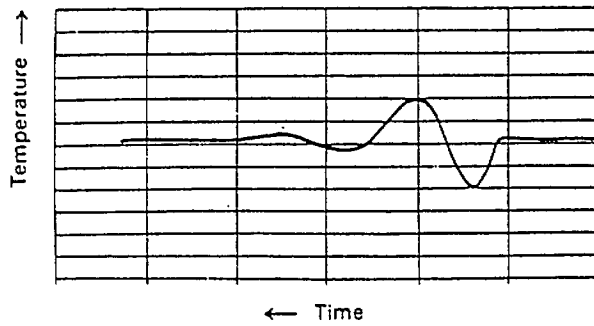


With "super" ON

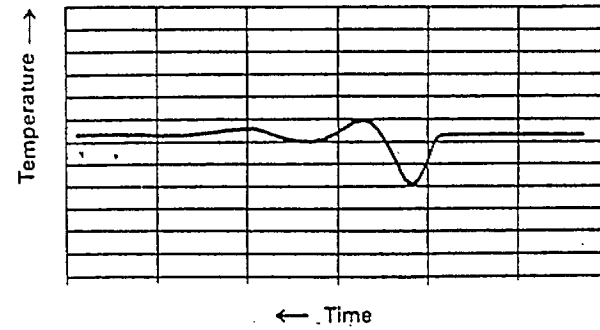


Response to a disturbance

With "super" OFF



With "super" ON

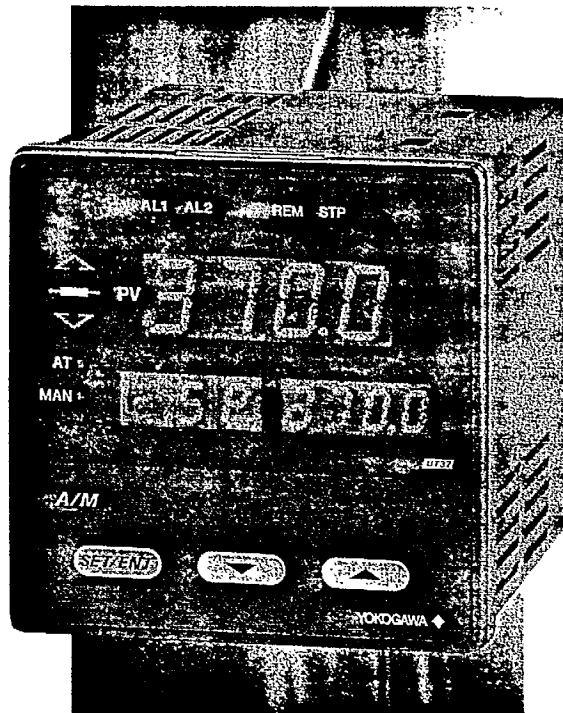


YOKOGAWA

NEW

UT37/UT38

Digital Indicating Controllers



UT37 and UT38 are advanced digital indicating controllers that are simple to use and feature universal input and output types.

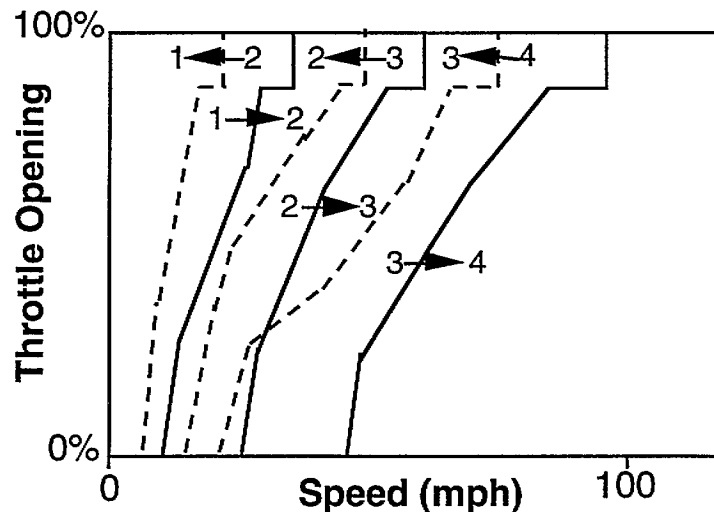
They utilize the exclusive fuzzy logic **SUPER** function to suppress overshoot and improve performance.

Selecting Discrete Control Option: Automatic Transmission (Nissan Motor)

Conventional shift controllers

- Only considers speed and throttle opening
- Do not always match driver's intention
- Do not consider driving condition
e.g., steep incline, passenger load

Typical Shift Pattern for Automatic Transmission



Examples of Bad Shifting:

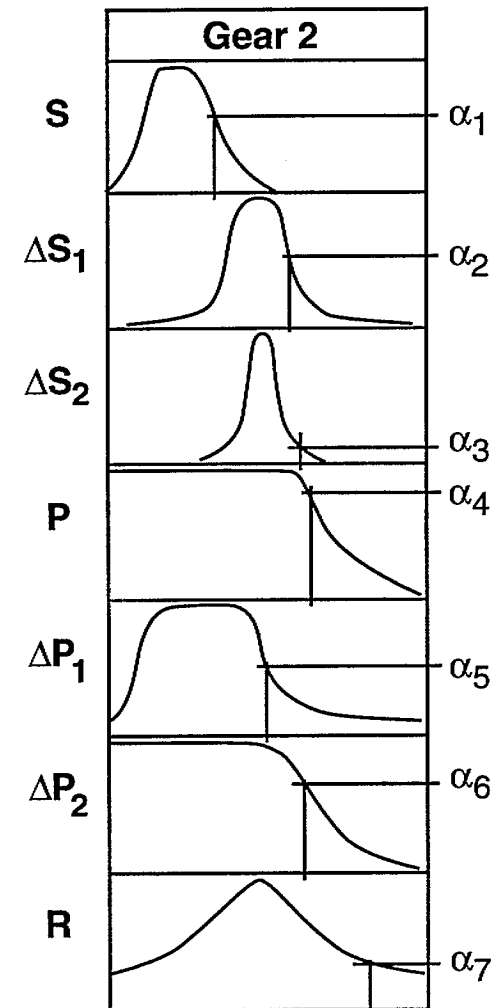
- Driver lets up on accelerator to enter a corner -> shifts to higher gear
- Driver lets up on accelerator to coast down steep incline -> shifts to higher gear

Determining Suitability of A Gear

Inputs to the fuzzy controller

- S = current speed
- P = current throttle opening
- ΔS_1 = change in speed during last 2 seconds
- ΔS_2 = change in speed during last 5 seconds
- ΔP_1 = change in throttle during last clock period
- ΔP_2 = change in throttle during last 2 clock periods
- R = running resistance
 - $R = 1$ corresponds to single driver on flat road
 - higher R means steep incline or increase in passengers
 - R is estimated from speed, throttle opening, and gear position

Suitability of choosing gear 2



For each gear, a set of membership functions describe the condition under which the gear should be chosen

$$G_k = \text{suitability of gear } k = \frac{\sum_{i=1}^7 \alpha_i}{7}$$

Fuzzy Shift Controller

Evaluate the function:

$$S = \frac{G_i * i + G_{up} * G_{i+1} - G_{down} * G_{i-1}}{G_i * i}$$

where

i = current gear number

G_k = suitability of using gear k for the present condition

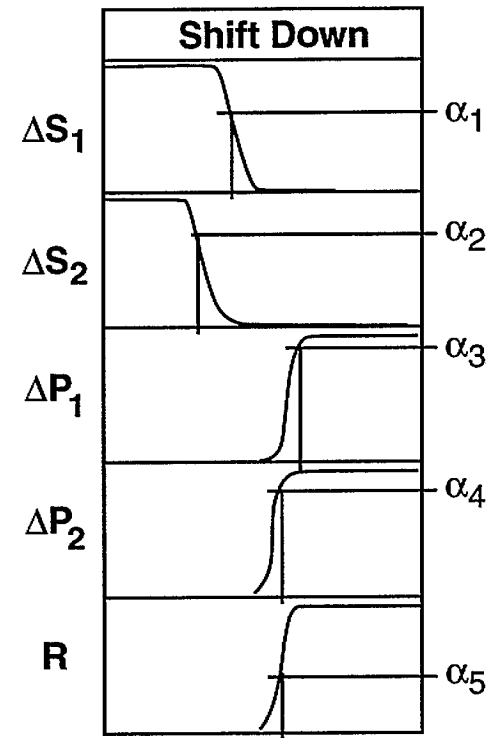
G_{up} = desirability of shifting up

G_{down} = desirability of shifting down

Command upshift if S is greater than 1 by some threshold

Command downshift if S is less than 1 by some threshold

Desirability of shifting down



$$G_{down} = \frac{\sum_{i=1}^5 \alpha_i}{5}$$

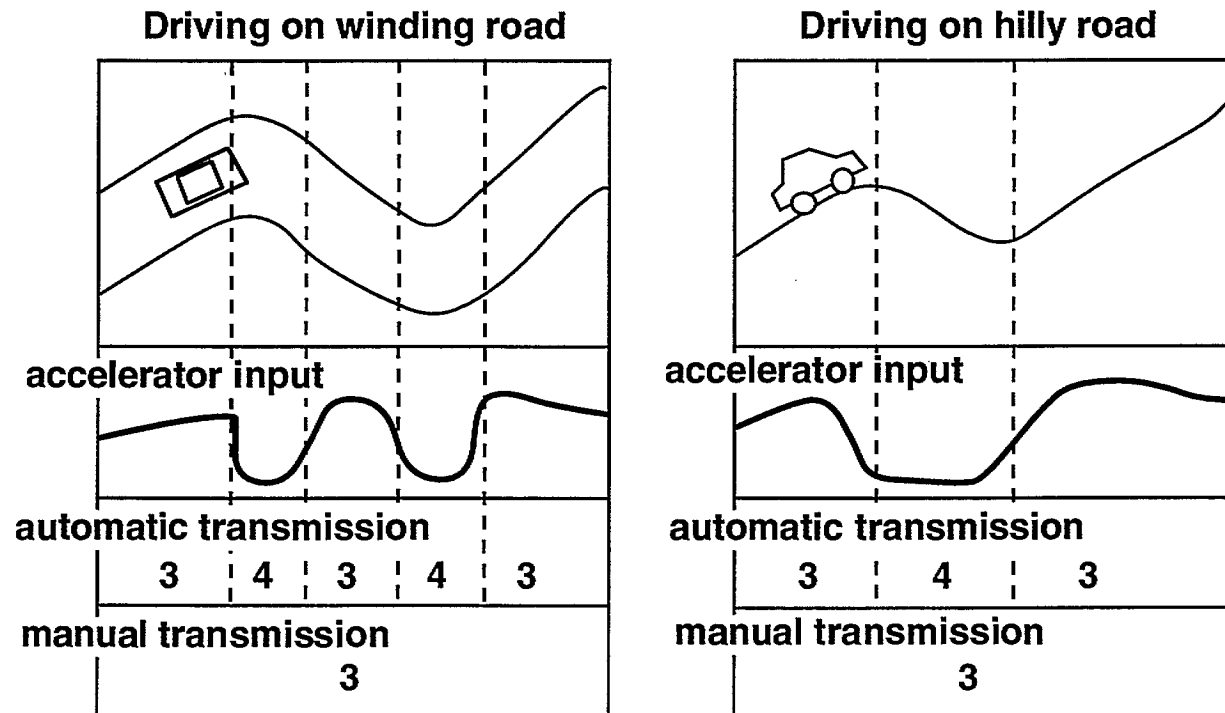
Notable Points in Shift Controller Design

- **A task-oriented fuzzy controller**
- **Fuzzy sets used only to determine degree of similarity between conditions**
 - degrees of similarity are parameters in an analytical criterion function
- **Fuzzy Control \neq Fuzzy Rule-Based Control**

Classification of Operating Environment (Nissan Motor)

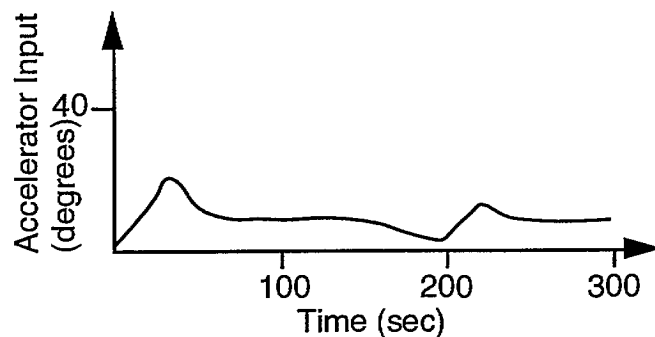
- Automatic transmission should have different shift pattern for driving in different environment, e.g., expressway vs. winding road
- Correct identification of driving environment allows selection of appropriate shift pattern

Gear Shift Behavior

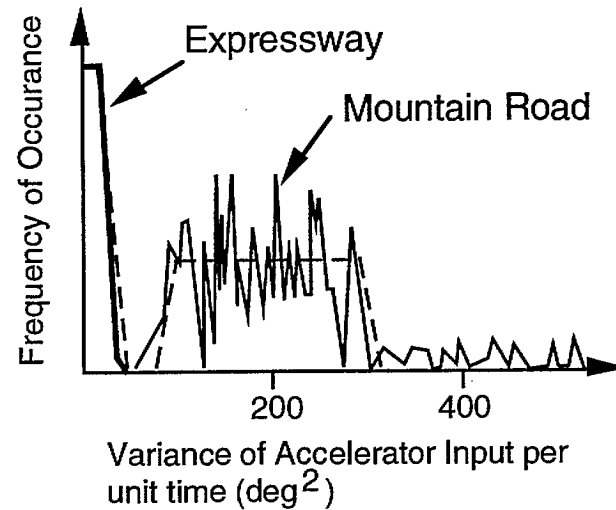
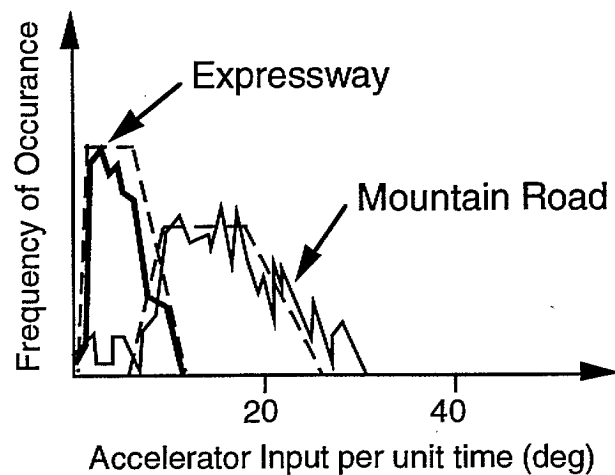
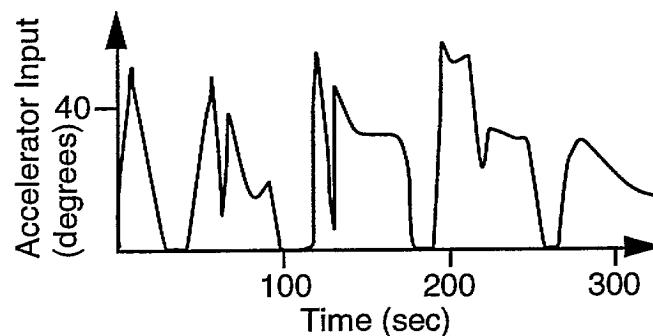


Determining Fuzzy Boundaries for Classification

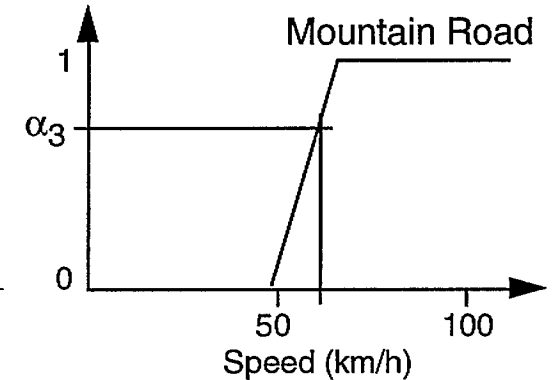
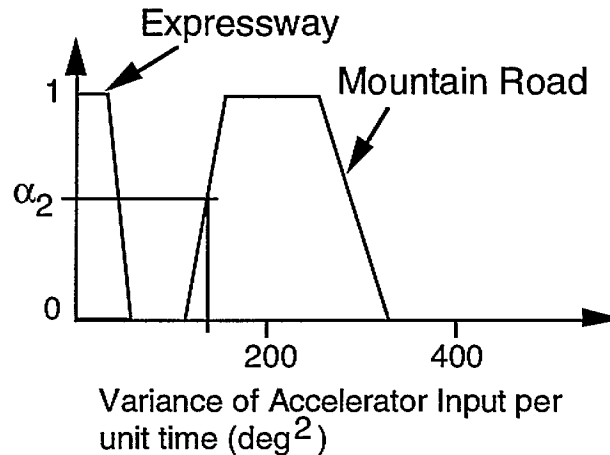
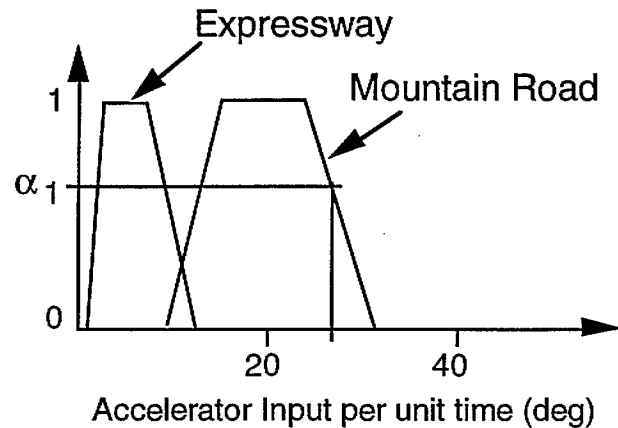
Driving on Expressway



Driving on Winding Mountain Road



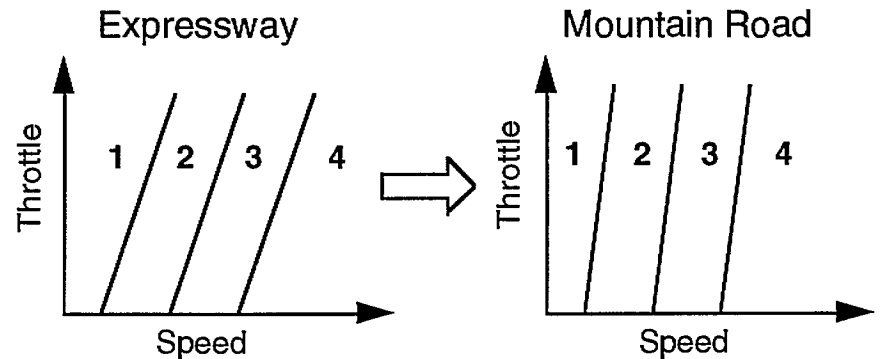
Determining the Class



Degree of match = $\min(\alpha_1, \alpha_2, \alpha_3)$

- **Environment is classified as mountain road if degree of match exceeds some threshold**
- **Change shift pattern according to classification**

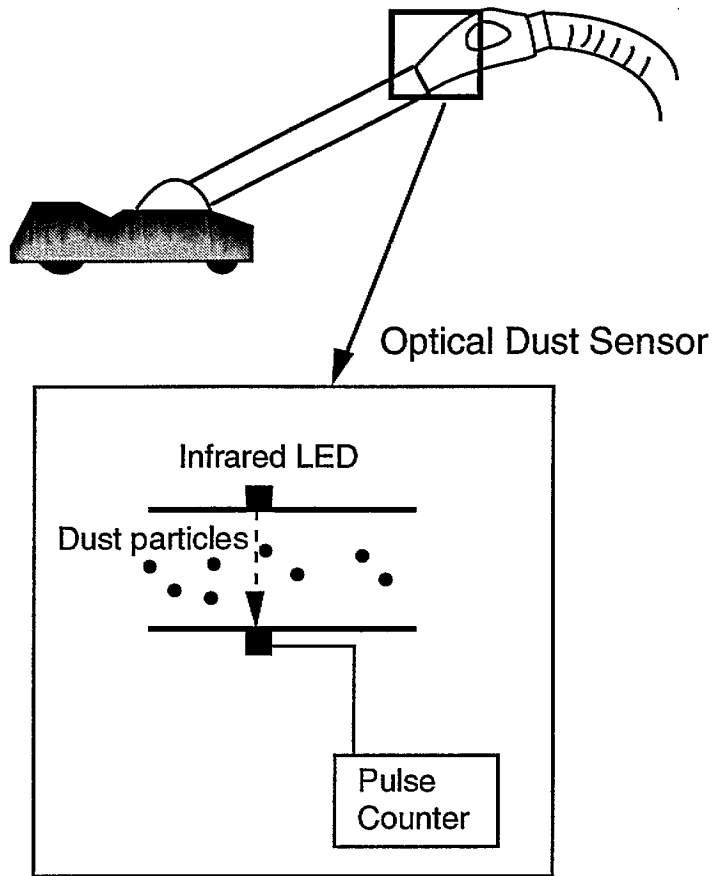
Change in Shift Pattern



Notable Points in Environment Classification

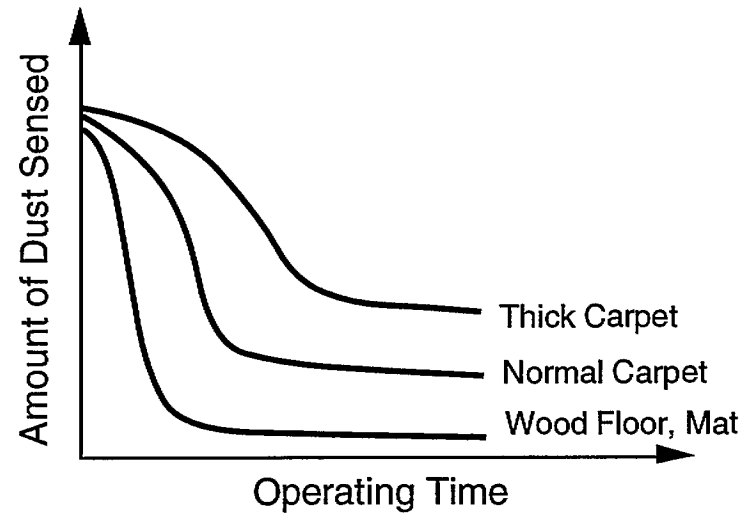
- **Membership functions determined from experimental data, not human description**
- **Used fuzzy logic to classify operating environment - determine which conventional control law to use**
- **No rules**
- **Extension: Classification of driver/user**
e.g., preference for sporty or comfortable drive
- **Used human driver as the sensor and infer the environment from driver behavior**
- **If we can't measure a parameter directly, can we infer it from measurement of some other variables?**

Fuzzy Vacuum Cleaner (Matsushita Electric)

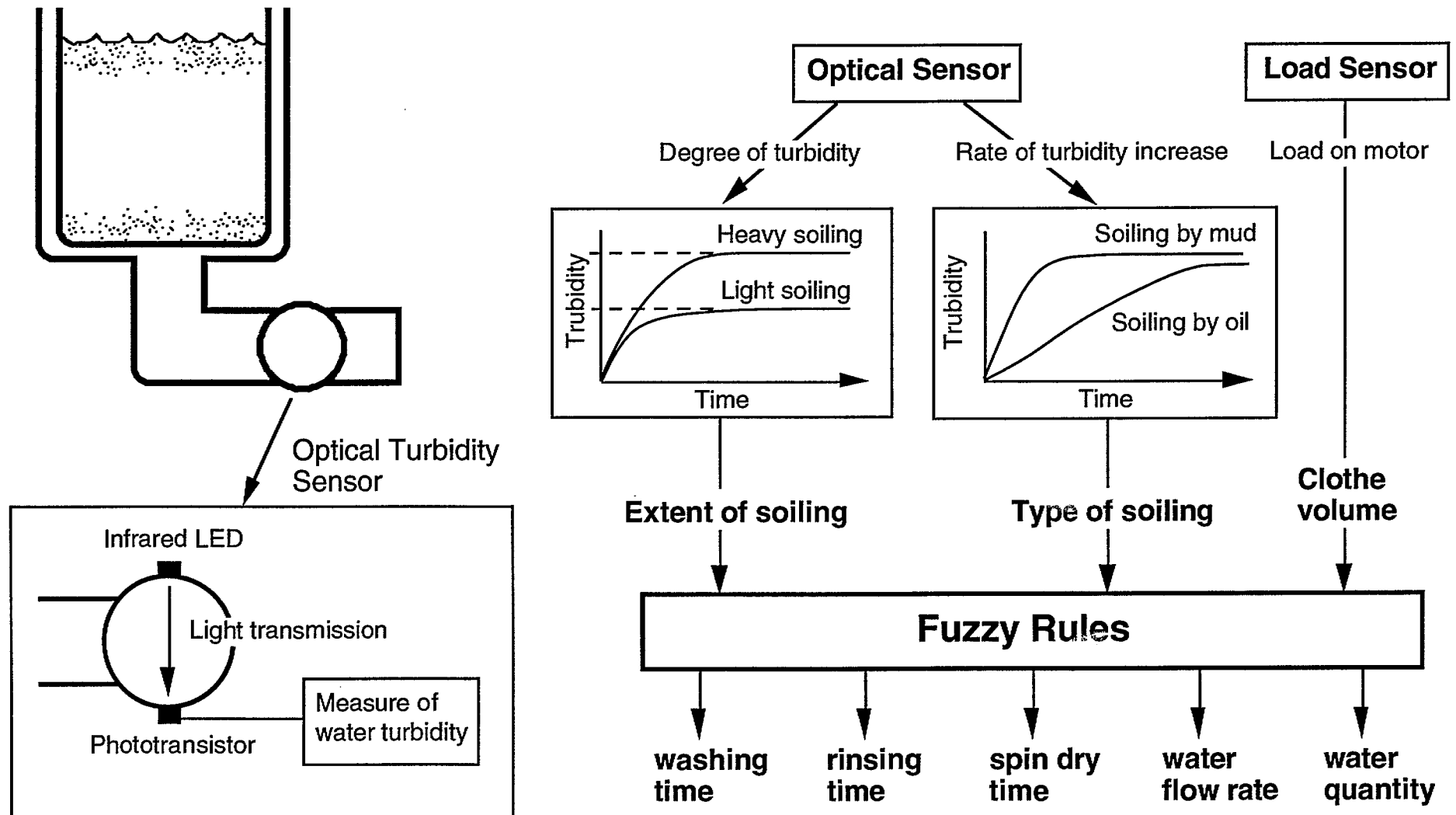


Vacuum power too high => difficult to operate
Vacuum power too low => poor dust pickup

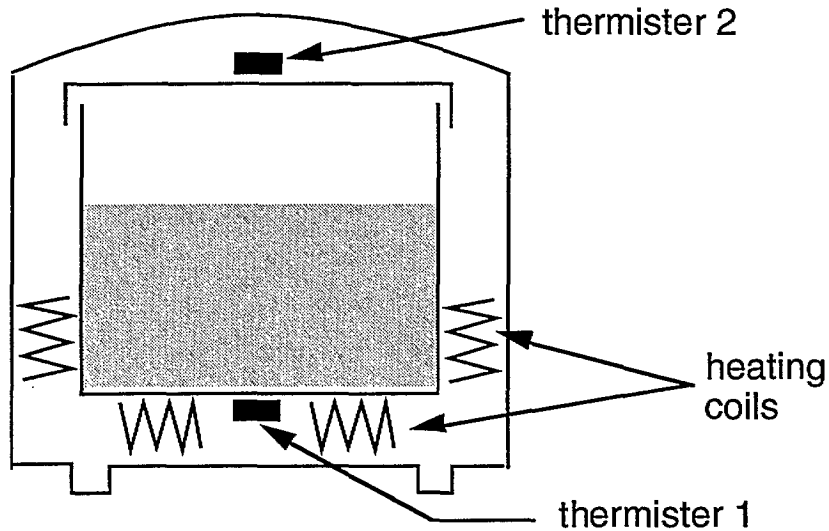
- Optimum vacuum power depends on amount of dust and floor type



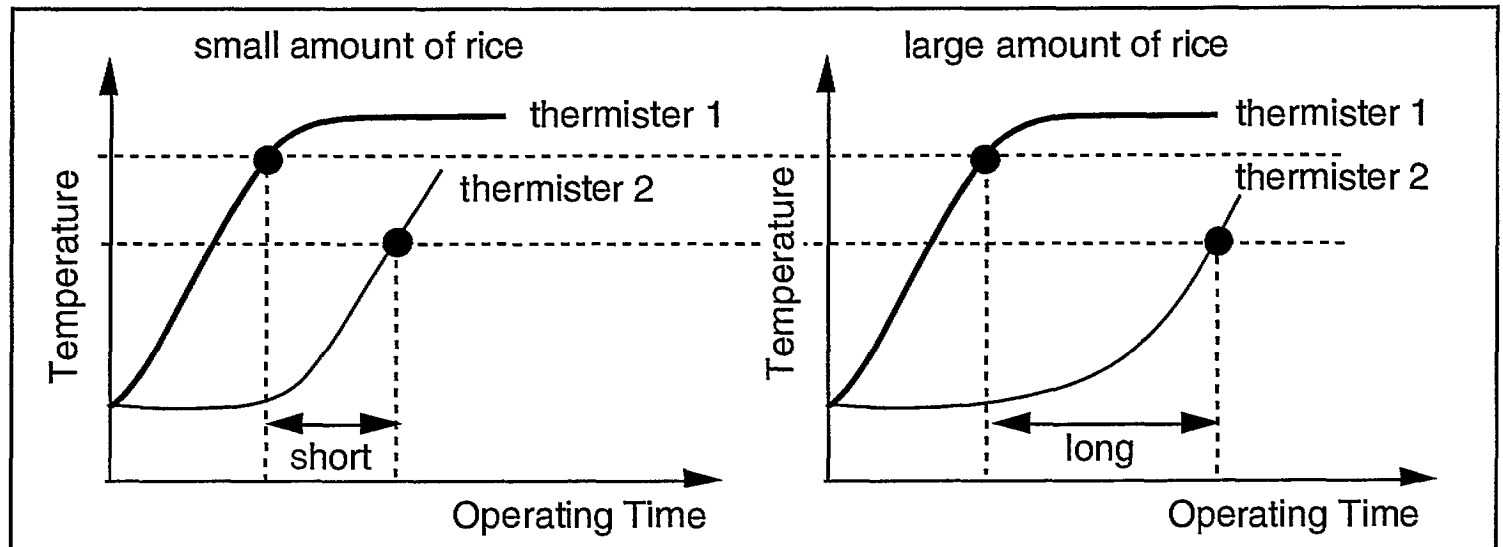
Fuzzy Washing Machine (Matsushita Electric)



Fuzzy Rice Cooker (Matsushita Electric)



- Optimum heating power depends on amount of rice & desired hardness



こんなこともカンタン

簡単にできます。

キーを押せば、液晶の表示が次の表示だけが呼び出せ、操縦の現金自動支払い機と

キーを押せば、好きなかたさに炊き分けられます。

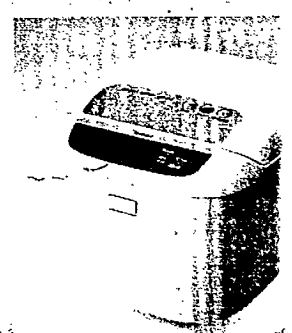
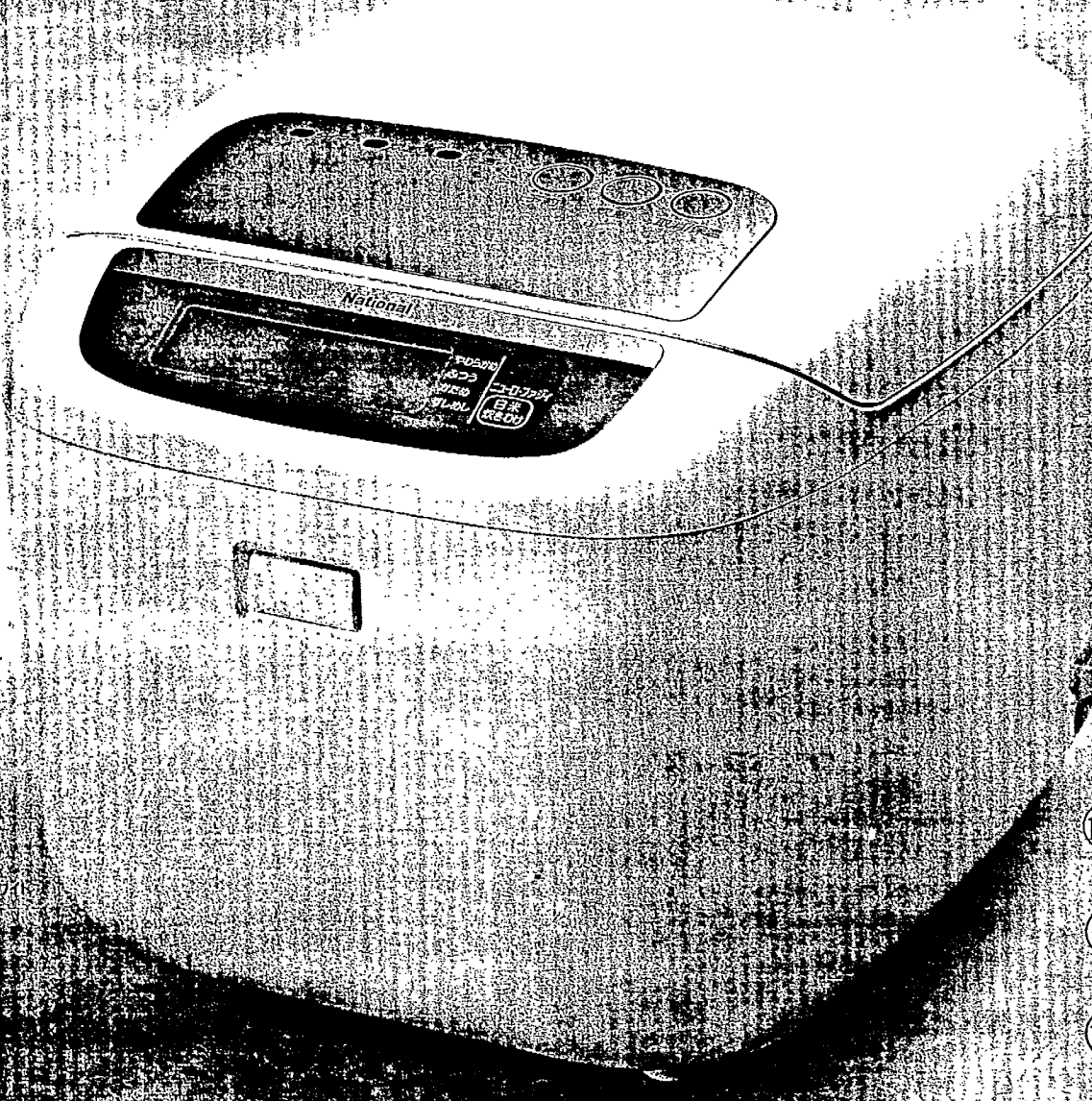
白米炊き分けキー
水加減しなくても、キーを押すだけで、好きなかたさに炊き分けられます。すしめしも水位線を合わせてキーを押せば上手に炊けます。

洗ってすぐでも少量でもおいしく炊けます。

マイコンコントロール
米をつけおきしなくても、マイコンが火力をコントロールして米に水を吸わせながら炊き上げます。少量でも、おいしい火加減が選べます。

食べたい時刻をセットすれば、その時刻に食べられます。

食べ時刻タイマー
例えば、朝の7時30分にはんが食べたい時刻に炊き上がります。



IH ジャー炊飯

- 10ℓ** SR-IH10X1
標準価格54,000円(税別)
消費電力(約):1,060W 大きさ(約):幅25
高さ24cm 色:-Wホワイト,-Cベージュ
- 15ℓ** SR-IH15X1
標準価格56,000円(税別)
消費電力(約):1,270W 大きさ(約):幅27
高さ25cm 色:-Wホワイト,-Cベージュ
- 18ℓ** SR-IH18X1
標準価格58,000円(税別)
消費電力(約):1,270W 大きさ(約):幅27
高さ27cm 色:-Wホワイト,-Cベージュ

早く炊けます。

5機能
ごはんが炊きたとき、お米が炊きたとき、
「白米高速」を選んでくださ
く炊き上がります。

つゆが出ないまま炊飯中は

余分なつゆがとれます。
蒸しらす
ふた部分についたふたヒーターが、余分なつ
ゆをとばしながら炊き上げます。つゆうけがない
のでお手入れもカンタンに。

ボタンを押すだけ、

指一本でふたが開けられます。
ワンタッチ自動オープンのふた
ボタンを軽く押すだけ。ふたが自動的に開き
ます。何かを持っているときや手がぬれていると
きなどはとくに便利です。

炊きこみごはんのほかにも

いろいろつくれます。
5メニュー選択キー
メニューキーを選べば、白米・炊き
ごんのほか、白米高速、おかゆ、玄米、
(おこわなど)もようすにつくれます。

掲載しております商品の価格には消費税は含まれておりませんので、ご購入の際、別途消費税額をお支払いください。

Notable Points in Many Fuzzy Consumer Products

- **Fuzzy approach PLUS additional sensor info provided new capability**
- **Fuzzy logic is a powerful paradigm, but it's not magic**
- **The solution to a problem often lies in finding creative ways to infer additional information**
 - "If I were to perform this task (or perform it better), what additional info would I need?"
 - "If I can't measure it directly, how can I infer it?"
- **Fuzzy logic fosters a new mindset in product development; opens up possibilities**

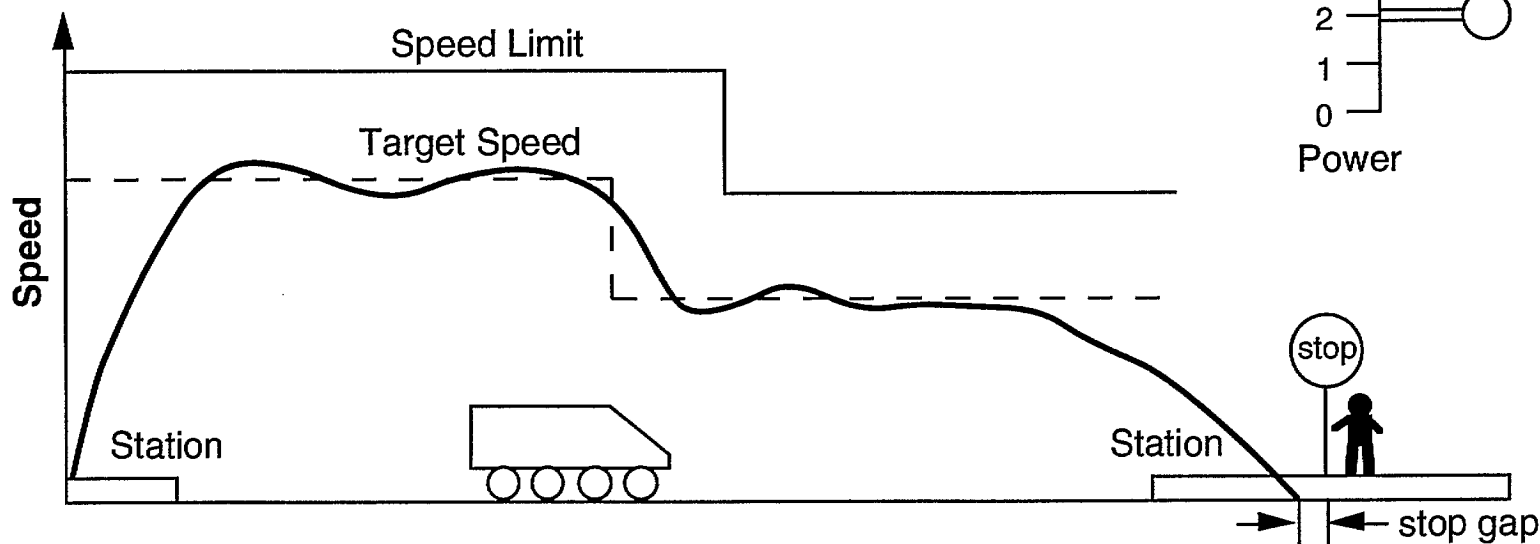
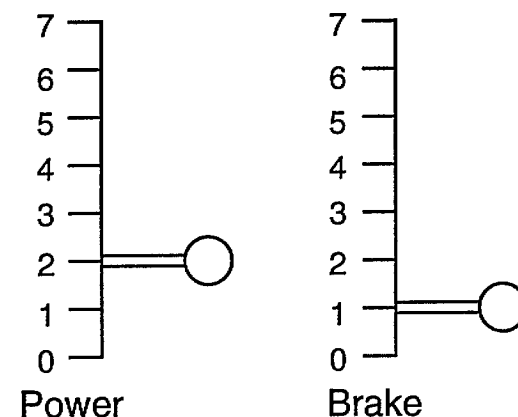
Predictive Fuzzy Control: Subway Train Operation (Hitachi)

*Sendai Subway System - 1987 - key application - repeatable results
Have raised credibility of F/L*

Train Operation Criteria:

- Safety = $F(\text{time to danger zone, speed})$
- Comfort = $F(\text{amount of notch change, time since last notch change})$
- Traceability = $F(\text{deviation from target speed})$
- Stop gap distance
- Energy consumption

Control Notches



Notable Points in Subway Train Controller

- Control based on prediction & ranking of possible control actions
- Fuzzy rules used to rank the results of candidate actions
- Balance of multiple performance criteria
- Qualitative factors, i.e., "comfort" and "safety", can be extracted from measurable parameters



Summary

- **Fuzzy control = using fuzzy logic in control application**
 - Implement nonlinear control function
 - Perform supervisory control
 - Classify operating environment/select conventional control law
 - Rank results of candidate control actions

- **Fuzzy logic allows you to express what's in your mind**

- **Two levels of fuzzy control**

- Low level, set-point oriented

- can use conventional techniques

High payoff — -High level, task oriented (\$\$\$!) cannot " " "

- **Fuzzy systems are usually based on simple, qualitative strategies, are easy to develop (fast time-to-market) and easy to understand (ease of maintenance)**

- **Commercial applications aimed at "human-friendly" machines**

- Increased convenience

- Increased match with human intentions/objectives



Software Tools for Fuzzy Control

**First Canadian Workshop on Fuzzy Logic & Industrial Applications
March 17, 1994**

Stephen L. Chiu

**Rockwell International Science Center
1049 Camino Dos Rios
Thousand Oaks, CA 91360
Email: slc@risc.rockwell.com**

**** Many viewgraphs used in the presentation of development tools are provided by courtesy of the following companies:
Apronix, Fuzzy Systems Engineering, HyperLogic, INFORM, Integrated Systems Inc., and Togai InfraLogic.**

Outline

- **What tools are available for fuzzy control product development?**

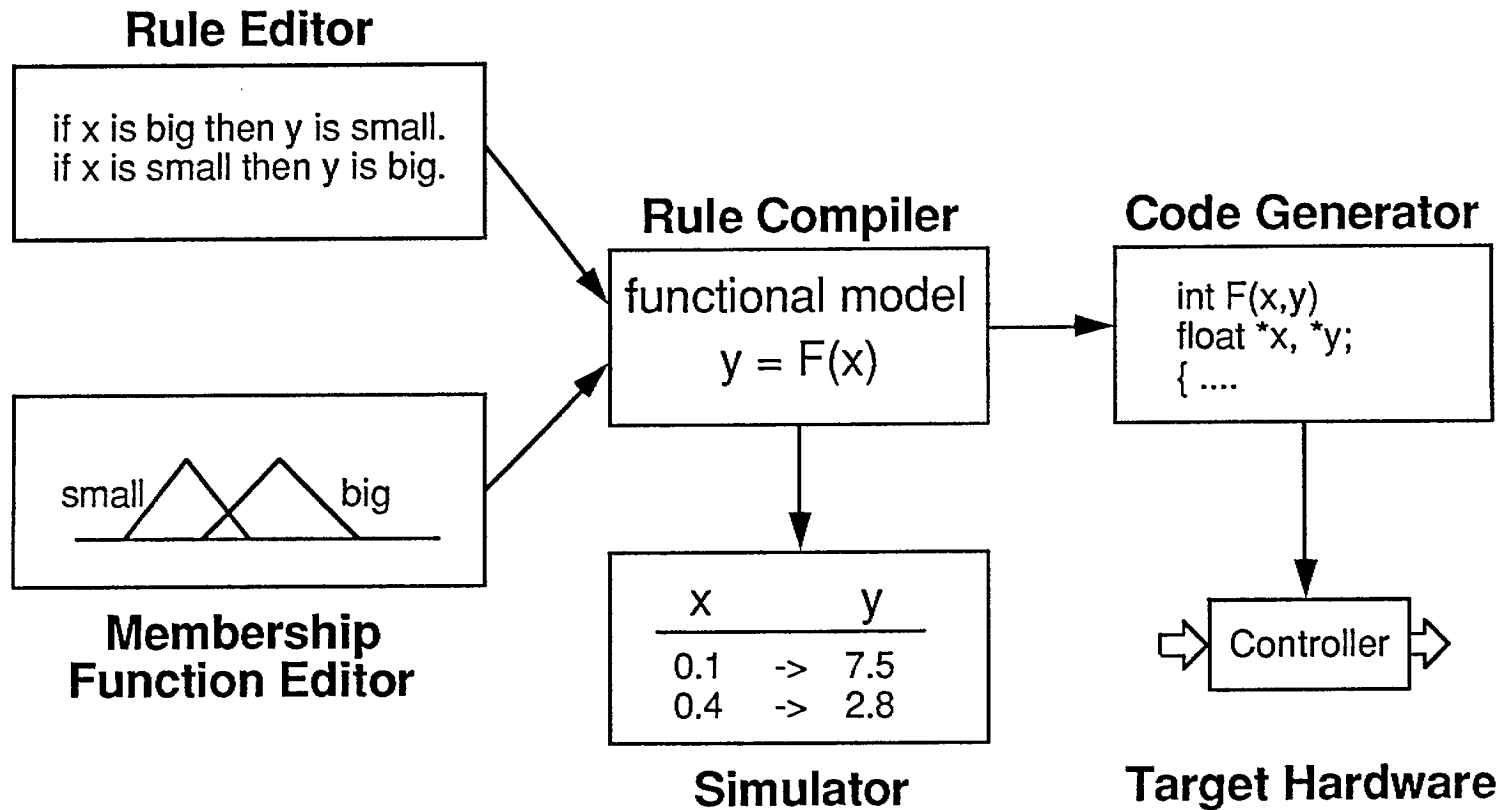
- CubiCalc (HyperLogic)
- TIL Shell (Togai InfraLogic)
- fuzzyTech (INFORM)
- FIDE (Apronix)
- RT/Fuzzy (Integrated Systems Inc.)
- A-B FLEX (Allen-Bradley)
- Manifold Graphics Editor (Fuzzy Systems Engineering)
- Fuzz-C (Byte Craft Ltd.)

...

- **Which one is best suited for my needs?**

Price range \$100 to \$25k

Common Features of Fuzzy Software Tools



CubiCalc

Rule Development

CubiCalc Shell

Code Generation

Run-time Compiler
(CubiCalc RTC)

Rule Base
Data Structure File

Object
Code Library

C Source Code
Library

80x86
Processor

Generic
Processor

- A Windows-based software for IBM PC

- Graphical fuzzy def. editor

- Test rules with data received from:

Interactive user input

File input

Other Windows Application (via DDE)

Built-in process simulator

- Designed for non-programmers

CubiCalc Displays (Fuzzy Definitions)

The screenshot displays the CubiCalc application window titled "CubiCalc: INVENT.CBC". The menu bar includes "File", "Edit", "Definitions", "Options", "Execute", and "Windows".

The main window is divided into two panes:

- Adjectives for SalesRate:** This pane shows a graphical editor for fuzzy sets. The vertical axis represents membership values from 0.0 to 1.0. A dashed line forms a V-shape, representing a fuzzy set. A "Tools" palette is visible, containing various graphical elements like triangles, rectangles, and arrows. Below the tools, the word "Falling" is displayed.
- Rules:** This pane contains a text editor with the following rules:

```
If OnOrder is high then Order should be small;  
If (OnOrder is medium or BackLog is normal)  
and SalesRate is not Falling  
then Order should be normal;  
If OnOrder is low and SalesRate is not Falling  
then Order should be large;
```

Graphical editor
for fuzzy sets

Define English-like rules
with builtin text editor

CubiCalc Displays (Rule Execution and Simulation)

CubiCalc: INVENT.CBC
File Edit Definitions Options Execute Windows

User Interaction

| | |
|------------|--------|
| SalesMax | 300.00 |
| SalesMin | 100.00 |
| NewSales | 233.00 |
| Iterations | 140.00 |

Output Log

| Shipped | TotalOnOrder | Delivered | NewSales |
|---------|--------------|-----------|----------|
| 264.00 | 1027.0 | 263.00 | 263.00 |
| 263.00 | 1012.0 | 257.00 | 260.00 |
| 257.00 | 1000.0 | 254.00 | 257.00 |
| 254.00 | 990.00 | 253.00 | 253.00 |
| 253.00 | 977.00 | 248.00 | 250.00 |
| 248.00 | 966.00 | 245.00 | 247.00 |
| 245.00 | 957.00 | 244.00 | 243.00 |
| 244.00 | 943.00 | 240.00 | 240.00 |
| 240.00 | 930.00 | 237.00 | 237.00 |
| 237.00 | 919.00 | 236.00 | 233.00 |

Plot: Units

Enter values
Interactively

Log to file
or window

Plot to scatter chart
or scrolling strip chart

CubiCalc Displays (Control System Simulation)

The screenshot shows the CubiCalc software interface. The main window title is 'CubiCalc TRUCK.CBG'. The menu bar includes 'File', 'Edit', 'Definitions', 'Options', 'Execute', and 'Windows'. A 'Restart Options' dialog box is open, with the following settings:

- Auto-Restart If:**
 - End-of-file reached:
 - Data off plot
- On Restart:**
 - Clear plots
 - Reset log file
 - Randomize inputs
 - Anywhere in range
 - Within 45% of initial value
 - Within 25% of initial value
 - Within 5% of initial value

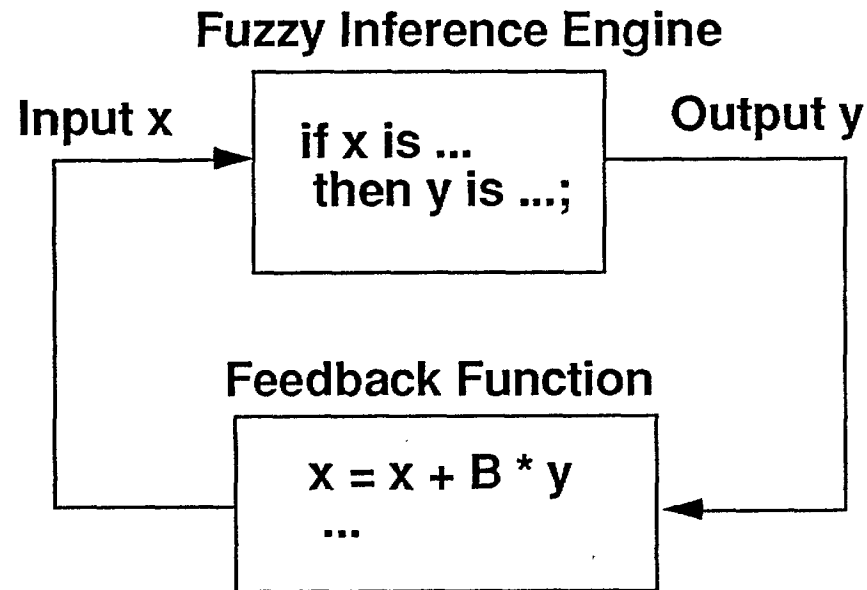
Buttons for 'OK' and 'Cancel' are at the bottom of the dialog. To the right, the 'Plot Truck Yard' window shows a graph with a vertical axis from 0.0000 to 100.00 and a horizontal axis from 0.0000 to 100.00. The plot shows a vertical line at x=50, with a horizontal line at y=80, and a curved path starting from (50, 80) and arching upwards. Below the plot is the 'Simulation' window, which contains the following code:

```
#  
# Calculate new coordinates.  
X = X + (Speed * cosd(Phi));  
Y = Y - (Speed * sind(Phi));
```

Generate random
test cases automatically

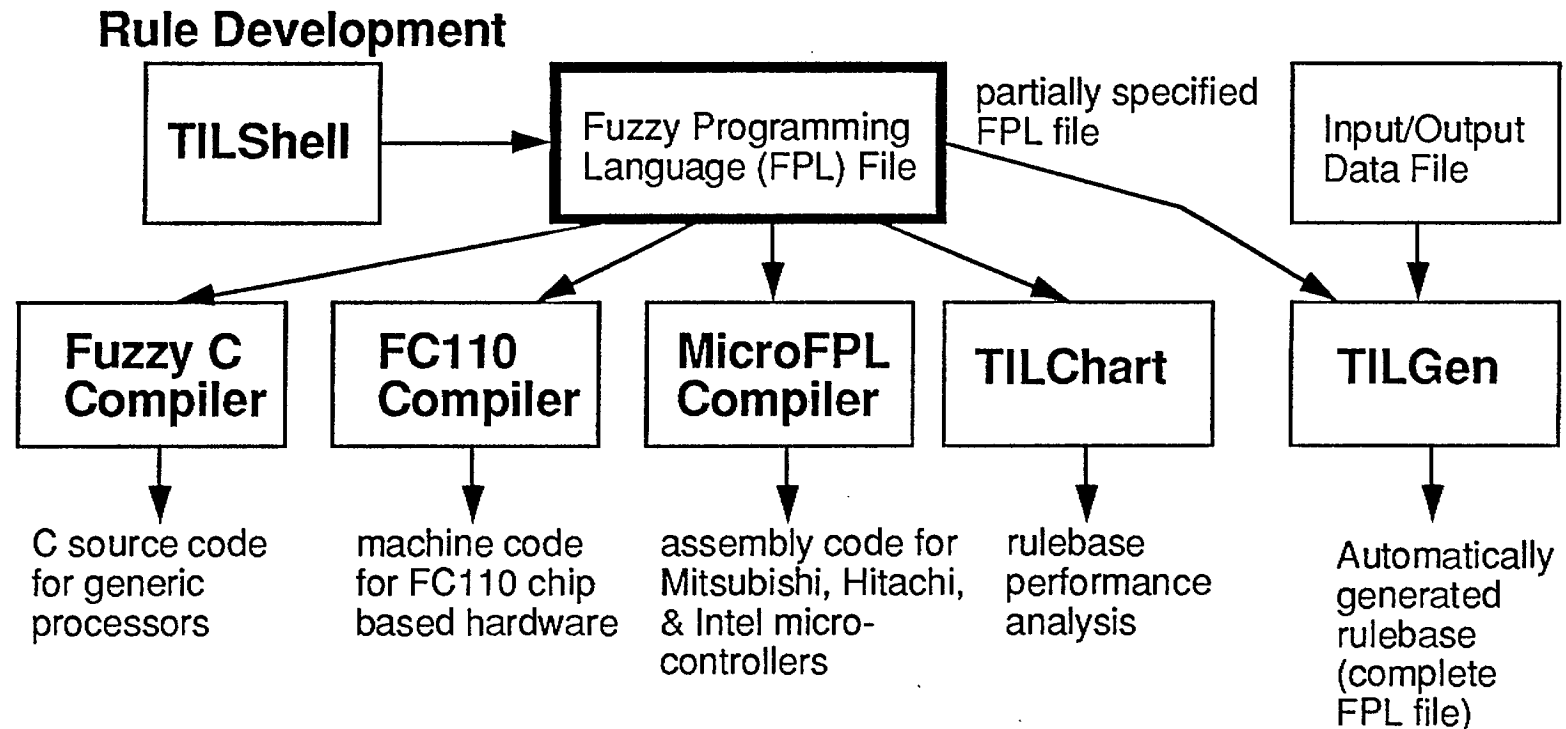
Simulate system
response

CubiCalc's Process Simulator



- **Feedback function specifies next input value**
- **Suitable for simulating simple processes**

TILShell

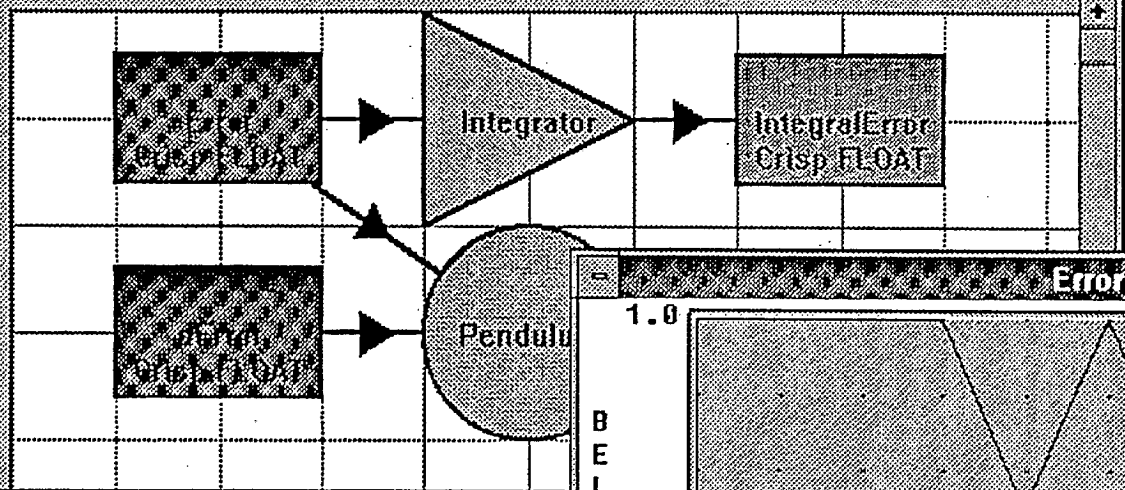


- **Sophisticated CASE-like tool for PC & SUN**
- **Graphical front-end for creating FPL files used by other TIL tools**
- **High-speed hardware support**
- **Designed for programmers & development engineers**

Legend Grid Full Graphics
 Full Screen Snap To Grid

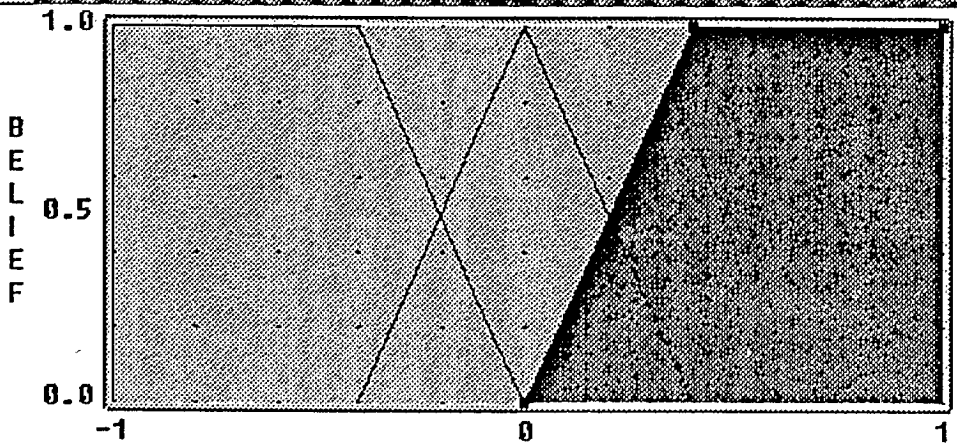
Pend

Project Manager



- [-] Pend
 - Pendulum
 - Error
 - dError
 - Current
 - IntegralError
 - Pend_Simulation

Error



Edit VAR

Set Min/Max

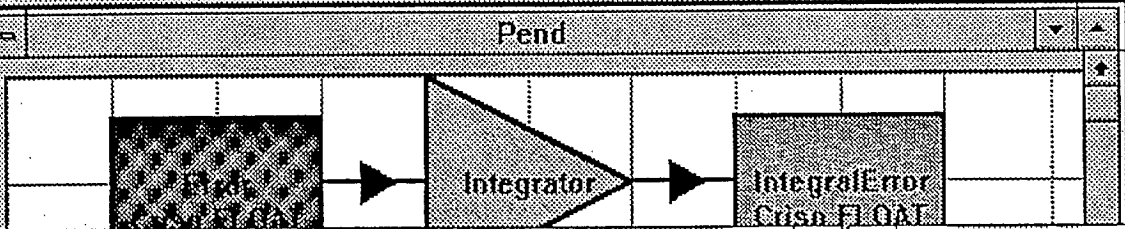
(+0.4, 1.00)

N
 Z
 P

Pendulum

| | | ERROR | | |
|----------------------------|---------------------------------|-------|----|----|
| | | N | Z | P |
| D E R R O R | C U R R E N T | | | |
| | N | | PS | NS |
| | Z | PB | Z | NB |
| P | PS | NS | | |

Name: Rule7 Weight: 100% Rules: 10



Project Manager

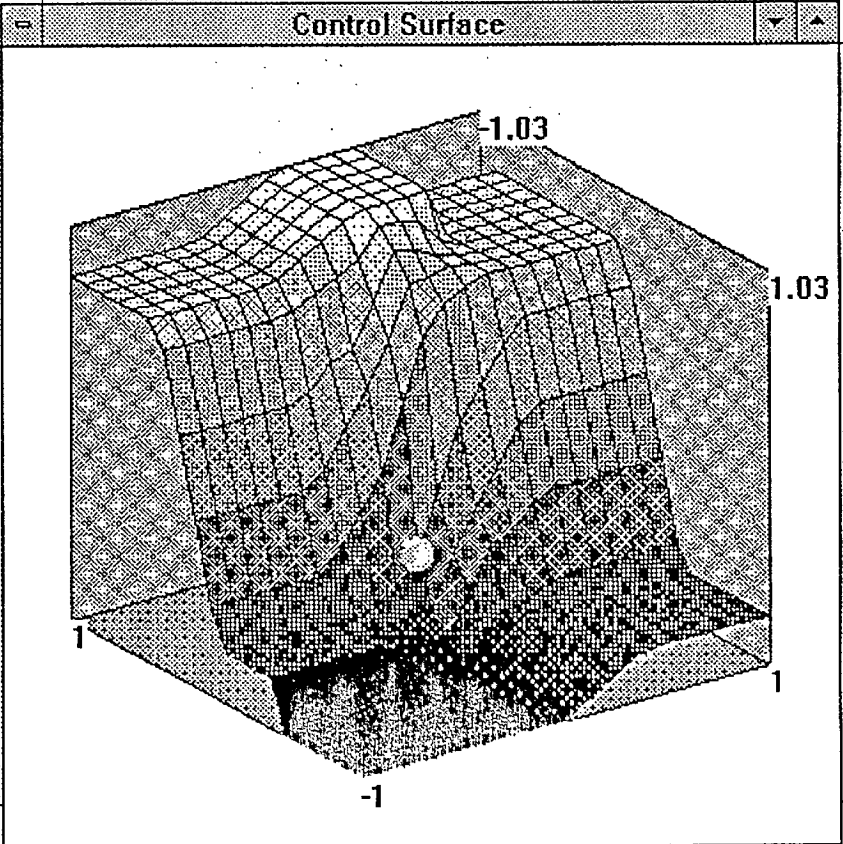
- Pend
 - Pendulum
 - Error
 - dError
 - Current

Pendulum

| | Name | Op. | Error | dError | Weight | Current |
|----|-------|-----|-------|--------|--------|---------|
| 1 | Rule1 | AND | N | Z | 100% | PB |
| 2 | Rule2 | AND | N | P | 100% | PS |
| 3 | Rule3 | AND | Z | P | 100% | NS |
| 4 | Rule4 | AND | Z | Z | 20% | Z |
| 5 | Rule5 | AND | Z | N | 100% | PS |
| 6 | Rule6 | AND | P | N | 100% | NS |
| 7 | Rule7 | AND | P | Z | 100% | NB |
| 8 | | | | | | |
| 9 | | | | | | |
| 10 | | | | | | |

```

RULE Rule7
  OPTIONS
  ICONCOLOR=65408
  END
  IF [Error IS P] AND [dError IS Z] THEN
    Current = NB
  END
  
```

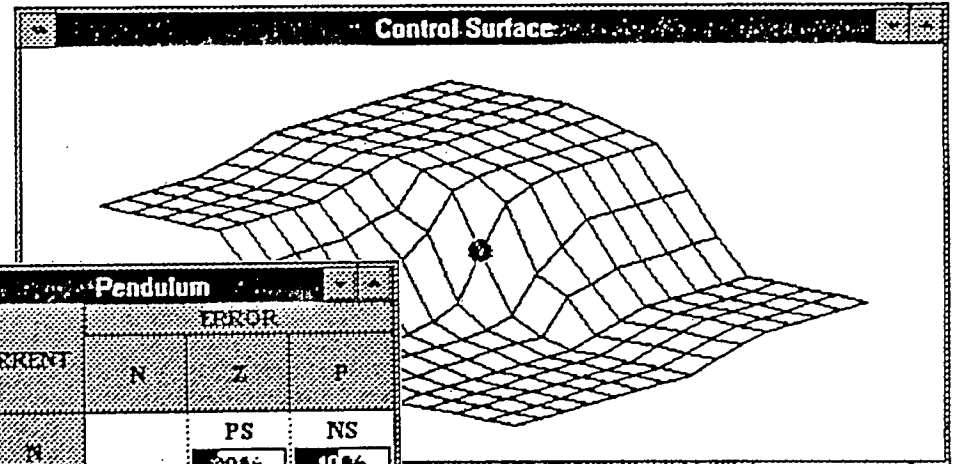


TILShell's Debugging Tools

| Pendulum (Tuning) | | | |
|-------------------|-------|-------|-----------------------|
| Name | Alpha | Count | Info |
| Rule1 | 63% | 32 | E W:100L:0 H:1 |
| Rule2 | 36% | 26 | E W:100L:0 H:0.36746 |
| Rule3 | 0% | 44 | E W:100L:0 H:0.931506 |
| Rule4 | 0% | 50 | E W:20%L:0 H:1 |
| | | | E W:100L:0 H:0.931506 |
| | | | E W:100L:0 H:1 |
| | | | E W:100L:0 H:1 |

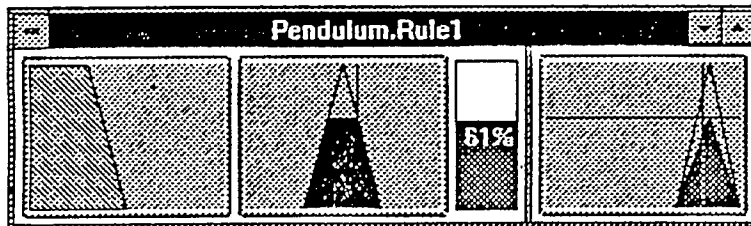
Disable Rule
 Change Rule Weight...
 Reset Alpha Min/Max
 Reset Rule Count
 View Rule Text

Rule4
 IF [Error IS Z] AND [dError IS Z] THEN
 Current = Z

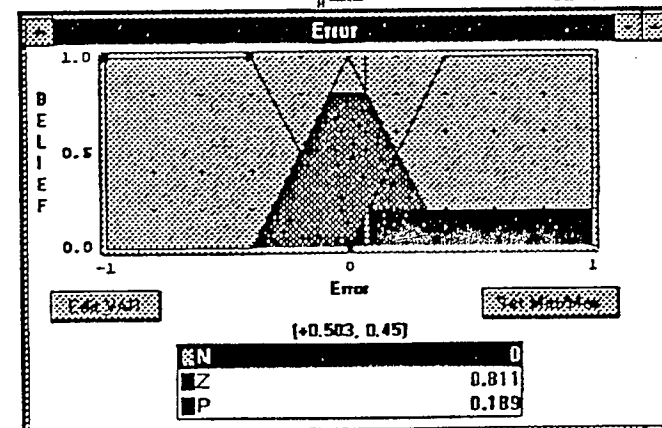


| | | ERROR | | |
|--|---|----------|-----------|-----------|
| CURRENT | | N | Z | P |
| D E R I V E R I T Y | N | | PS 29% | NS 49% |
| | Z | PB 0% | Z 29% | NB 50% |
| | P | PS 0% | NS 0% | |

| Watch | |
|---------|---------|
| Name | Value |
| Error | -0.0234 |
| dError | 0.1030 |
| Current | -0.1565 |
| Alpha | -0.4488 |
| Theta | -0.0207 |
| time | 1.5200 |



| Quick Test | | | |
|---------------|-----------|-------|--------|
| Error | -0.400000 | Value | 0.4000 |
| dError | 0.400000 | Step | 0.1% |
| Current | 0.765000 | | 50 |
| IntegralError | -2.600000 | | |



Debug/Tune Rulebase During Simulation or On-Line

Debug/Tune during Running Simulation

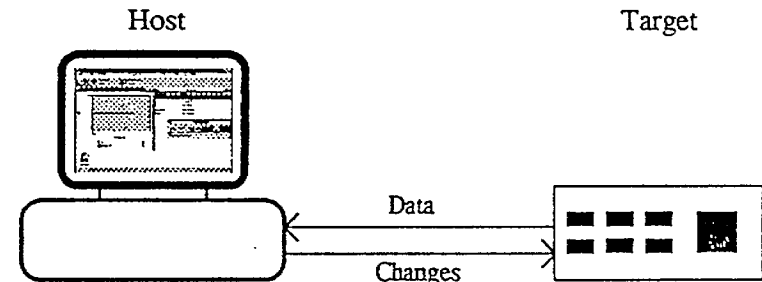
- Define process model via C-like script language
- TILShell debugging windows updated during simulation
- Knowledge base can be modified interactively during simulation

```
Torque = motorK * Current;  
Accel = Torque/Inertia;  
Vel = Vel + Accel*dT;  
Pos = Pos + Vel*dT + Accel*dT*dT;  
  
if Pos > LimitRight then  
    Pos = LimitRight;  
end  
if Pos < LimitLeft then  
    Pos = LimitLeft;  
end  
graphic  
dError = Vel;  
Error = Pos - Setpoint;
```

Process Model

Debug/Tune a Running External Controller

- Compile a debugging version of control code for target processor
- Target proc. communicates w/ TILShell on host computer
- TILShell debugging windows updated to reflect real-time data
- Changes to knowledge base in TILShell enacted in target processor



Board-Level Solutions

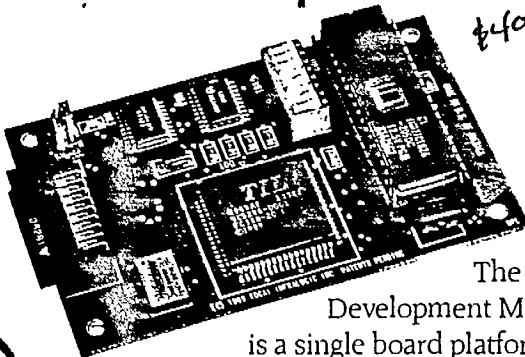
Togai InfraLogic (TIL) offers more ways to integrate fuzzy logic into your applications than anyone else. TIL's line of board-level products ranges from fuzzy logic accelerator boards to embedded control subsystems.

\$40-70 US

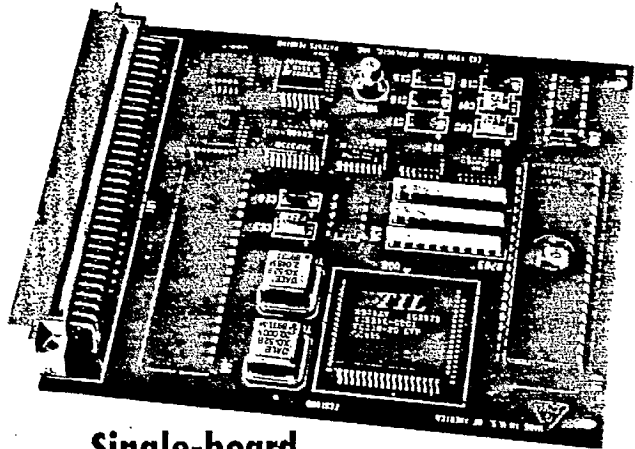
The FC110 Foundation

A unique device, the FC110 Digital Fuzzy Processor (DFP™), is at the heart of all Togai InfraLogic hardware solutions. Designed from the ground up for real-time, embedded fuzzy logic control applications, the CMOS FC110 can perform more than 200,000 fuzzy rule evaluations per second.

FC110 Development Module



The FC110 Development Module is a single board platform for developing FC110-based embedded expert systems. The board is designed to be connected to a host system requiring acceleration of fuzzy logic inferencing.

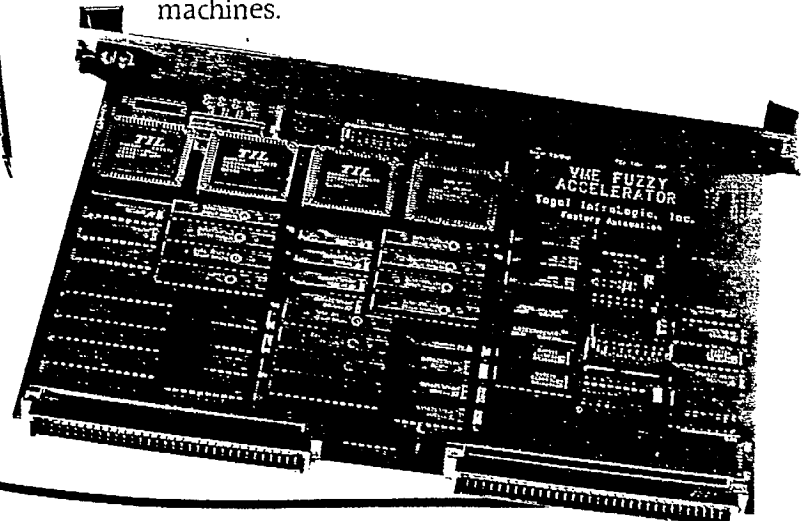


Single-board Fuzzy Controller

TIL's Single-board Fuzzy Controller is a powerful stand alone unit designed for fuzzy logic control applications. In addition to the FC110, the 5" x 4" board provides the resources necessary to form a complete fuzzy control module.

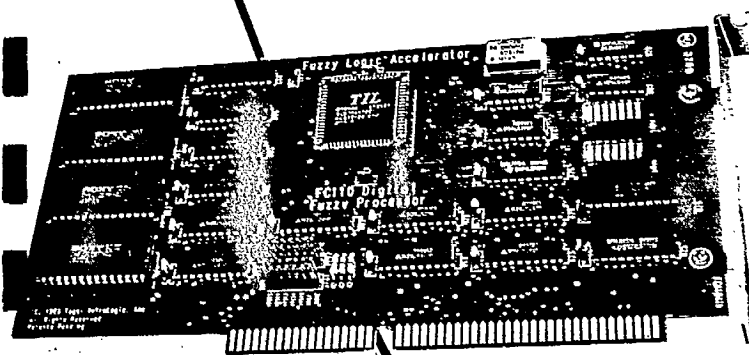
VME Accelerator Board

A high performance single board fuzzy logic accelerator, the VME Accelerator Board is designed for the development and evaluation of complex real-time fuzzy logic applications on VME-based machines.



AT Accelerator Board

Designed for the IBM PC/AT™ bus, the AT Accelerator Board allows the development and evaluation of complex fuzzy logic applications on a personal computer.



Benchmarking Fuzzy Hardware

Togai InfraLogic FC110 Chip*

| Rule Base Size | Rule Base Evaluation Time | # Rules Per Second |
|----------------------------------|---------------------------|--------------------|
| 2-inputs, 1-output, 7 rules | 32 μ sec | 218,750 |
| 5-inputs, 2-outputs, 20 rules | 114 μ sec | 175,000 |
| 7-inputs, 3-outputs, 25 rules | 172 μ sec | 145,350 |
| 10-inputs, 3-outputs, 35 rules | 266 μ sec | 131,580 |
| 20-inputs, 10-outputs, 100 rules | 2,110 μ sec | 47,393 |
| 30-inputs, 15-outputs, 125 rules | 3,810 μ sec | 32,808 |
| 50-inputs, 10-outputs, 150 rules | 4,682 μ sec | 32,038 |
| 50-inputs, 10-outputs, 175 rules | 5,449 μ sec | 32,116 |

* Data provided by Togai InfraLogic, based on FC110 operating at 20MHz

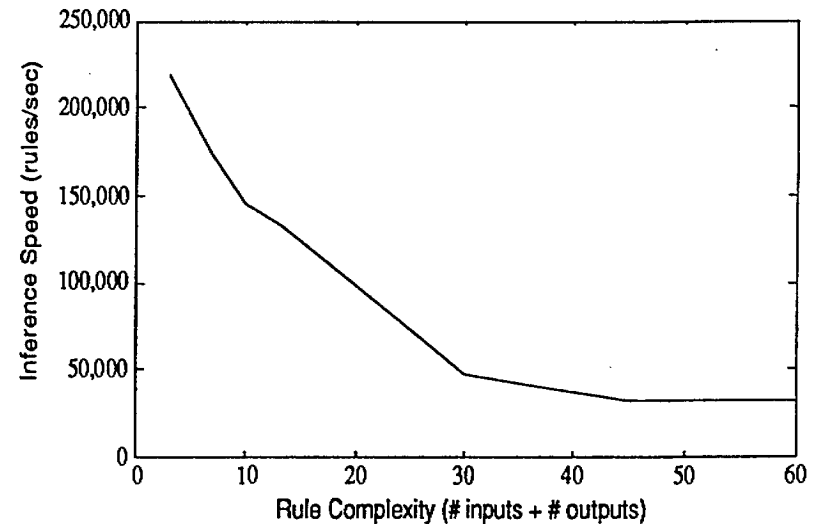
- Inference speed highly dependent on number of inputs & outputs, mildly dependent on number of rules
- No standardized benchmark for fuzzy inference
- Inference speed only meaningful w.r.t. rule complexity & memb. fn. resolution

S. Chiu
Rockwell Science Center

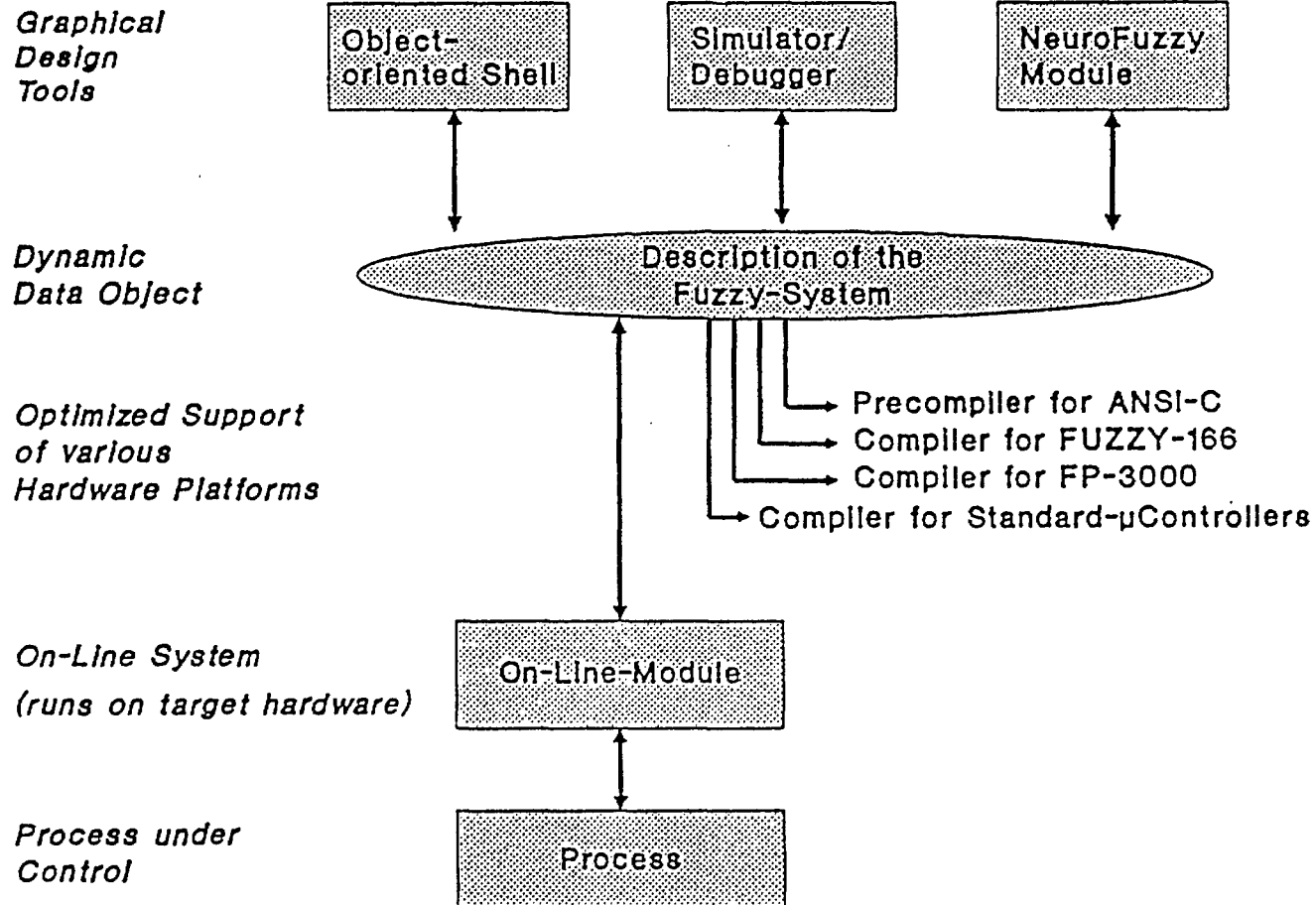
Rule Format:

"If input-1 is A & input-2 is B,
then output-1 is C and output-2 is D"

Membership functions discretized
into 256 levels horizontally & vertically.



The *fuzzy*TECH Workbench



fuzzyTECH™ Enables Full Graphical Development

fuzzyTECH - MOTOR1.FTL

File Edit Debug Analyzer Compile Options Window Help

Spreadsheet Rule Editor

| Matrix # | IF | | THEN | |
|----------|-----------|--------------|------|------------|
| | PosError | SlopeOfError | DoS | Volts |
| 1 | zero | zero | 0.50 | zero |
| 2 | zero | pos_small | 1.00 | zero |
| 3 | zero | pos_big | 0.50 | pos_medium |
| 4 | zero | neg_small | 1.00 | zero |
| 5 | zero | neg_big | 0.50 | neg_medium |
| 6 | pos_small | zero | 1.00 | zero |
| 7 | pos_small | pos_small | 0.70 | pos_medium |
| 8 | pos_small | pos_big | 1.00 | pos_medium |

Time Plot

Project Editor

Position Control of DC Motor

Input Interfaces: PosError, SlopeOfError

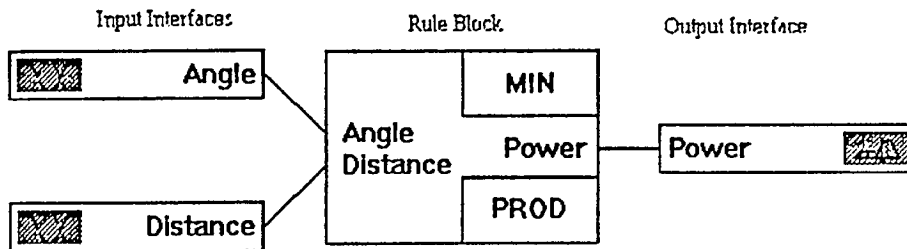
Rule Block: PosError, SlopeOfError, MIN, Volts, PROD

Output Interface: Volts

Linguistic Variable Editor

fuzzyTech's Parameterized Operators

- Assume all rule conjunctions are "and"s
- Meaning of "and" depends on aggregation operator & its parameter value
 - MIN-MAX(val), MIN-AVG(val), GAMMA(val)
- One operator at a given parameter value applies to entire rule block
 - cannot mix "and" and "or"



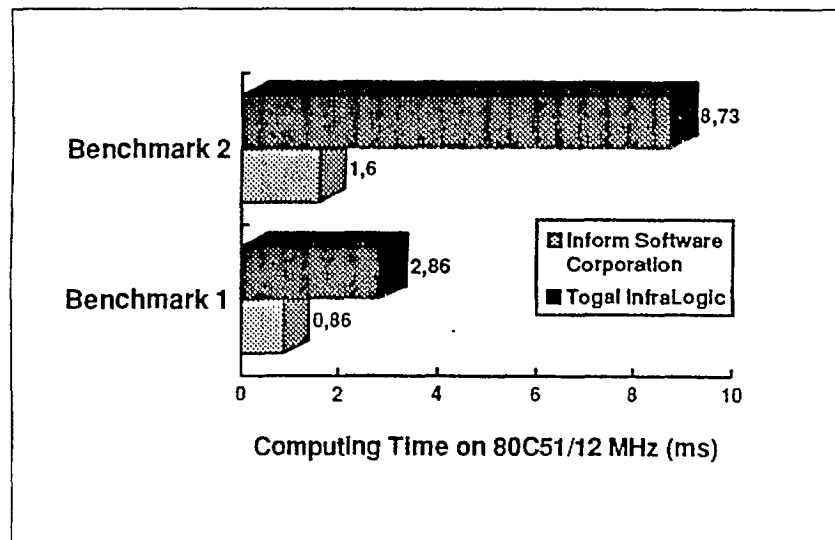
The 'Aggregation' dialog box shows the 'Operator' list with the first option selected. The 'Parameter' field is set to 0.00. The 'Resulting Operator' is 'MIN'. Buttons for 'Ok', 'Cancel', and 'Help' are visible.

The 'Composition' dialog box shows the 'Operator' list with the third option selected. The 'Parameter' field is set to 0.00. The 'Resulting Operator' is 'PROD'. Buttons for 'Ok', 'Cancel', and 'Help' are visible.

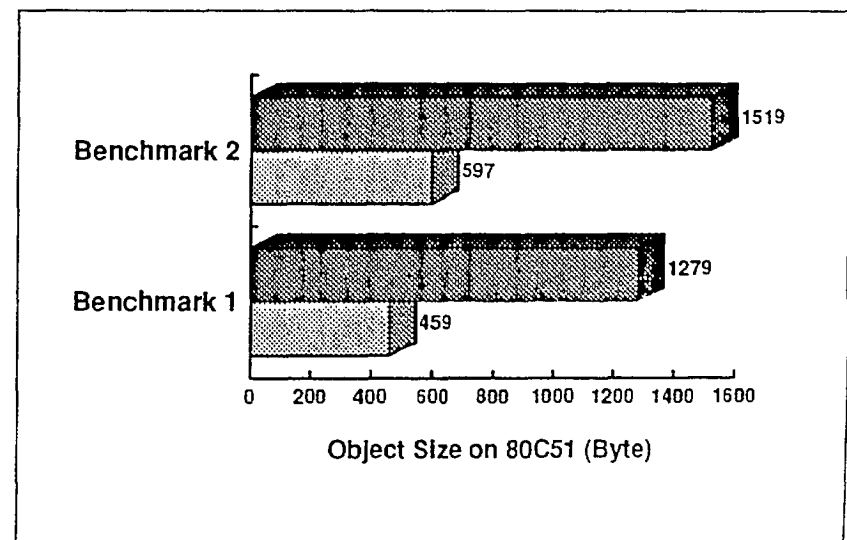
fuzzyTECH™ is Europe's Leading Fuzzy Logic Software Tool

- Only Tool to Support Full Graphical Design, Optimization and Systems Verification
- Only Tool to Implement Online Development on a Running System ("on-the-fly" modifications)
- Supports Fuzzy Associative Maps (FAM-Inference) for more efficient fine-tuning
- Integrates Neural Network Technologies for NeuroFuzzy System Design
- Open Standards: all *fuzzyTECH* Interfaces and Data Formats are Public, allowing Integration, Customizations and User Extensions
- Integrates Simulations Written in Any Language Under MS-Windows™
- Allows Full Interactive Simulation of System Design to Speed Up Time-To-Market
- Supports Almost Every Target Hardware
- Only Quality ISO9000 Approved Fuzzy Logic Design Tool

Fastest Code Generation



Most Compact Code

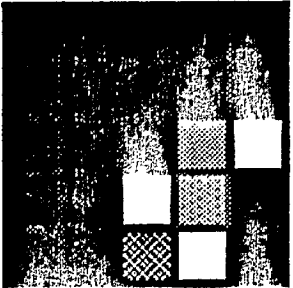


Matrix Rule Editor

Distance neg_close
zero
close
medium
far

Angle

pos_big
pos_small
zero
neg_small
neg_big



Show ...

Degree of Support

Input Aggregation

Composition with Degree of Support

Degree of Support

IF

Angle

pos_big
pos_small
zero
neg_small
neg_big

Distance

neg_close
zero
close
medium
far

THEN

Power

neg_high
neg_medium
zero
pos_medium
pos_high

Ok
Cancel
Help
Aggregation...
Composition...
3-D Picture...

INTERACTIVE DEBUGGING

File Edit Debug Analyzer Compile Options Window Help

Angle

Term

- pos_big
- pos_small
- zero
- neg_small
- neg_big

x: 59.904

y: 1

Graph: pos_big

Y-axis: 0 to 1

X-axis: -90 to 90 degree

Value: -6.32

Distance

Term

- neg_close

Graph: neg_close

Y-axis: 0 to 1

X-axis: 30

Debug

Inputs:

Angle: 6.3243

Distance: 19.8233

Outputs:

Power: 16.8091

Value: -6.3243

Steps [%]: 0.10

neg_high

Term

- neg_high
- neg_medium
- zero
- pos_medium
- pos_high

x: -30

y: 0

Graph: neg_high

Y-axis: 0 to 1

X-axis: -30

Value: 16.8091 KW

Spreadsheet Rule Editor

| Matrix | IF | THEN | | |
|--------|-----------|----------|------|------------|
| # | Angle | Distance | DoS | Power |
| 1 | zero | far | 1.00 | pos_medium |
| 2 | neg_small | far | 0.60 | pos_high |
| 3 | neg_small | medium | 1.00 | pos_high |
| 4 | neg_big | medium | 1.00 | pos_medium |
| 5 | pos_small | close | 1.00 | neg_medium |
| 6 | zero | close | 1.00 | zero |
| 7 | neg_small | close | 1.00 | pos_medium |
| 8 | pos_small | zero | 1.00 | neg_medium |

LV

Debug/Tune Rulebase During Simulation or On-Line

Debug/Tune during Running Simulation

- Define process model via external program that communicates w/ fuzzyTech via DDE-like routines
- fuzzyTech debugging windows updated during simulation
- Knowledge base can be modified interactively during simulation

```
/* all data are passed through a
data structure called FTLINK */

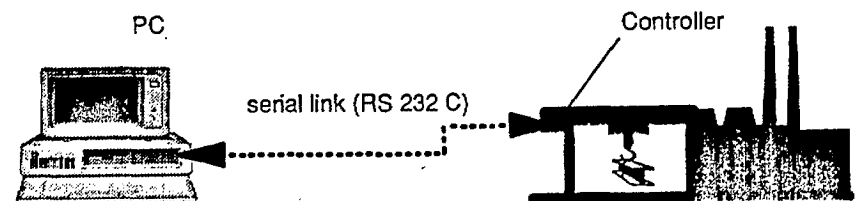
/* allocate memory for an FTLINK */
myFtlink = FtIAllocMem(...);

while (...) {
:
FtISetInput(myFtlink, inputNames);
FtICallFuzzy(mySimWindow, myFtlink);
FtIGetOutput(myFtlink, outputNames);
}
```

External Program

Debug/Tune a Running External Controller

- Compile a debugging version of control code for target processor
- Target proc. communicates w/ fuzzyTech on host computer
- fuzzyTech debugging windows updated to reflect real-time data
- Changes to knowledge base in fuzzyTech enacted in target processor



INFORM

Fuzzy Technologies Division
Pascalstr. 23 · D-5100 Aachen · Tel. (024 08) 94 56-180 · Fax 60 90

FUZZY-166

Quick Reference Guide

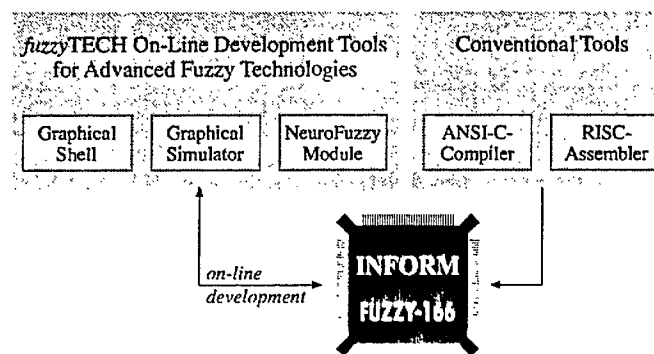
The FUZZY-166 is a 16-bit fuzzy logic processor designed for high speed fuzzy logic based systems. It is the first fuzzy processor to contain both a full conventional instruction set and a fuzzy logic functionality. With plenty of on-chip periphery, it is best suited for the integrated implementation of fuzzy and nonfuzzy functionality on a single chip.



The FUZZY-166 uses the most advanced technologies in fuzzy logic, like On-Line-Optimization and Fuzzy Associative Maps. On-Line-Optimization allows to debug and optimize a fuzzy system at runtime. Fuzzy Associative Maps (FAM) form the link to neural network technology and also render even complex non-linear systems easy to comprehend. In a special development mode, the FUZZY-166 itself establishes communication with the *fuzzyTECH* workbench on power-up for download of On-Line-Optimization.

Complete Tool Set for the FUZZY-166

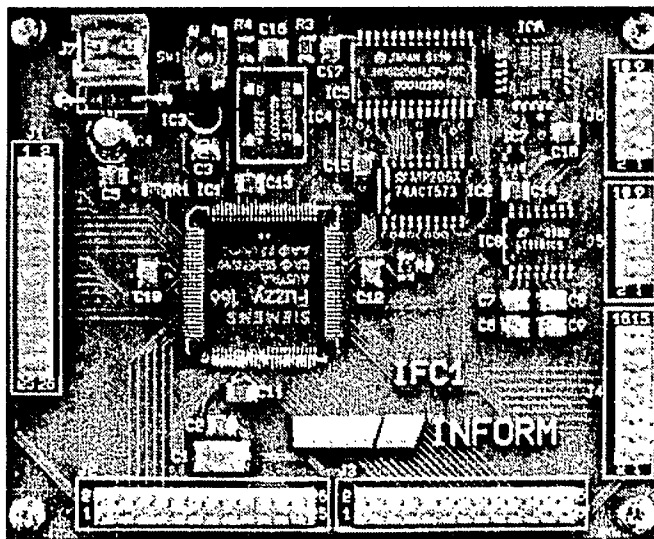
For the FUZZY-166, a complete set of development tools exists. A C-Compiler and a RISC-Assembler can be used for programming the conventional part of the system. To implement a fuzzy logic system on the FUZZY-166, all design tools of the *fuzzyTECH* family may be used.



The FUZZY-166 is fully pin-compatible with the SAB80C166/83C166 standard microcontroller series from SIEMENS. Any application based on this microcontroller can be converted to a fuzzy logic application by exchanging the chip. All Software development tools for the SAB80C166/83C166 can be used with the FUZZY-166.

Evaluation Board for FUZZY-166

To get started with fuzzy logic applications, the FUZZY-166 Evaluation Board can easily be connected to existing hardware. In addition to digital and analog periphery, the FUZZY-166 Evaluation Board has two RS 232 serial ports, which are usable for on-line development with all *fuzzyTECH* development tools.



Fuzzy Logic Function Set

The entire Fuzzy Logic Function Set is implemented in the internal FUZZY-166 firmware and contains three function groups:

1. *fuzzyTECH* Kernel (Fuzzy Function Set)

- X Fuzzification for linear and S-shaped membership functions with up to 9 defining points
- X Fuzzy-Operators: MIN-MAX, GAMMA, MIN-AVG (parameter interval partial supported)
- X Defuzzification Methods: Center-of-Area, Center-of-Maximum and Fuzzy-Output. All functions are fully supported by the *fuzzyTECH*-Precompiler for the FUZZY-166. However, they may be used from C-code level and assembly code level just as well. The full function set is documented in the FUZZY-166 reference manual.

2. *fuzzyTECH* On-Line-Module

- X Communication functions for serial interfaces S0 and S1
- X On-Line development functions:
 - Change of membership functions definition at runtime
 - Change of rule strategy at runtime
 - Polling of any fuzzy inference data in the system at runtime
 - Tracing of control variables at runtime

The integrated On-Line-Module is fully supported by all *fuzzyTECH* design tools. However, they may be used by other software as well. The full feature set is documented in the FUZZY-166 reference manual.

3. Communications Manager

- X Program download via serial interface S1
- X Utility functions to control program execution

Fuzzy Logic Performance

- X Fuzzification of 4 linear terms: 39 μ s
- X FAM-inference of 51 rules: 204 μ s
- X COM-defuzzification of 3 linear terms: 25 μ s
- X COA-defuzzification of 3 linear terms with 64-step numerical integration: 2220 μ s

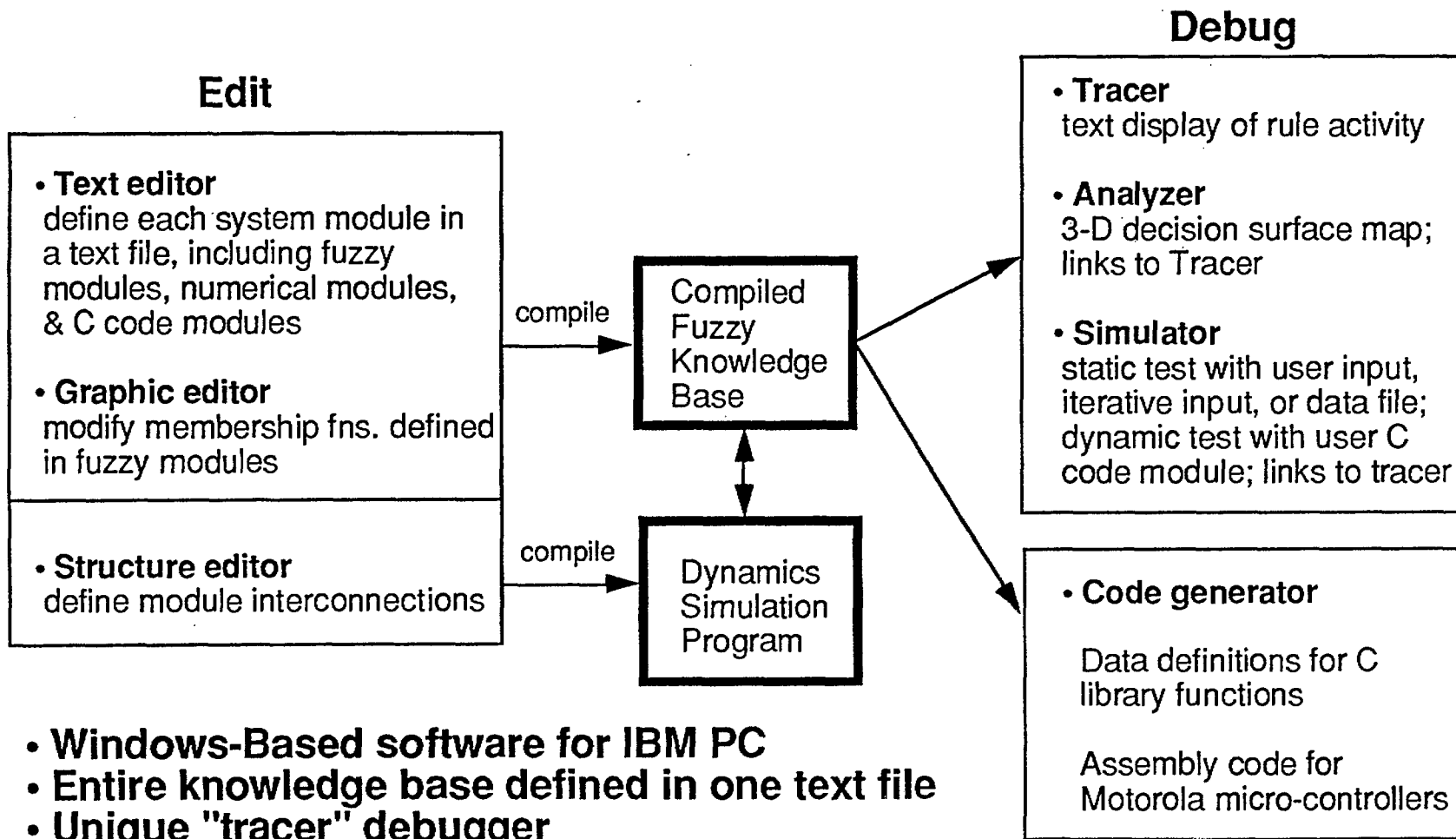
All times average performance with 8-bit external data bus, all data located in external RAM and zero waitstates. Locating data in the FUZZY-166 internal RAM will increase the speed for 20% and using an 16-bit external data bus will increase the speed for 10%.

Periphery and Specifications

- X Packaging: 100-pin plastic quad flat package (PQFP 100)
 - X High-Performance 16-bit RISC-CPU with four stage pipeline, 100% compatible to SAB 80C166/83C166
 - X 100 ns minimum instruction cycle time
 - X 500 ns 16-bit multiplication
 - X Direct adressability of 4 Kbits for peripherals and user defined flags
 - X 1 KB internal RAM
 - X 4 different bus configuration modes
 - X 8-channel peripheral event controller
 - X 10-channel 10-bit A/D converter, 9.75 μ s conversion time
 - X 16-channel capture/compare unit
 - X 5 16-bit timers 200 ns and 400 ns resolution
 - X 2 serial channels
 - X watchdog timer with programmable time intervals
 - X 76 I/O lines with individual bit adressability
- For further specifications, see the SAB 80C166/83C166 user's manual

*Simpler/cheaper than
Catalan, Tilshell & FuzzyTech
fuzzytech*

FIDE (Fuzzy Inference Development Environment)



- **Windows-Based software for IBM PC**
- **Entire knowledge base defined in one text file**
- **Unique "tracer" debugger**

Module Definition

```
fiu tvfi (Min Max) *8;
```

```
Invar temperaturare "degree": -110(1)110 [
```

```
  cold (@30,1,@38,1,@45,0),
```

```
  cool (@40,0,@50,1,@60,0),
```

```
  warm "fle_wm",
```

```
  hot (@70,0,@80,1,@90,1)];
```

```
outvar fan_speed."rpm": 0 (5) 1000 * (
```

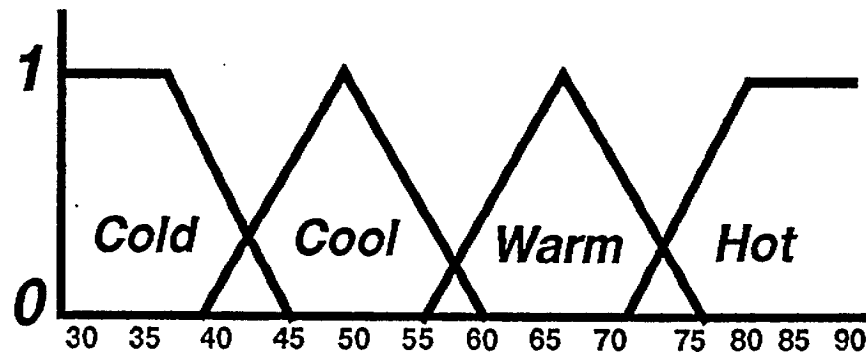
```
  low = 200,
```

```
  medium = 500,
```

```
  high = 800);
```

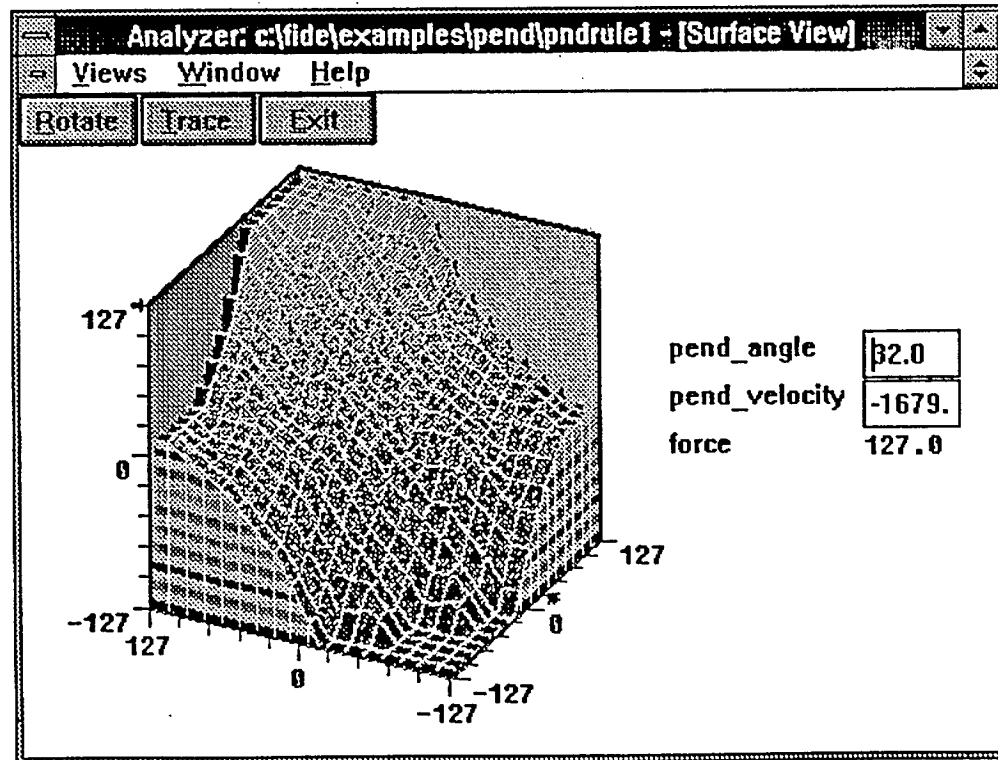
```
if temperature is warm then fan_speed is low;
```

```
if temperature is hot then fan_speed is high; ...
```



Analyzer

Surface View



Tracer

Source Rules

Tracer: Select Variable

Unit Name: c:\ide\examples\ans\anrule1

| Input Variables | Output Variables |
|-------------------------|---|
| temperature diff 110.00 | hot_fan_spd 000.00 cool_fan_spd 0.00 |

Tracer: Select Output Label

Unit Name: c:\ide\examples\ans\anrule1

Variable: hot_fan_spd
Units: rpm
Range: [0.000000, 1800.000000]
Value: 800.000000

| Labels | Grades |
|----------|--------|
| zero | 0.00 |
| low | 0.00 |
| medium | |
| high | |
| veryhigh | |

Tracer: Select Rule

Unit Name: c:\ide\examples\pend\pendr Variable: force = 1
Label: P_Large

```

rule (Line 69 Col 46) pend_velocity is P_Large : 1.00
  (Line 69 Col 17) pend_angle is P_Small : 0.00
  AND = 0.00
> rule (Line 75 Col 47) pend_velocity is P_Medium : 0.00
  (Line 75 Col 17) pend_angle is P_Medium : 0.00
  AND = 0.00
> rule (Line 76 Col 47) pend_velocity is P_Large : 1.00
  (Line 76 Col 17) pend_angle is P_Medium : 0.00
  AND = 0.00
rule (Line 81 Col 46) pend_velocity is P_Small : 0.00
  (Line 81 Col 17) pend_angle is P_Large : 1.00
  AND = 0.00
    
```

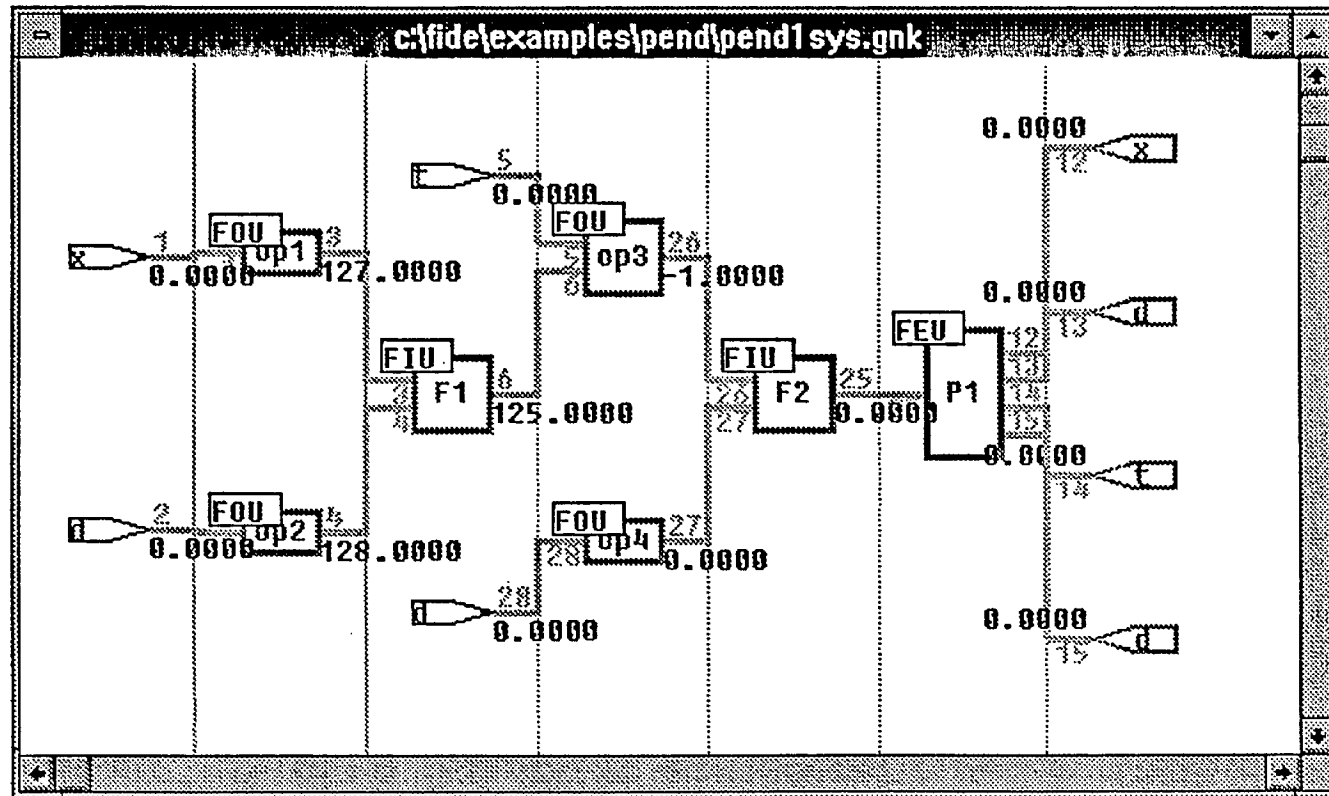
Tracer: Select Rules

Unit Name: c:\ide\examples\ans\anrule1 Variable: hot_fan_spd = 800
Label: Nigh = 1.00

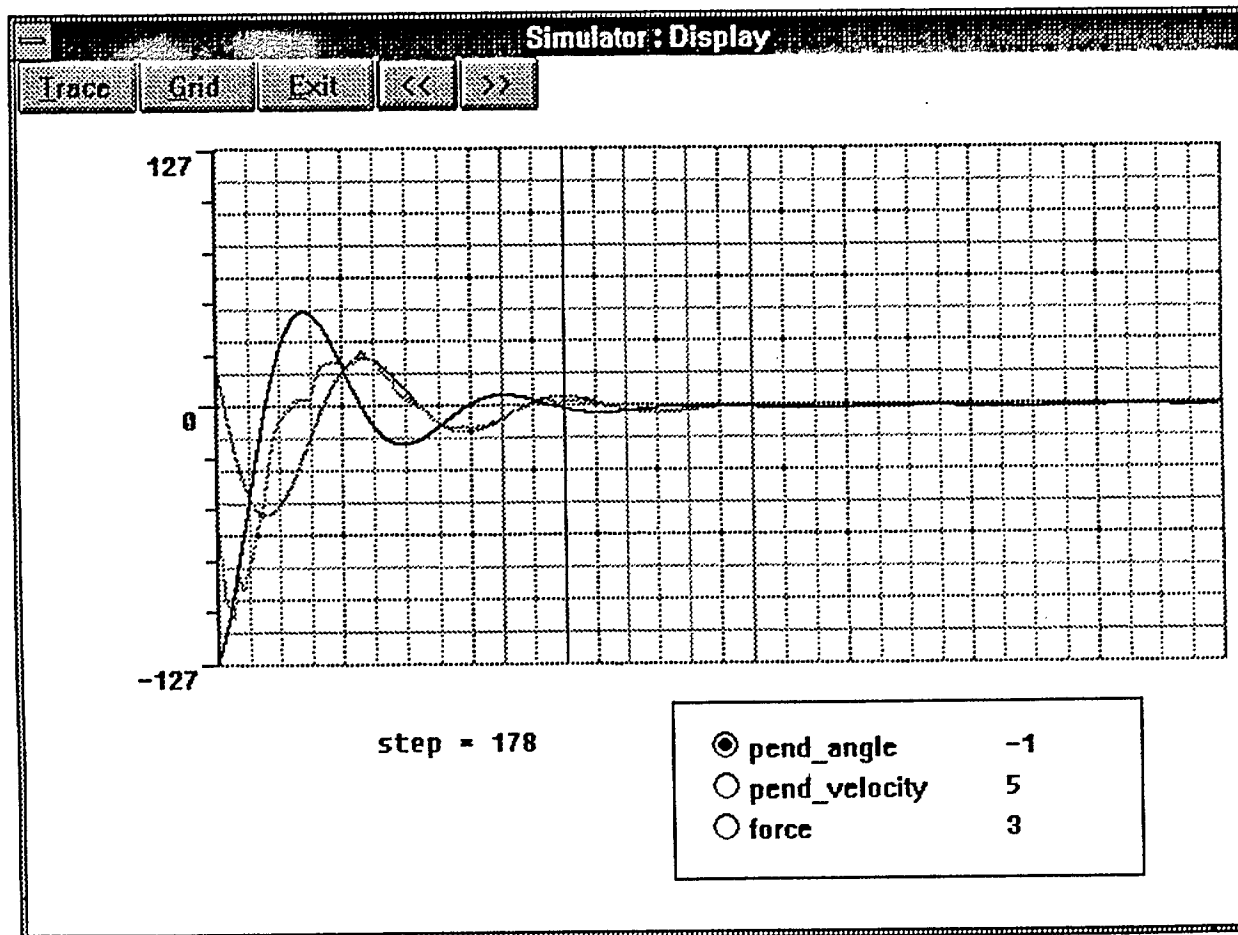
```

> rule (Line 45 Col 23) temperature diff is PositiveBigDiff : 1.00
  AND = 1.00
  OR = 1.00
    
```


Data Flow Display

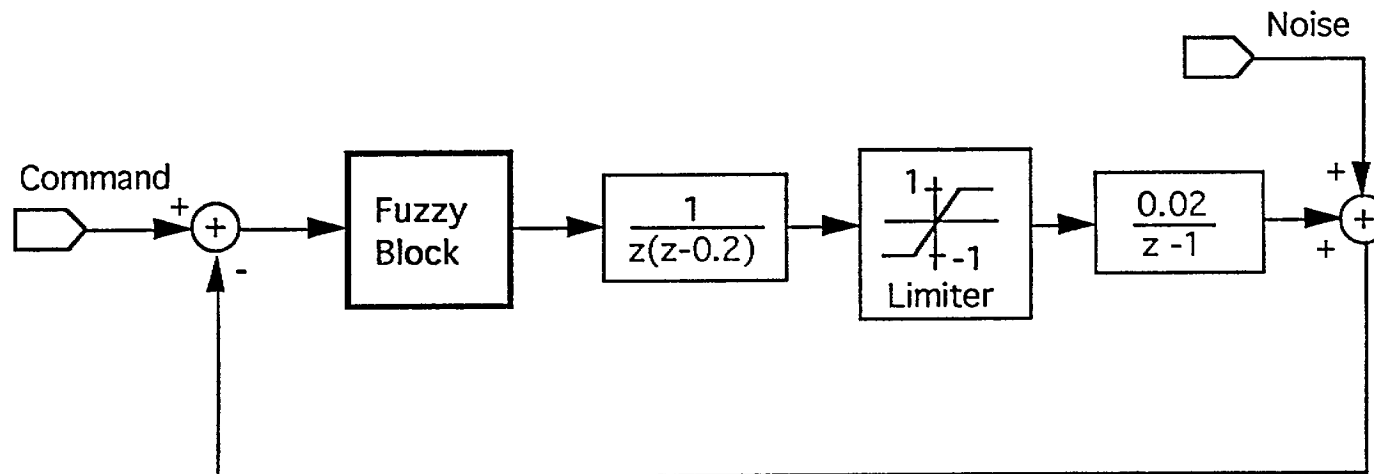


Simulator



RT/Fuzzy (Run Time/Fuzzy) for MATRIXx

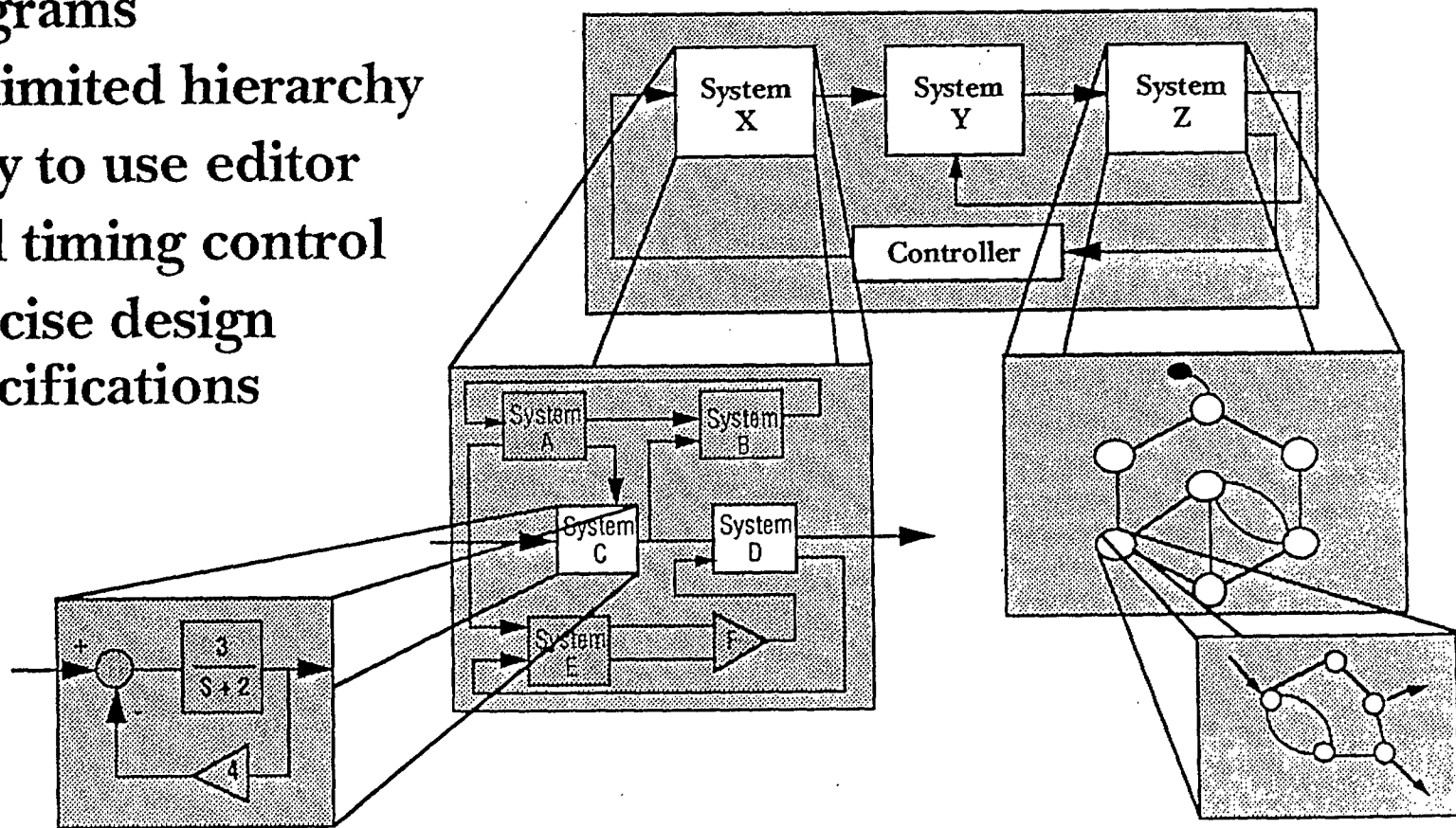
- Fuzzy Logic option added to one of the best conventional control system development environment (*MATRIXx*)
- RT/Fuzzy creates fuzzy block for MATRIXx SystemBuild
- Available for most workstations (*not PC*)



SystemBuild: MATRIXx's Block Diagram Simulation Environment

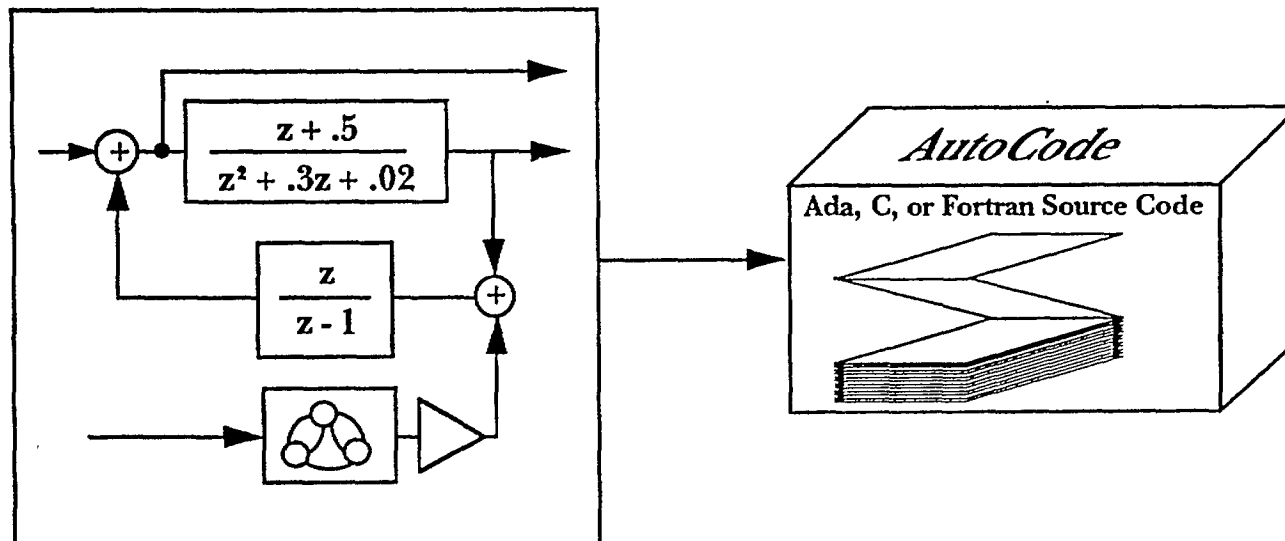
Modeling with the SystemBuild Block Editor

- ◆ Familiar block diagrams
- ◆ Unlimited hierarchy
- ◆ Easy to use editor
- ◆ Full timing control
- ◆ Precise design specifications



Automatic Code Generator

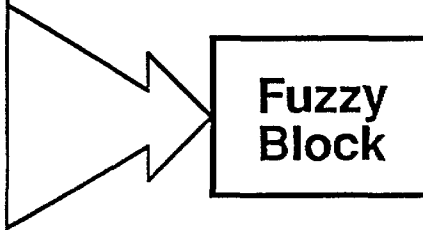
SystemBuild Diagrams



- ◆ Fast, accurate code generation without programming
- ◆ Generates real-time code or callable procedures
- ◆ Allows programmers to focus on performance critical modules code optimization, and system integration
- ◆ Interfaces to target hardware through standard software layer

Fuzzy Logic Block Construction

```
IF ERR IS SMALL;  
THEN TORQUE IS LOW;  
  
IF ERR IS BIG;  
THEN TORQUE IS HIGH;  
  
DATA ERR;  
RANGE [0 2.5];  
...  
SMALL [1, 0.5, 0, 0, 0];  
BIG   [0, 0, 0, 0.5, 1];  
...  
  
Connective : Min-Max  
Defuzzification: Centroid
```



- Primitive text interface for rule development
- Integrates fuzzy logic into a powerful control system development environment
- Supported by MATRIXx's C and Ada code generators

Fuzzy Block: Defining Membership Functions

| BLOCK NAME | | INPUTS | OUTPUTS |
|---------------------------------------|---|-------------------------------------|----------|
| Access Name : CLASSES | | 2 | 8 |
| Access Field | | | |
| NEG_MEDIUM | $\text{SIN}(\text{PI} * (\text{X} + 0.5)) ** 9;$ | | |
| NEG_SMALL | $\text{SIN}(\text{PI} * (\text{X} + 0.25)) ** 9;$ | | |
| ZERO | $\text{SIN}(\text{PI} * \text{X}) ** 9;$ | | |
| POS_SMALL | $\text{SIN}(\text{PI} * (\text{X} - 0.25)) ** 9;$ | | |
| POS_MEDIUM | $\text{SIN}(\text{PI} * (\text{X} - 0.5)) ** 9;$ | | |
| Connective Method..... : Max-Min | | | |
| Implication Method..... : Mamdani | | | |
| Defuzzification Method... : Centroid | | | |
| Aggregation Method..... : Arithmetic | | | |
| 1-by-6 Database Parameters | | | |
| 0.1 | 0. | 1. | 0. 0. 1. |
| Number of Points in Curve : 50 | | | |
| Optimization Preference.. : Speed | | | |
| 1-by-2 Linearization Delta | | | |
| 0.004 | 0.04 | | |
| Input External_Signals | | Output Labels | |
| 1 "Angle" | | 1 "Force" | |
| 2 "Delta" | | 2 "Rule 1" | |
| | | 3 "Rule 2" | |
| | | 4 "Rule 3" | |
| COMMENTS | | | |
| <input type="button" value="CANCEL"/> | VIEW_INPUT | COLOR | ICON |
| | External_Signals | 6 | Special |
| | | IN_PINS | OUT_PINS |
| | | Show_All | Show_All |
| | | LABELS | ON |
| | | <input type="button" value="DONE"/> | |

Fuzzy Block: Defining a Rule

| BLOCK NAME | | INPUTS | OUTPUTS | | | | |
|--|------------------|--------|---------|----------|----------|--------|------|
| Access Name : RULE NS_PS | | 2 | 8 | | | | |
| Access Field | | | | | | | |
| <pre> RULE NS_PS; IF ANGLE IS NEG_SMALL AND; DELTA IS POS_SMALL; THEN FORCE IS ZERO; RULE_3; WEIGHT 1; Connective Method..... : Max-Min Implication Method..... : Mamdani Defuzzification Method... : Centroid Aggregation Method..... : Arithmetic 1-by-6 Database Parameters 0.1 0. 1. 0. 0. 1. Number of Points in Curve : 50 Optimization Preference.. : Speed 1-by-2 Linearization Delta 0.004 0.04 Input External_Signals 1 "Angle" 2 "Delta" Output Labels 1 "Force" 2 "Rule 1" 3 "Rule 2" 4 "Rule 3" COMMENTS VIEW_INPUT COLOR ICON IN_PINS OUT_PINS LABELS External_Signals 6 Special Show_All Show_All ON </pre> | | | | | | | |
| CANCEL | VIEW_INPUT | COLOR | ICON | IN_PINS | OUT_PINS | LABELS | DONE |
| | External_Signals | 6 | Special | Show_All | Show_All | ON | |

Fuzzy Block: The Rulebase Information Manager

RT/Fuzzy Information Manager

| Name of Rule | SELETED INFO If | Then | Weight |
|----------------|--------------------|------|--------|
| FILL_FEEDWATER | 4 | 1 | 1 |
| SET_GAS_HIGH | 2 | 2 | 1 |
| SET_GAS_LOW | 2 | 2 | 1 |
| SET_GAS_MEDIUM | 2 | 2 | 1 |
| TURN_GAS_OFF | 1 | 2 | 1 |

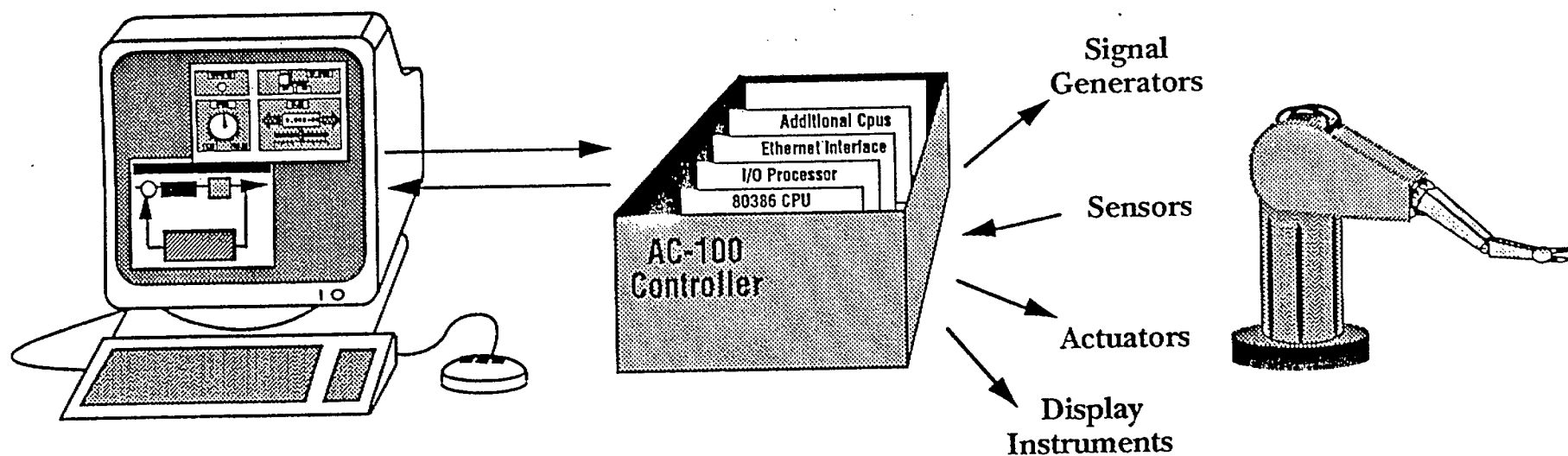
Filename (Save/Load) : RT_FUZZY.SAV SORT INFO **SELECT INFO**

Select Rules Keyword : Alphabetical All Rules

LOAD SAVE UPDATE INPUTS OUTPUTS CLASSES QUALIFIERS

CANCEL PLOT COPY NEW RULE NEW DATA DELETE DONE

AC-100 Real-Time Testing and Debugging



- ◆ Interactive control algorithm debug
 - Display sensor measurements
 - Alter actuator commands
 - Tweak control algorithm variables

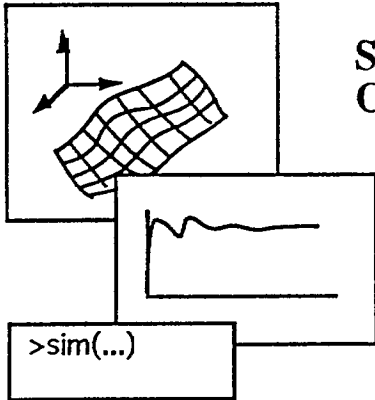
A-B FLEX (Allen-Bradley Fuzzy Logic EXplorer)

- A research & prototyping tool for Mac & PC

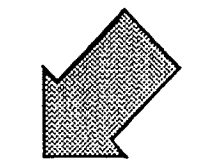
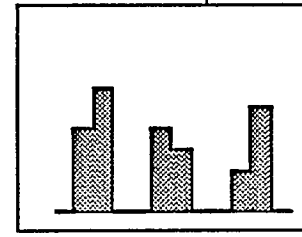
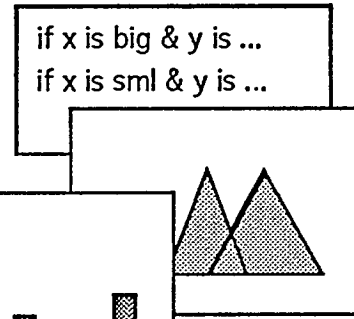
- Leverages simulation & analysis capabilities of Matlab/Simulink

Popular simulation packages

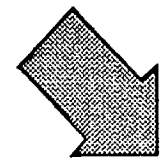
**MATLAB/
SIMULINK**
Simulation & Analysis



A-B FLEX
Rule Development



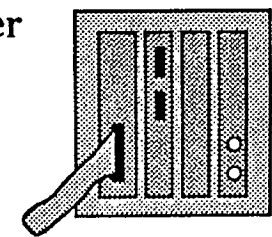
Simulation Code



C & Ada
Source Code
or
A-B Controller
Program

**Generic
Processor or
A-B PLC**

Fuzzy Control
Execution



Rockwell International
Science Center

A-B FLEX Screen

The screenshot displays the A-B FLEX software interface. At the top, a menu bar includes "File", "Edit", "Utilities", "Mode", and "Info". The "Mode" menu is open, showing options: "Fuzzy Dynamics" (checked), "Matlab" (checked), "Simulink", "C", "Ada", and "Data Hwy".

Below the menu, a text area contains the following text:
"My control rules"
"inputs are veloci
input vel.err -0.4
"output is surface
output defl -0.23
if vel.err is p.bi
if vel.err is p.me

To the right, a window titled "mycontrol.rules" shows the text:
"acceleration"
.0 20.0;

Below this is a window titled "KB: mycontrol.rules" containing the text:
Rule 11: if vel.err is near.zero & accel is...

Two graphs are shown on the left side:
1. A graph titled "vel.err" with a triangular wave pattern. The x-axis has labels -0.40, 0.1040, and 0.40.
2. A graph titled "defl" with a triangular wave pattern. The x-axis has labels -0.23, 4.026E-02, and 0.23. A scale of 1.0 is indicated.

On the right side, there are two vertical sliders:
1. A slider for "vel.err" with a value of -4.4.
2. A slider for "defl" with a value of 4.026E-02.



Rockwell International

Science Center

Defining Rules & Membership Functions

```
Text Edit: mycontrol.rules

"inputs are velocity error and acceleration"
input vel.err -0.5 0.5 accel -20.0 20.0;
"output is surface deflection"
output defl -0.23 0.23;

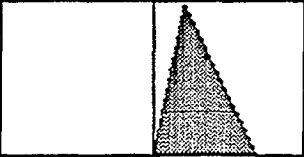
if vel.err is p.big then defl is p.big;
if vel.err is p.med then defl is p.med;
if vel.err is p.sml then defl is p.sml;
if vel.err is zero then defl is zero;
if vel.err is n.sml then defl is n.sml;
if vel.err is n.med then defl is n.med;
if vel.err is n.big then defl is n.big;

0.3 if vel.err is near.zero and accel is p.big then defl is p.big;
0.2 if vel.err is near.zero and accel is p.med then defl is p.med;
0.2 if vel.err is near.zero and accel is p.sml then defl is p.sml;
0.3 if vel.err is near.zero and accel is zero then defl is zero;
0.2 if vel.err is near.zero and accel is n.sml then defl is n.sml;
0.2 if vel.err is near.zero and accel is n.med then defl is n.med;
0.3 if vel.err is near.zero and accel is n.big then defl is n.big;
```

Dictionary

my.defs

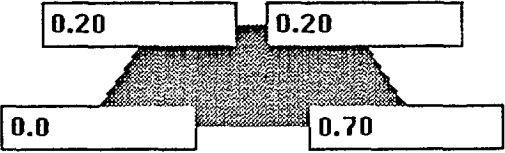
- n.big
- n.med
- n.sml
- p.big
- p.med
- p.sml**
- zero



Add Edit

Remove Scale

Name: **p.sml**



0.20 0.20

0.0 0.70

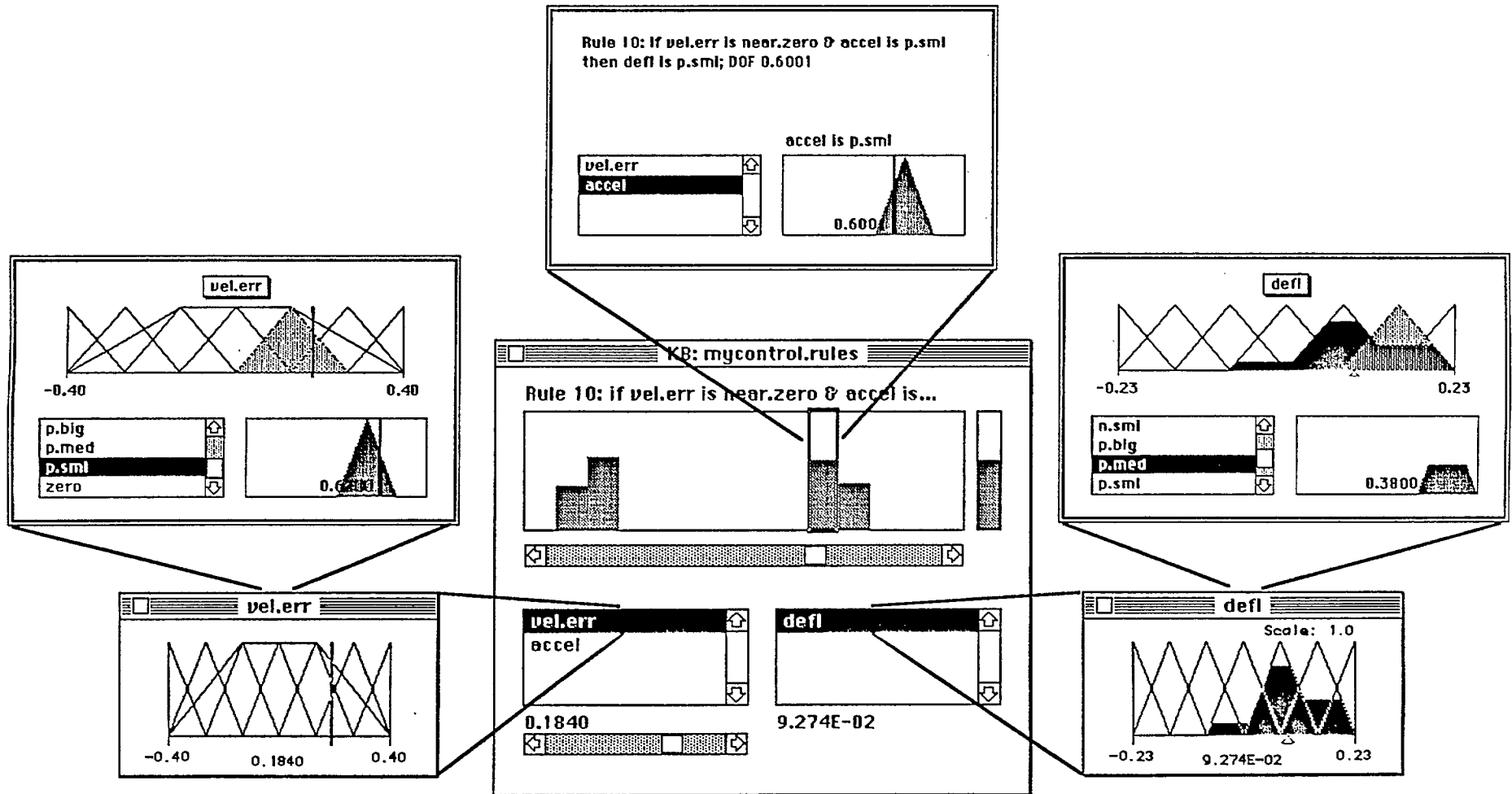
OK Cancel



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Rule Base Inspector



Rockwell International

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Process Simulation Interface

- Save a rule base as a MATLAB function or SIMULINK block definition

Save as MATLAB function, e.g., "mydecision()"

In MATLAB, use the function interactively by:

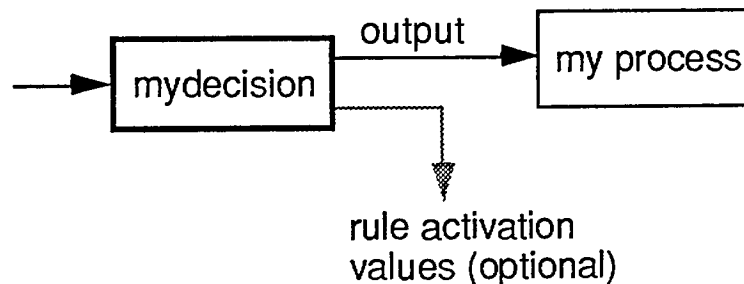
```
> x = [ 0.2 16 ] (set input values, for 2-input case)
> y = mydecision(x) (output values are returned in y)
```

Can incorporate the function in any MATLAB program

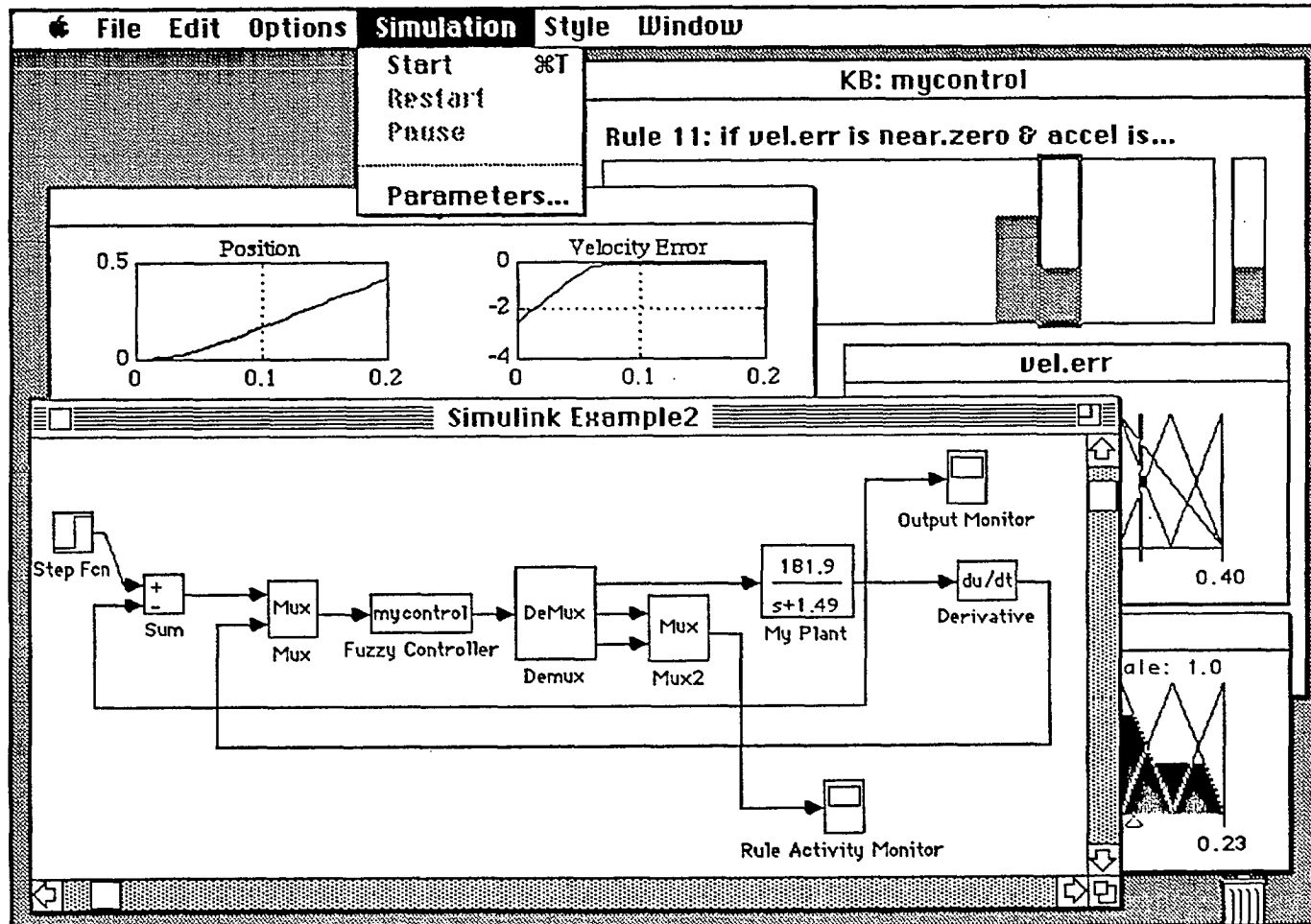
Save as SIMULINK block definition

In SIMULINK:

- create a graphical block using the given name
- specify sampling time for the block
- connect with other blocks



A-B FLEX with SIMULINK



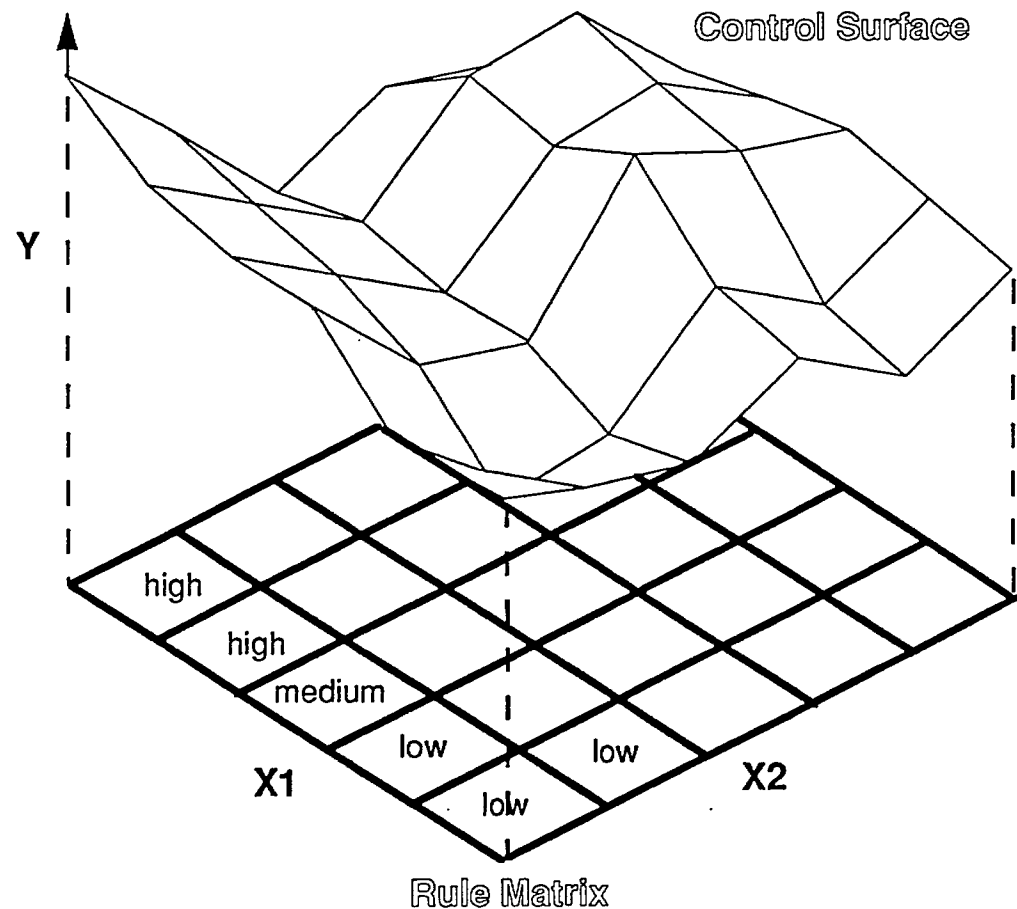
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Manifold Graphics Editor

from 1 man co. in San Diego

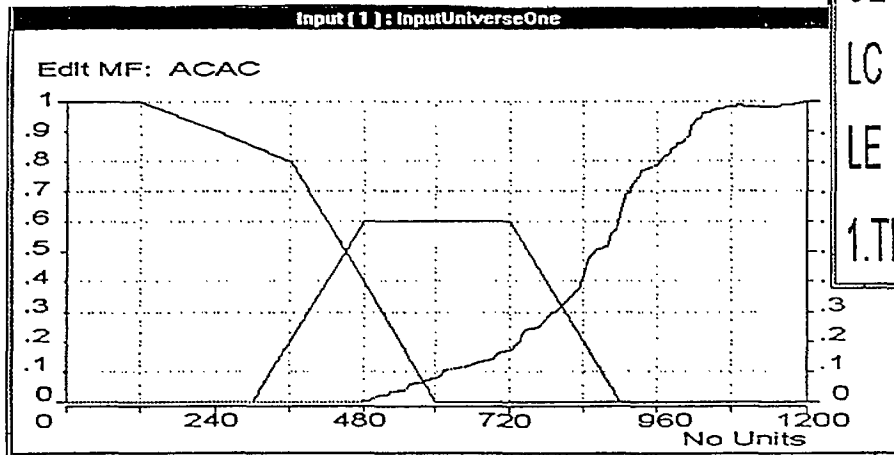
If X1 is ... & X2 is ... then Y is ...

- A highly intuitive rulebase editor for building a high-dimensional control surface
- Generates knowledge base data files in C, Basic, Fortran, & various microcontroller assembly languages
- Generates knowledge base files in TILShell, FIDE, & Fuzz-C formats
- User must provide inference code
- Runs under Windows



Manifold Graphics Editor: Editing Rules

- Each matrix cell represents an input condition
- Define up to 11 inputs & 2 outputs (11-dimensional rule matrix)
- Cellular automata algorithm for filling in missing rules



Manifold Graphics Editor - TRKTRL[3] - [Rule Matrix - Steering Angle]

File Setup Windows Rules Sets Tools Build Help

Rule Matrix - Steering Angle

2. POS

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| RI | PB | PB | PB | PM | PM | PS | PS |
| RC | PB | PB | PM | PM | PS | PS | PS |
| CE | PM | PM | PS | ZE | PS | PS | PS |
| LC | PM | PS | PS | PS | PS | PS | PS |
| LE | PS | PS | PS | PS | PS | PB | PB |

1.TKA RB RU RV V LV LU LB 3.TLA : NE

Rule

IF (Truck Angle

1. Left Upper

 Dock Position

2. Left Center

 Trailer Angle

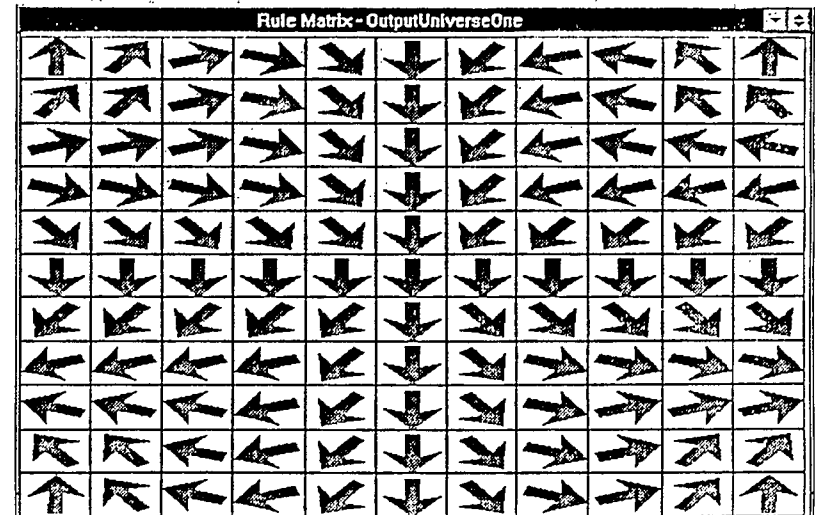
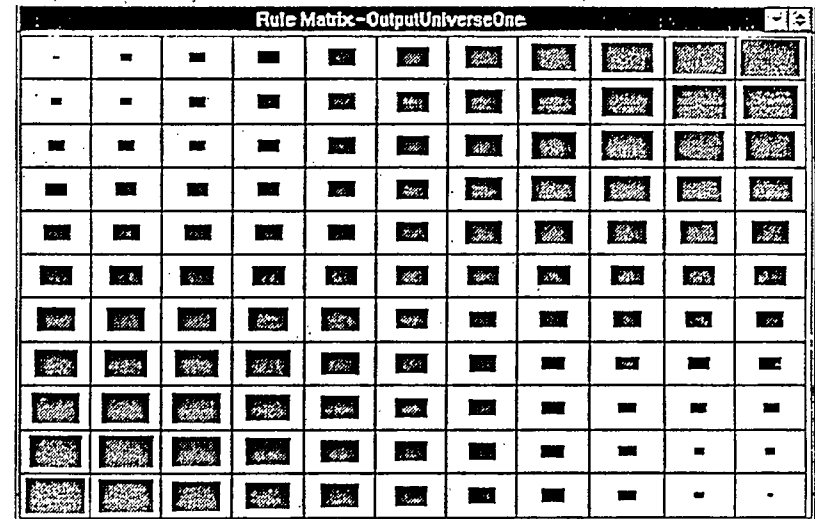
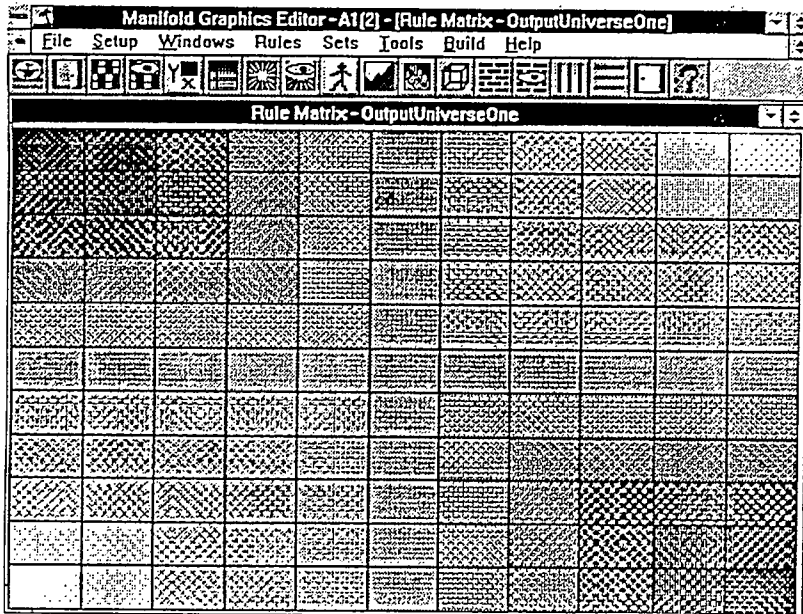
3. Negative

THEN Steering Angle

1. Positive Small

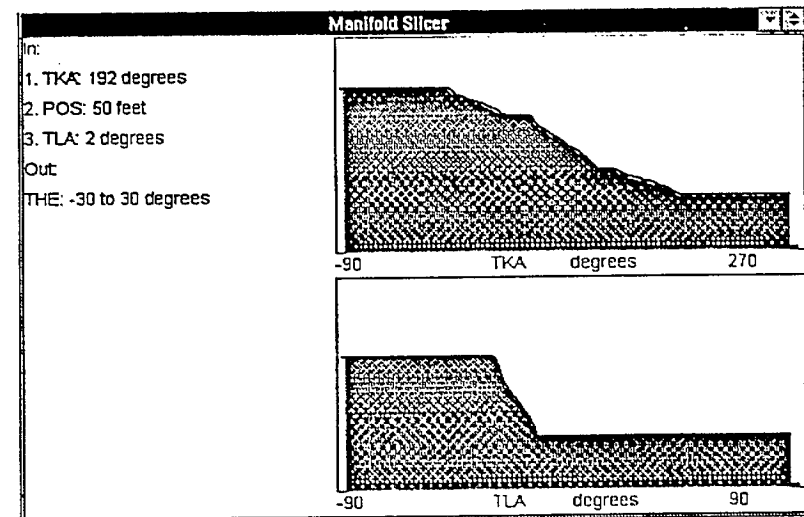
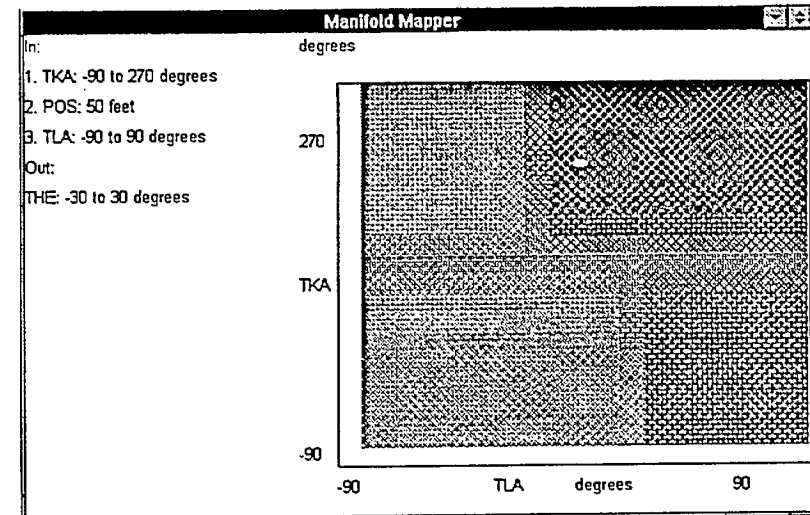
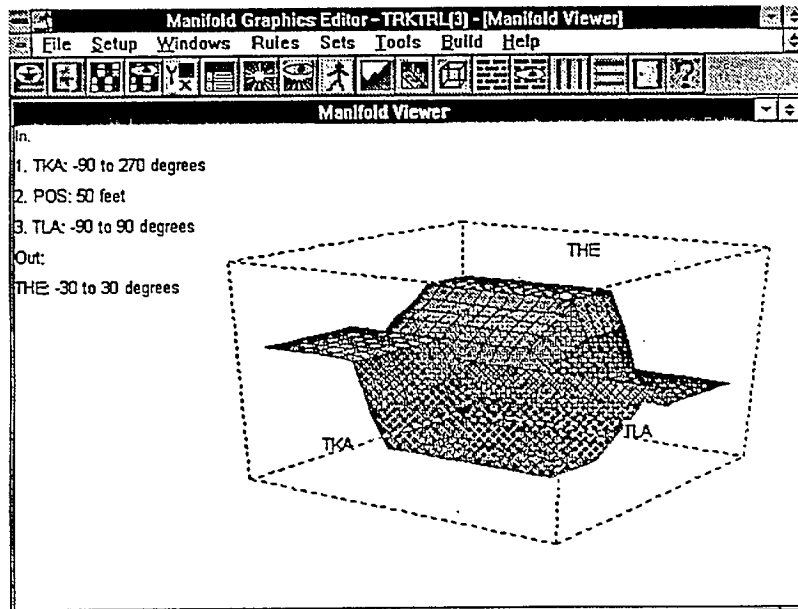
Displaying Rule Matrix via Graphic Cues

- Cell content cued by text, color, shape size, arrow direction
- Provides mental picture of control surface



Displaying the Control Surface

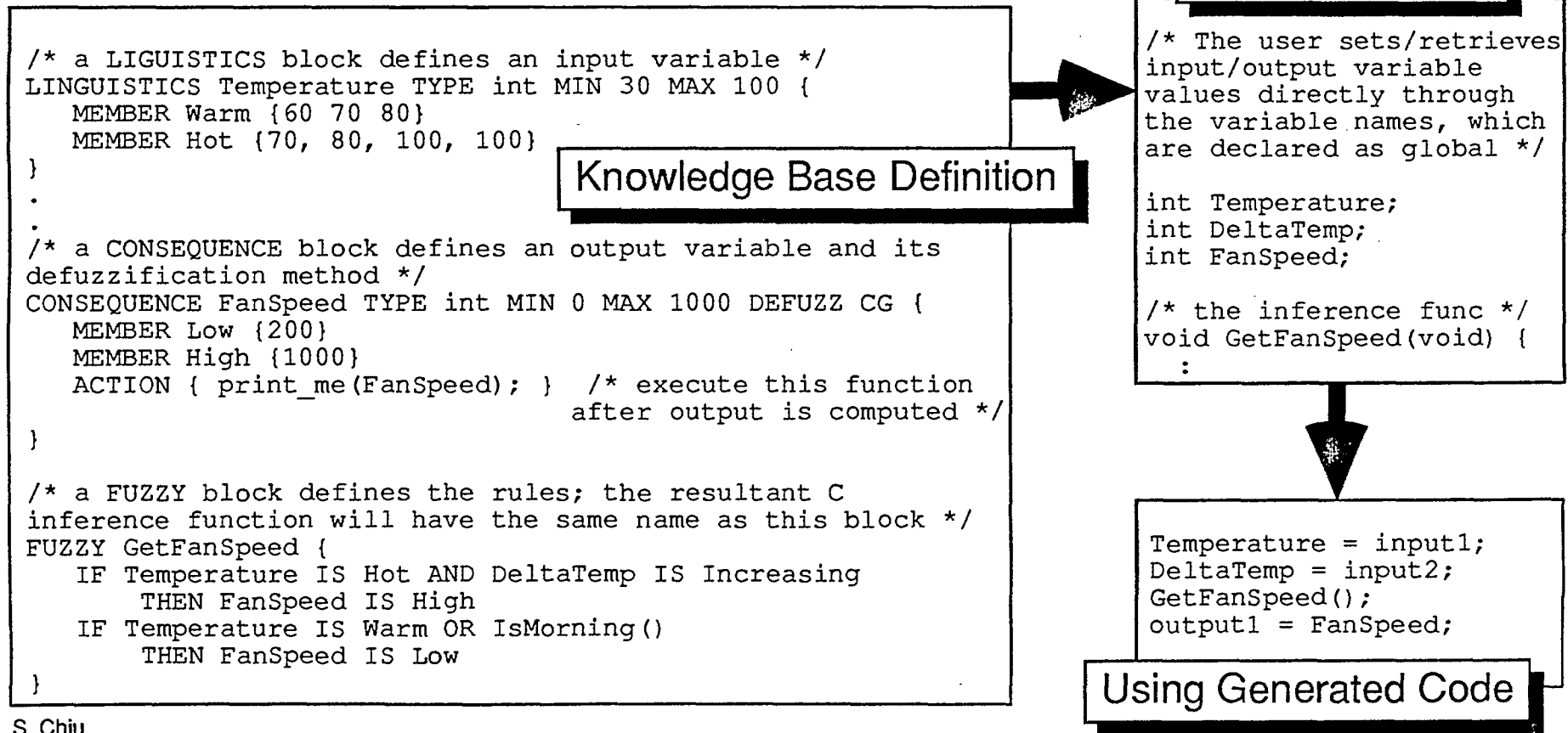
- Shows 3-D surface + 2-D contour & cross sections
- Rule matrix intuitively correlated with control surface



Fuzz-C

C Preprocessor for Fuzzy Logic

- Translates a knowledge base definition file into C code
- Not an environment; run program using DOS command line
- Call fuzzy functions from C and vice versa



Comparison of Software Tools

| Software | Platform | Cost | Comments |
|----------|-------------|--|--|
| CubiCalc | IBM PC | \$500 (1) \$800 (2) \$2500 (3) | <ul style="list-style-type: none"> • Excellent for exploring fuzzy control & prototyping • Has all essential capabilities & more • Built-in numerical comp. & process simulation language • Easy to use & flexible • Ideal for non-programmers & education |
| TILShell | IBM PC, Sun | \$1800 (3) \$3500, (3) + rule learning + on-line debugger | <ul style="list-style-type: none"> • Sophisticated CASE-like tool, packed with features • High flexibility in memb. fn. & rule definition; allows user-defined fuzzy operators • Built-in numerical comp. & process simulation language • Graphical debugging features • Debug & tune rules during simulation or on-line • Rule learning module available • Compilers available for Mistsubishi, Hitachi, & Intel microcontrollers & Togai's FC110 fuzzy chip |
| FIDE | IBM PC | \$1000, (2) + 8-bit μ \$3500, (2) + 8,16,32-bit μ + MATLAB | <ul style="list-style-type: none"> • Define entire knowledge base in one text file • Unique "tracer" debugger • Easily integrates user C code modules for simulation • Includes compiler for Motorola μ-controllers • Compiler available for Omron's FP-3000 fuzzy chip • A practical, low-cost tool for microcontroller applications |

(1) Basic software environment without code generator. (2) Software environment with C run-time library.
 (3) Software environment with C source code generator.

Comparison of Software Tools

| Software | Platform | Cost | Comments |
|------------------|-----------------------------|---|--|
| fuzzyTech | IBM PC | Many versions avail. from \$1000 - \$6900 \$2500 (3) \$6900, (3) + on-line debugger | <ul style="list-style-type: none"> • Can define rules via Fuzzy Assoc. Map matrix • Only one type of connective operator per rulebase • Graphical debugging features • Dynamics simulation via external program • Debug & tune rules during simulation or on-line • Rule-learning module available (\$900) • Target hardware-specific versions available for Intel, Siemens, & SGS Thomson microcontrollers & INFORM's FUZZY-166 chip |
| MATRIXx RT/Fuzzy | Sun, HP, Apollo, VaxStation | \$5000 (1) (\$15000 for MATRIXx SystemBuild) | <ul style="list-style-type: none"> • An add-on block to MATRIXx SystemBuild • Primitive user interface for rule development • High flexibility in memb. fn. definition & inferencing • Simulation support for multi-discipline, integrated sys. • Code generation requires interface to AutoCode (\$5K) and AutoCode itself (\$19K for C, \$25K for Ada) |
| A-B FLEX | IBM PC, Mac | TBD (4) (\$800 for Matlab; \$3000 for Simulink) | <ul style="list-style-type: none"> • Designed for research & fast prototyping • Graphical debugging features • Dynamics simulation & analysis via Matlab/Simulink • Auto. program download to A-B factory controller |

(1) Software environment without code generator. (3) Software environment with C source code generator.

(4) Software environment with C & Ada source code generators.

Comparison of Software Tools

| Software | Platform | Cost | Comments |
|--------------------------|----------|-------|---|
| Manifold Graphics Editor | IBM PC | \$500 | <ul style="list-style-type: none">• A highly intuitive control surface editor• Currently, has the only high-dimension, conventional (i.e., not Fuzzy Assoc. Map) rule matrix editor• Supports only matrix editor - limited rule structure• Generates data files (i.e., "include" files) in C, Basic, Fortran, & many microcontroller assembly languages• Generates knowledge base files in TILShell, FIDE, & Fuzz-C format• Intended for experienced fuzzy system developers |
| Fuzz-C | IBM PC | \$150 | <ul style="list-style-type: none">• Translaes text description of knowledge base into C code• Purely a code translator, not an environment• Allows fuzzy rules to call C functions |

Company Addresses

For information on development tools, contact:

CubiCalc: HyperLogic Corp., 1855 E. Valley Parkway, Suite 210, Escondido, CA 92027, USA, (619) 746-2765.

TIL Shell: Togai InfraLogic Inc., 5 Vanderbilt, Irvine, CA 92718, USA, (714) 588-3800.

fuzzyTech: INFORM Software Corp., 1840 Oak Street, Evanston, IL 60201, USA, (708) 866-1838.

FIDE: Apronix Inc., 2150 N. First St., San Jose, CA 95131, USA, (408) 428-1888.

R/T Fuzzy: Integrated Systems Inc., 3260 Jay St., Santa Clara, CA 95054, USA, (408) 980-1500.

A-B FLEX: Allen-Bradley Co., 747 Alpha Dr., Highland Heights, OH 44143, USA, (216) 646-3436; Contact person: Mr. Chia Day.

Manifold Graphics Editor: Fuzzy Systems Engineering, 12223 Wilsey Way, Poway, CA 92064, USA, (619) 748-7384.

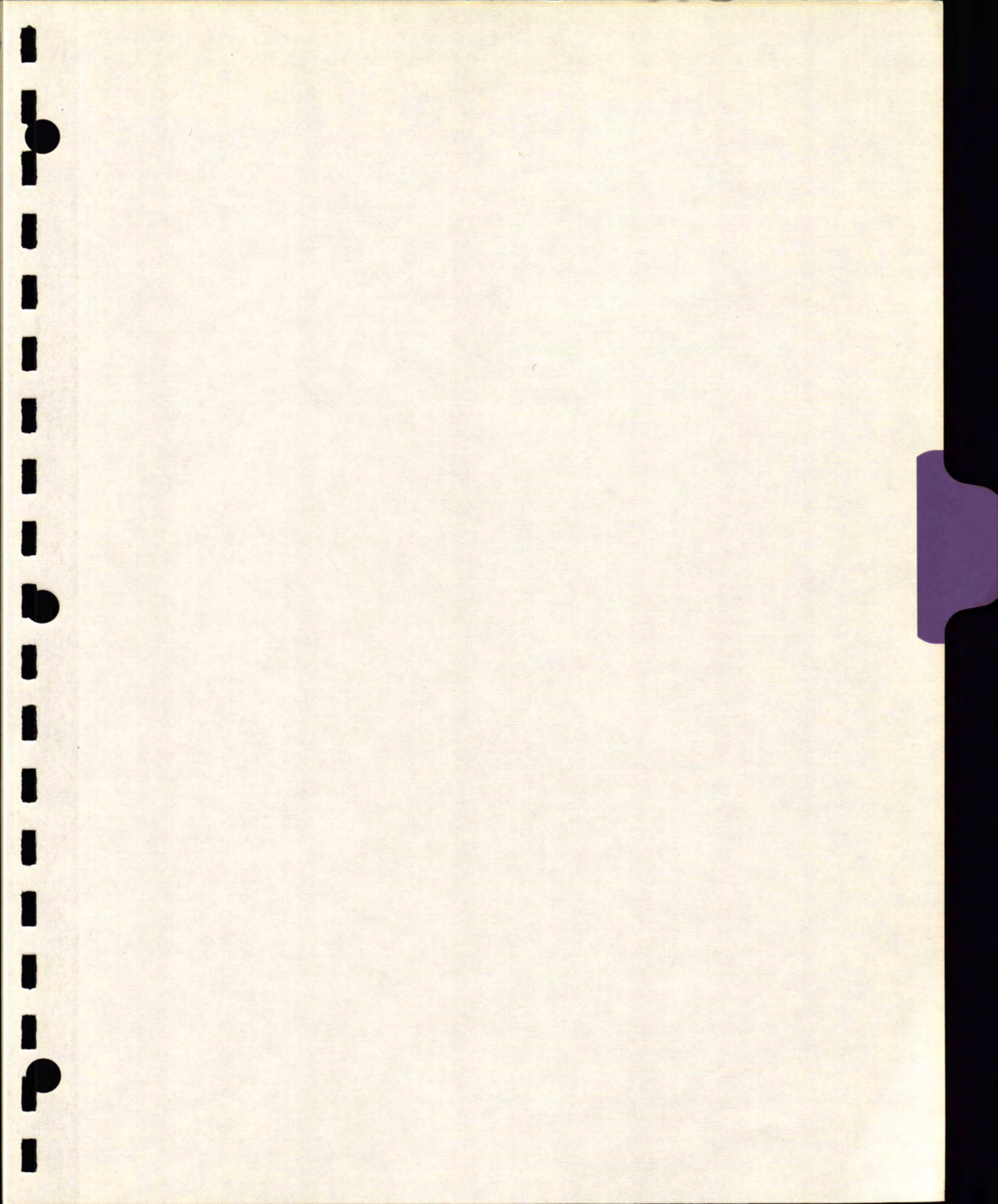
Fuzz-C: Byte Craft Ltd., 421 King St., North Waterloo, Ontario, Canada N2J 4E4, (519) 888-6911.

Some software not included in the presentation:

FUZZYSOFT (similar to fuzzyTech): GTS Trautzl GmbH, Gottlieb-Daimler-Straße 9, D-2358 Kaltenkirchen, Germany, (04191) 8711.

NeuFuz (rule learning program): National Semiconductor, 2900 Semiconductor Dr., Santa Clara, CA 95052, USA, (800) 272-9959.

FuziCalc (fuzzy spreadsheet program): FuziWare Inc., 316 Nancy Lynn Lane, Suite 10, Knoxville, TN 37919, USA, (615) 588-4144.



IMPACT OF FUZZY THEORY ON SCIENCE AND TECHNOLOGY*

Professor Dr. I. B. Türkşen
Principal Investigator - MRCO
University of Toronto
Toronto, Ontario
M5S 1A4

Tel: 416-978-1278
Fax: 416-978-1280
e-mail: turksen@ie.utoronto.ca

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- b) NSERC - Natural Science and Engineering Council of Canada
- c) Industrial Technology Transfer Companies

TRADITION OF QUEST AND RESPECT FOR

WHAT IS QUANTITATIVE AND PRECISE

AND DISDAIN FOR

WHAT IS QUALITATIVE AND IMPRECISE

"BEING" AND HENCE
"NOTHINGNESS"
PARAMENIDES OF ELEA

"BECOMING" AND HENCE
"GRADEDNESS"
HERACLITUS OF EUPHESUS

"THE LAW OF CONTRADICTION"

"THE LAW OF EXCLUDED MIDDLE"

METAPHYSICS -ARISTOTLE (384-
322 BC)

LOGIC CHANGES FROM ITS VERY
FOUNDATIONS IF WE ASSUME
THAT IN ADDITION TO TRUTH AND
FALSEHOOD THERE IS ALSO SOME
THIRD LOGICAL VALUE OR
SEVERAL SUCH VALUES [1920]
LUKASIEWICZ (1978-1955)

QUANTIFIERS: \exists , \forall .

**ALL TRADITIONAL
LOGIC HABITUALLY
ASSUMES THAT PRECISE
SYMBOLS ARE BEING
EMPLOYED. IT IS,
THEREFORE, NOT
APPLICABLE TO THIS
TERRESTRIAL LIFE BUT
ONLY TO AN IMAGINED
CELESTIAL EXISTENCE,
LOGIC TAKES US
NEARER TO HEAVEN
THAN OTHER STUDIES.**

BERTRAND RUSSELL

L. A. ZADEH-FUZZY THEORY

THREE SEMINAL PAPERS THREE INNOVATIVE IDEAS

- i) FUZZY SETS - (1965)
- ii) COMPOSITIONAL RULE OF
INFERENCE (1973)
- iii) GENERALIZED SYLLOGISMS
(1985)
INTRODUCTION OF FUZZY
QUANTIFIERS TO SYLLOGISMS
 - i) REPRESENTATION
 - ii) - iii) INFERENCE

— "BEING" AND HENCE "NOTHINGNESS"

KNOWLEDGE REPRESENTATION

AS A CONSEQUENCE OF HAVING THE
CAPABILITY TO DEAL WITH:

- (A) FUZZY PREDICATES;
- (B) FUZZY TRUTH VALUES;
- (C) FUZZY QUANTIFIERS;
- (D) FUZZY PROBABILITIES; AND
- (E) FUZZY HEDGES.

FUZZY LOGIC HAS A FAR GREATER
EXPRESSIVE POWER THAN TRADITIONAL
SYSTEMS OF LOGIC.

CLASSICAL APPROACH

1. TWO VALUED LOGIC

- a) LAW OF EXCLUDED MIDDLE
- b) LAW OF CONTRADICTION
- c) LAW OF EQUIVALENCE

⋮

2. ANALYTICAL EQUATIONS

- a) LINEAR AND NON-LINEAR
- b) DIFFERENTIAL & INTEGRAL
- c) POINT- TO - POINT

⋮

$M \rightarrow P$

FUZZY APPROACH

1. MULTI AND INFINITE VALUED LOGICS

- QUALIFIED {
- a) EXCLUDED MIDDLE
 - b) CONTRADICTION
 - c) EQUIVALENCE

⋮

2. RULE BASES

- a) LINGUISTIC & COGNITIVE
 - i) LINGUISTIC VARIABLES
 - ii) LINGUISTIC VALUES
 - iii) CONNECTIVES
- b) CLUSTER TO CLUSTER

⋮

$$[M' \circ [M \rightarrow P]] \rightarrow P'$$

PROPERTIES OF DATA

1. CLASSICAL APPROACH

- a) ABSOLUTE SCALE •
- b) RATION SCALE +
- c) INTERNAL SCALE AVE
- d) ORDINAL SCALE (MAX, MIN)

MAXIMALLY SPECIFIC
- CAN NOT EXPLOIT TOLERANCE -

2. FUZZY APPROACH

- a) ORDINAL SCALE (T, S)
- b) INTERVAL SCALE (AVE)
- c) RATIO SCALE +
- d) ABSOLUTE SCALE •

MINIMALLY SPECIFIC
-CAN EXPLOIT TOLERANCE -

| SCALE TYPE | ADMISSIBLE <u>TRANSFORMATION</u> |
|------------|-------------------------------------|
|------------|-------------------------------------|

| | |
|---------|-----------|
| ORDINAL | MONOTONIC |
|---------|-----------|

$$\phi^* = f(\phi)$$

| | |
|----------|-----------------|
| INTERVAL | POSITIVE LINEAR |
|----------|-----------------|

$$\phi^* = c_1\phi + c_2, c_1 > 0$$

| | |
|-------|------------|
| RATIO | SIMILARITY |
|-------|------------|

$$\phi^* = c_1\phi$$

| | |
|----------|----------|
| ABSOLUTE | IDENTITY |
|----------|----------|

$$\phi^* = 1 \cdot \phi$$

HARDNESS, TEMPERATURE, LENGTH,
MEMBERSHIP, PROBABILITY, COUNT

MAX, MIN, AVERAGE, ADDITION,
MULTIPLICATION

LINGUISTIC CONNECTIVES

"AND", "OR", "IF ... THEN"

EXPRESS A MULTIPLICITY OF
MEANINGS REFLECTING
DIFFERENT SEMANTIC
INTERACTION OF ITS
CONSTITUENT PROPOSITIONS
WITH EACH OTHER AND OTHER
KNOWLEDGE.

INTERCLAUSAL RELATIONSHIPS
OF "AND" CONNECTIVE
(PETERSON AND MCCABE, 1987)

- i) COORDINATION OR
ADDITIVE: EXPRESSING
CO-OCCURENCE OF
INDEPENDENT EVENTS
- ii) TEMPORAL (BETTER
EXPRESSED BY "THEN"):
INDICATING TEMPORAL
AND/OR CAUSAL
SEQUENCE
- iii) CAUSAL (BETTER EXPRESSED
BY "BECAUSE" OR "SO")
- iv) ADVERSATIVE (BETTER
EXPRESSED BY "BUT")

SYMMMETRIC - ASYMMETRIC
CONJUNCTION: "AND"
(FILLENBAUM, 1977)

1. "HE HAD A COFFEE AND READ
THE PAPER"

- SYMMETRIC, UNORDERED
(COMMUTATIVITY AXIOM)

2. a) "HE DIED AND WAS BURIED"

b) "HE WAS BURIED AND DIED"

ORDERED: TEMPORAL AND/OR
CAUSAL

(NON-COMMUTATIVITY AXIOM)

A FUZZY EXPERT SYSTEM FOR COST-ACCOUNTING

a)

IF PRODUCTION EFFORT IS HIGH
"AND" PRICE IS LOW

"AND" PROFITABILITY IS HIGH
THEN SET FLAG TO 1

b)

IF FLAG IS 1 "AND" LABOUR
INTENSITY IS LOW

"AND" PRIORITY SCHEDULE
DISPLACEMENT IS LOW

THEN SOLUTION IS SYSTEM 1

SYMMETRIC - ASYMMETRIC
DISJUNCTION: "OR"
(FILLENBAUM, 1977)

1. "IT WILL BE SUNNY OR THE
SKYDOME ROOF WILL BE
CLOSED"

SYMMETRIC, UNORDERED
(COMMUTATIVITY AXIOM)

2. "YOU'D BETTER LEAVE OR
HE'LL GET MAD"

ORDERED: TEMPORAL
AND/OR CAUSAL
(NON-COMMUTATIVITY AXIOM)

Alternative Definitions for Fuzzy-Set Intersection

- Zadeh Intersection:

$$(A \cap B)(x) = \min [A(x), B(x)]$$

- Product Intersection:

$$(A \cap B)(x) = A(x) \cdot B(x)$$

- Lukasiewicz Intersection

$$(A \cap B)(x) = \max [A(x) + B(x) - 1, 0]$$

Operators that satisfy reasonable axioms for a truth-functional definition of intersection are called *triangular norms* (or *T-norms*)

Alternative Definitions for Fuzzy-Set Union

- Zadeh Union:

$$(A \cup B)(x) = \max [A(x), B(x)]$$

- Product Union:

$$(A \cup B)(x) = A(x) + B(x) - A(x) B(x)$$

- Lukasiewicz Union

$$(A \cup B)(x) = \min [A(x) + B(x), 1]$$

Operators that satisfy reasonable axioms for a truth-functional definition of union are called *triangular conorms* (or *T-conorms*)

De Morgan Triples

De Morgan Laws for Conventional Sets:

$$\overline{A \cap B} = \overline{A} \cup \overline{B}$$

$$\overline{A \cup B} = \overline{A} \cap \overline{B}$$

- Triples consisting of an Intersection operator, Union operator, and Complement functions that generalize the DeMorgan Laws are called *DeMorgan triples*.

Examples:

- Zadeh: $\{\min(\alpha, \beta), \max(\alpha, \beta), 1 - \alpha\}$
- Product: $\{\alpha\beta, \alpha + \beta - \alpha\beta, 1 - \alpha\}$
- Lukasiewicz: $\{\max(\alpha + \beta - 1, 0), \min(\alpha + \beta, 1), 1 - \alpha\}$

AXIOMS

- BOUNDARY
- MONOTONICITY
- COMMUTATIVITY
- ASSOCIATIVITY
- DISTRIBUTIVITY
- IDEMPTENCY
- ABSORPTION

•

•

•

EXCLUDED MIDDLE

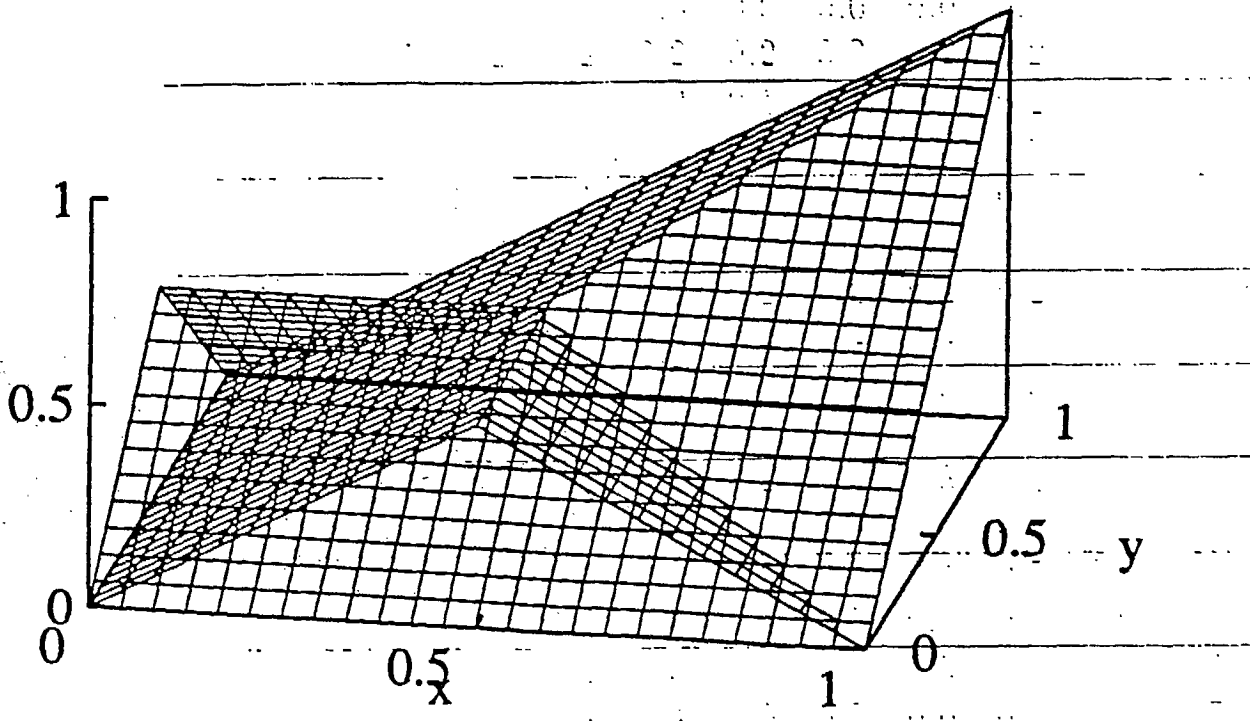
CONTRADICTION

$$A \cup \bar{A} = I, A \cup \bar{A} \subseteq I$$

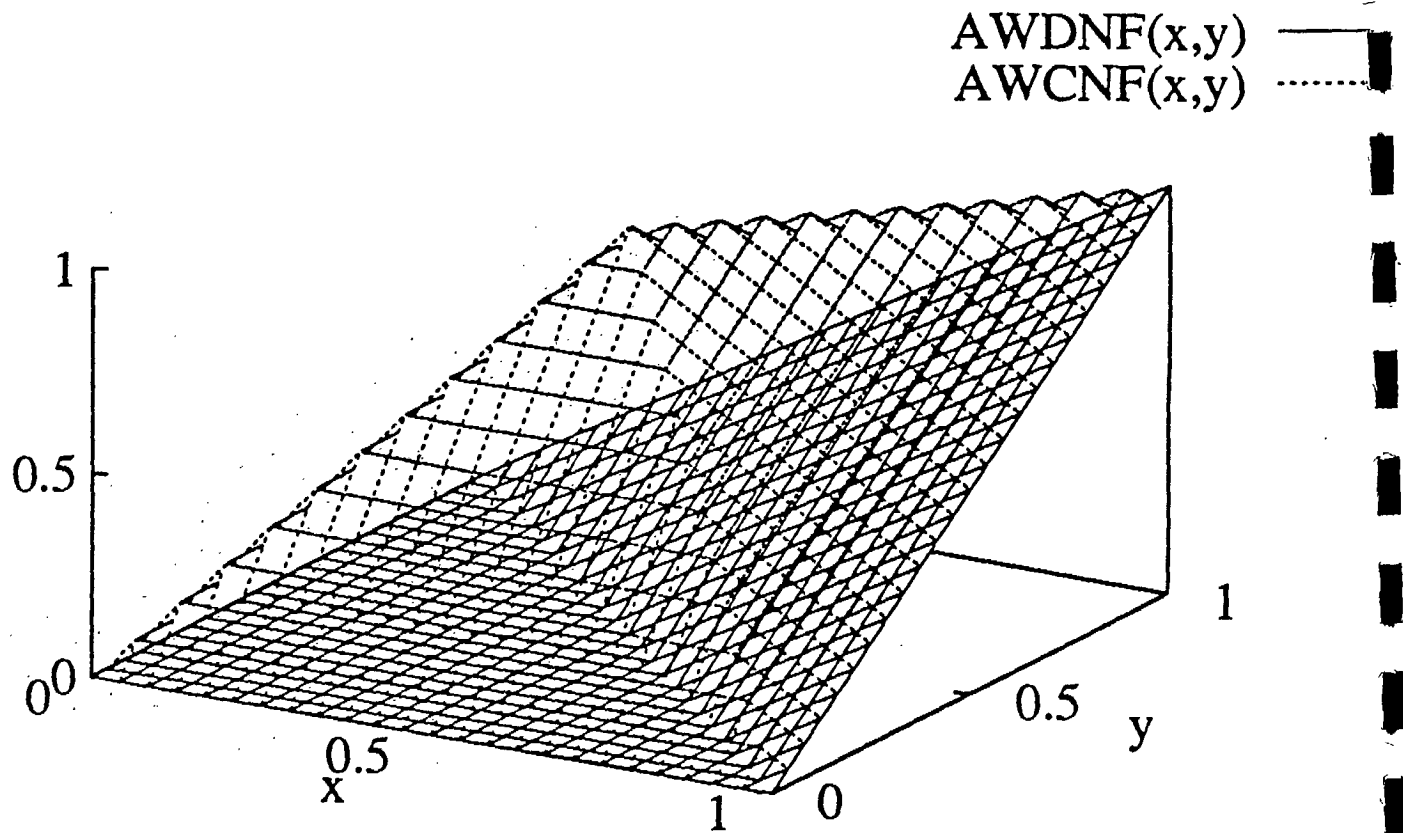
$$A \cap \bar{A} = \emptyset, A \cap \bar{A} \supseteq \emptyset$$

DNF and CNF of AND with $\langle \min, \max, N \rangle$

AMDNF(x,y) ———
AMCNF(x,y) - - - - -

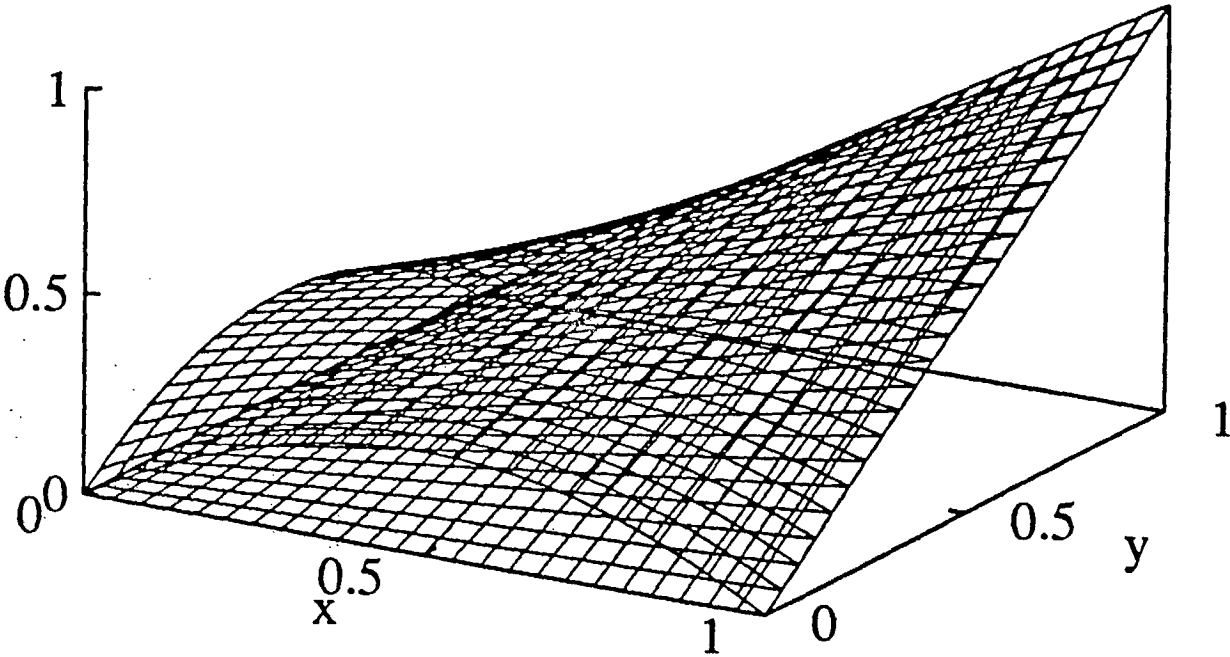


DNF and CNF of AND with Lukasiewicz triples



DNF and CNF of AND with Algebraic triples

AADNF(x,y) ———
AACNF(x,y) - - - - -



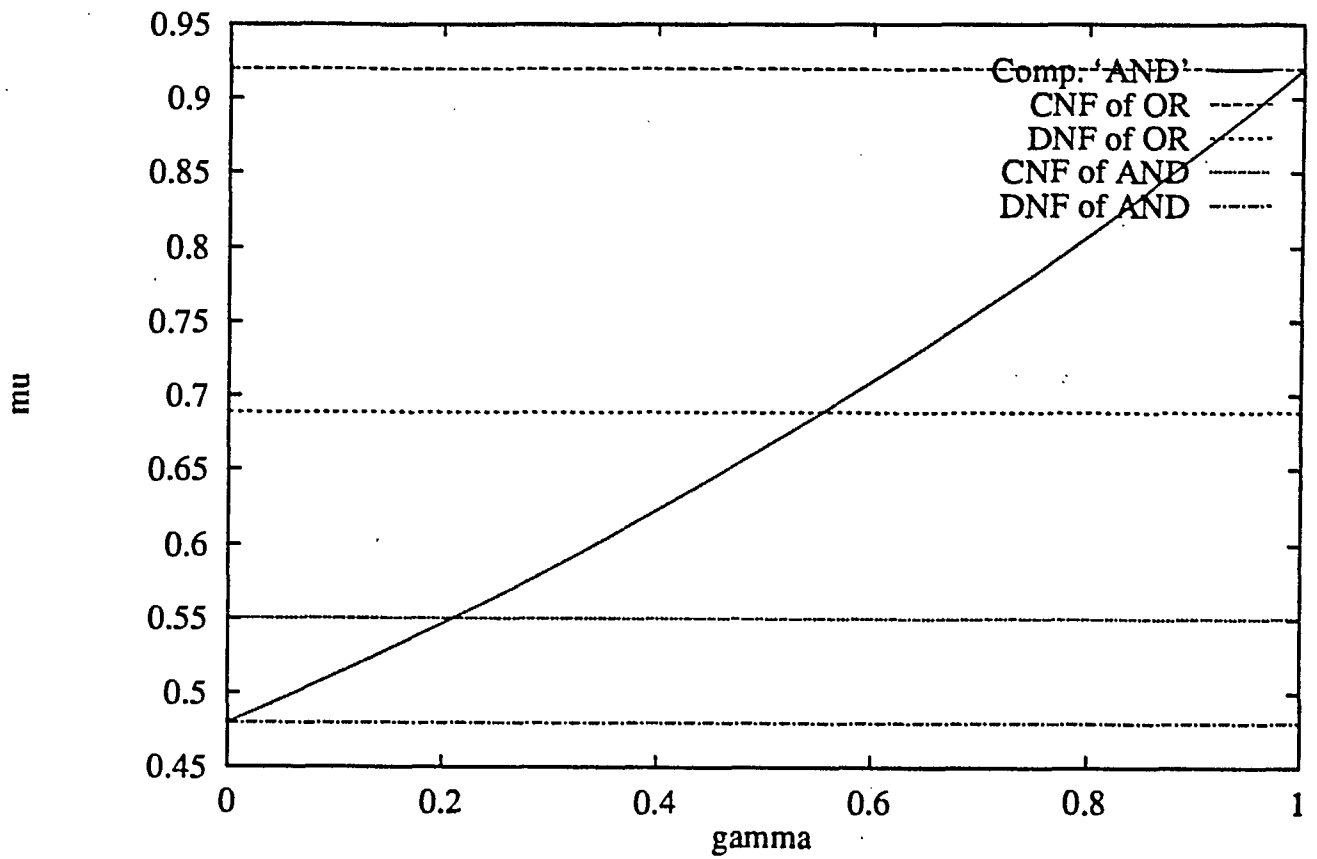
COMPENSATORY 'AND'

$$\mu_{A \theta B} = \mu_{A \cap B}^{1-\gamma} \mu_{A \cup B}^{\gamma} \quad (1)$$

or as:

$$\mu_{A \theta B} = (1 - \gamma) \mu_{A \cap B} + \gamma \mu_{A \cup B} \quad (2)$$

Figure 1: IVFS "A AND B", "A OR B", expressed in DNF and CNF and "Exponential Compensatory AND" using algebraic sum-product for realization of t-conorm and t-norm for $\mu_A = 0.8, \mu_B = 0.6$ and $\gamma \in [0, 1]$.



S-Implications

Definition 1 *S-implications are functions $f_S: [0, 1] \times [0, 1] \rightarrow [0, 1]$ defined by*

$$f_S(a, b) = S(1 - a, b)$$

where S is a continuous t -conorm.

Examples:

| $S(a, b)$ | $f_S(a, b)$ | |
|------------------|----------------------|---------------|
| $a \vee b$ | $(1 - a) \vee b$ | Kleene-Dienes |
| $a + b - ab$ | $1 - a + ab$ | Reichenbach |
| $1 \wedge a + b$ | $1 \wedge 1 - a + b$ | Lukasiewicz |

R-Implications

Definition 2 *R-implications* are functions $f_R: [0, 1] \times [0, 1] \rightarrow [0, 1]$ defined by

$$f_R(a, b) = \sup\{x \in [0, 1] \mid T(a, x) \leq b\}$$

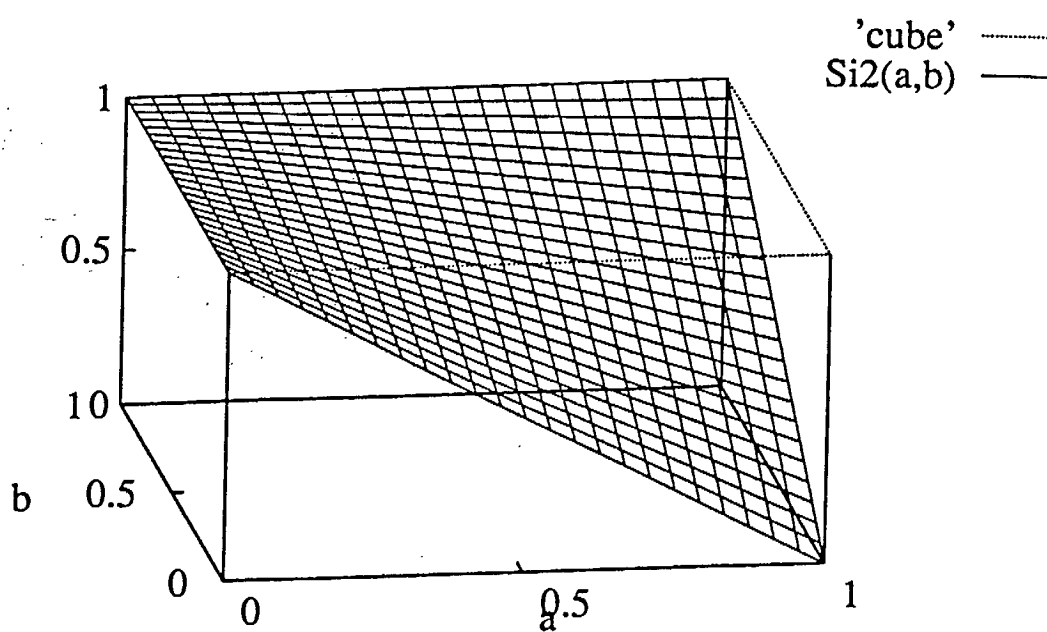
for which a continuous *t*-norm T exists.

Examples:

| $T(a, b)$ | $f_R(a, b)$ | |
|--------------------|---|-------------|
| $a \wedge b$ | $\begin{cases} 1, & \text{if } a \leq b; \\ b, & \text{otherwise.} \end{cases}$ | Gödel |
| ab | $\begin{cases} 1, & \text{if } a = 0; \\ 1 \wedge \frac{b}{a}, & \text{otherwise.} \end{cases}$ | Goguen |
| $0 \vee a + b - 1$ | $1 \wedge 1 - a + b$ | Łukasiewicz |

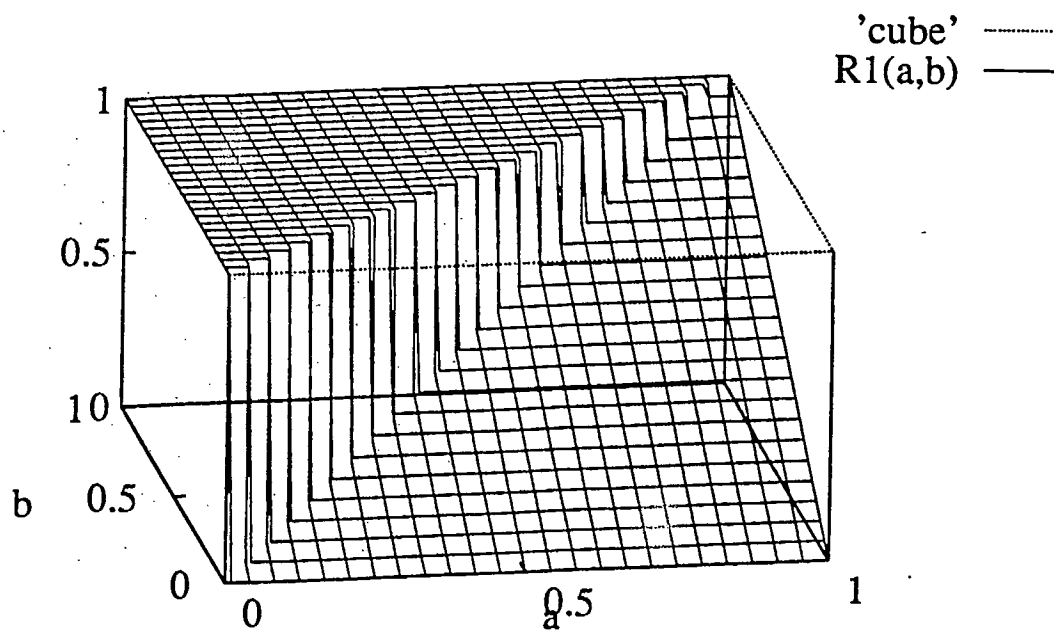
Reichenbach Implication:

$$f_S(a, b) = 1 - a + ab$$



Gödel Implication:

$$f_R(a, b) = \begin{cases} 1, & \text{if } a \leq b; \\ b, & \text{otherwise.} \end{cases}$$



From axiomatic point of view, the following properties have been requested for a 2-place operation I that represents an implication function, Dubois and Prade (1991):

I1: if $a \leq a'$ then $I(a, b) \geq I(a', b)$,

I2: if $b \geq b'$ then $I(a, b) \geq I(a, b')$,

I3: $I(0, b) = 1$ (falsity implies anything),

I4: $I(1, b) = b$ (tautology cannot justify anything),

I5: $I(a, b) \geq b$,

I6: $I(a, a) = 1$ (identity principle),

I7: $I(a, I(b, c)) \leq I(b, I(a, c))$ (exchange principle),

I8: $I(a, b) = 1$ iff $a \leq b$ (implication defines an ordering),

I9: $I(a, b) = I(n(a), n(b))$ for some strong negation n (contraposition law),

I10: I is continuous.

General form of S and R -implications

S and R -implications could be merged into a single family provided that the class of t -norms is enlarged to *non-commutative conjunction operators*, Dubois and Prade 1984).

The general form of the implication functions is:

$$f_{\mathcal{M}}(a, b) = \sup\{x \in [0, 1] \mid \mathcal{M}(a, x) \leq b\}. \quad (1)$$

| t -norm $T(a, b)$ | Pseudo-conjunction $T^*(a, b)$ |
|------------------------|---|
| $a \wedge b$ | $\begin{cases} 0, & \text{if } a + b \leq 1; \\ b, & \text{otherwise.} \end{cases}$ |
| ab | $\begin{cases} 0, & \text{if } a = 0; \\ 0 \vee \frac{a+b-1}{a}, & \text{otherwise.} \end{cases}$ |
| $0 \vee a + b - 1$ | $0 \vee a + b - 1$ |

It is also possible to enlarge the class of t -conorms to *non-commutative disjunction operators* (N) to generate the R -implications through the form $N(1 - a, b)$.

The general form of the implication functions becomes:

$$f_N(a, b) = N(1 - a, b) \quad (2)$$

| t -cnorm $S(a, b)$ | Pseudo-disjunction $S^*(a, b)$ |
|-------------------------|---|
| $a \vee b$ | $\begin{cases} 1, & \text{if } a + b \geq 1; \\ b, & \text{otherwise.} \end{cases}$ |
| $a + b - ab$ | $\begin{cases} 1, & \text{if } a = 1; \\ 1 \wedge \frac{b}{1-a}, & \text{otherwise.} \end{cases}$ |
| $1 \wedge a + b$ | $1 \wedge a + b$ |

If N is chosen as a t -conorm S in (2) then the implication is an S -implication.

If N is chosen as a pseudo-disjunction in (2) then the implication is an R -implication.

APPROXIMATE REASONING

INFERRING CONCLUSIONS FROM A FUZZY RULE BASE AND AN OBSERVATION

A. SOME OF OUR CONCERNS

- i) REASONING METHODS FOR
DECISION AND CONTROL**
- ii) PRESERVATION OF
CLASSICAL RESULTS**

Rules of Inference

1. Modus Ponens

$$p \rightarrow q$$
$$p$$
$$\therefore q$$

2. Modus Tollens

$$p \rightarrow q$$
$$\neg q$$
$$\therefore \neg p$$

3. Hypothetical Syllogism

$$p \rightarrow q$$
$$q \rightarrow r$$
$$\therefore p \rightarrow r$$

B. SOME OF THE APPROACHES

ii) EFFECTIVE HEURISTICS

ZADEH-MAMDANI-ASSILIAN: FUZZY GRAPH

WANG-MENDEL: FAM, . . .
SUGENO, ET.AL.: P, P-G, P & P-G

TÜRKŞEN: IVCRI

TÜRKŞEN, ET. AL: IVAAR

TÜRKŞEN, ZHAO: ILFSI

MUKAIDONO, SHEN, DING, WANG:
RPIV-REVISION PRINCIPLE AND ITS
VARIATIONS

iii) DEFUZZIFICATION METHODS

CGM
MMVM

fuzzy reasoning is based on linguistic rules .

R^1 : if X_1 is A_1^1 and ... and X_j is A_j^1 then Y is B^1

⋮ ⋮

R^I : if X_1 is A_1^I and ... and X_j is A_j^I then Y is B^I

X_1 is A_1' and ... and X_j is A_j'

Y is B'

(i) ZADEH'S COMPOSITIONAL RULE OF INFERENCE
(POINT-VALUED)(CRISP CONNECTIVES)

- Implication:

$$R^i = A^i \rightarrow B^i$$

- Aggregation of antecedent:

$$A^i = \bigcap_{j=1}^J A_j^i$$

- Aggregation of observations:

$$A' = \bigcap_{j=1}^J A'_j$$

- Compositional Rule of Inference: (CRI)

$$B^{i'} = A' \circ R^i$$

- The final estimation of consequence:

$$B' = \bigoplus_{i=1}^I B^{i'}$$

where $\bigoplus \in \{ \vee, \wedge \}$

The point-valued membership value of inferred consequence

$$h_{B'}(y) = \bigcup_{i=1}^I \sup_{x_1, \dots, x_J} [T\{ \bigwedge_{j=1}^J h_{A'_j}(x_j), (\bigwedge_{j=1}^J h_{A_j^i}(x_j) \rightarrow h_{B^i}(y)) \}]$$

where $h_{A_j^i}(x_j)$, $h_{A'_j}(x_j)$, $h_{B^i}(y)$, and $h_{B'}(y)$ are the corresponding membership function values for the fuzzy sets, A_j^i , A'_j , B^i , B' , respectively, and T is t-norms operator.

sup-min operations in the model

$$h_{B'}(y) = \bigcup_{i=1}^I [\sup_{x_1, \dots, x_J} (\bigwedge_{j=1}^J h_{A_j'}(x_j)) \wedge (\bigwedge_{j=1}^J h_{A_j^i}(x_j) \rightarrow h_B^i(y))] .$$

IMPLICATION: " \rightarrow "

$$h_{RC}^i(x, y) = h_A^i(x) \wedge h_B^i(y) \quad (\text{Mamdani})$$

$$h_{Ra}^i(x, y) = (1 - h_A^i(x) + h_B^i(y)) \quad (\text{Lukasiewicz})$$

$$h_{Ra}^i(x, y) = \frac{h_B^i(y)}{h_A^i(x)} \wedge 1 \quad (\text{Goguen})$$

$$h_{Rg}^i(x, y) = \begin{cases} 1, & h_A^i(x) \leq h_B^i(y) \\ h_B^i(y), & h_A^i(x) > h_B^i(y) \end{cases} \quad (\text{Gödel})$$

where $h(x, y)$ means;

$$h_{R^i}(x_j, y) = \bigwedge_{j=1}^J h_{A_j^i}(x_j) \rightarrow h_B^i(y) .$$

MODUS PONENS

$$A \rightarrow B$$

$$A$$

$$B$$

$$A \circ (A \rightarrow B) = A \circ (\neg A \cup B)$$

$$a_i \in A, b_j \in B \quad a_i, b_j \in \{0,1\}$$

$$A = (1/1, 1/2, 0/3) \quad B = (0/1, 1/2, 1/3)$$

$$\neg A \cup B = \begin{matrix} & 0 & 1 & 1 \\ 0 & \left(\begin{matrix} 0 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{matrix} \right) \end{matrix}$$

$$A \circ (A \rightarrow B) = (1, 1, 0) \begin{pmatrix} 0 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \\ = (1, 1, 0)$$

$$b_j = \bigvee_i a_i \wedge (\neg a_i \vee b_j)$$

GENERALIZED MODUS PONENS

$$A \rightarrow B$$

$$\frac{A'}{B'}$$

$$a \in A, b \in B, a' \in A', b' \in B'$$

$$A' \circ (A \rightarrow B)$$

$$A' \circ (\neg A \cup B)$$

$$b'_j = \bigvee_i a'_i \wedge (\neg a_i \vee b_j)$$

$$A = (1/1, 7/2, 0/3)$$

$$B = (0/1, 6/2, 1/3)$$

$$A' = (1/1, 6/2, 2/3)$$

$$TAVB = \begin{matrix} & 0 & .6 & 1 \\ 0 & \left(\begin{matrix} 0 & .6 & 1 \\ .3 & .6 & 1 \\ 1 & 1 & 1 \end{matrix} \right) \\ .3 & & & \\ 1 & & & \end{matrix}$$

$$(1, .6, 2) \begin{pmatrix} 0 & .6 & 1 \\ .3 & .6 & 1 \\ 1 & 1 & 1 \end{pmatrix} =$$

$$(.3, .6, 1) = B' \neq B$$

$$\alpha = .3$$

$$B'_{\alpha=.3} = B$$

B. SOME OF THE APPROACHES

i) FORMAL LOGICAL MODELS

ZADEH'S: CRI

ZAHEH'S: INTERPOLATIVE
REASONING

ZAHEH'S: SYLLOGISTIC REASONING

DUBOIS-PRADE, TRILLAS-VALVERDE:
DESIRABLE CHARACTERISTICS
DECOMPOSITION-INFERENCE

FUZZY GRAPH-INTERPOLATION: FGI ZADEH-MAMDANI-ASSILIAN

$$\begin{aligned}
 h_{B'}(y) &= \bigvee_{i=1}^I \left[\bigvee_{x_1, \dots, x_J} \left(\bigwedge_{j=1}^J h_{A_j'}(x_j) \right) \wedge \left\{ \bigwedge_{j=1}^J (h_{A_j^i}(x_j) \wedge h_{B^i}(y)) \right\} \right] \\
 &= \bigvee_{i=1}^I \left[\bigwedge_{j=1}^J \left(\bigvee_{x_j} (h_{A_j'}(x_j) \wedge h_{A_j^i}(x_j)) \right) \wedge h_{B^i}(y) \right] .
 \end{aligned}$$

FGI IS A "REDUCTION" TYPE INFERENCE

000 INFERENCE METHODS - I

00 GENERALIZED MODUS PONENS: GMP(CRI)

(ZADEH, 1973)

0 SINGLE RULE: $A \rightarrow C$

$$A' \circ (A \rightarrow C) = C'$$

a) EXPANSION TYPE INFERENCE
 $C \subseteq C'$ ALWAYS

b) REDUCTION TYPE INFERENCE
 $C' \subseteq C$ ALWAYS

c) OTHER TYPES

AT TIMES $C \subseteq C'$

AT OTHER TIMES $C' \subseteq C$

d) IF $A' = A$, THEN USUALLY

$$A' \circ (A \rightarrow C) \neq C$$

000 INFERENCE METHODS - II

00 GENERALIZED MODUS PONENS

0 INFERENCE WITH MULTIPLE RULES (TURKSEN-TIAN, 1992)

a) FITA

$$A' \circ (A_k \rightarrow C_k) = C'_k \quad K=1, \dots, K,$$

$$C' = \oplus C'_k$$

b) FATI

$$R = \oplus R_k = \oplus (A_k \rightarrow C_k)$$

$$C' = A' \circ R = A' \circ [\oplus (A_k \rightarrow C_k)]$$

i) TYPE OF AGGREGATION (COMBINATION) OPERATOR?

$$\oplus \in \{T, S\}, \oplus \in \{\wedge, \vee\}$$

000 INFERENCE METHODS - II

00 GENERALIZED MODUS PONENS

0 INFERENCE WITH MULTIPLE RULES (TURKSEN-TIAN, 1992)

ii) TYPE OF INFERENCE?

1) EXPANSION TYPE, $C \subseteq C'$: $\oplus = \wedge$

2) REDUCTION TYPE, $C' \subseteq C$: $\oplus = \vee$
(SUBJECT TO CONSTRAINTS
AND CONDITIONS)

MP1 - IF $A' = A_{k^*}$ THEN $C' = C_{k^*}$

i.e., $C' = \bigoplus_k C_k = C_{k^*}$

MP2 - IMPLICATION CONSTRAINTS

000 INFERENCE METHODS - I

00 GENERALIZED MODUS PONENS

0 SINGLE RULE

b) RESPONSES TO P1:

i) $\alpha\text{-cut} = \bigvee_i (a_i \wedge (1 - a_i))$

(TURKSEN - YAO, 1984)
FROM "DNF" AND "CNF"
REPRESENTATION

ii) PSEUDO-CONJUNCTION
(DUBOIS-PRADE, 1984, 1989)
(TABLES 1 AND 2)

$$f_M(a,b) = \sup\{x \in [0,1] \mid M(a,x) \leq b\}$$

iii) Given " \circ ", THEN DERIVE " \rightarrow "
(DUBOIS-PRADE, 1984, 1991)

iv) Given " \rightarrow ", THEN DERIVE " \circ "
(TRILLAS-VALVERDE, 1985)

Compositional Rule of Inference

Single antecedent inference with fuzzy input and fuzzy output.

$$\begin{array}{r} \text{Rule: } (A \Rightarrow C) \\ \text{Observation: } A' \\ \hline \text{Conclusion: } C^* \end{array}$$

Or in short,

$$C^* = A' \circ_{\mathcal{M}} (A \Rightarrow C),$$

where $\circ_{\mathcal{M}}$ is the *Max-M* composition.

In membership domain,

$C^* = A' \circ_{\mathcal{M}} (A \Rightarrow C)$, becomes

$$\mu_{C^*}(k) = \forall_i \mathcal{M}[\mu_{A'}(i), \mu_A(i) \Rightarrow \mu_C(k)], \forall k.$$

Dubois & Prade (1984) and Trillas & Valverde (1984) identified the functions for \Rightarrow and \mathcal{M} that should be used together so that C^* will satisfy the following four properties P1–P4.

Desired Properties of Inference:

- P1- $C \subseteq C^*$,
- P2- $C^* = C$ when $A' = A$,
- P3- If $A' \subseteq A''$ then $C^{*'} \subseteq C^{*''}$,
- P4- For $A' = \bar{A}$, $C^* = I$.

Suggested operator selection table:

| | Implication: \Rightarrow | Operator: \mathcal{M} |
|----|----------------------------|-------------------------------|
| 1- | Gödel | minimum |
| 2- | Goguen | product |
| 3- | Lukasiewicz | bold-intersection |
| 4- | Kleene-Dienes | $\mathcal{M}(\text{minimum})$ |
| 5- | Reichenbach | $\mathcal{M}(\text{product})$ |

Where:

| Implication | $a \Rightarrow b$ |
|---------------|---|
| Gödel | $\begin{cases} 1, & \text{if } a \leq b; \\ b, & \text{otherwise.} \end{cases}$ |
| Goguen | $\begin{cases} 1, & \text{if } a = 0; \\ 1 \wedge \frac{b}{a}, & \text{otherwise.} \end{cases}$ |
| Lukasiewicz | $1 \wedge 1 - a + b$ |
| Kleene-Dienes | $(1 - a) \vee b$ |
| Reichenbach | $1 - a + ab$ |

and,

| Operator | $\mathcal{M}(a, b)$ |
|-------------------------------|---|
| minimum | $a \wedge b$ |
| product | ab |
| bold-intersection | $0 \vee a + b - 1$ |
| $\mathcal{M}(\text{minimum})$ | $\begin{cases} 0, & \text{if } a + b \leq 1; \\ b, & \text{otherwise.} \end{cases}$ |
| $\mathcal{M}(\text{product})$ | $\begin{cases} 0, & \text{if } a = 0; \\ 0 \vee \frac{a+b-1}{a}, & \text{otherwise.} \end{cases}$ |

Max-min composition with Kleene-Dienes implication is also among the most popular operator combinations, inspite of the fact that it violates property P2.

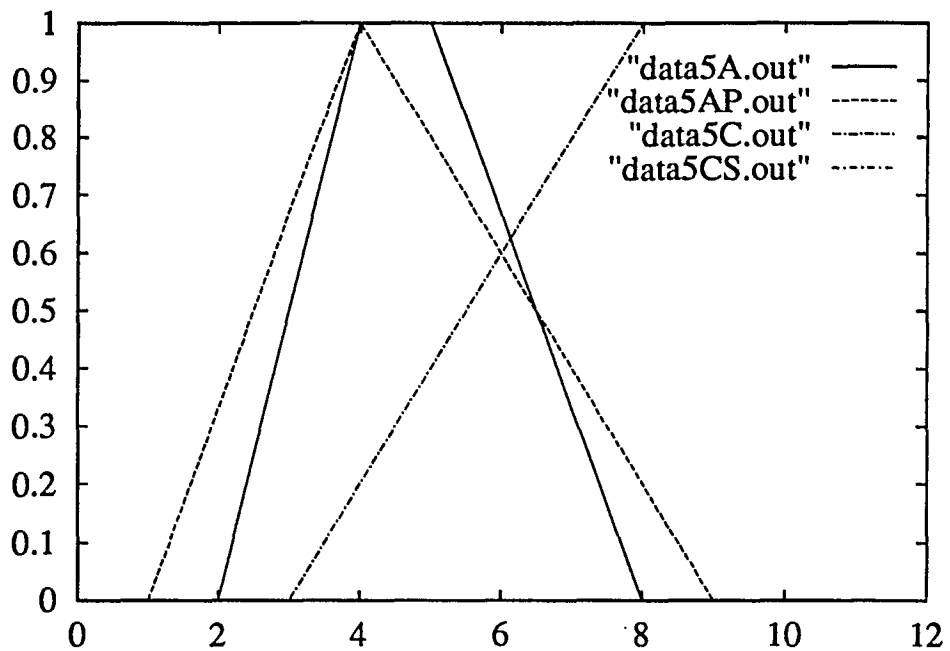
Consider

$$A = (0/1, 0/2, .50/3, 1/4, 1/5, .66/6, .33/7, 0/8, 0/9, 0/10)$$

$$C = (0/1, 0/2, 0/3, .20/4, .40/5, .60/6, .80/7, 1/8, 1/9, 1/10)$$

$$A' = (0/1, .33/2, .67/3, 1/4, .80/5, .60/6, .40/7, .20/8, 0/9, 0/10)$$

throughout the examples.



What is C^* ?

Example 1: *Max-min-Gödel* composition.

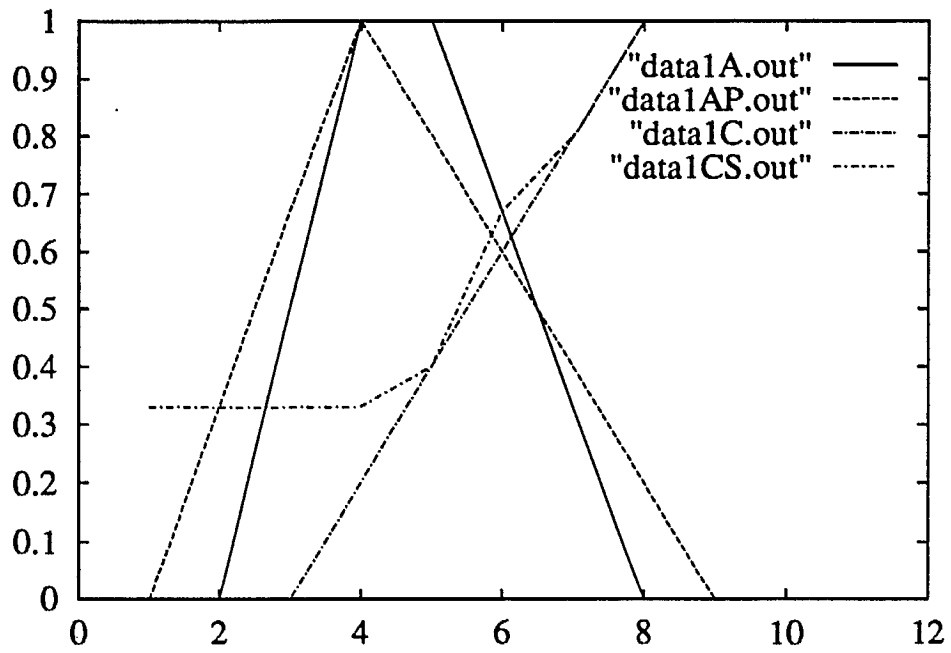
$$\mu_{C^*}(k) = \bigvee_i [\mu_{A'}(i) \wedge \mu_A(i) \Rightarrow \mu_C(k)], \quad \forall k$$

where,

$$\mu_A(i) \Rightarrow \mu_C(k) = \begin{cases} 1, & \text{if } \mu_A(i) \leq \mu_C(k); \\ \mu_C(k), & \text{otherwise.} \end{cases}$$

$$\begin{bmatrix} 0.00 \\ 0.33 \\ 0.67 \\ 1.00 \\ 0.80 \\ 0.60 \\ 0.40 \\ 0.20 \\ 0.00 \\ 0.00 \end{bmatrix} \wedge \begin{bmatrix} 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 0.0 & 0.0 & 0.0 & 0.2 & 0.4 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 0.0 & 0.0 & 0.0 & 0.2 & 0.4 & 0.6 & 0.8 & 1.0 & 1.0 & 1.0 \\ 0.0 & 0.0 & 0.0 & 0.2 & 0.4 & 0.6 & 0.8 & 1.0 & 1.0 & 1.0 \\ 0.0 & 0.0 & 0.0 & 0.2 & 0.4 & 0.6 & 1.0 & 1.0 & 1.0 & 1.0 \\ 0.0 & 0.0 & 0.0 & 0.2 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \end{bmatrix} = \begin{bmatrix} 0.33 \\ 0.33 \\ 0.33 \\ 0.33 \\ 0.40 \\ 0.67 \\ 0.80 \\ 1.00 \\ 1.00 \\ 1.00 \end{bmatrix}$$

Example 1: *Max-min-Gödel* composition, *continued*.



**DOMAIN SPECIFIC
METHODOLOGIES**

FUZZY

NEURAL

STOCHASTIC

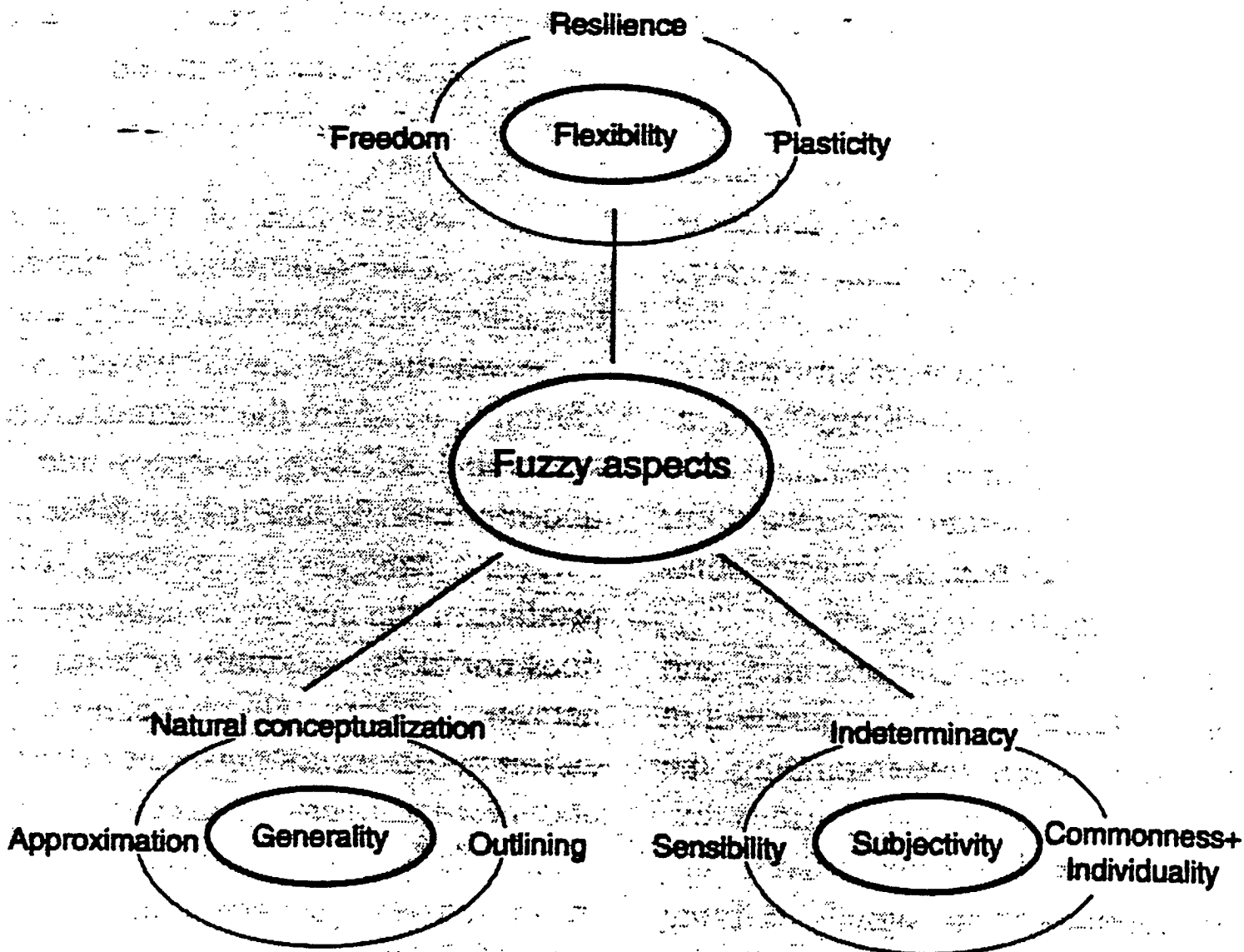
AI - EXPERT SYSTEMS

**FUZZY THEORY ENHANCES AND ENRICHES
CAPABILITIES OF CLASSICAL THEORIES AND
METHODOLOGIES.**

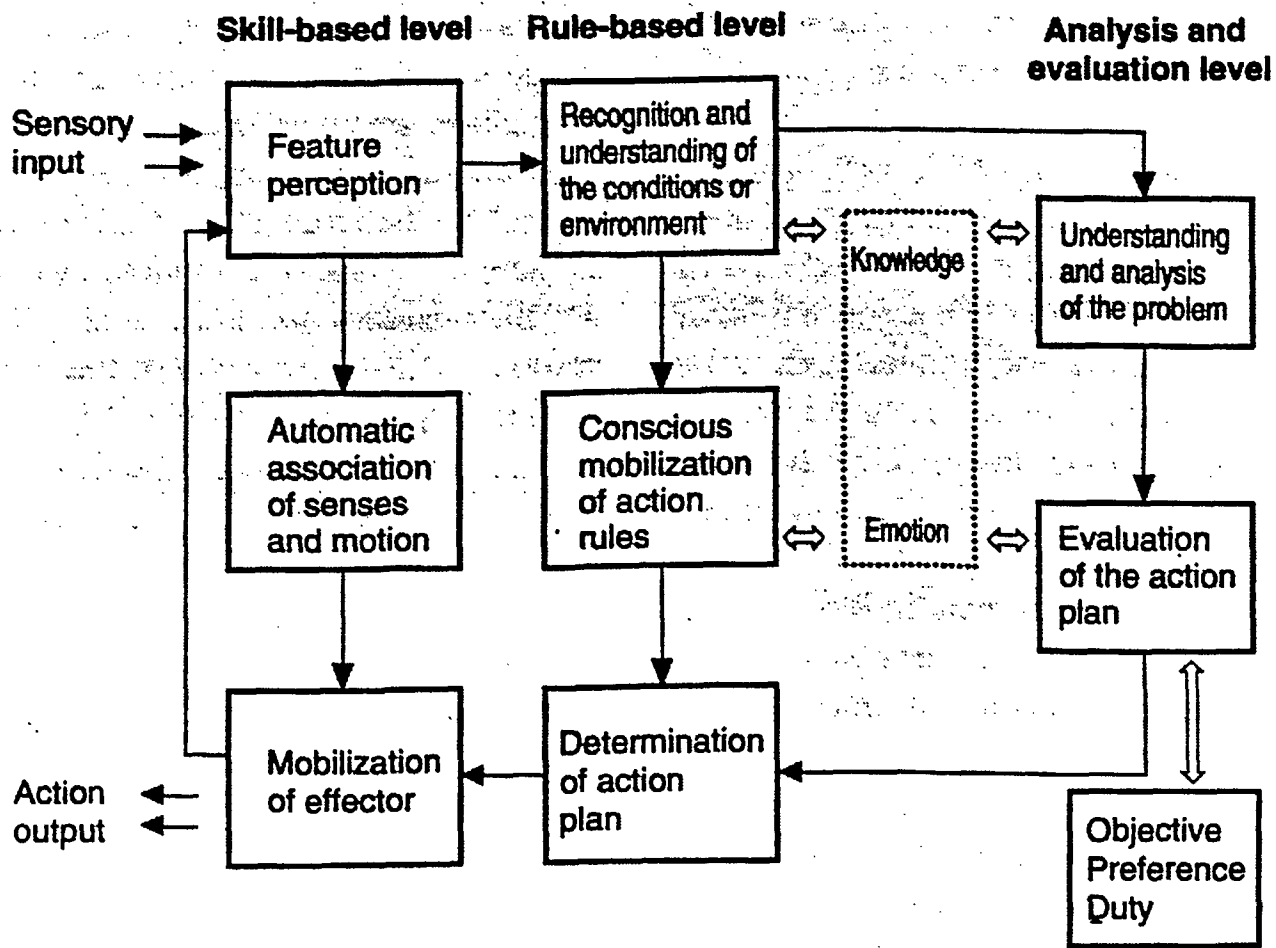
Levels of Information Processing in Human Communication

Table 1

| LEVEL | INFORMATION PROCESSING | EXAMPLES |
|--|------------------------|---|
| I Senses | Symbol | Sound, line, color |
| II Recognition | Signal | Language, contours (shape) |
| III Understanding (of micro knowledge) | Local meaning | Meanings of words, single objects |
| IV Understanding (of macro knowledge) | Global meaning | Meanings of sentences, complex objects |
| V Understanding (of emotions and intentions) | Impression, conception | Association, imagination, the arts, personality |



Aspects of fuzziness in human information processing



Framework of human information processes in decision making

SUMMARY

FUZZY SETS AND LOGICS
HAS A DEFINITE IMPACT

ON

1) OUR SCIENTIFIC THINKING
AND MODEL BUILDING

a) KNOWLEDGE REDPRESENTATION

b) APPROXIMATE REASONING

2) OUR TECHNOLOGICAL
IMPLEMENTATION

a) FLEXIBLE

b) ROBUST

c) ENERGY SAVING

d) COST EFFECTIVE

⋮

APPLICATIONS OF FUZZY THEORY*

Professor Dr. I. B. Türkşen
Principal Investigator - MRCO
University of Toronto
Toronto, Ontario
M5S 1A4

Tel: 416-978-1278
Fax: 416-978-1280
e-mail: turksen@ie.utoronto.ca

* Supported in part by:

- a) MRCO - Manufacturing Research Corporation of Ontario
- b) NSERC - Natural Science and Engineering Council of Canada
- c) Industrial Technology Transfer Companies

B. APPROACHES (CONT')

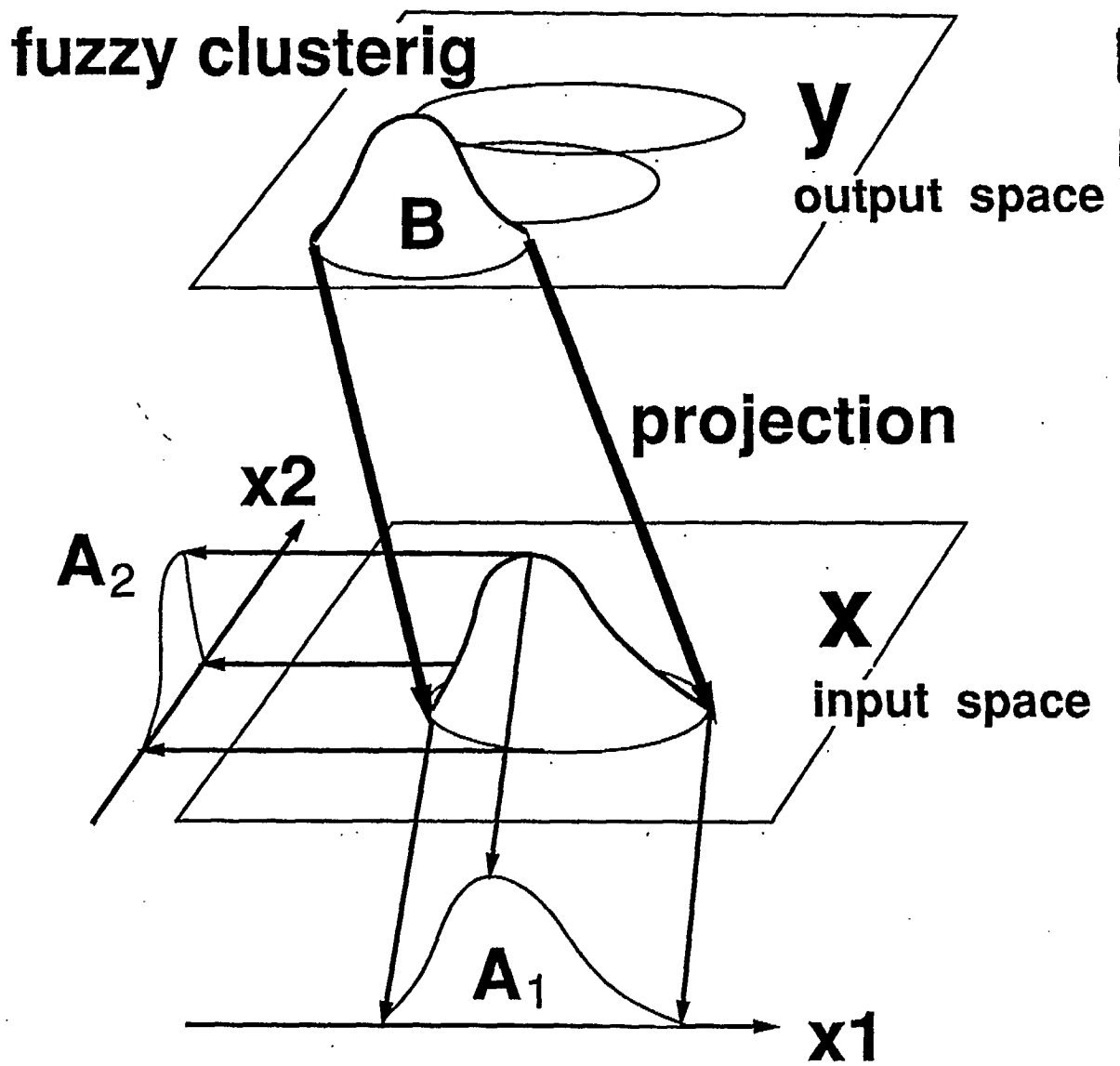
II) INPUT - OUTPUT

**A) FUZZY CLUSTER ANALYSIS
(BEZDEK - SUGENO)**

**B) FUZZY ASSOCIATIVE
MEMORY
(WANG - MENDEL)**

**C) INDUCTIVE LEARNING
FUZZY CLASSIFICATION
(QUINLAN - TURKSEN - ZHAO)**

Formation of Fuzzy Rules based on Fuzzy Clustering



R; If x_1 is A_1 and x_2 is A_2 then

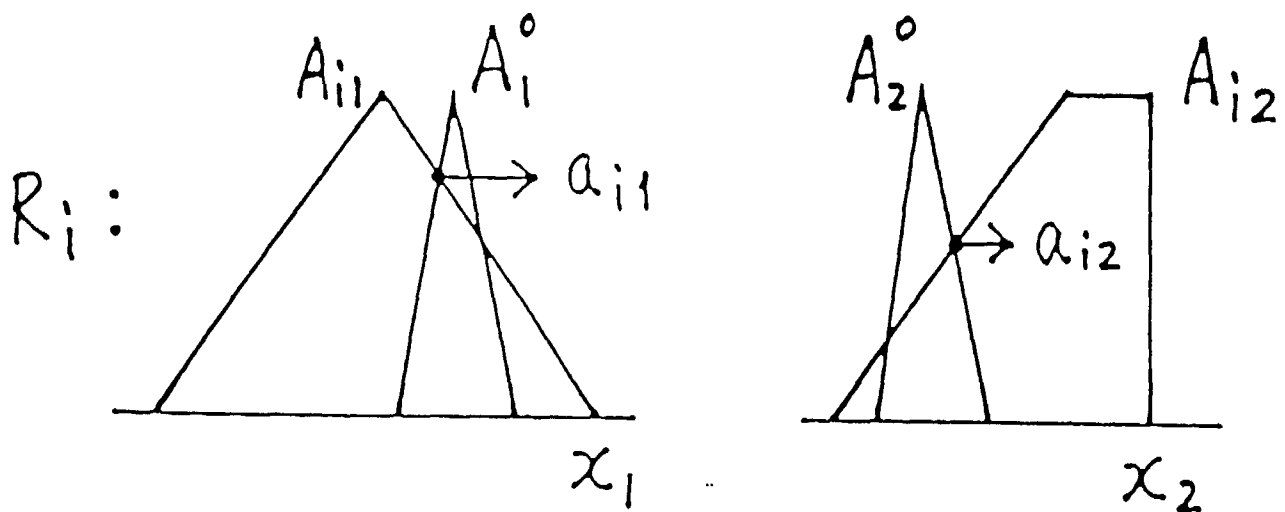
y is B .

Steps in Fuzzy Reasoning

- (1) Compatibility of Premises
- (2) Reasoning by Single Rule
- (3) Aggregation and Defuzzification

Compatibility of Premise with Fuzzy Input

$$w_i = a_{i1} * a_{i2}$$



$A_1^{\circ}, A_2^{\circ} : \text{Fuzzy Inputs}$

$$a_{i1} = \max_{x_1} [A_{i1}(x_1) \wedge A_i^{\circ}(x_1)]$$

(1) Compatibility of Premises

$$w_i = A_{i1}(x_1^{\circ}) \otimes A_{i2}(x_2^{\circ})$$

x_1°, x_2° : singleton inputs

\otimes : min or multiplication

2) Reasoning by Single Rule

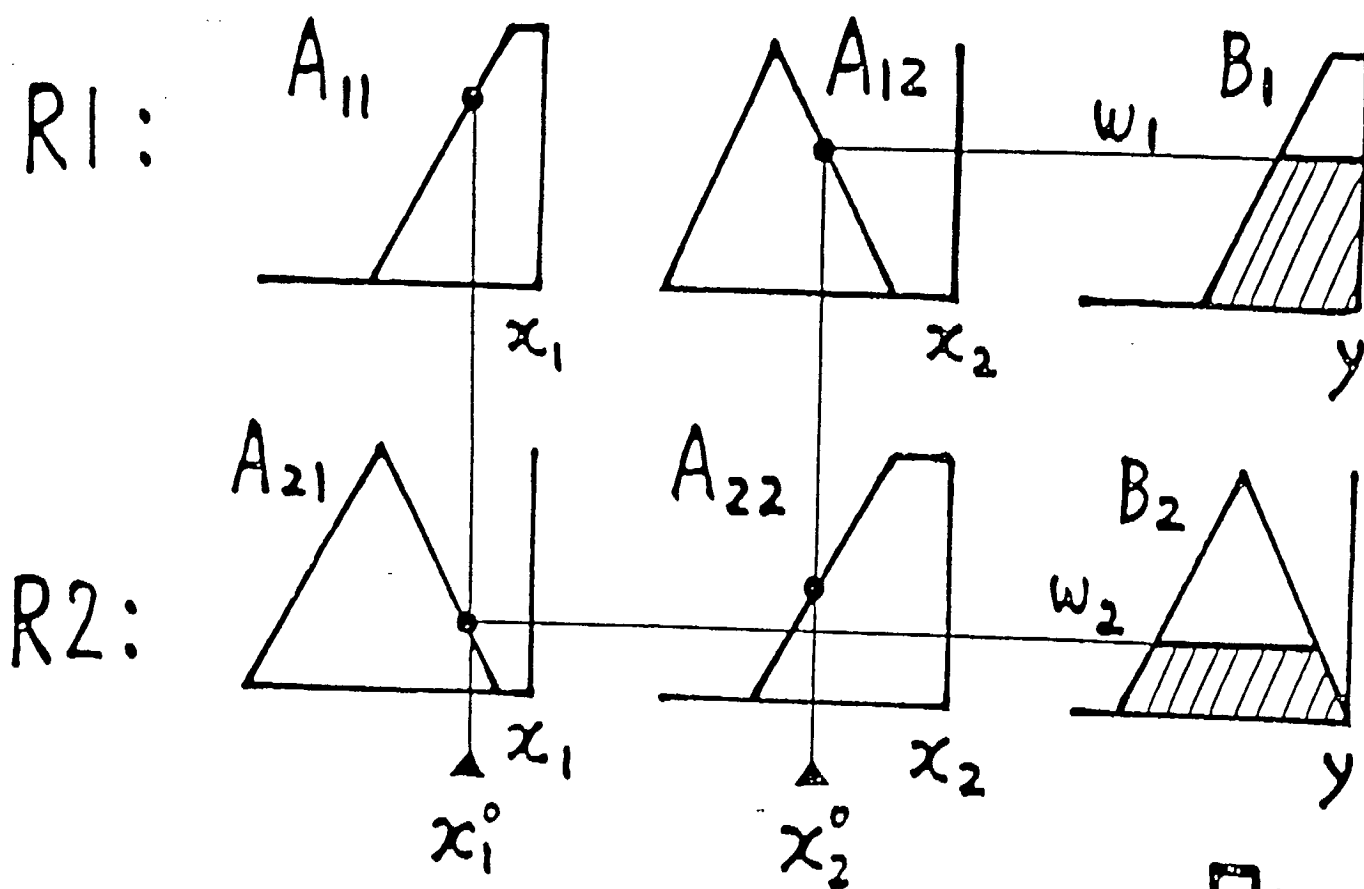
$$B_i^*(y) = w_i \otimes B_i(y)$$

B_i : Consequent of a Rule

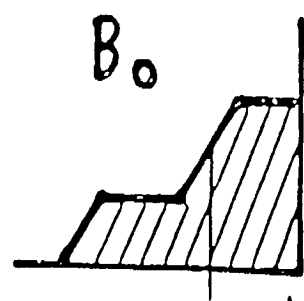
B_i^* : Result by Reasoning

\otimes : min or multiplication

Mamdani's Method of Reasoning for Fuzzy Control

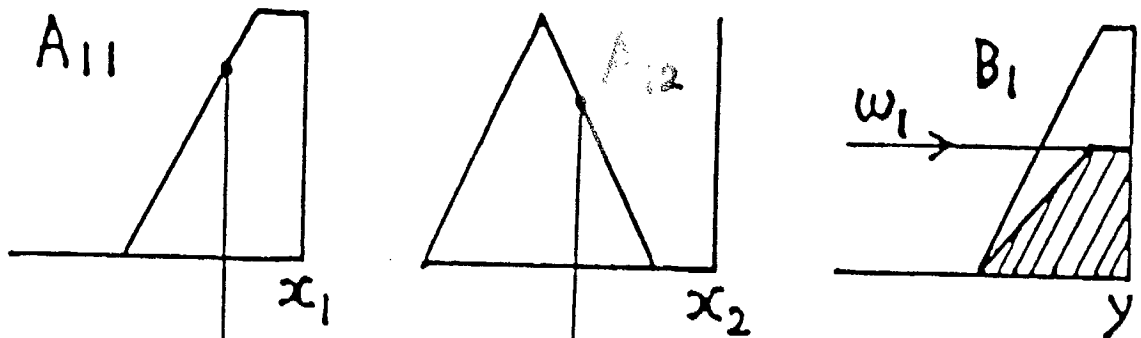


Min - Max Aggregation

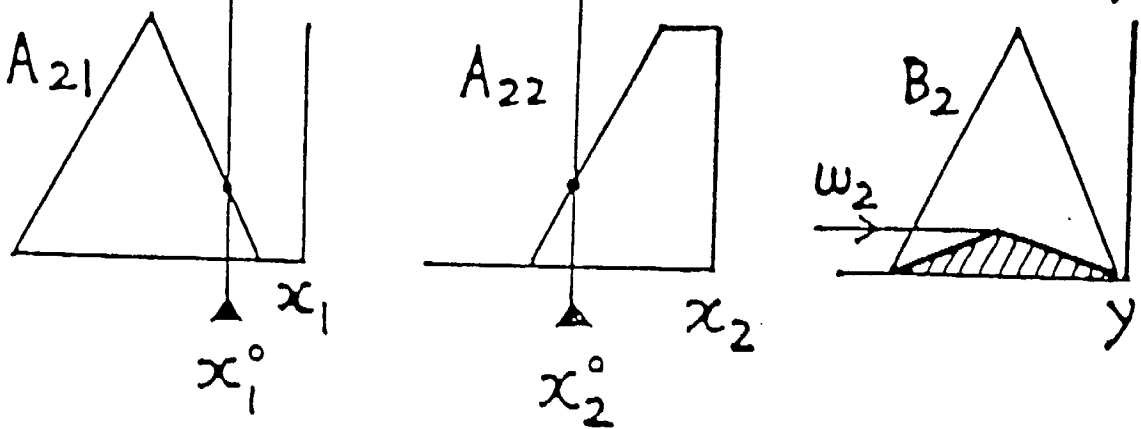


Modified Mamdani's Method

R1:

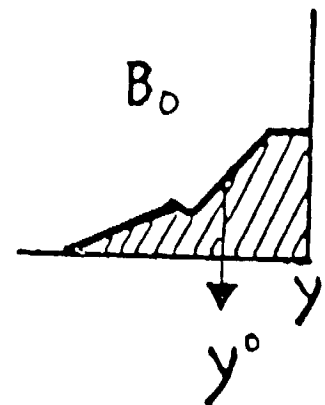


R2:



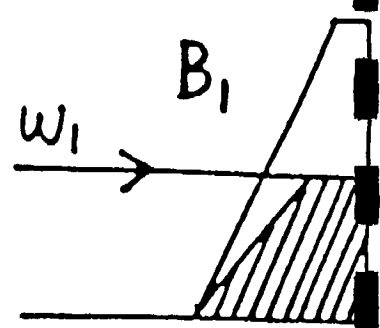
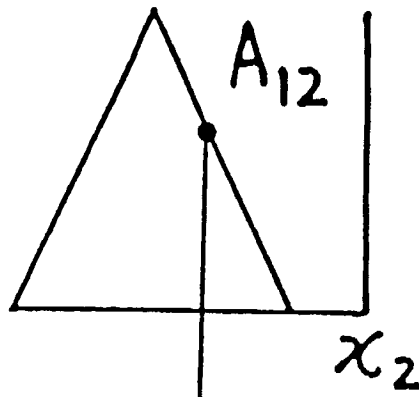
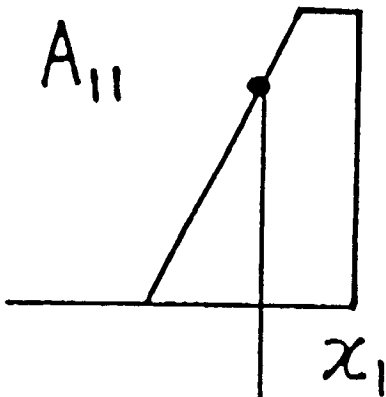
Multiplication

- Max Aggregation

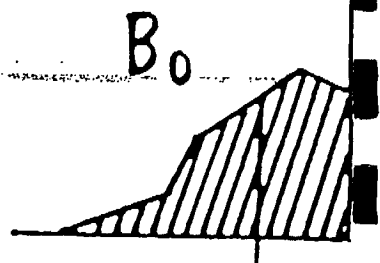
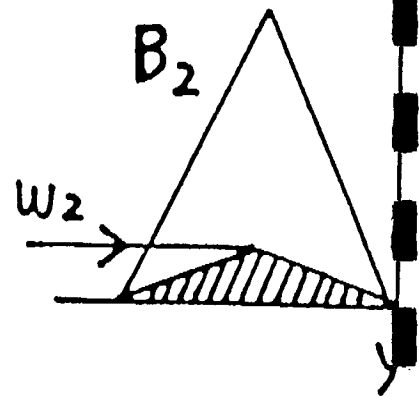
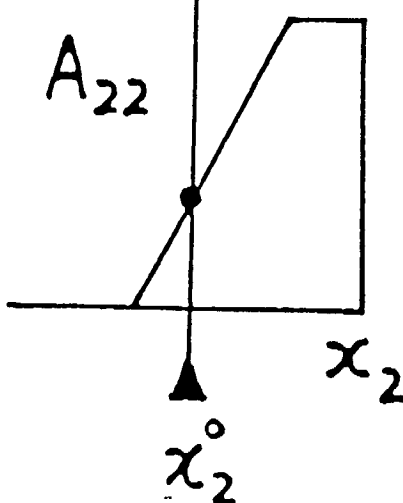
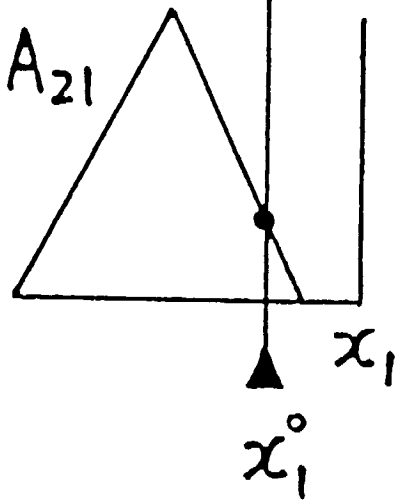


Multiplication - Additive Aggregation

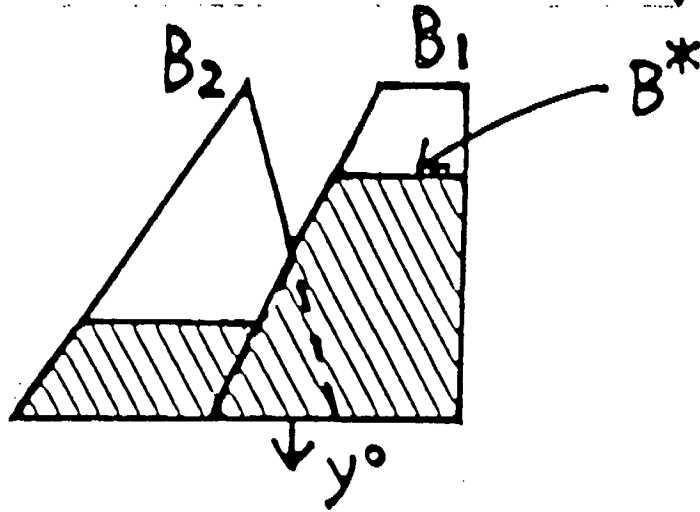
R1:



R2:

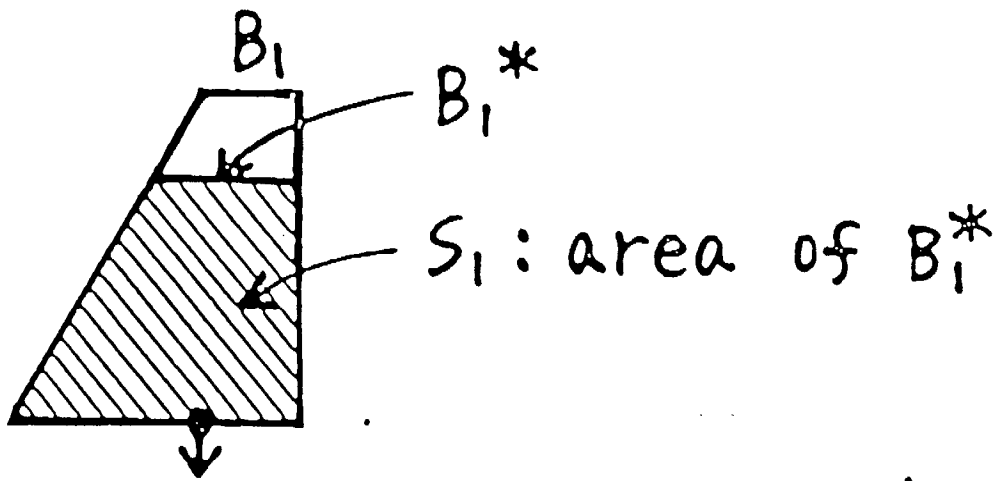


Center of Gravity Method

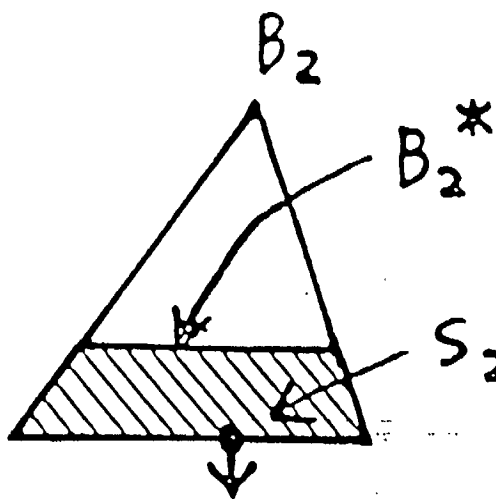


$$y^0 = \frac{\int B^*(y) y dy}{\int B^*(y) dy}$$

Area Method



b_1 : center of gravity of B_1



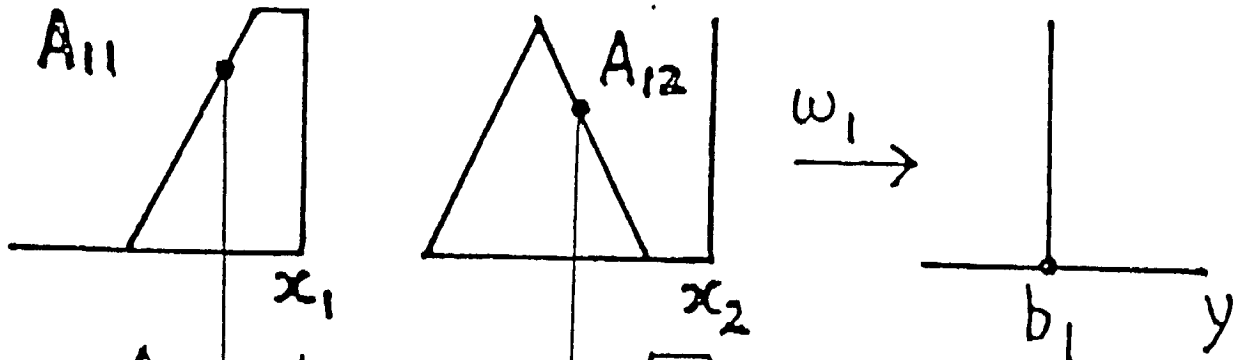
$$y^0 = \frac{b_1 S_1 + b_2 S_2}{b_1 + b_2}$$

S_2 : area of B_2^*

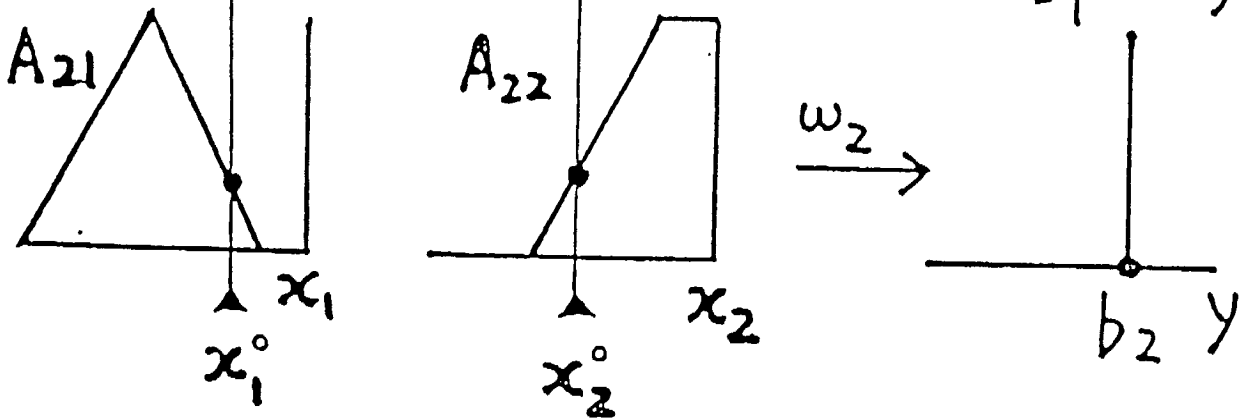
b_2 : center of gravity of B_2

Fuzzy Control Rules with Singleton Consequents

R1:



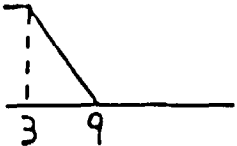
R2:

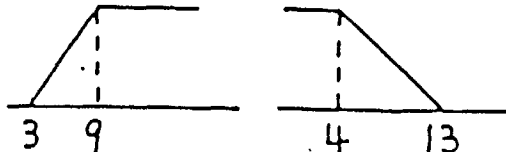


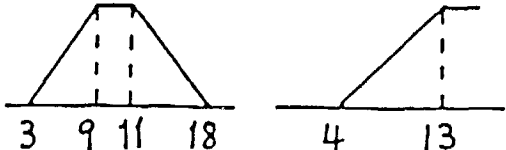
$$(1) \quad y^{\circ} = \frac{w_1 b_1 + w_2 b_2}{b_1 + b_2}$$

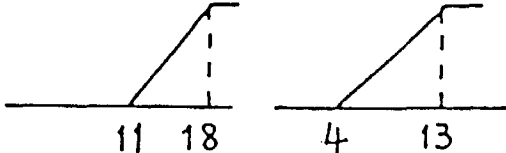
(2) $y^{\circ} = b_i$ with the greatest compatibility w_i

Fuzzy Control Rules with Functional Consequents

R1:  $\rightarrow y^1 = 1.0x_1 + 0.5x_2 + 1.0$

R2:  $\rightarrow y^2 = 0.1x_1 + 4.0x_2 + 1.2$

R3:  $\rightarrow y^3 = 0.9x_1 + 0.7x_2 + 9.0$

R4:  $\rightarrow y^4 = 0.2x_1 + 0.1x_2 + 0.2$

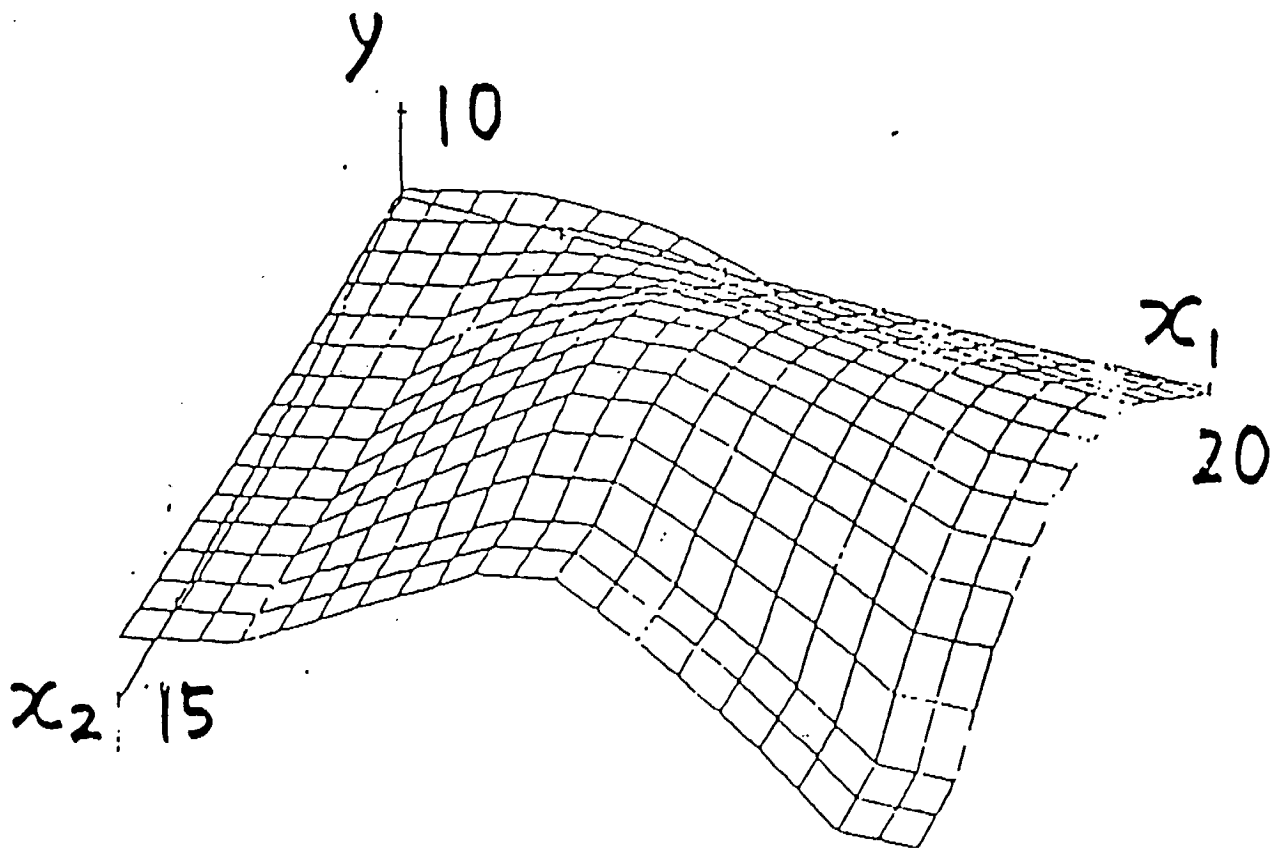
R^i : if x_1 is A_{i1} and x_2 is $A_{i2} \dots$
 then $y^i = f^i(x_1, x_2, \dots)$

$$w^i \triangleq \prod_j A_{ij}(x_j^0)$$

$$y^0 = \frac{\sum w^i y^i}{\sum w^i}$$

$$= \frac{\sum w^i f^i(x^0)}{\sum w^i}$$

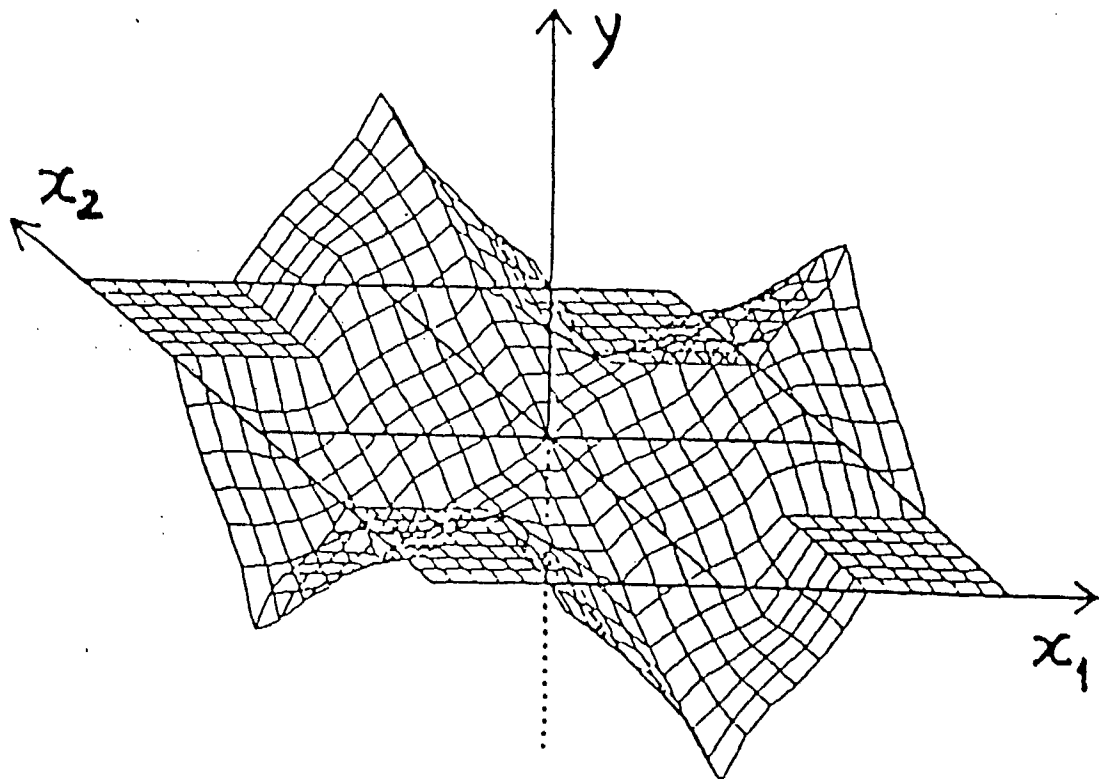
INPUT - OUTPUT RELATION

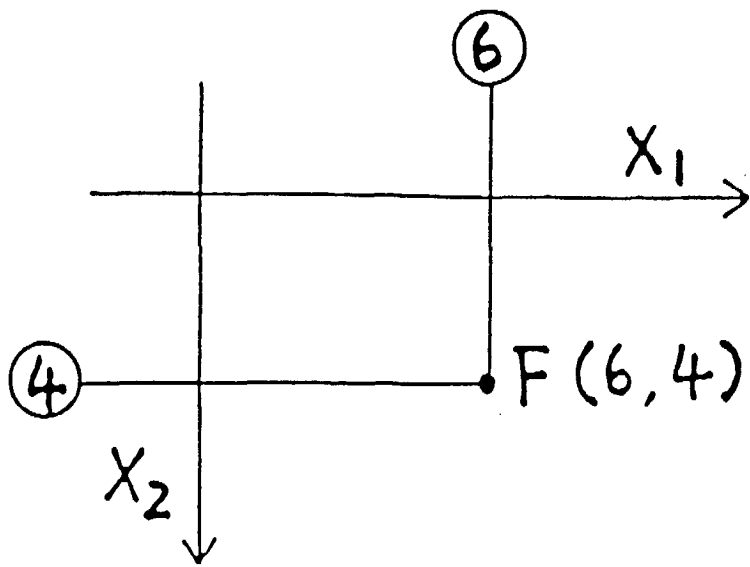


Characteristic of Fuzzy Rule Table

$$(x_1, x_2) \rightarrow y$$

| $x_1 \backslash x_2$ | NB | NM | NS | ZO | PS | PM | PB |
|----------------------|----|----|----|----|----|----|----|
| NB | | | | NB | | | |
| NM | | | | NM | | | |
| NS | | | | NS | | | |
| ZO | NB | NM | NS | ZO | PS | PM | PB |
| PS | | | | PS | | | |
| PM | | | | PM | | | |
| PB | | | | PB | | | |

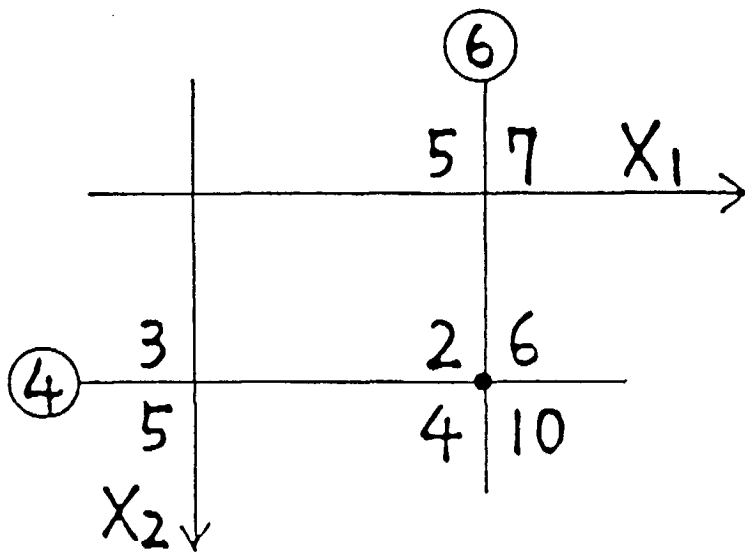




$$Y = F(X_1, X_2)$$



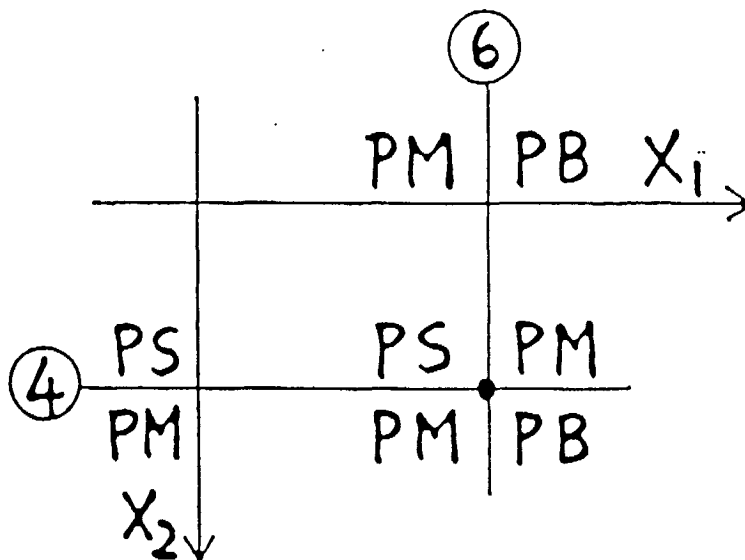
Substitution



Numerical Table



Interpolation



Fuzzy Rule Table



Reasoning

Design Elements in Fuzzy Control

1. Rule Format

2. Reasoning Method

3. Structure

3.1 Premise Variables

3.2 Fuzzy Partition of Premise Space

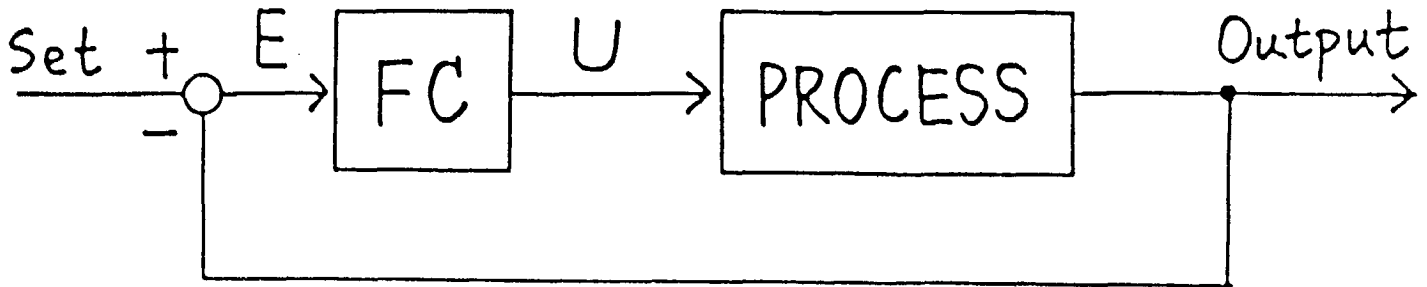
3.3 Number of Rules

4. Parameter: Membership Function

Design of Fuzzy Controller

- 1) Operator's Experience
- 2) Control Engineer's Knowledge on Objective System
- 3) Use of Simulator/Experiment
- 4) Fuzzy Model of Operator's Control Actions
- 5) Fuzzy Model of Objective System

FUZZY CONTROL



FUZZY CONTROL RULE

$E = \text{Error}$, $\Delta E = \text{Change of Error}$

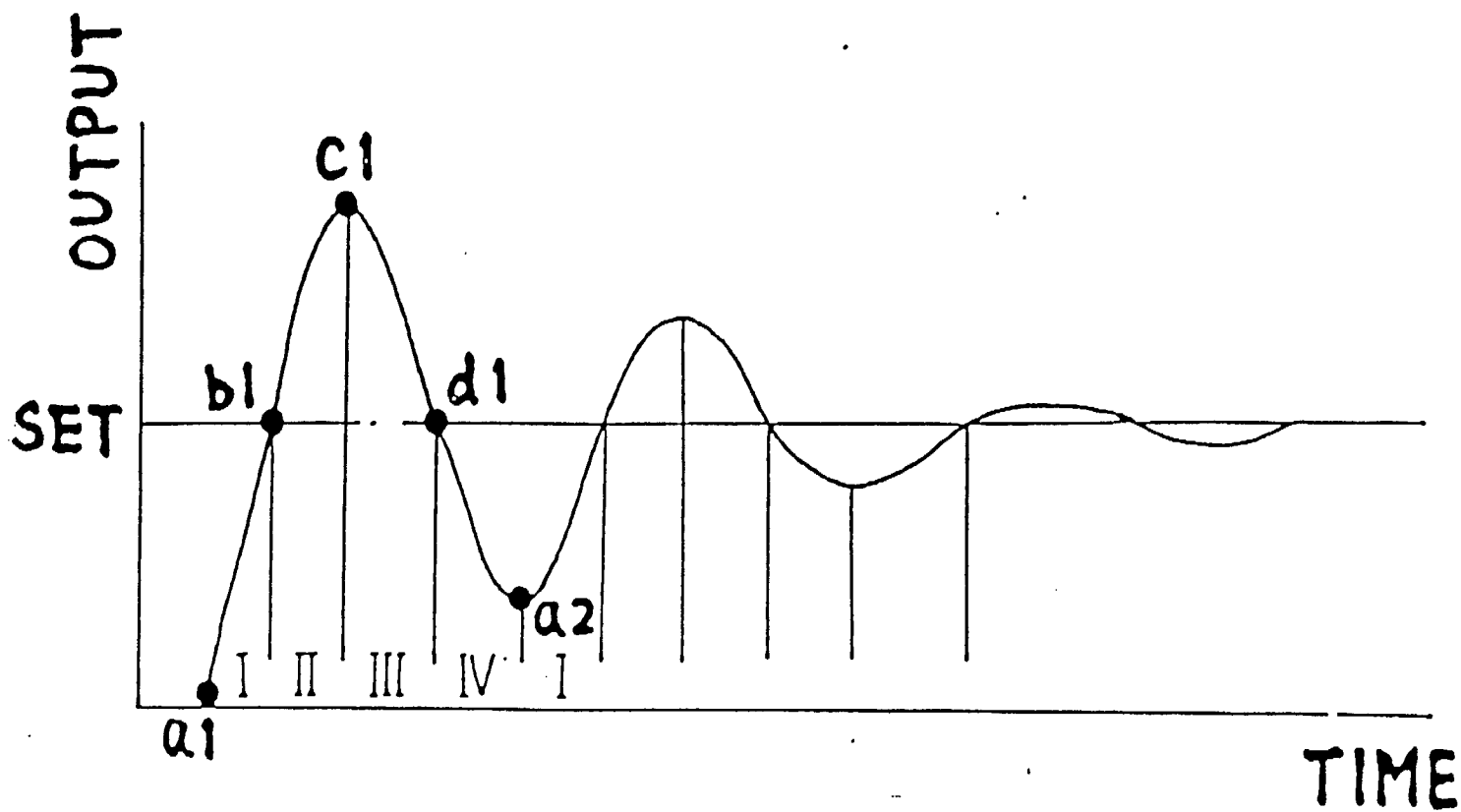
$U = \text{Control}$, $\Delta U = \text{Change of Control}$

1) $E = \text{Negative Big}$, $\Delta E = \text{Zero}$

$\longrightarrow \Delta U = \text{Positive Big}$

2) $E = \text{Negative Small}$, $\Delta E = \text{Positive Medium}$

$\longrightarrow \Delta U = \text{Negative Small}$



$$a1) E = NB, \quad \Delta E = ZO \rightarrow \Delta U = PB$$

$$b1) E = ZO, \quad \Delta E = PB \rightarrow \Delta U = NB$$

$$c1) E = PB, \quad \Delta E = ZO \rightarrow \Delta U = NB$$

$$d1) E = ZO, \quad \Delta E = NB \rightarrow \Delta U = PB$$

$$a2) E = NM, \quad \Delta E = ZO \rightarrow \Delta U = PM$$

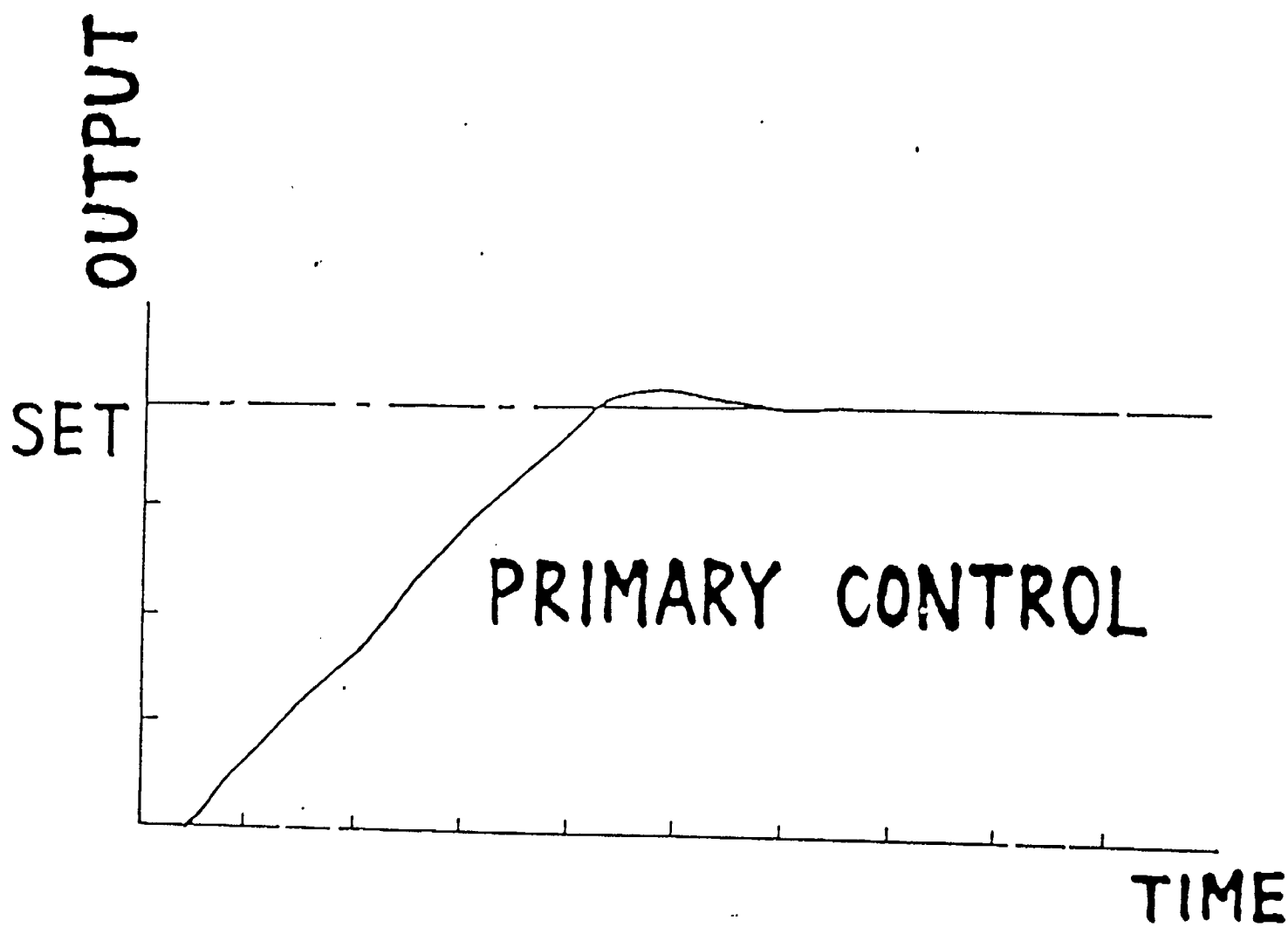
$$b2) E = ZO, \quad \Delta E = PM \rightarrow \Delta U = NM$$

Primary Rule Table

ΔE

| | | NB | NM | NS | ZO | PS | PM | PB |
|---|----|----|----|----|----|----|----|----|
| E | NB | | | | | | | PB |
| | NM | | | | | | | PM |
| | NS | | | | | | | PS |
| | ZO | PB | PM | PS | ZO | NS | NM | NB |
| | PS | | | | | | | NS |
| | PM | | | | | | | NM |
| | PB | | | | | | | NB |

Results of fuzzy control

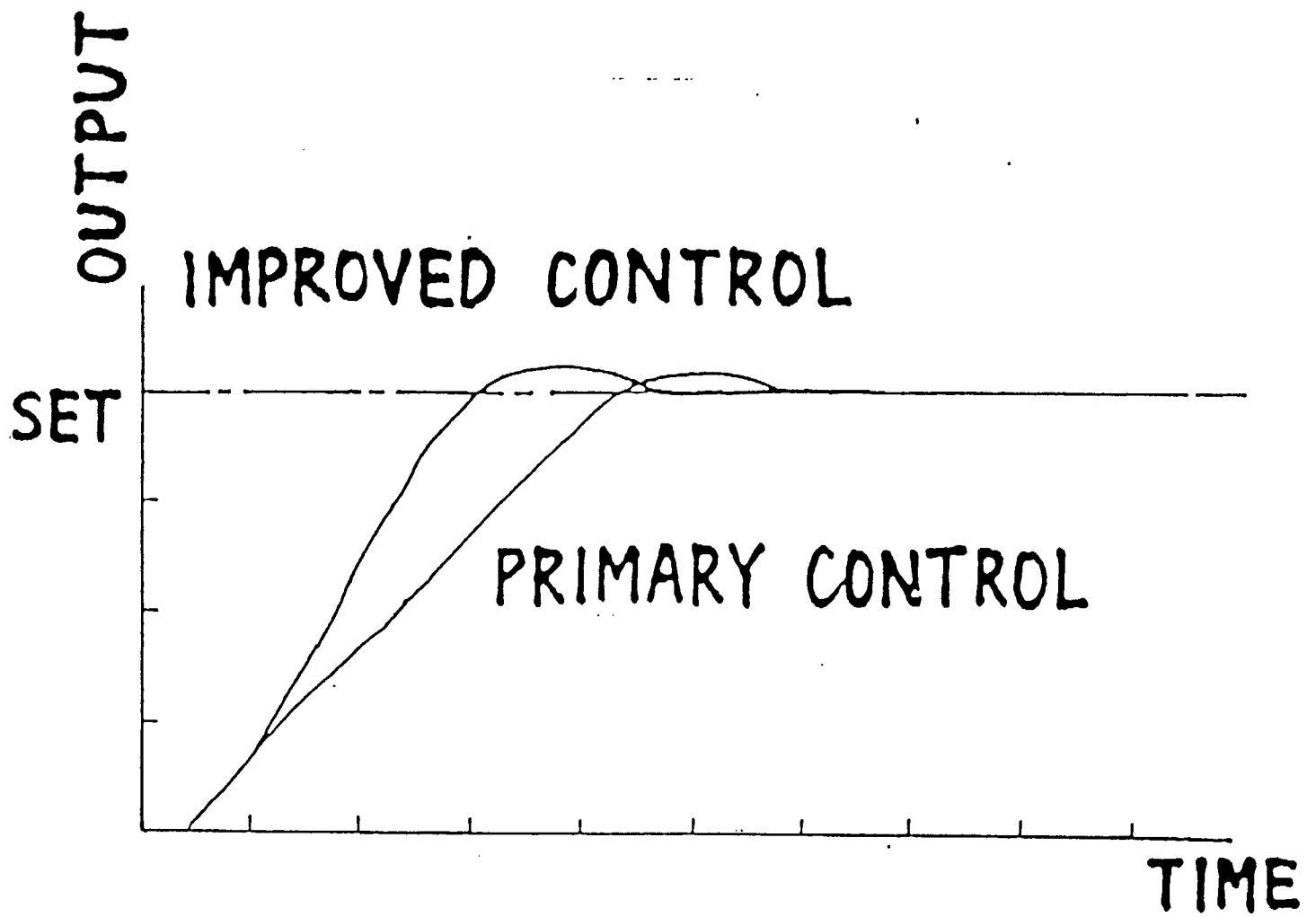


Improved Rule Table

ΔE

| | NB | NM | NS | ZO | PS | PM | PB |
|----|----|----|----|----|----|----|----|
| NB | | | | PB | PM | | |
| NM | | | | PM | | | |
| NS | | | | PS | ZO | | NM |
| ZO | PB | PM | PS | ZO | NS | NM | NB |
| PS | PM | | ZO | NS | | | |
| PM | | | | NM | | | |
| PB | | | NM | NB | | | |

Results of fuzzy control



SUGENO'S METHOD

• i-th rule

$R^i : \text{IF } X_1 \text{ is } A_1^i \text{ AND } \dots \text{ AND } X_J \text{ is } A_J^i \text{ THEN } Y \text{ is } B^i,$
 $(i=1, \dots, I) ,$

(i) Position type reasoning method

• DETERMINATION OF SINGLETON CONSEQUENT FORM

$R^i : \text{if } X_1 \text{ is } A_1^i \text{ and } \dots \text{ and } X_J \text{ is } A_J^i \text{ then } Y \text{ is } b^i,$
 $(1 \leq i \leq I) .$

$$b^i = v_{fi} = \frac{\sum_{n=1}^N (h_{in})^w y_n}{\sum_{n=1}^N (h_{in})^w}$$

• Final estimation of the consequence

$$y = \frac{\sum_{i=1}^I h^i b^i}{\sum_{i=1}^I h^i}$$

where

$$h^i = h_{A_1^i}(x_1^0) \cdot \dots \cdot h_{A_J^i}(x_J^0)$$

(ii) Position-Gradient type fuzzy model

R^i : if X_i is A_1^i and ... and X_J is A_J^i then Y is b^i

and $\frac{\partial Y}{\partial X_1}$ is c_1^i and ... and $\frac{\partial Y}{\partial X_j}$ is c_j^i

($1 \leq i \leq I$)

• Final estimation of the consequence

$$y = \frac{\sum_{i=1}^I \{ \psi(n, i) \cdot (b^i + \sum_{j=1}^J (d_j(i, n) \cdot c_j^i)) \}}{\sum_{i=1}^I \psi(n, i)}$$

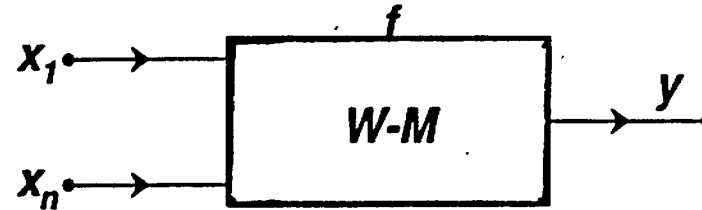
where

$$\psi(n, i) = \exp\{-D(n, i)\}$$

$$D(n, i) = \min \sqrt{\sum_{j=1}^J (x_j^0 - x_j^{ic})^2} ; x_j^{ic} \in \{x_j \mid h_{A_j^i}(x_j) = 1, x_j \in X_j\} ,$$

UNIVERSAL APPROXIMATOR

Wang-Mendel n -input one-output approximator



$$x = (x_1, \dots, x_n), \quad y = f(x)$$

$$f(x) = \frac{\sum_{i=1}^K y^i m^i}{\sum_{i=1}^K m^i} = \frac{\sum_{i=1}^K y^i \prod_{1 \leq j \leq n} [m_j^i(x_j)]}{\sum_{i=1}^K \prod_{1 \leq j \leq n} [m_j^i(x_j)]}$$

$$m^i = \prod_{1 \leq j \leq n} [m_j^i(x_j)]$$

= degree of match for i -th rule

y^i = center of output for i -th rule

theorem

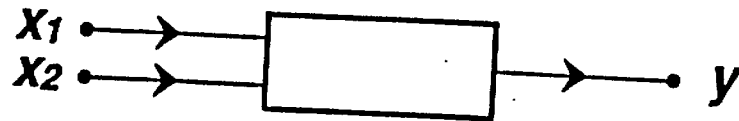
f is capable of approximating to any desired accuracy any real continuous function from a compact set

$$Q = [a_1, b_1] \times \dots \times [a_n, b_n] \subset R^n$$

to the real line R

INDUCTION OF FUZZY RULES FROM NUMERICAL OBSERVATIONS

Wang-Mendel approach



• problem : given m input-output pairs

$$(x_1^{(1)}, x_2^{(1)}, y^{(1)}), (x_1^{(2)}, x_2^{(2)}, y^{(2)}), \dots$$

derive n fuzzy if-then rules of the form

Y is B_i if (X_1 is A_{i1} and X_2 is A_{i2})

• algorithm.

1. Treat x_1, x_2, y as linguistic variables with $2N+1$ values

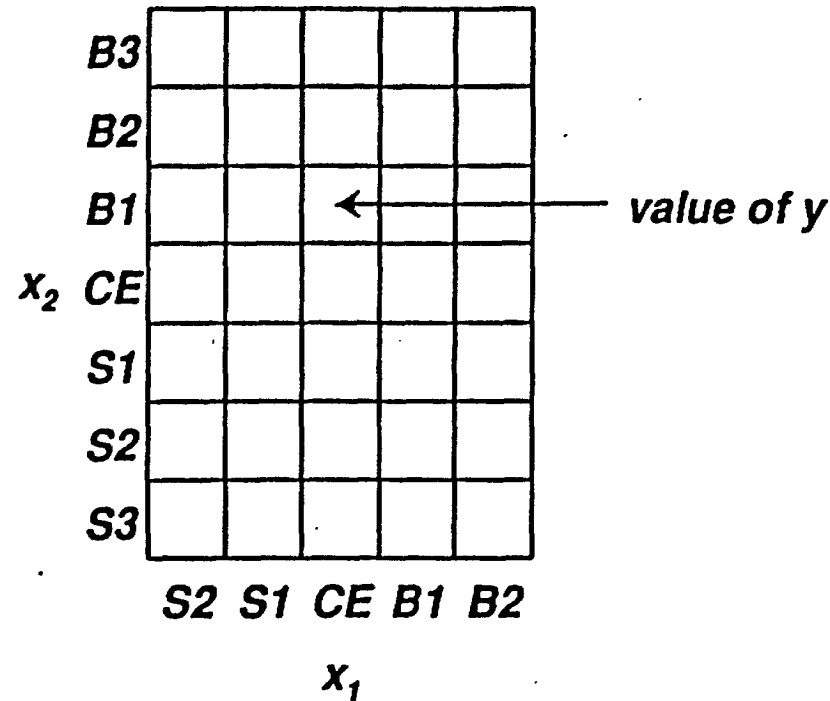
$SN, \dots, S1, CE, B1, \dots, BN$

\uparrow small \uparrow center \uparrow big

$N, SN, \dots, S1, CE, B1, \dots, BN$ are
variable dependent

WANG-MENDEL ALGORITHM

2. Set up a FAM (fuzzy associative memory) bank for fuzzy if-then rules

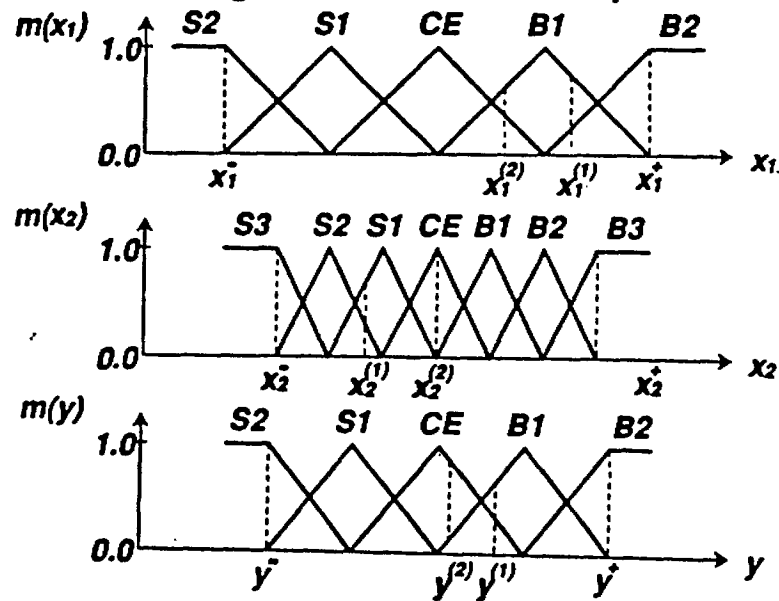


y is B₃ if x₁ is CE and x₂ is B₁

WANG-MENDEL ALGORITHM

3. generate fuzzy rules

given an input-output pair $(x_1^{(1)}, x_2^{(1)}; y^{(1)})$
 assign the pair to a cell in FAM with
 maximal grades of membership



$x_1^{(1)}$ is assigned to B1

$x_2^{(1)}$ is assigned to S1

$y^{(1)}$ is assigned to CE

Induced rule :

y is CE if x_1 is B₁ and x_2 is S₁

WANG-MENDEL ALGORITHM

4. assign a degree to each rule

$(x_1^{(1)}, x_2^{(1)}; y^{(1)}) \rightarrow y$ is CE if x_1 is B_1 and x_2 is S_1

$$D(\text{rule}) = m_{B_1}(x_1^{(1)}) m_{S_1}(x_2^{(1)}) m_{CE}(y^{(1)}) m^{(1)}$$

↑
degree

↑
goodness of data pair

conflict resolution

if there is a conflict in consequents, choose the rule which has the highest degree

5. use weighted centroid defuzzification

for j th rule

$$m_{O_j} = m_{I_1}(x_1) m_{I_2}(x_2)$$

↑ ↑
output input

$\bar{y}_j =$ centroid of j th rule

WANG-MENDEL ALGORITHM

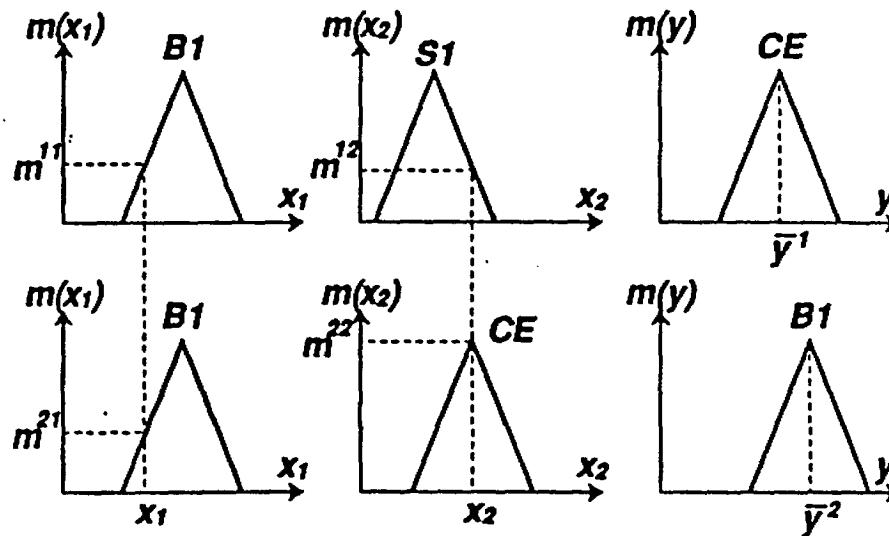
output

$$y = \frac{\sum_{j=1}^k m_{O^j}^i \bar{y}^j}{\sum_{j=1}^k m_{O^j}^i}$$

• example

rule 1 : y is CE if x_1 is B₁ and x_2 is S₁

rule 2 : y is B₁ if x_1 is B₁ and x_2 is CE



$$y = \frac{m_{CE}^1 \bar{y}^1 + m_{B_1}^2 \bar{y}^2}{m_{CE}^1 + m_{B_1}^2}$$

$$m_{CE}^1 = m^{11} m^{12}$$

$$m_{B_1}^2 = m^{21} m^{22}$$

(iii) TURKSEN' S IVAAR

Characteristic feature of AAR

1) *Similarity measures and/or subsethood measures* are used for *pattern matching* between rules and their observations to determine the rules to be fired.

2) And Approximate reasoning is carried out through the *modification of each rule consequent* by pattern matching measures without CRI.

AAR with point-valued fuzzy sets(PVAAR)

Generally, the final consequence derived through PVAAR, as, the aggregation of modified original consequent of each rule which is defined as follows:

$$h_{B'}(y) = \bigcup_i f(h_{B_i}(y), SM^i)$$

where f is the modification function which gives the "Expansion" modification or "Reduction" modification of $h_{B_i}(y)$, and SM^i is a similarity measure of i -th rule between antecedents and observations.

Selection of f and SM^i has wide flexibility.

If we chose $f = \wedge$, and

$$SM^i[A', A^i] = \bigwedge_{j=1}^J \sup_{x_j} (h_{A_j'}(x_j) \wedge h_{A_j^i}(x_j)) ,$$

and $\mathcal{U} = \bigvee_{i=1}^I$, then it is the equivalent form to MCRI

With the values of SM , the rules which satisfy the following conditions are fired.

$$\tau < SM^i$$

where τ is an appropriate threshold.

There are two types of modification which
which were proposed by Turksen, namely:

1)Expansion form:

$$h_{B_{ex}}^i = \min\left(1, \frac{h_{B^i}}{SM^i}\right)$$

2)Reduction form:

$$h_{B_{re}}^i = SM^i \cdot h_{B^i}$$

AAR with interval-valued fuzzy set(IVAAR)

A similarity measure between antecedents and observations is calculated for both the upper bound and the lower bounds as follows:

$$SM^{iL} = SM[L_{AND}^i(J), L'_{AND}(J)]$$

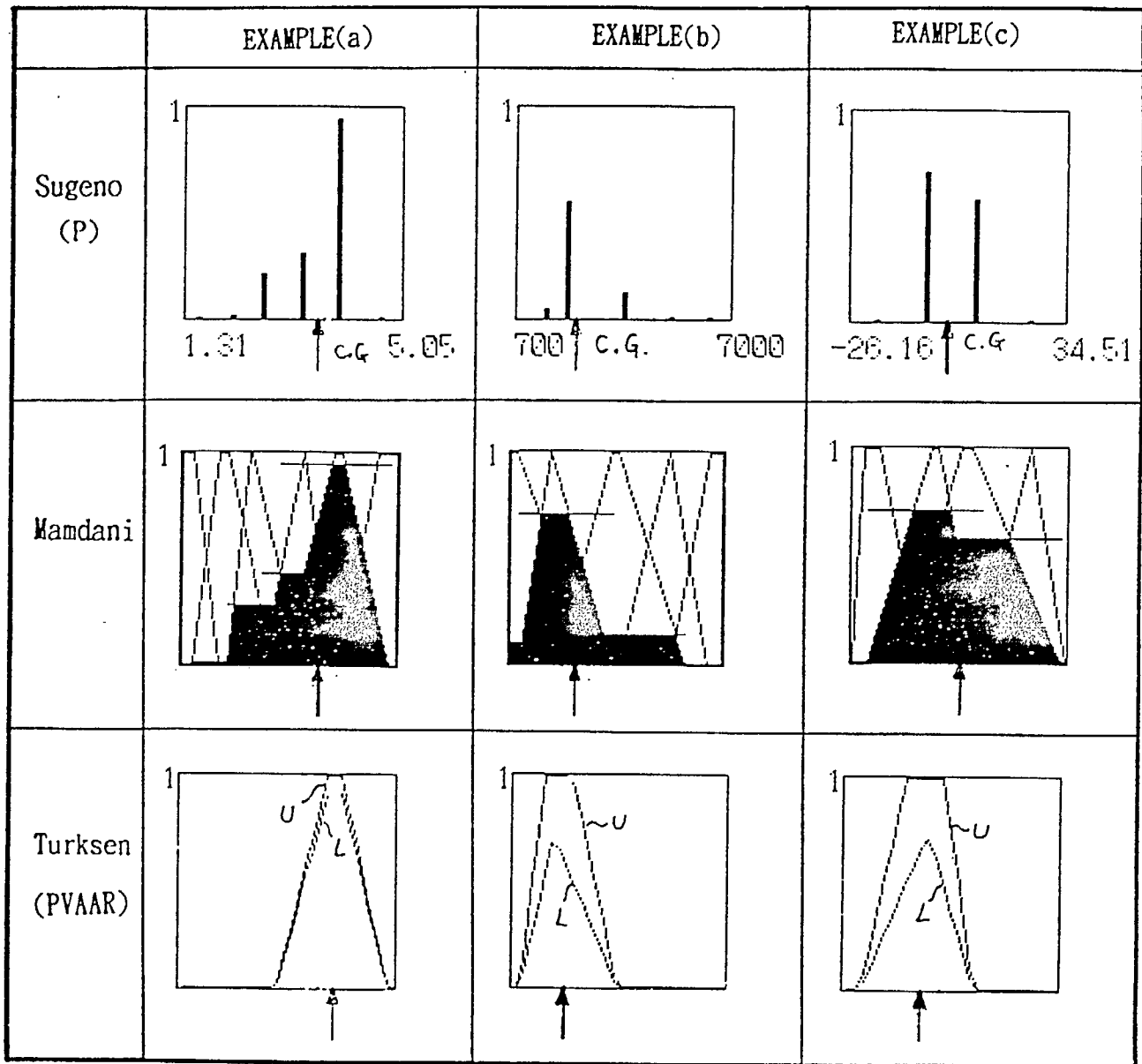
$$SM^{iU} = SM[U_{AND}^i(J), U'_{AND}(J)]$$

where SM is a similarity measure defined with a Disconsistency measure, S , as a distance measure. That can be defined generally:

$$SM[A, B] = 1 - S[A, B] = \sup_{x \in X} h_{A \cap B}(x), \quad A, B \in X .$$

TABLE II. Specification of Model Variables and Rules*

| | Number of variables | Number of rules |
|------------|---------------------|-----------------|
| EXAMPLE(a) | 2 | 6 |
| EXAMPLE(b) | 2 | 5 |
| EXAMPLE(c) | 3 | 4 |



U:Upper bound
L:Lower bound

Fig. 3(a) Examples of consequences by Point-Valued reasoning methods

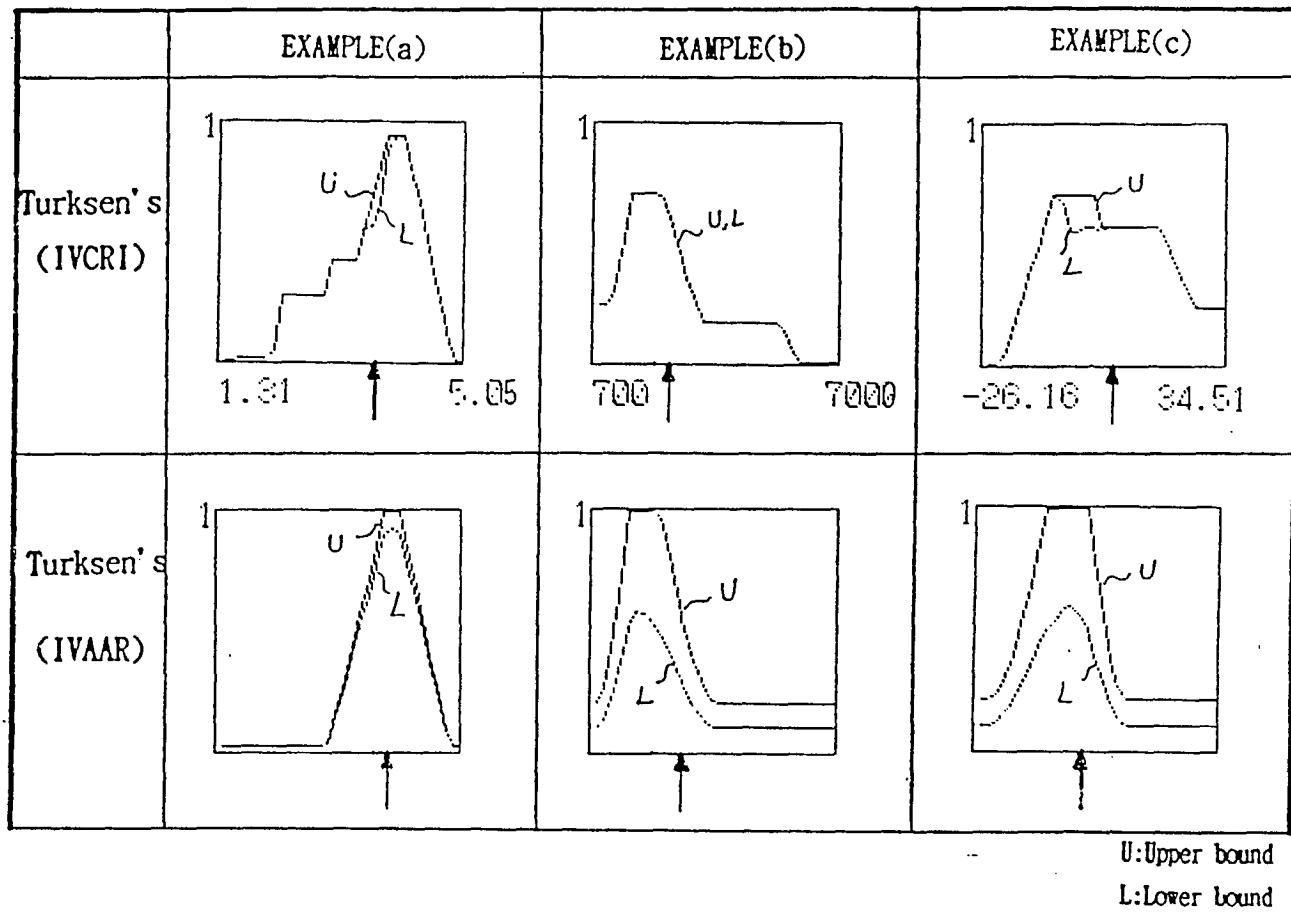


Fig. 3(b) Examples of consequences by Interval-Valued reasoning methods

TABLE 2

PREDICTION ACCURACY FOR COMPARISON AMONGST DIFFERENT APPROACHES

| | Sugeno' (P&P-G) | Sugeno' (P) | Sugeno' (P-G) | Mamdani' | Turksen' (IVCRI) | Turksen' (IVAAR) | Proposed (ILFSI) |
|----|--------------------|----------------|------------------|---------------|---------------------|---------------------|---------------------|
| G1 | 19/25 =76% | 18/25 =72% | 20/25 =80% | 18/25 =72% | 21/25 =84% | 14/25 =56% | 84% |
| G2 | 34/35 =97% | 34/35 =97% | 29/35 =83% | 34/35 =97% | 32/35 =91% | 33/35 =94% | 97% |
| G3 | 42/50 =84% | 41/50 =82% | 40/50 =80% | 41/50 =82% | 39/50 =78% | 43/50 =86% | 84% |

Package available -
"job shop scheduler"
Better than Mark Fox's
"expert based system".
scheduler.

FLES - Fuzzy Logic Expert System Scheduler

Main Menu

- [1] Part Route Information
- [2] Order Information
- [3] Schedule Generation
- [4] Knowledge Base**
- [5] Reports and Statistics
- [6] Order Generation

ENTER: Select Esc: Exit

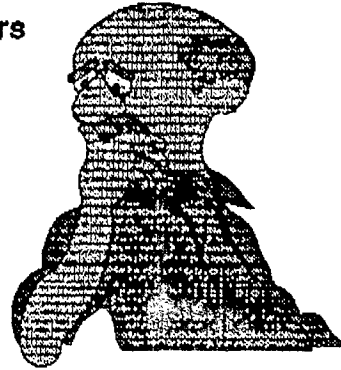
What is the Problem ?

Customer Orders

Due Dates

WIP

Down-Up M/C



Meet Due dates

Reduce Cycle Time

Reduce WIP

Reduce Cost

Step 1: Define Linguistic Variables

what are the lot variables in a fab ?

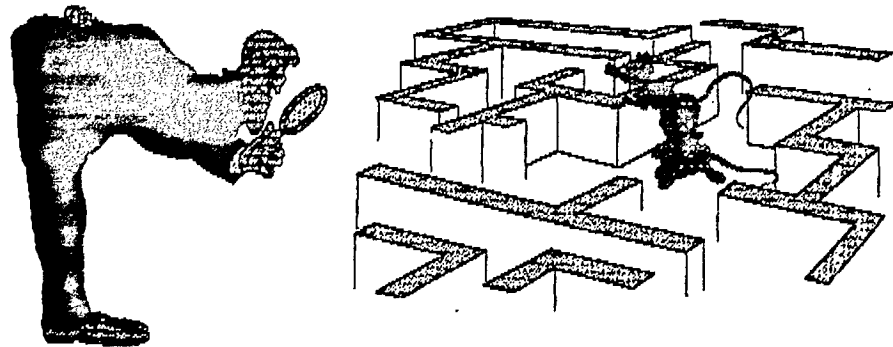
- priority of a lot (hot lot)
- slack time (due date - work left)
- earliest start date (input parts)
- remaining processing time

Step 2: Use Linguistic Values

quantify variables using linguistic values

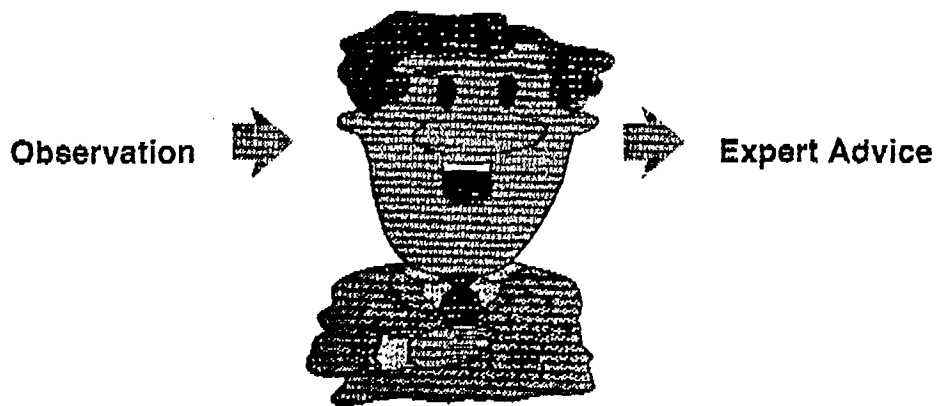
- Very Low (VL)
- Low (L)
- Somewhat Low (SL)
- Medium (M)
- Somewhat High (SH)
- High (H)
- Very High (VH)

Step 3: Rule Selection - Pattern Matching



pattern matching by similarity measures

Step 4: Inferencing



FLES versus Well-known Dispatching Rules

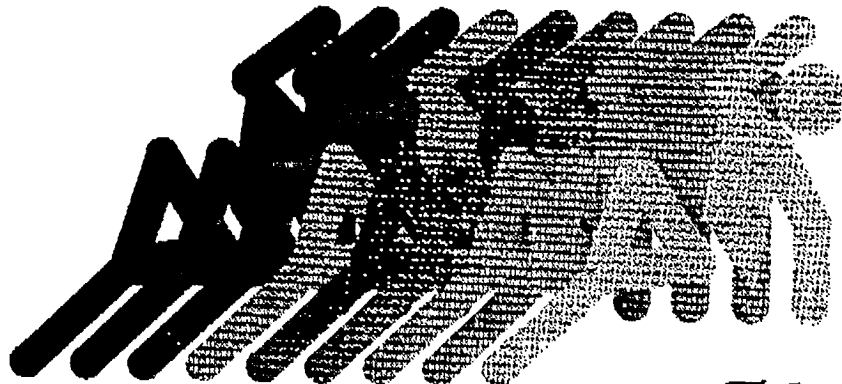


FLES

- shorter cycle times
- less tardy jobs
- less WIP
- no more overloaded systems
- self-learning decision engine



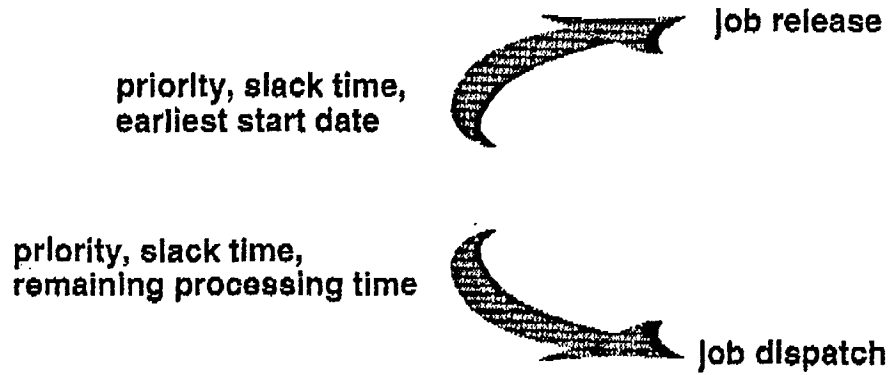
Software Demo



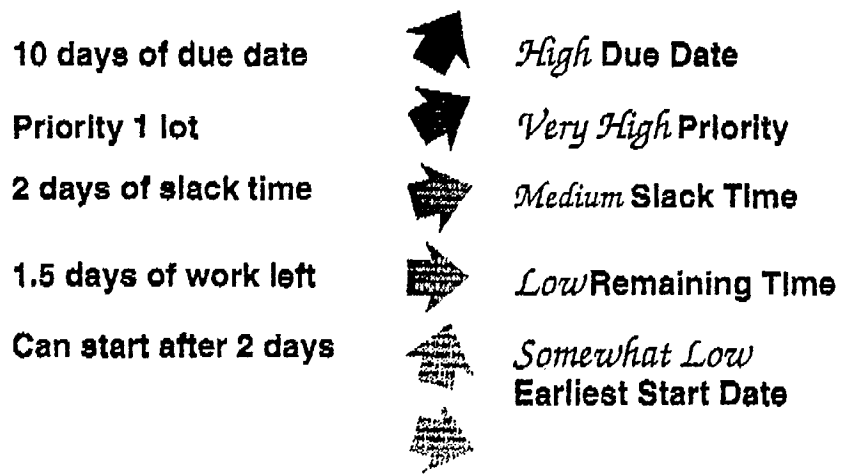
FLES

How Does FLES Work ?

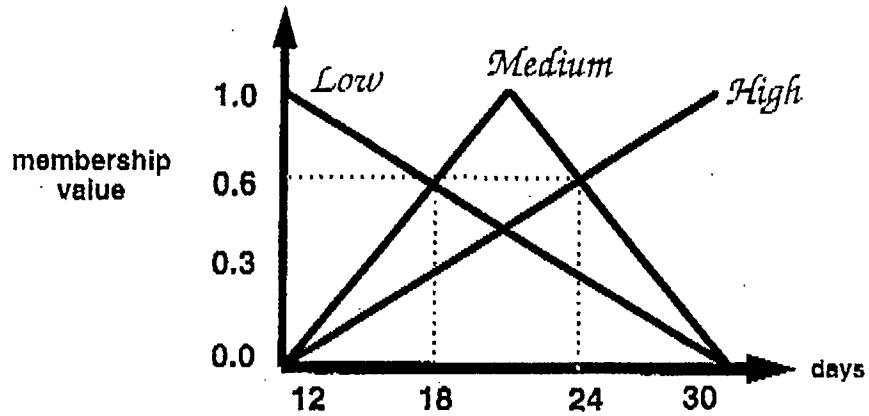
Step 1 : User Input > Observed System State



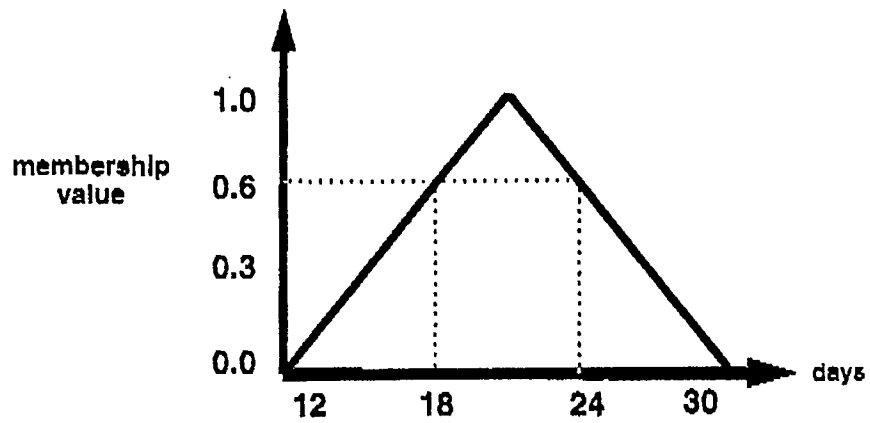
Step 2: Fuzzify User Input



Step 3: Define Fuzzy Sets



cycle time with fuzzy sets



medium cycle time

Step 4: Construct the Rule Base

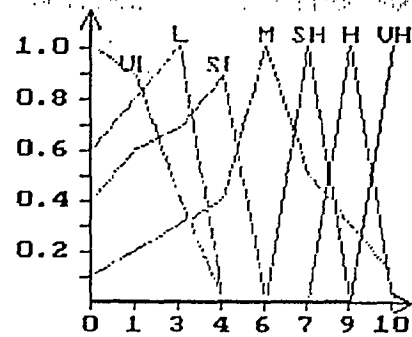
expert's knowledge is specified
in the form of
production rules

IF premise *THEN* conclusion

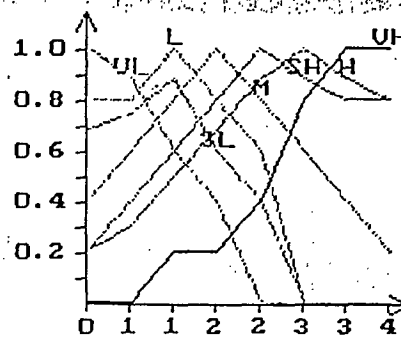
Rule Base in FLES

IF priority is high *AND* slack time is low *AND* due date is low
THEN selectability of the lot for releasing is high

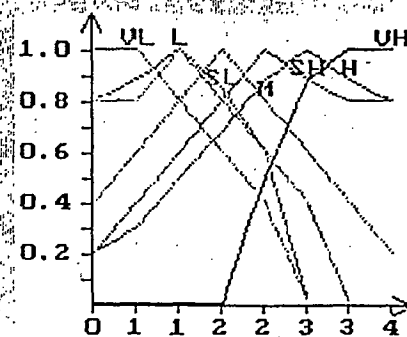
IF priority is low *AND* slack time is high *AND* remaining processing time is low
THEN selectability of lot for next dispatching is low



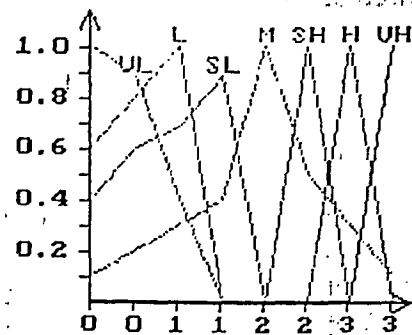
PRIORITY



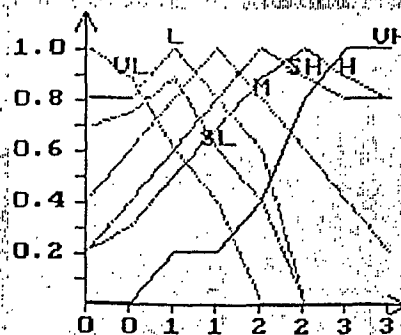
1SLACKTIME



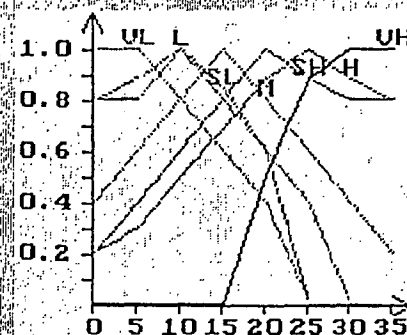
REQSTARTDATE



PROCESSINGTIME



2SLACKTIME



SELECTABILITY

>_

Format = <Lin. Variable, Lin. Value, val1, val2, ..., val8>

ESC: Exit

1G 1I

2W 2Z 13 15 36 33 1C 38

WC-1

37 32 34 1M

2T 2U 2U 2S 1D 2X 3U 2Y

WC-5

14 1E 1F 1T 03 0G

2B 2K 25

2L 1U 2Q

WC-2

0B 1D 0A 2A 28 2P

2R 2Q

2 2D

WC-3

0Q

24

WC-4

2N

27 2H

WC-6

2I 2E 1Q 29

WC-8

2F

18

WC-9

26 2C

23 22

WC-7

0U 0S 1B 1S

1Y 1O 1J

WC-10

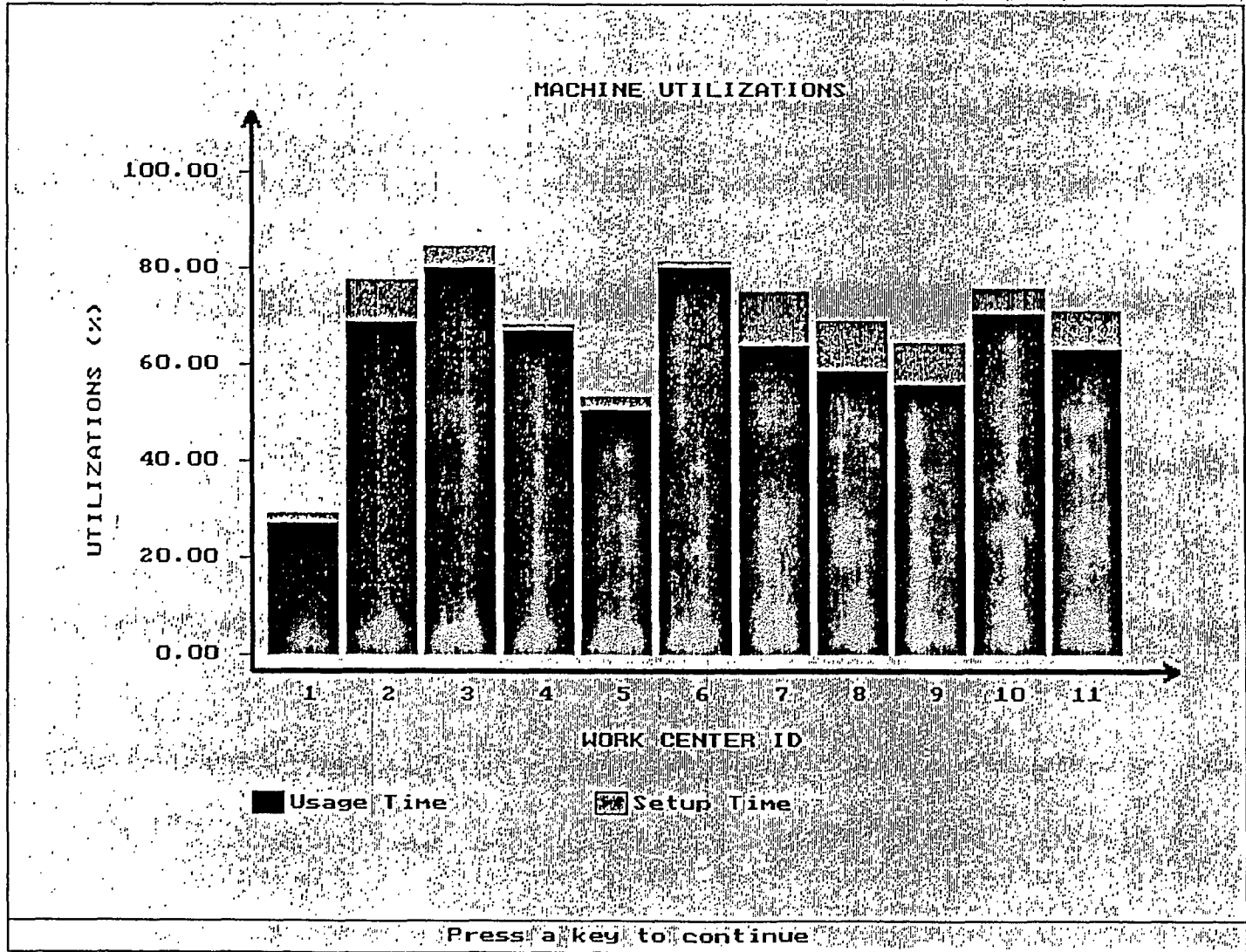
16 21 0D 17

1N 1E 2Q 1R

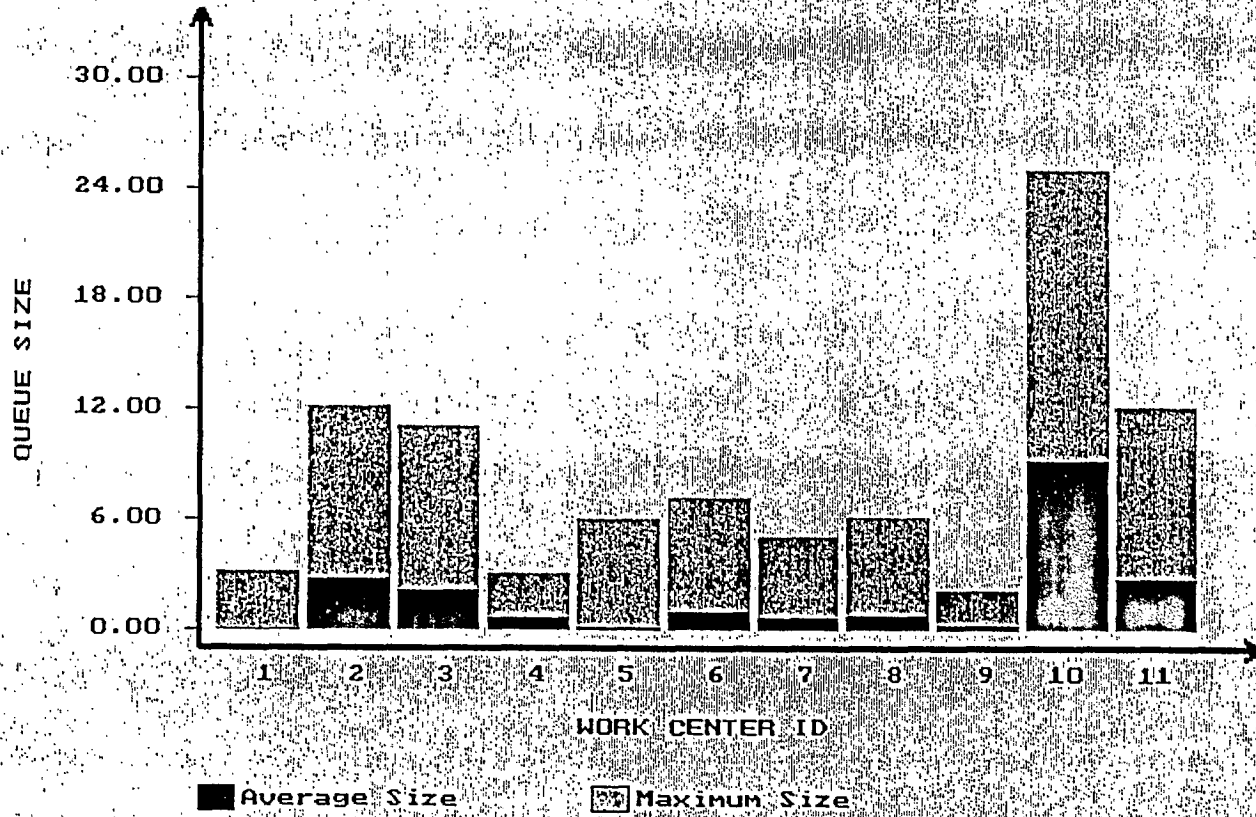
WC-11

UL L SL M SH H UH

F1: Pause F2: Display Off F3: Statistics ESC: Exit



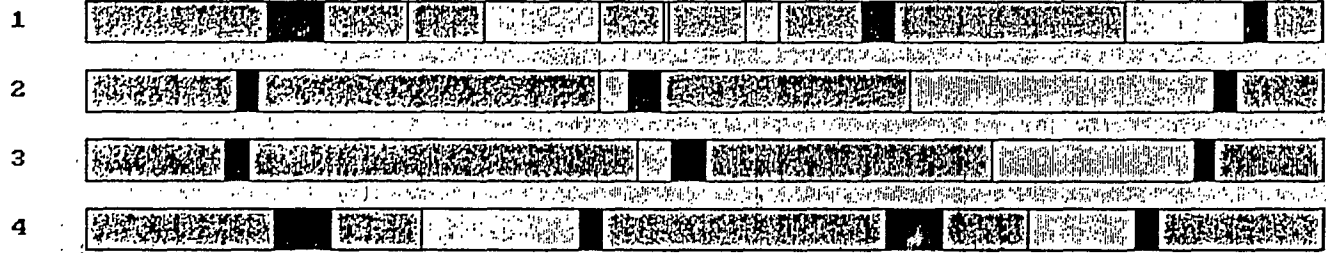
QUEUE STATISTICS



Press a key to continue

WORK CENTER ID 8

M/C ID



21/May/92 02:00 21/May/92 20:00 22/May/92 14:00

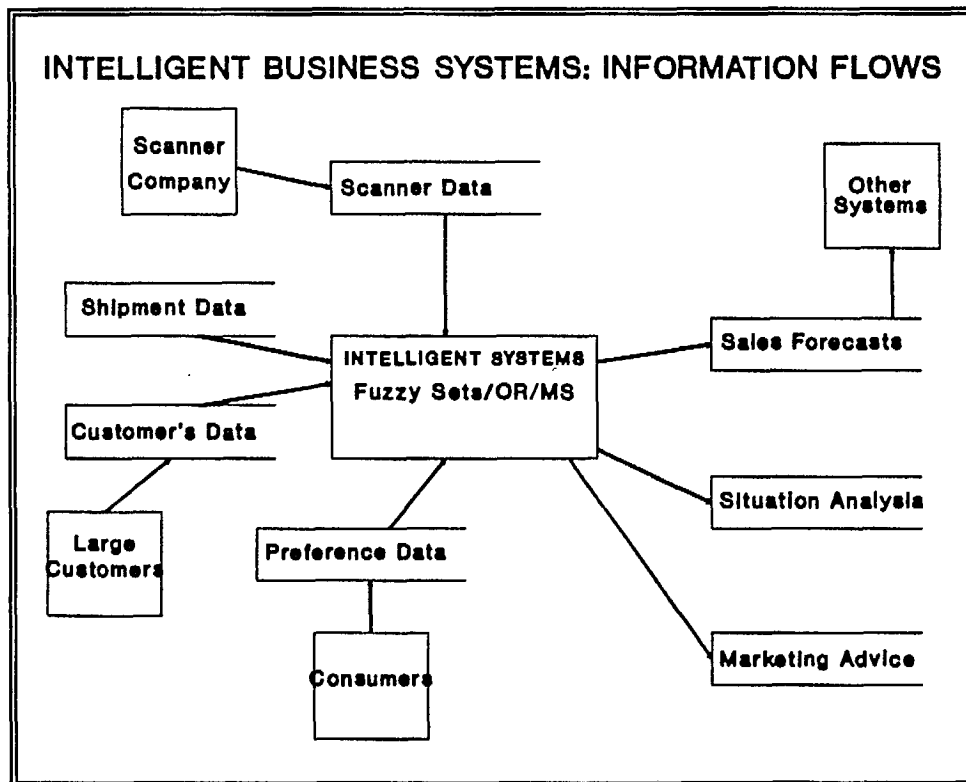
■ Setup

▣ Process

F1: Move Backward F2: Move Forward F3: Change Work Center ESC: Exit

INTELLIGENT BUSINESS SYSTEMS

- Integrate fuzzy set expert systems, conventional expert systems and OR/Management Science models as needed
- Preference data from consumers can be combined with scanner, shipment and customer data
- Market share estimates continually update other systems, such as distribution and production scheduling



CONSUMER PREFERENCE MODELS

CONSUMERS:

- Use linguistic ratings ("very good")
- Often use linguistic attributes ("roomy interior" for car instead of 95 cu. feet)
- Differ as to salient attributes, attribute values and the meaning of linguistic ratings
- Provide meaningful ratings for only a small number of individually adjusted product profiles

PREFERENCE MODELS:

- Must accurately represent ratings in the model
- Must allow individual variations in attributes, attribute values and rating definitions
- Should be easily implemented with a small number of profile ratings using automated data collection software
- High predictive validity and accurate market share estimation for product design and market segmentation

PREFERENCE MODELS

LINGUISTIC PREFERENCE MODEL:

$$\mu_{B'}(y_j, m) = \sum_{I=1}^T \frac{w_i}{\sum_{K=1}^T w_k} \times \mu_{A_i}(x_j, m)$$

Where:

- μ is the fuzzy set membership function for A, B, B'
- A_i is the linguistic rating for the i th attribute
- B_i, B' are the actual and predicted overall ratings
- m is a holdout product profile
- x_j, y_j are domain values (0-100 subjective evaluations)
- w_i are elicited attribute importance weights (1-7)

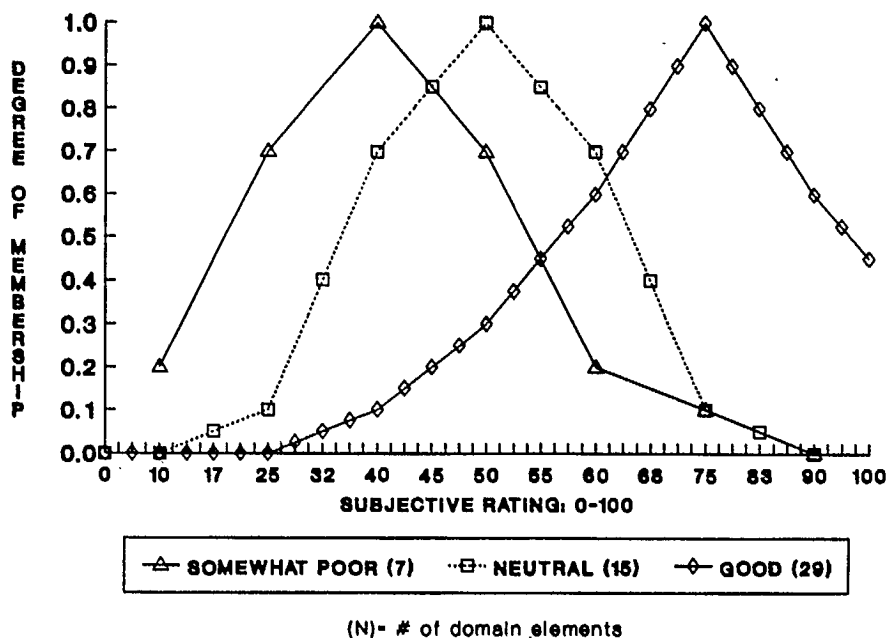
CRISP VECTOR MODEL:

$$y(m) = \sum_{I=1}^T (w_i \times e_i(m)) + w_0$$

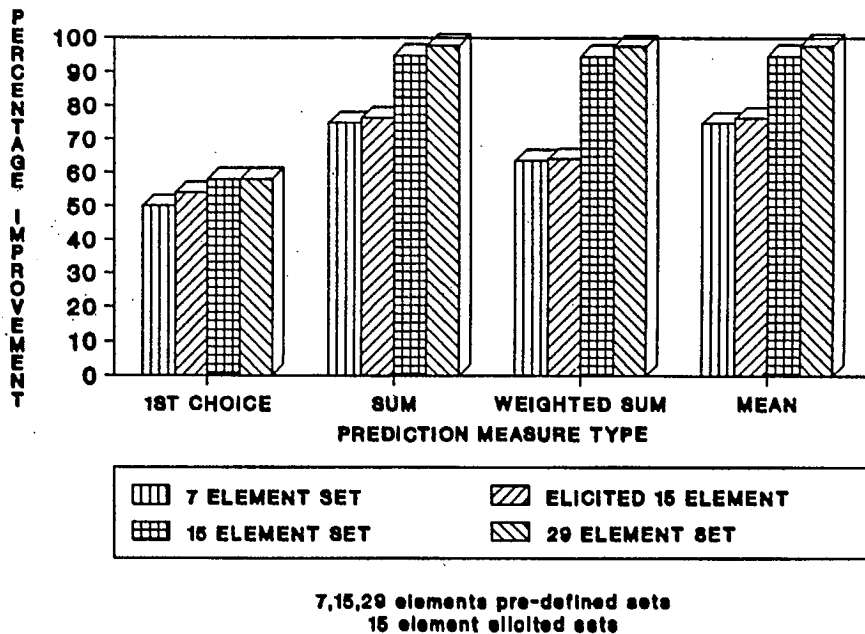
Where:

- $y(m)$ calculated overall evaluation
- $e_i(m)$ is evaluation of the i th attribute (1-7)
- w_i are individually estimated attribute importance weights (OLS regression from 18 estimation profiles)

7, 15, 29 ELEMENT FUZZY SETS



PERCENTAGE IMPROVEMENTS FUZZY MODELS OVER CRISP CONJOINT MODEL



PREDICTION RESULTS

| <u>Prediction Measure:</u> | <u>Naive Model</u> | <u>Crisp Model</u> | <u>Fuzzy Model*</u> |
|-------------------------------------|--------------------|--------------------|---------------------|
| 1st choice rate: | 17% | 48% | 76% |
| Sum of choices: | 31 | 135 | 263 |
| Weighted sum measure: | 56 | 287 | 559 |
| Overall Improvement (Fuzzy -Crisp): | | | 83% |
| Mean prediction: | 0.28 | 0.97 | 1.89 |
| t-value of mean (fuzzy - crisp): | | | 0.92 (p < .001) |

N = 139, * Standard pre-defined 15 element sets

MARKET SHARE PREDICTION

MARKET SHARE MODEL:

The probability of choosing a given alternative m from a choice set is given by

$$P(m) = \left(e^{\beta y(m)} / \sum_{p=1}^6 e^{\beta y(p)} \right)$$

Where:

- $P(m)$ is the probability of selecting holdout product m , given a crisp preference score $y(m)$

FUZZY TO CRISP CONVERSION:

$$y(m) = \sum_{N=1}^{15} (\mu_{B'}(y_n, m) \times n) / 15$$

Where:

- $y(m)$ converted crisp preference score
- $\mu_{B'}(y_n, m)$ is the membership function for holdout m
- n is the weight for each set element, as well as the summation index for domain elements y_n

MARKET SHARE ESTIMATES

| <u>Attribute Level</u> | <u>Crisp Conjoint</u> | | <u>Fuzzy Conjoint</u> | |
|------------------------|-----------------------|--------------------|-----------------------|--------------------|
| | <u>Error</u> | <u>Corr.</u> | <u>Error</u> | <u>Corr.</u> |
| Pizza Product: | | | | |
| Good Level: | 6.26 | 0.627 | 5.31 | 0.917 ^a |
| Average Level: | 6.02 | 0.828 ^b | 4.74 | 0.901 ^a |
| Poor Level: | 4.00 | 0.866 ^b | 3.32 | 0.906 ^a |
| Car Product: | | | | |
| Good Level: | 10.34 | -0.191 | 5.95 | 0.412 |
| Average Level: | 11.73 | 0.044 | 5.98 | 0.298 |
| Poor Level: | 7.51 | 0.538 | 5.28 | 0.837 ^a |

^a $p < .01$. ^b $p < .05$. Abs. = Absolute Value

Error = Mean absolute market share error (predicted - actual)

Corr. = Correlation between predicted and actual share

Levels are the average of all 4 attributes for all subjects ($n = 104$ for pizza, 96 for compact car).

CONCLUSIONS

- High rates of predictive validity (> 80% 1st choice) by representing ratings with fuzzy sets
- Improved accuracy of market share estimates
- Greater improvement for subjects that prefer, or for products that involve, linguistic attribute information
- Adaptive computer software combined with simple but flexible models improve predictive validity with less data
- Good results over 4 studies, 300 subjects, 2 products and relative to existing conjoint models

SUMMARY OF EXPERIMENTS

| <u>Experiment:</u> | <u>N</u> | <u>CC</u> | <u>FC</u> | <u>% Adv.</u> |
|--------------------|------------|--------------|--------------|---------------|
| Written Studies | 63 | 57% | 71% | 35% |
| Software #1 | 62 | 65% | 71% | 33% |
| Software #2 | 50 | 50% | 82% | 138% |
| Software #3 | 139 | 48% | 76% | 83% |
| Average | 314 | 53.5% | 75.0% | 72% |

N = Number of subjects

CC = Crisp Conjoint Model 1st choice rate (6 holdouts)

FC = Fuzzy Conjoint Model 1st choice rate (6 holdouts)

% Adv. = Overall improvement FC - CC (3 measures)

Japanese History of Fuzzy Engineering Research

1972 Working Group on Fuzzy Systems,
TIT

1972 Annual report "General Problems
↓
1981 on Fuzzy Systems"

1972 Workshop on Fuzzy Systems by
Society for Instrumentation and
Control Engineers

1983 Fuzzy Control Application to Water
Purification Process, Fuji Elec. &
TIT

1984 IFSA Japan Chapter

1984 Annual Symposium on Fuzzy Systems
↓
present

1987 Fuzzy Control Application to
Subway in Sendai City, Hitachi

1987 Second IFSA Congress, Tokyo

1987 1st "Fuzzy Vogue"

1988 International Workshop on Fuzzy
Systems Application in Iizuka

1989 LIFE Project, MITI

↓

1994

1989 Fuzzy Systems Research Project,

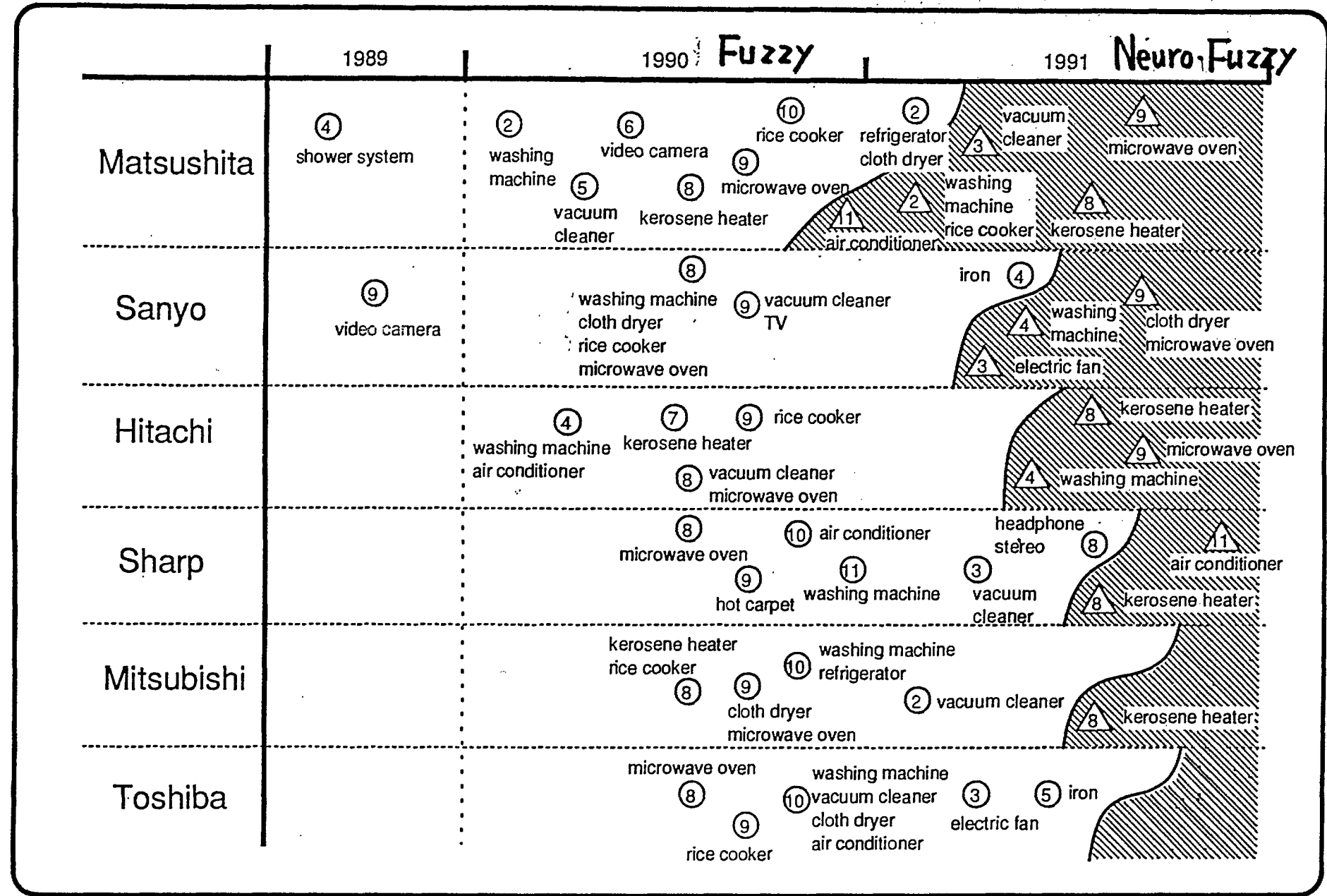
↓

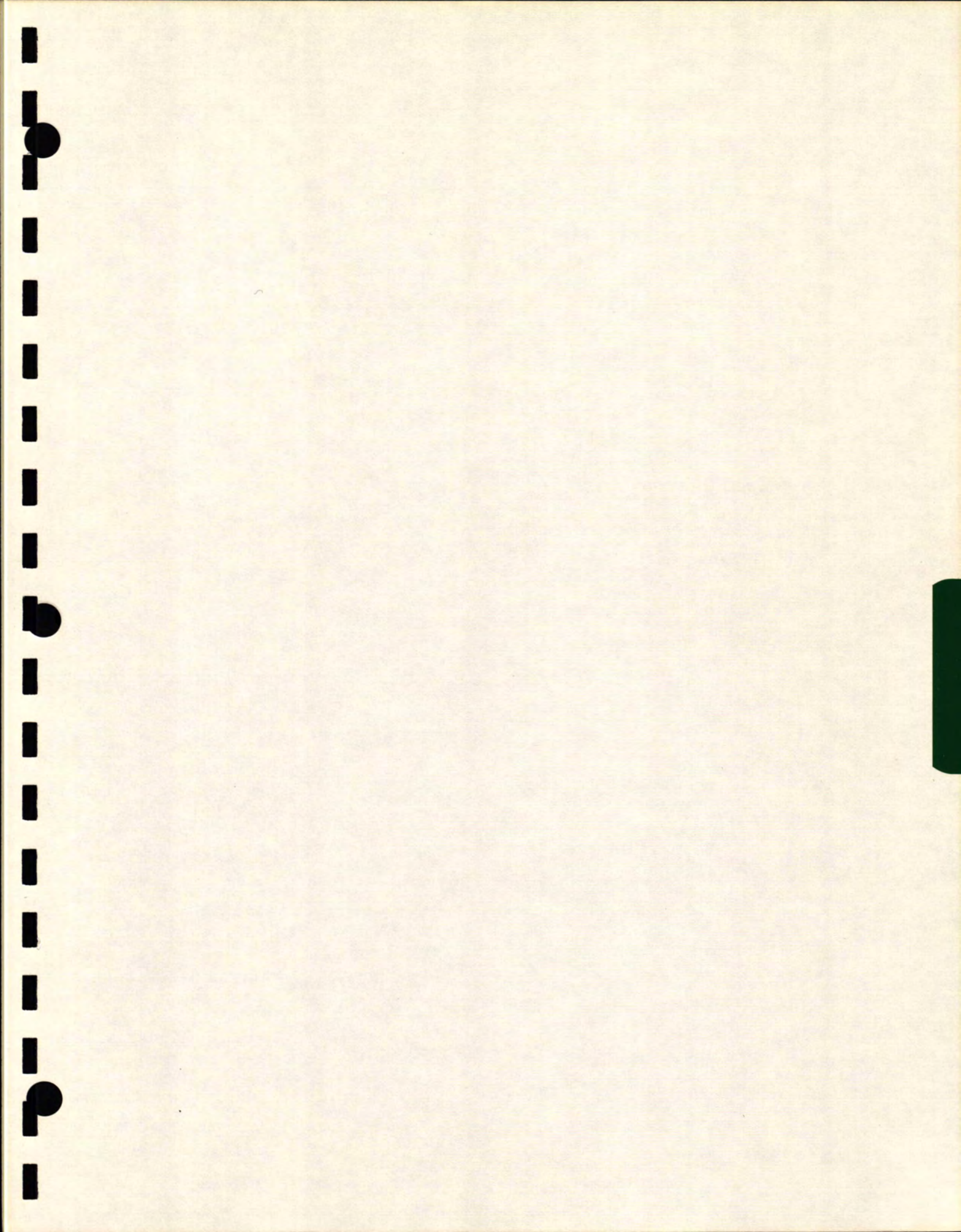
1993 STA

1989 Society for Fuzzy Theory and
Systems (SOFT)

1989 Fuzzy Control Application to Hot
Water Supply Unit for Home Use,
Matsushita

- 1989 Honda Prize to Prof. Zadeh
- 1990 2nd "Fuzzy Vogue"
- 1990 International Conference on Fuzzy Logic & Neural Network, Iizuka
- 1990 Sino-Japan Joint Meeting on Fuzzy Sets and Systems, Beijing
- 1991 International Fuzzy Engineering Symposium, Yokohama
- 1991 AI - Fuzzy Center
- 1992 Korea - Japan Joint Symposium on Fuzzy Systems, Seoul

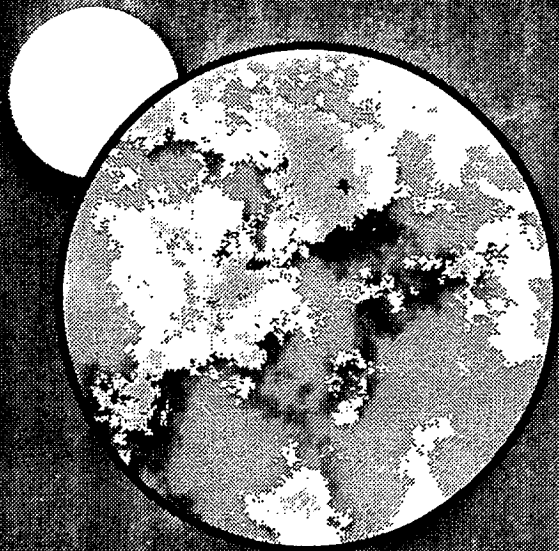






**FUZZY LOGIC:
A NEW WORLD TECHNOLOGY**

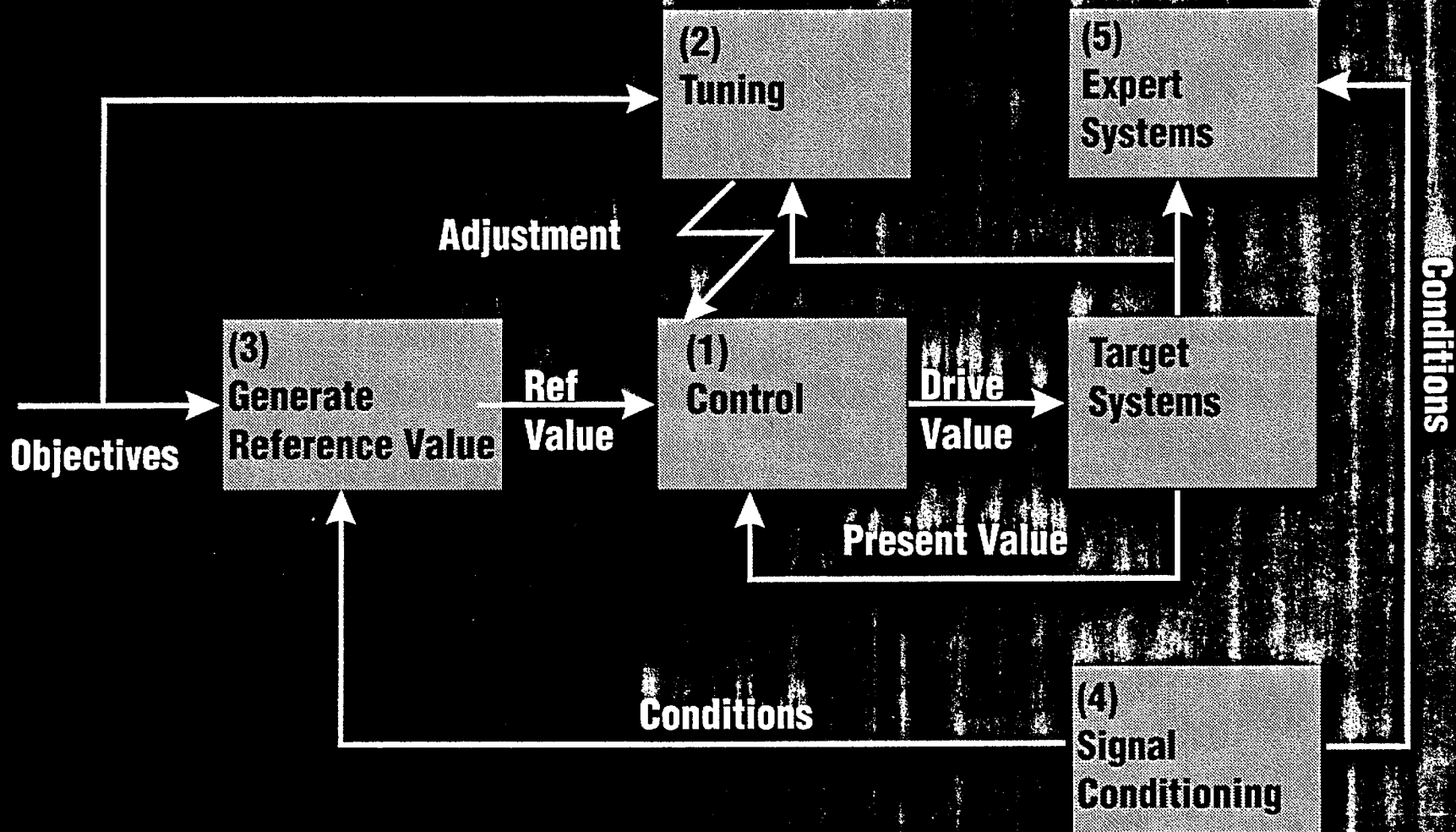
OMRON Canada Inc.



FUZZY

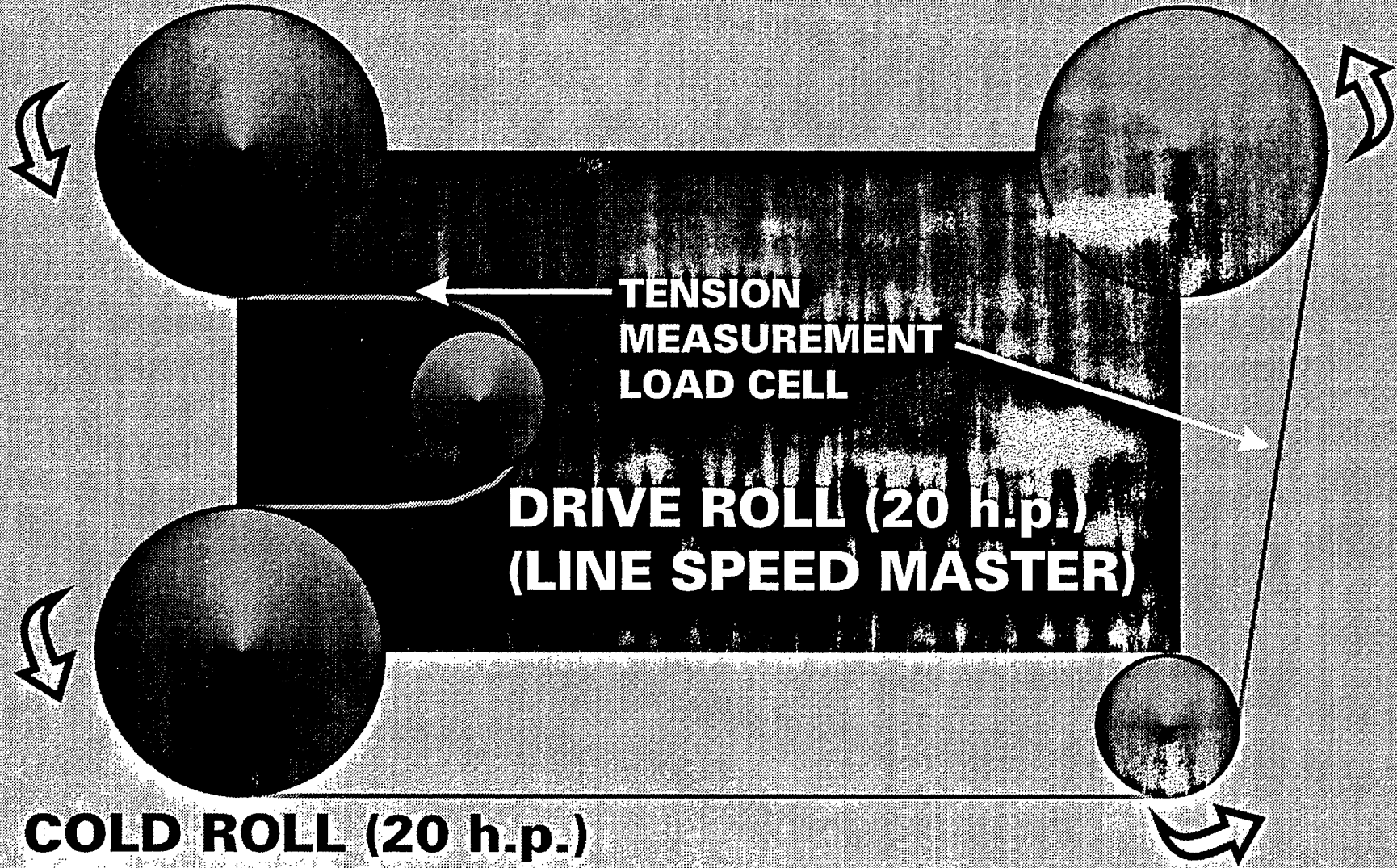
**NEW
WORLD
TECHNOLOGY**

WHERE TO EMPLOY FUZZY



REWIND

UNWIND (40 h.p.)

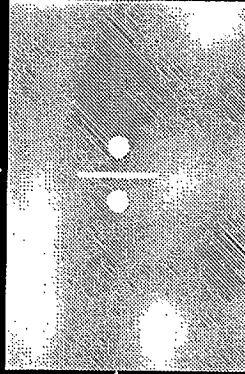
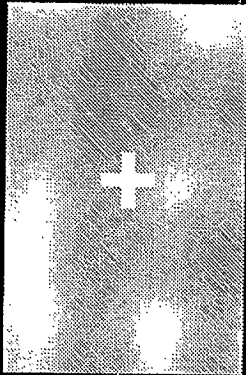
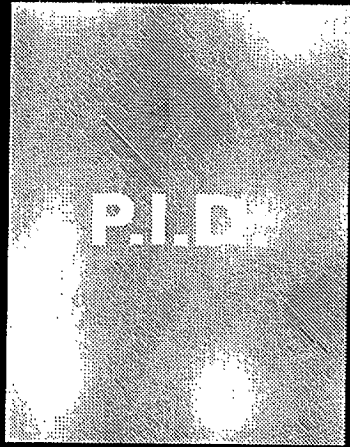


**TENSION
MEASUREMENT
LOAD CELL**

**DRIVE ROLL (20 h.p.)
(LINE SPEED MASTER)**

**COLD ROLL (20 h.p.)
(FOLLOWER)**

Load Cells Tensions



Speed Set Point



Tension Set Point

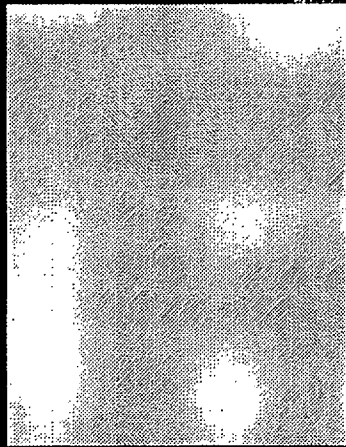


Scaled Line Speed



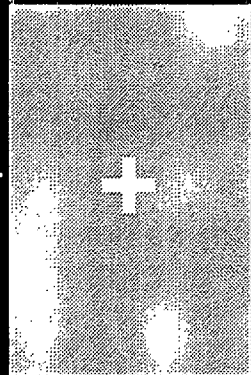
Diameter Calculated During Run

Load Cells



ERR

DEL
ERR



Speed
Set Point

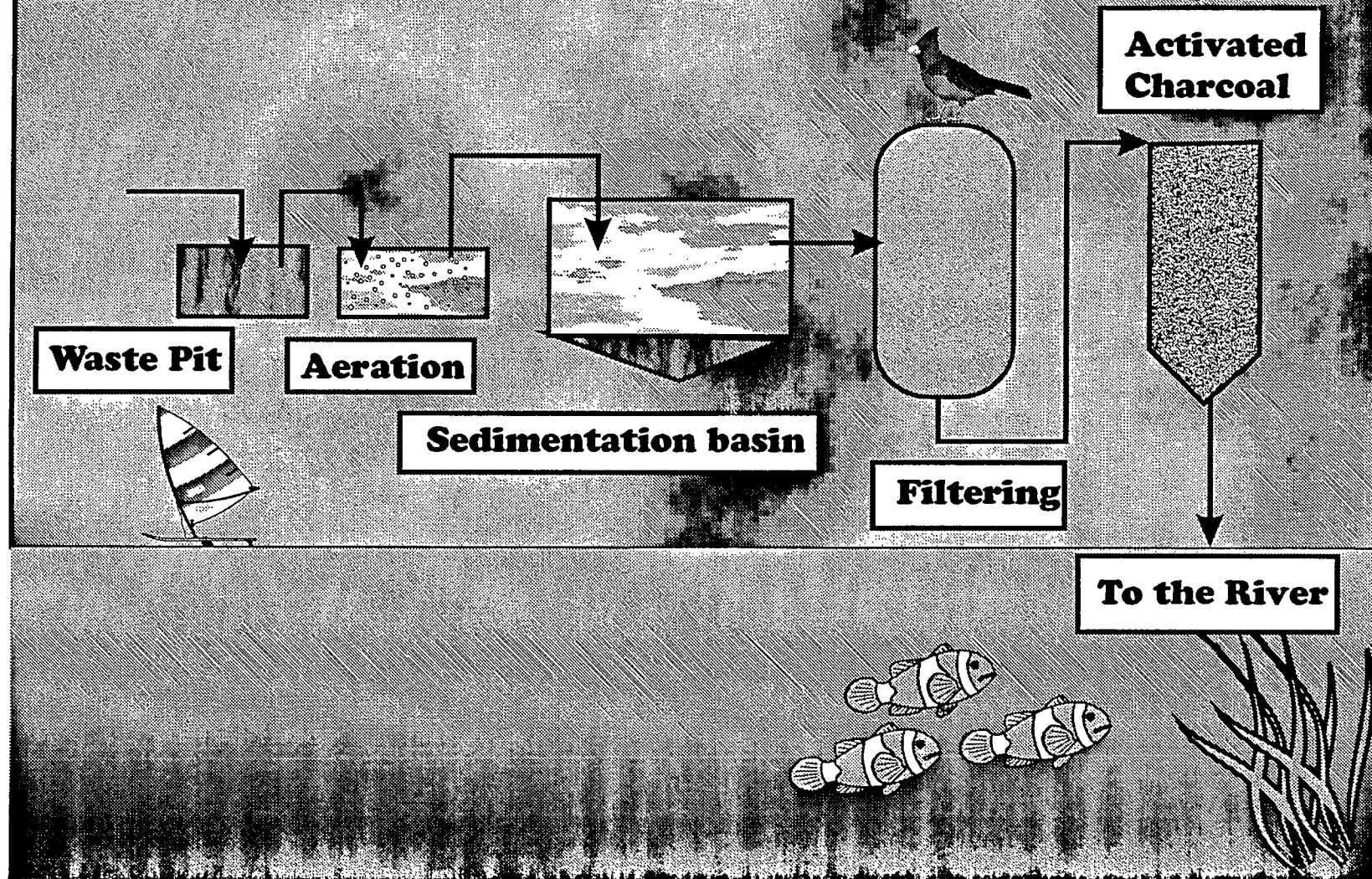
Speed Set Point



Tension Set Point



AERATION CONTROL OF FACTORY SEPTIC TANK

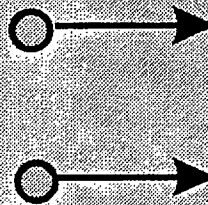


EFFECTS

Stabilizes the quantity of oxygen contained in the sewage of septic tank system (1.2 to 1.8 from 0.3 to 5.0 ppm).

Reduces the electricity required by the system by 22%

Dissolved Oxygen Sensor



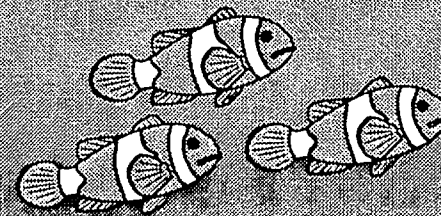
C200H Fuzzy Controller

Inverter

M

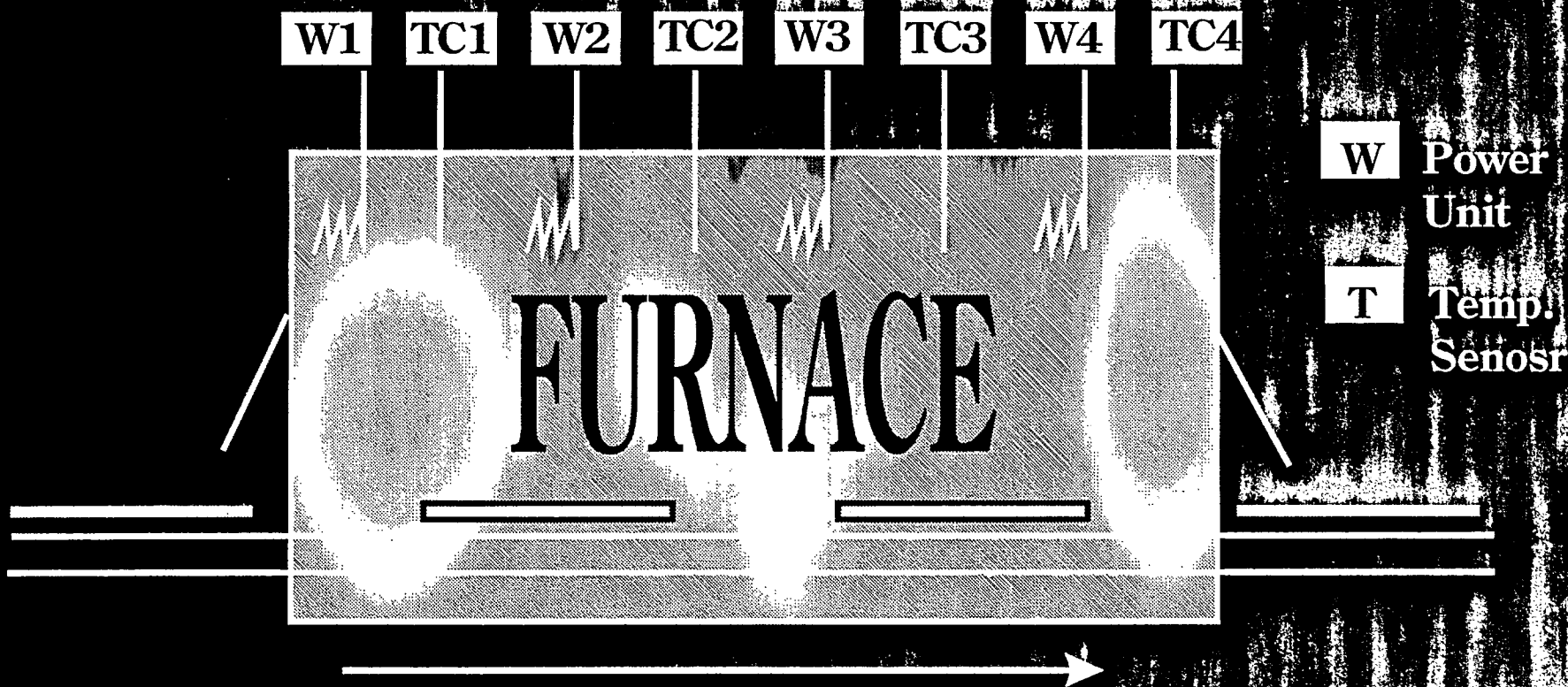
Temperature Sensor

Aeration Motor



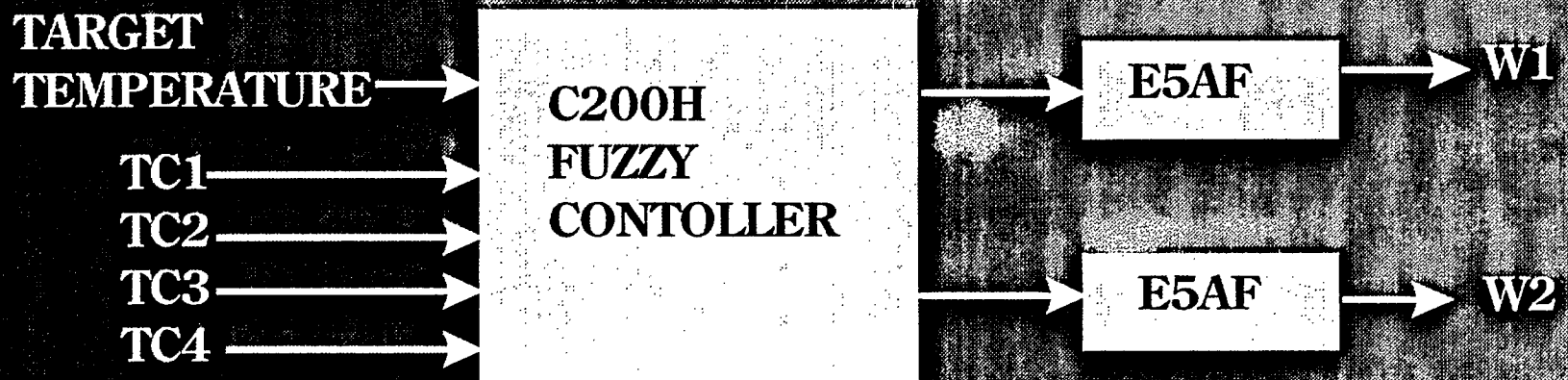
TEMPERATURE CONTROL OF REINFORCED GLASS FURNACE

In a conventional large furnace, the internal temperature is not uniform and does vary due to the interference by the adjacent heaters. Fuzzy Inference makes it possible to keep the temperature of every part of the furnace uniform.

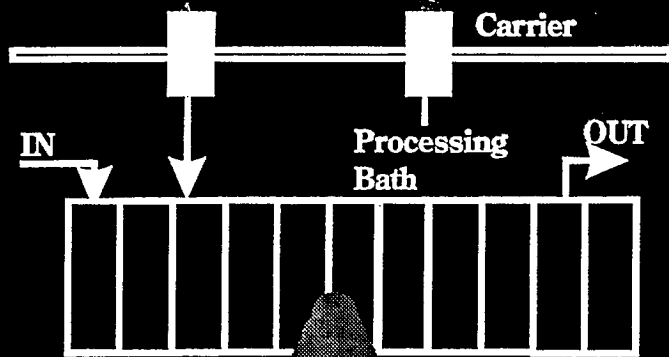


EFFECT

Improves the quality of reinforced glass processed by a furnace by reduced temperature fluctuations.

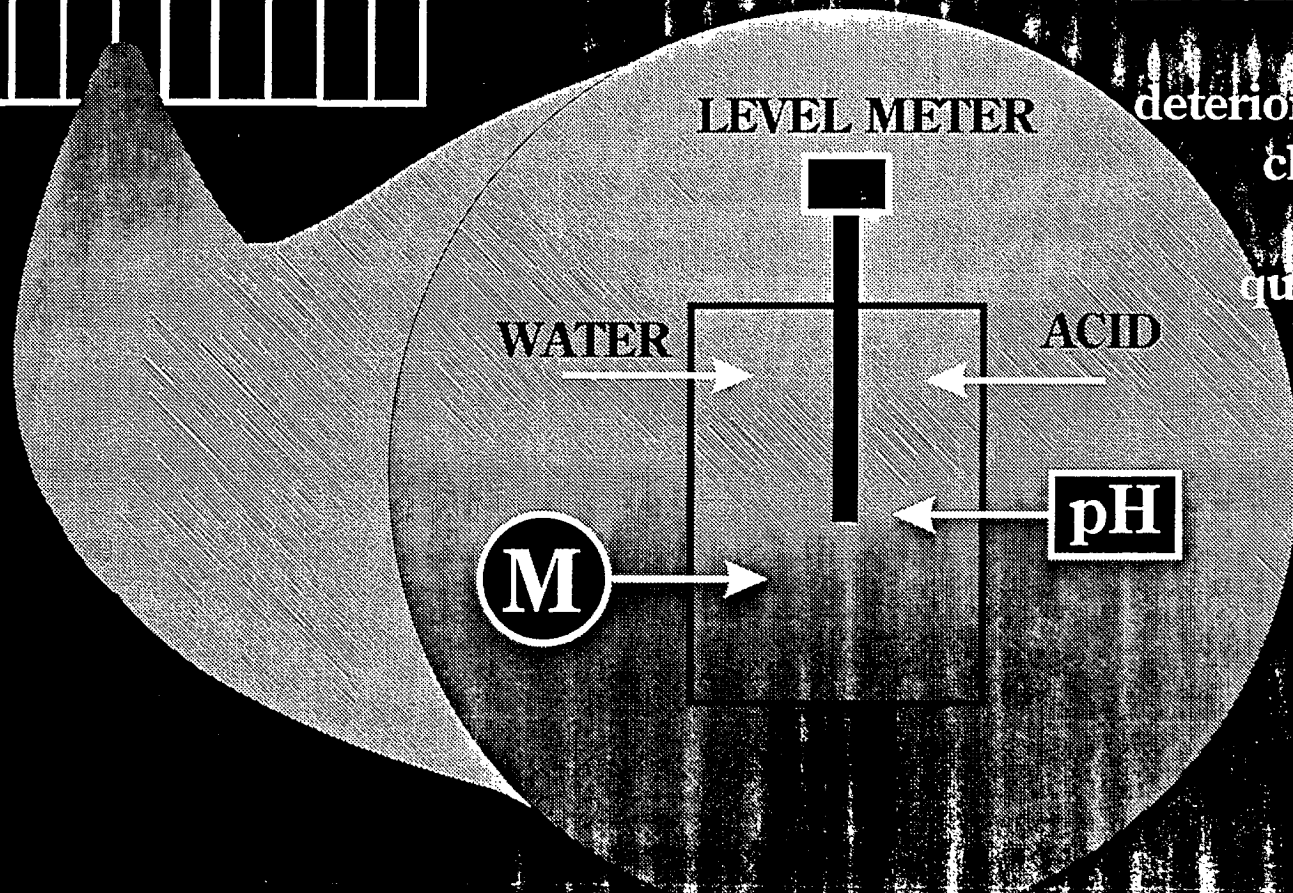


CONCENTRATION CONTROL OF PLATING CHEMICAL



The fuzzy controller predicts the change in Ph value and controls the supply of acid and water

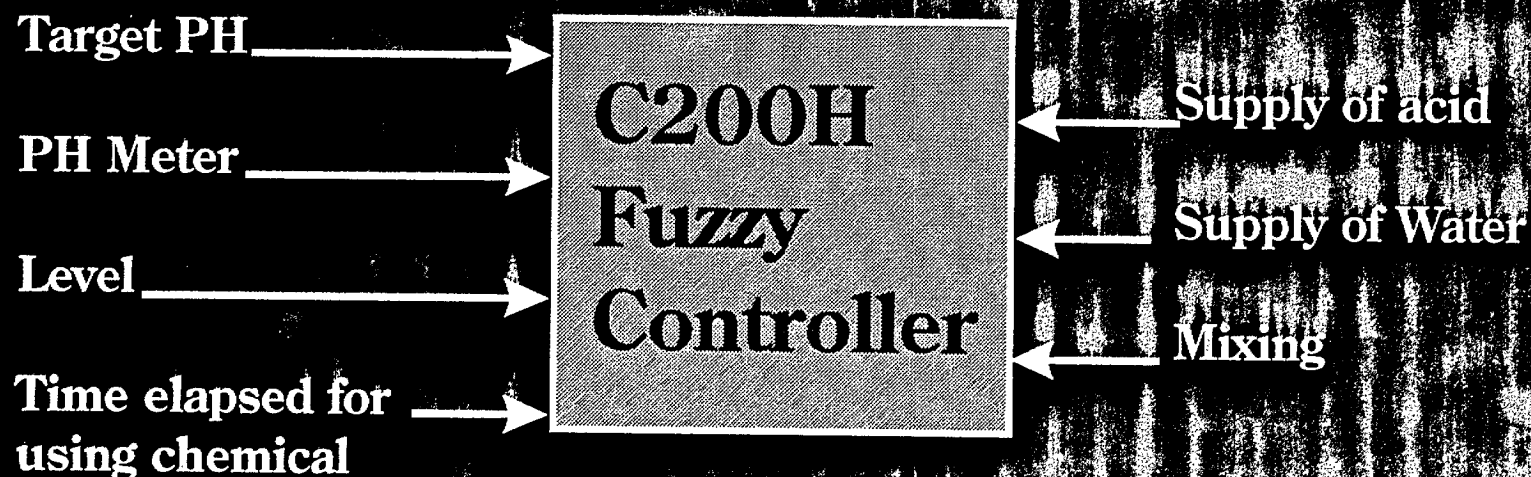
The fuzzy controller judges the deterioration of the chemical and adjusts the quantity of the chemical to be added to the system

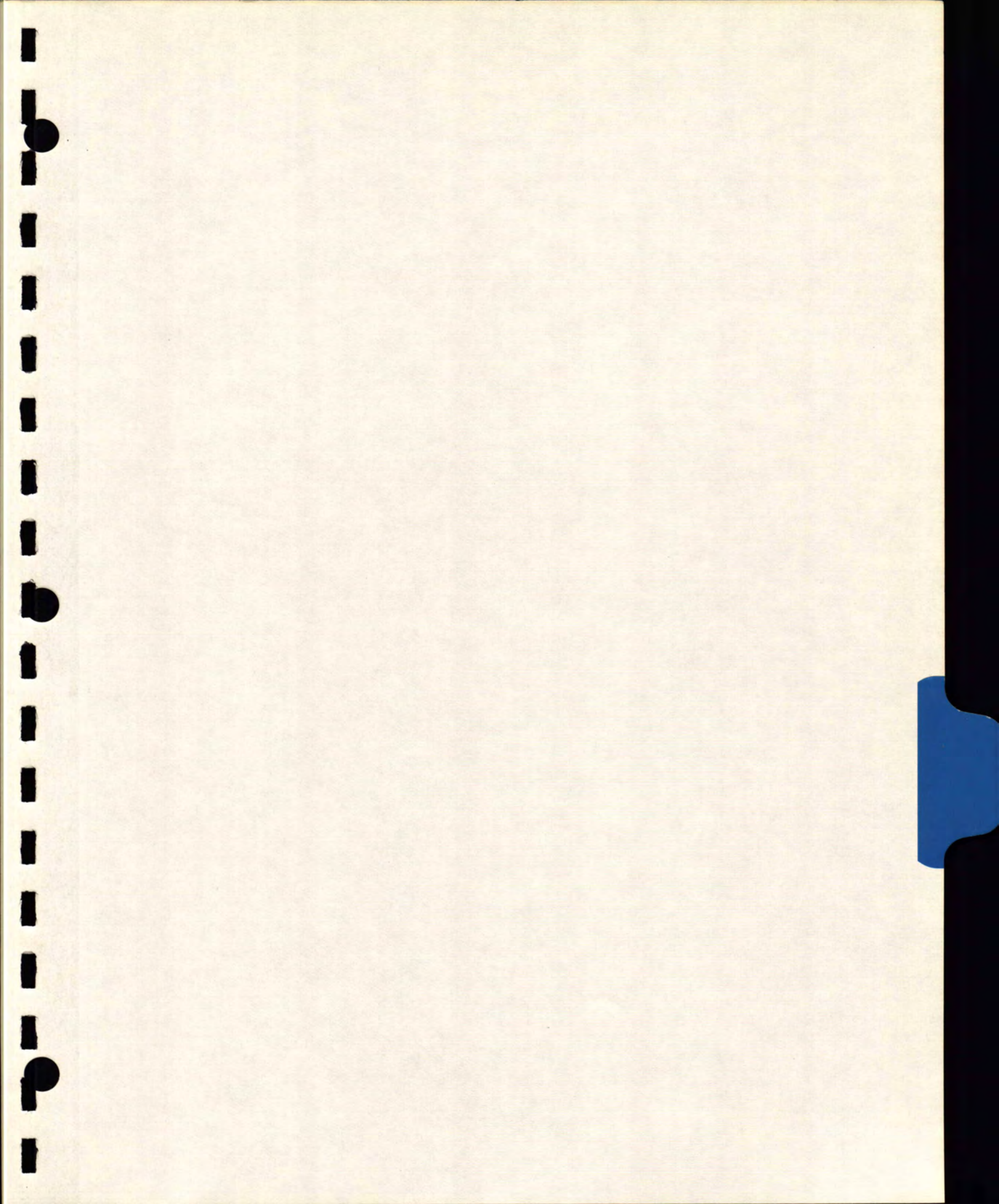


EFFECTS

Reduces the quantity of chemicals used in a plating system and improves the quality of plating by keeping the concentration of the chemicals consistent.

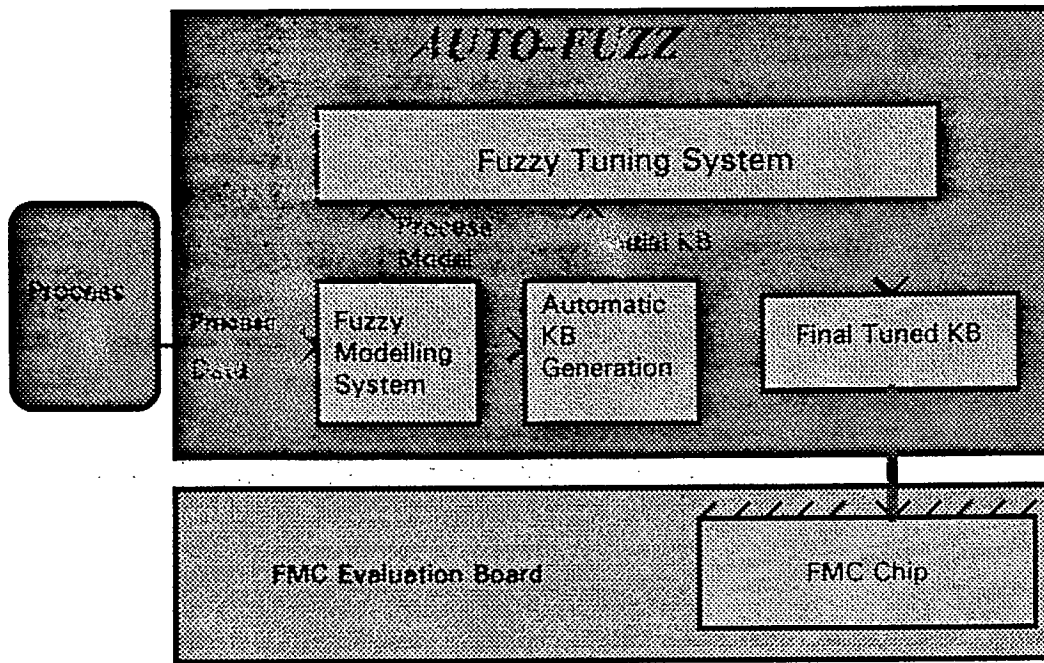
Well-trained operators are not required to operate a fuzzy-controlled plating system because the complicated fine-tuning of the system is handled automatically.

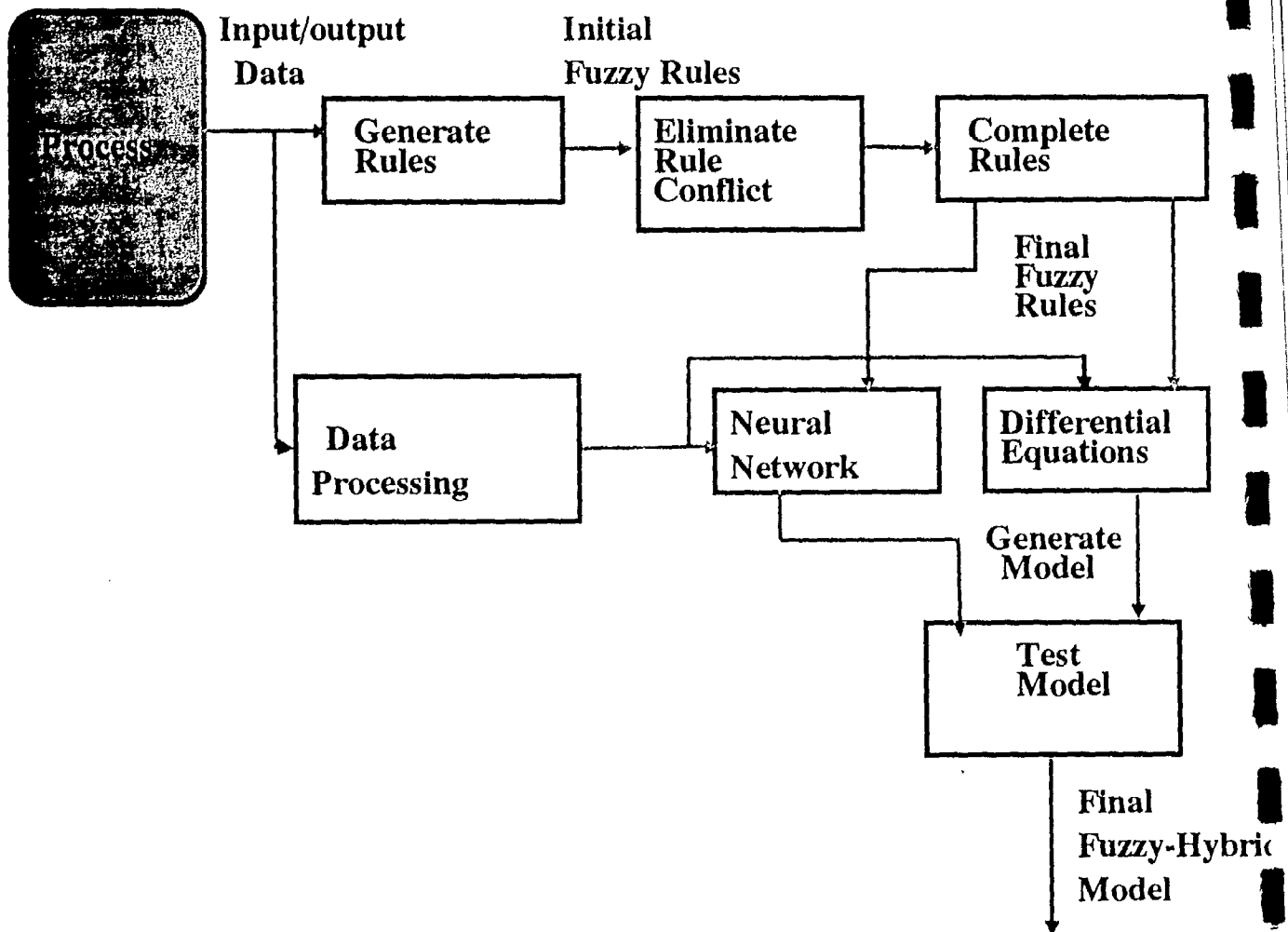




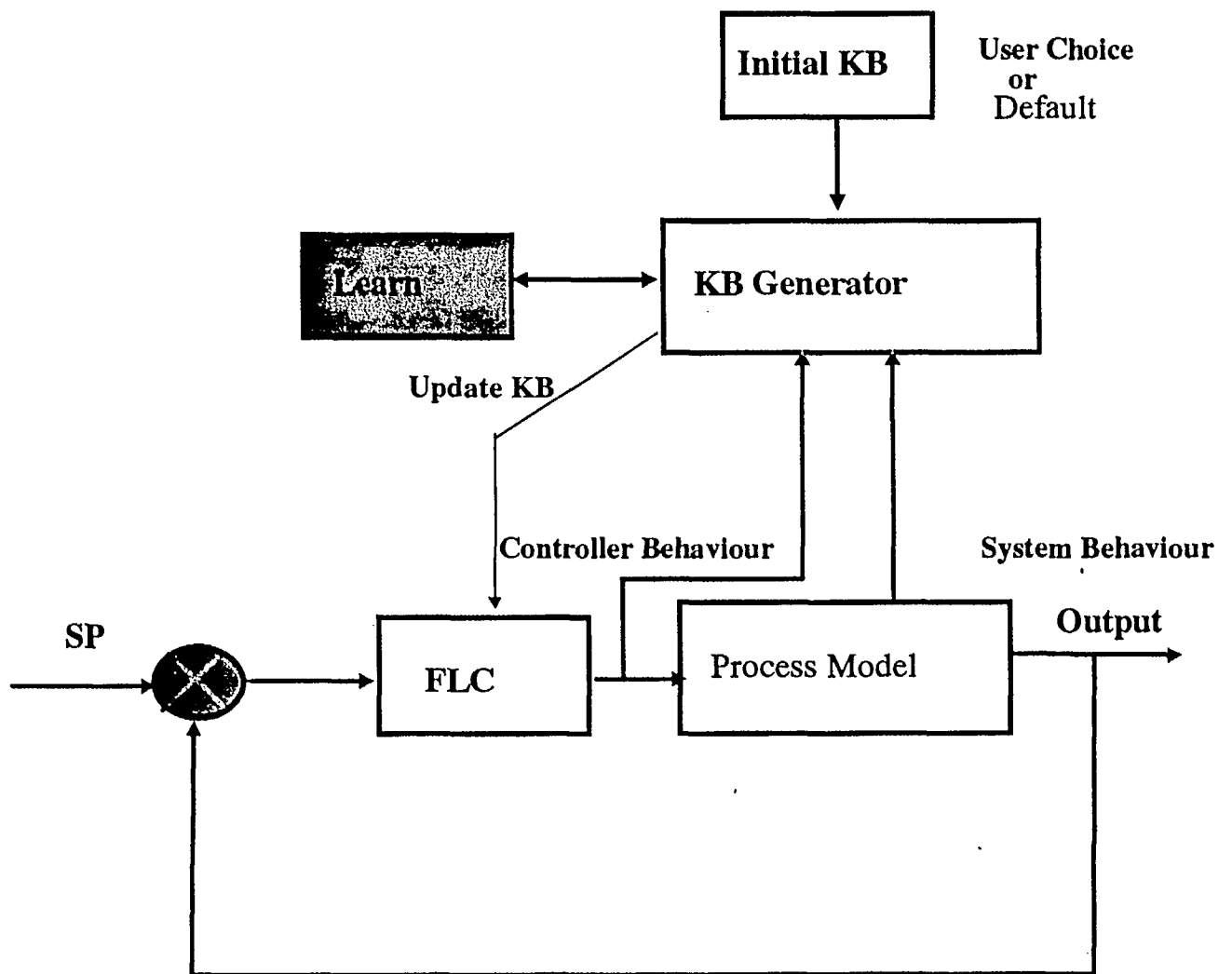
**AutoFuzz: A System For Automatic Fuzzy Controller
Applications Development**

**Dr. Talib Janabi
Director of Technology
Mentalogoc Systems Inc. (MSI)
Markham, Ontario**

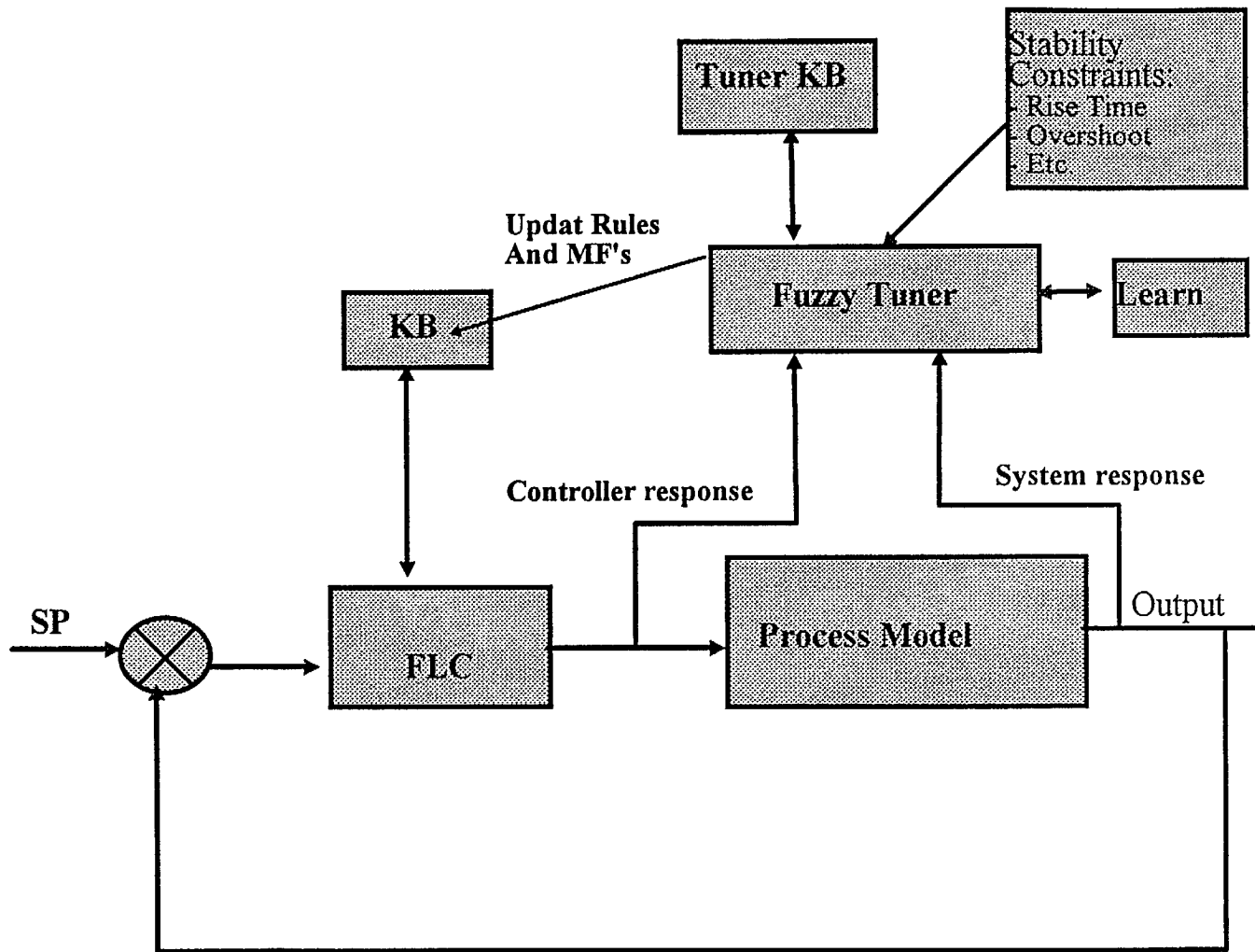




MSI HYBRID MODELLING



MSI KNOWLEDGE-BASE
GENERATOR



MSI FUZZY TUNER

WHAT IS AUTO-FUZZ ?

AUTO-FUZZ IS AN ADVANCED FUZZY EXPERT SYSTEM FOR AUTOMATIC FUZZY KNOWLEDGE BASE GENERATION AND OPTIMIZATION. IT:

- **OPERATES COMPLETELY AUTOMATICALLY**
- **OR AS INTERACTIVE DESIGN TOOL**

OPTIONS ARE GIVEN TO YOU TO:

- **INTERFER TO OPTIMIZE THE SOLUTION**
- **CHANGE SPECIFICATIONS**
- **DECLARE YOUR CONSTRAINTS ON THE PROCESS RESPONSE**
- **RELAX THESE CONSTRAINTS**
- **OR MAKE THEM MORE STRINGENT TO ELIMINATE OVERSHOOTS AND OBTAIN FASTER RISE TIME**

ADVANTAGES OF AUTOFUZZ

- **EASY TO LEARN**
- **SIMPLE TO USE**
- **IT REDUCES THE APPLICATION DEVELOPMENT TO NO MORE THAN A SIMPLE EASY EXERCISE**
- **NON EXPERIENCED ENGINEER MAY TAKE A DAY TO GENERATE THE OPTIMIZED KNOWLEDGE-BASE**
- **EXPERIENCED ENGINEERS WILL TAKE FEW HOURS, OR EVEN FEW MINUTES TO GENERATE THEIR OPTIMIZED KNOWLEDGE-BASE**
- **YOU CAN GENERATE MANY OPTIMIZED KNOWLEDGE BASES FOR DIFFERENT CONSTRAINTS AND CHOOSE THE ONE YOU PREFER**

WHAT DOES AUTOFUZZ NEED FROM YOU ?

- IT NEEDS INPUT/OUTPUT DATA FROM YOUR PROCESS
- AUTOFUZZ WILL GENERATE A MODEL OF YOUR PROCESS TO WORK ON WHETHER YOUR DATA IS LINEAR OR NON-LINEAR
- IF YOU ALREADY HAVE YOUR MODEL, AUTOFUZZ WILL WORK ON YOUR MODEL WHETHER IT IS LINEAR OR NON-LINEAR

WHAT IS THE AUTOFUZZ MODELLING SYSTEM?

- **IT IS AN EXPERT SYSTEM WHICH USES INPUT/OUTPUT DATA TO GENERATE A HYBRID MODEL:**
 - **FUZZY-MATHEMATICAL**
 - **FUZZY-NEURAL**
- **IT GENERATES FUZZY RULES**
- **ELEMINATE RULE CONFLICT**
- **GENERATE EXTRA RULES TO REPRESENT KNOWLEDGE UNREVIELLED BY DATA**

AUTOFUZZ AUTOMATIC KNOWLEDGE-BASE GENERATOR

THE AUTOFUZZ AKBG IS:

- **INCORPORATES MACHINE LEARNING AND INTELLIGENT DECISION MAKING TO GENERATE THE FUZZY RULES AND MEMBERSHIP FUNCTIONS FOR THE APPLICATION**
- **OPTIMIZES THE NUMBER OF FUZZY RULES AND MEMBERSHIP FUNCTIONS**
- **GENERATES THE KNOWLEDGE-BASE REQUIRED FOR YOUR APPLICATION :**
 - **OBJECTIVELY**
 - **IN A VERY SHORT TIME.**

IT FREES YOU FROM THIS PAINSTAKING AND TIME CONSUMING EFFORT

THE AUTOFUZZ TUNER

THE AUTOMATIC FUZZY TUNER IS:

- **A POWERFUL INTELLIGENT SYSTEM FOR TUNING AND OPTIMIZING THE FUZZY CONTROLLER KNOWLEDGE-BASE**
- **EMPLOYS ADVANCED AND INTELLIGENT METHODS IN ITS SEARCH FOR OPTIMUM SOLUTIONS**
- **IT AUTOMATICALLY ADJUSTS THE CONTROLLER KNOWLEDGE BASE TO OBTAIN CONSISTENT AND OPTIMIZED FUZZY RULES AND MEMBERSHIP FUNCTIONS TO YIELD OPTIMUM PROCESS RESPONSE**
- **YOU CAN DECLARE YOUR REQUIREMENTS AND CONSTRAINTS ON THE RESPONSE PARAMETERS**
- **MSI FUZZY TUNER IS A NEW GENERATION OF FUZZY EXPERT SYSTEMS AND THE FIRST OF ITS KIND FOR THE SOLUTION OF THE FUZZY KNOWLEDGE-BASE OPTIMIZATION**

Learning Systems
Development

Fuzzy Process Modeling

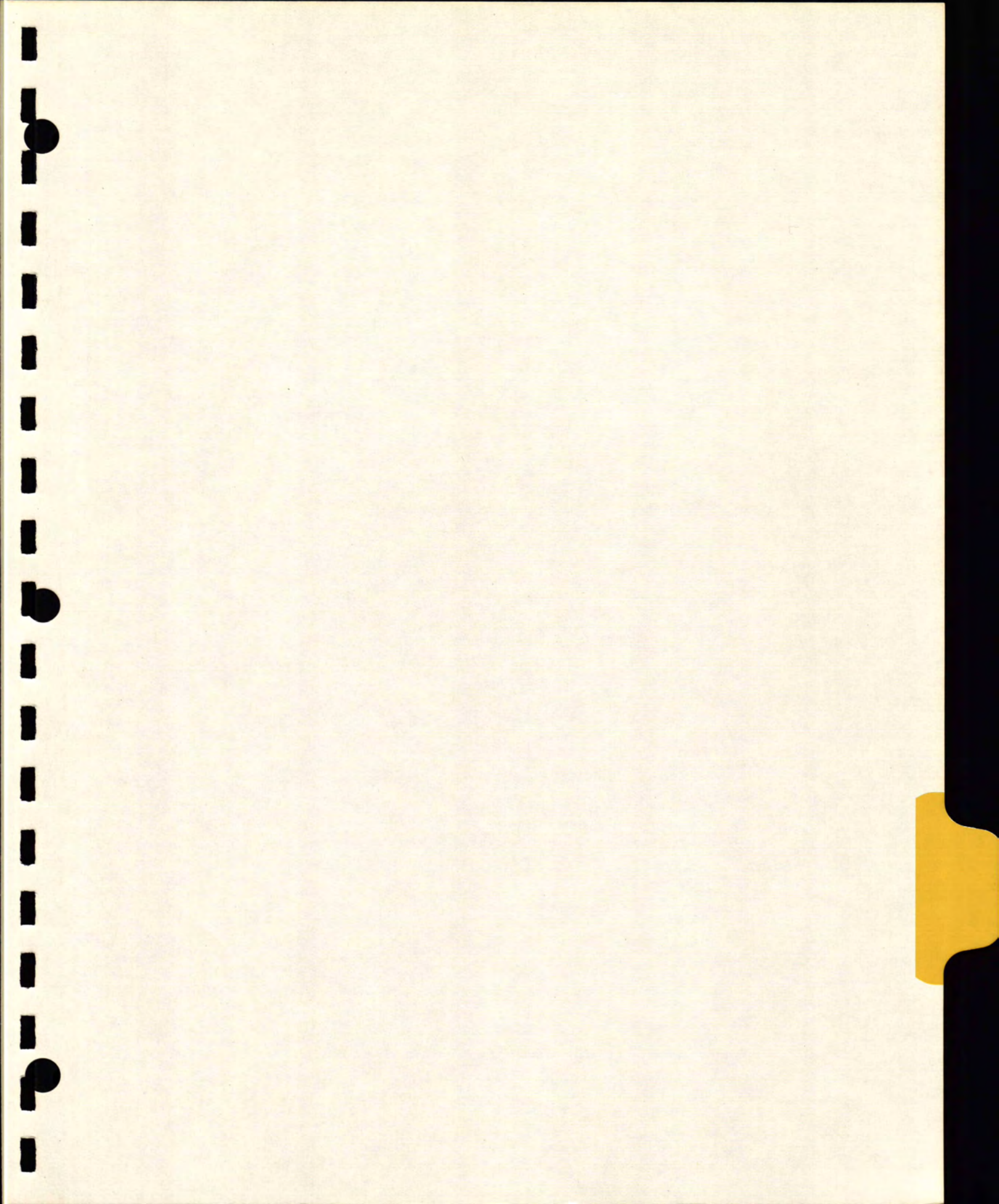
(A Hybrid of Mathematical and Fuzzy Modeling)

Automatic Fuzzy Rules Generation

(Advanced Reinforcement Learning)

Fuzzy Process Modeling and Behaviour
Prediction

- Neural and Fuzzy Modeling
- Inductive and Fuzzy Learning



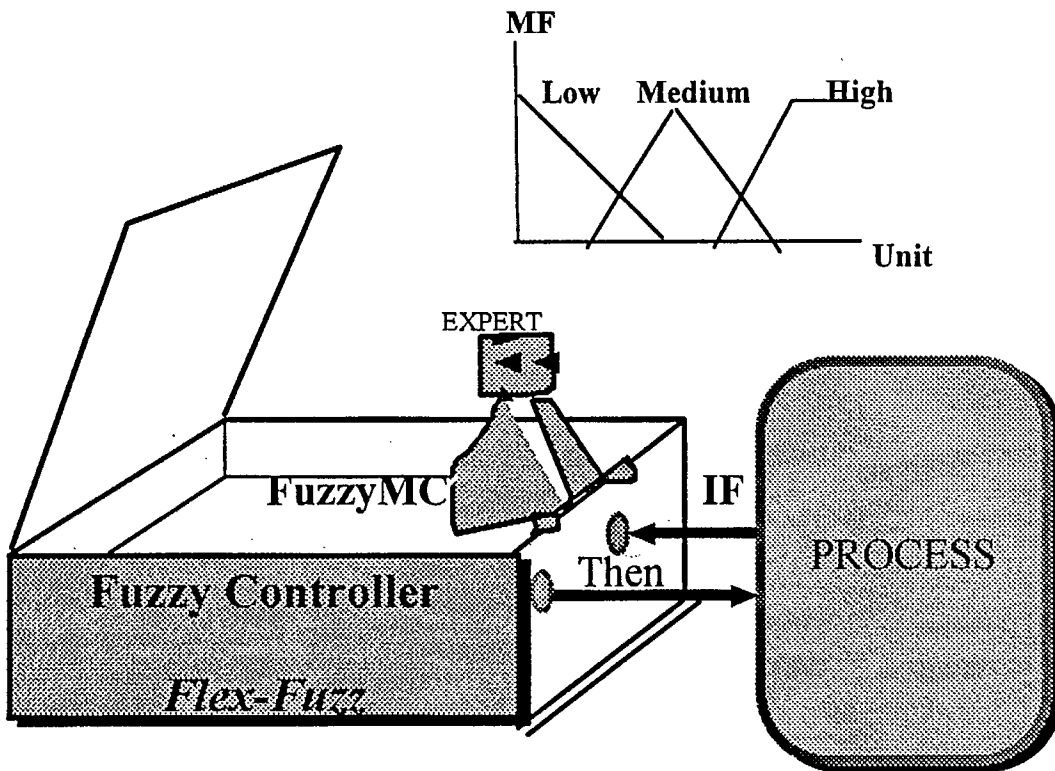
The Canadian Industrial Fuzzy Control Systems
Overview of MSI Fuzzy Logic Technology Developments

Dr. Labib Sultan

Director of Research and Development

Mentalogic Systems Inc. (MSI)
Markham, Ontario L3R 9R6

MSI Fuzzy Technology Overview



MSI Fuzzy:
“Friendly, Powerfull and Low Cost”

**Mentalogic Systems Inc.
(MSI)**

**Established in 1991 Under the
Canadian Federal Law**

**Specializes in Fuzzy Logic and AI Based
Technology
(Systems Development and Industrialization)**

**The R&D involves Five Departments and
More than 20 Scientists and Engineers**

**Good linkage with the Canadian Industry,
Government and Research communities**

Growing International Role in Fuzzy Technology

**More than 12 basic Fuzzy technology products will be
available to the Market in 1994 and other 8 basic
Fuzzy technology products are planned for 1995**

**MSI
DIVISIONS**

Fuzzy Controller Chip Development

Expert Systems Development

Embedded Control Systems

Learning Systems Development

Process Fuzzy Control

**Fuzzy Control Application
Development**

**Canadian & Int'l
Marketing**

MSI Fuzzy Controller Development

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graph TD; A[MSI Fuzzy Controller Development] --- B[Development of High-Performance Fuzzy Inference Engine (The CT-FLC)]; A --- C[Development of Real-Time Fuzzy Reasoning Machine for Fuzzy Coordinator and Multiple FLC and Fuzzy-PLC in one FMC.]; A --- D[Development of Fuzzy Microcontroller Chips (FMC) (Motorola, Intel, NSC, Zilog, NEC, etc.)]; A --- E[Development of Application Evaluation Systems for the FMC]; A --- F[Design of Special Purpose Fuzzy Controller ASIC Chips];
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Development of High-Performance Fuzzy Inference Engine (The CT-FLC)

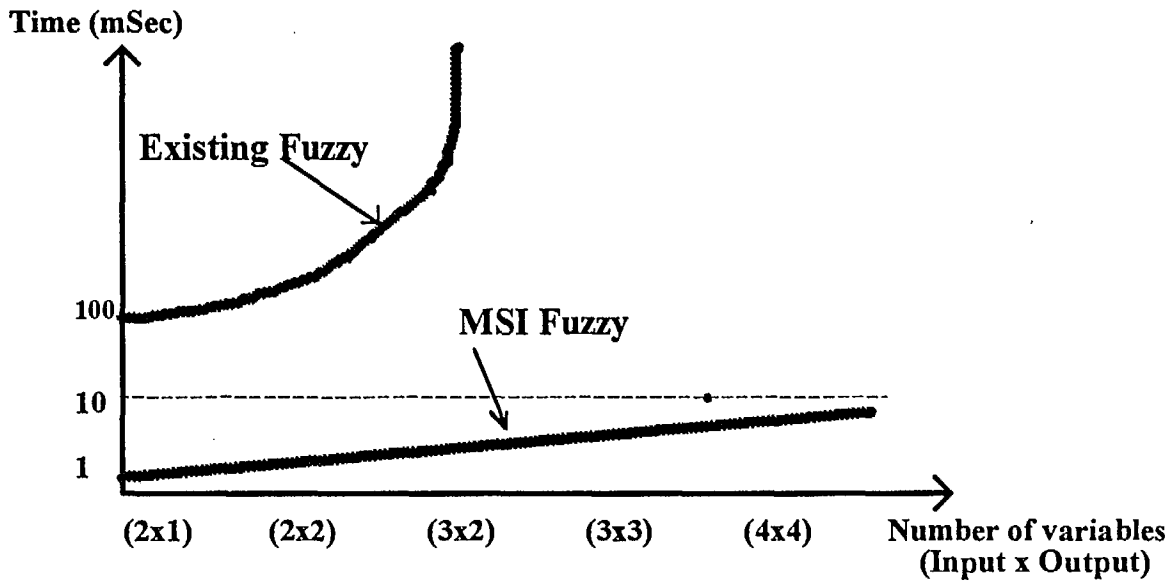
Development of Real-Time Fuzzy Reasoning Machine for Fuzzy Coordinator and Multiple FLC and Fuzzy-PLC in one FMC.

Development of Fuzzy Microcontroller Chips (FMC) (Motorola, Intel, NSC, Zilog, NEC, etc.)

Development of Application Evaluation Systems for the FMC

Design of Special Purpose Fuzzy Controller ASIC Chips

A Comparison Between the Real-Time Response and Memory Requirement of MSI and Existing Fuzzy Solutions



| <i>The Application Input x Output Variables</i> | <i>The estimated memory required by MSI fuzzy controller chip (k Byte)</i> | <i>The estimated memory required by the existing fuzzy controller chips (K Byte)</i> |
|---|--|--|
| <i>1x1</i> | <i>0.2</i> | <i>1.2</i> |
| <i>2x1</i> | <i>0.4</i> | <i>4</i> |
| <i>3x1</i> | <i>0.8</i> | <i>6</i> |
| <i>4x1</i> | <i>1.2</i> | <i>8</i> |
| <i>2x2</i> | <i>2</i> | <i>8</i> |
| <i>3x2</i> | <i>3</i> | <i>24</i> |
| <i>3x3</i> | <i>6</i> | <i>36</i> |
| <i>4x4</i> | <i>16</i> | <i>72</i> |

**Cost Comparison Between Fuzzy Controller Solutions and
Traditional MP Based Solutions**

| <i>Item of Evaluation</i> | <i>MSI Fuzzy Solution</i> | <i>Existing Fuzzy Solution</i> | <i>Traditional MPU Solution</i> |
|------------------------------------|---------------------------|--------------------------------|---------------------------------|
| <i>Average time of development</i> | <i>1-4 weeks</i> | <i>3-6 months</i> | <i>12-18 months</i> |
| <i>Average Cost of development</i> | <i>Low</i> | <i>Medium</i> | <i>High</i> |

Fuzzy Microcontroller Chips Supported by MSI in 1994

| FMC Chip Code | Description |
|----------------------|---------------------------|
| FMC-M68HC11 | FMC - Motorola M68HC11 |
| FMC -M68HC05 | FMC - Motorola M68HC05 |
| FMC -M68HC08 | FMC - Motorola M68HC08 |
| FMC -NSC-COP8 | FMC - NSC COP8 family |
| FMC -NSC-HPC16 | FMC - NSC HPC16 |
| FMC-I8051 | FMC - Intel I8051 family. |
| FMC-Z8 | FMC - Zilog Z8 family |

EMBEDDED FUZZY
CONTROL
DEVELOPMENT

Fuzz-Flex

A Series of Fuzzy Controllers for Fast and Low-Cost Fuzzy Applications Development

AC Fuzz-Drive

DC Fuzz-Drive

A Series of Fuzzy Controller Drivers for AC and DC Motors

Fuzz-Comfort

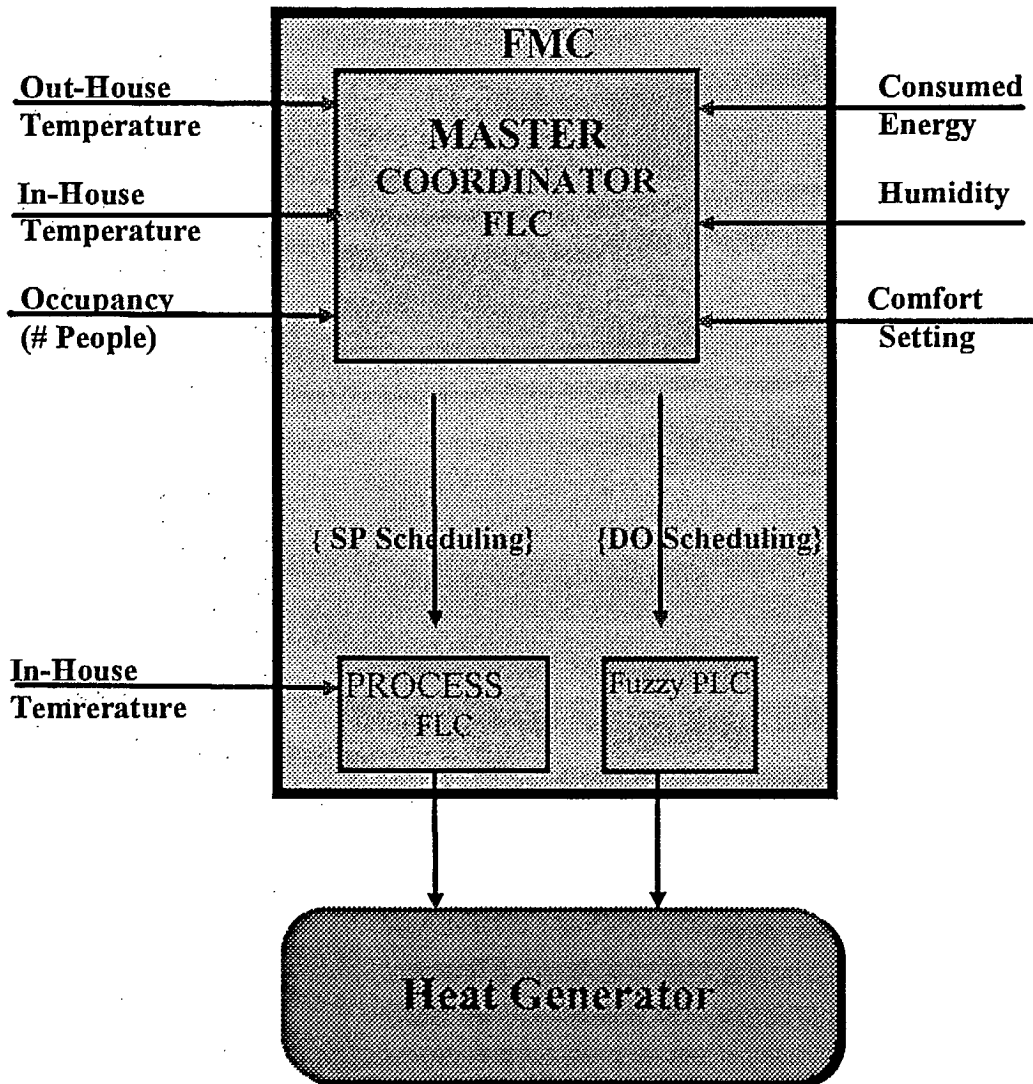
A series of Fuzzy Controllers for Home and Office Buildings Heating, Ventilation and Air Conditioning Systems (HVAC)

Fuzz-NET

Low-Cost Distributed Fuzzy Control System

Home and Industrial HVAC Control

Flex-Fuzz / Fuzz-Comfort



MSI Fuzzy Technology Products for Embedded Control Applications (1994)

| Product Code | Product Designation |
|--|---|
| <p>FCDS-Emb-01</p> <p>FCDS-Sim-01</p> <p>FCDS-Emb-02</p> <p>FCDS-Emb-03</p> | <p>Fuzzy Controller Design Stations (FCDS) and Expert Systems</p> <p>Fuzzy Controller Design Station with "<i>MSI-Fuzz</i>" system for FMC Customization and Evaluation</p> <p>Fuzzy Controller design Station for Training and Simulation</p> <p>Fuzzy Controller Design Station with "<i>Auto-Fuzz</i>" system for Automatic Fuzzy KB Generation and Tuning</p> <p>Fuzzy Controller Development Station with "<i>Quick-Fuzz</i>" for the Customization of "<i>Flex-Fuzz</i>" Fuzzy Controller Boards</p> |
| <p>FMC-M68HC11</p> <p>FMC-M68HC05</p> <p>FMC-M68HC08</p> <p>FMC-NSC-COP8</p> <p>FMC-NSC-HPC16</p> <p>FMC-I8051</p> <p>FMC-Zilog-Z8</p> | <p>Fuzzy Microcontroller Chips (FMC)</p> <p>FMC - Motorola M68HC11</p> <p>FMC - Motorola M68HC05</p> <p>FMC - Motorola M68HC08</p> <p>FMC - NSC COP8 family</p> <p>FMC - NSC HPC16</p> <p>FMC - Intel I8051 family.</p> <p>FMC - Zilog Z8 family</p> |
| <p>MSI-EVB-HC11</p> <p>MSI-EVB-HC05</p> <p>MSI-EVB-HC08</p> <p>MSI-EVB-COP8</p> <p>MSI-EVB-HPC16</p> <p>MSI-EVB-I8051</p> <p>MSI-EVB-Z8</p> <p>FLCB-HPC</p> <p>FLCB-MHC11</p> <p>FLCB-I8751</p> <p>MSI-AIO-1.0</p> | <p>Evaluation Boards for FMC</p> <p>Evaluation board for Motorola MCU M68HC11</p> <p>Evaluation board for Motorola MCU M68 HC05</p> <p>Evaluation board for Motorola MCU M68HC08</p> <p>Evaluation board for NSC MCU COP8</p> <p>Evaluation board for NSC HPC 16</p> <p>Evaluation board for Intel MCU I8051</p> <p>Evaluation board for Zilog MCU Z8</p> <p>Fuzzy Controller Boards "<i>Flex-Fuzz</i>" Series</p> <p>Fuzzy Controller Board with NSC HPC FMC</p> <p>Fuzzy Controller Board with Motorola HC11 FMC</p> <p>Fuzzy Controller Board with Intel I8751 FMC</p> <p>Input-Output Boards with Auto-calibration</p> <p>General purpose I/O board with 8 channels analog input and 4 channels analog output with facilities for sensor and signal auto-calibration</p> |

Fuzzy Expert System Development

MSI-Fuzz

Expert System for the Customization and
Evaluation of Fuzzy Microcontroller Chips (FMC)

AUTO-Fuzz

Expert System for Process Modeling
Expert System for Fuzzy KB Auto-Generation
Expert System for Fuzzy Controller Auto-Tuning

Quick-Fuzz

- Expert System for Fast Fuzzy Controller Applications
Development
- Expert System for Multiple Fuzzy Controllers and Fuzzy
PLC Configuration and Coordination
(To Customize *Flex-Fuzz* Series of Fuzzy Controllers)

Monitoring-Fuzz

Expert System For Process Monitoring
Expert System for Production Management and Planning

PROCESS FUZZY CONTROL

Design of Fuzzy Controller Boards
(VME, STD 32, PC BUS, Multibus, ISBX)

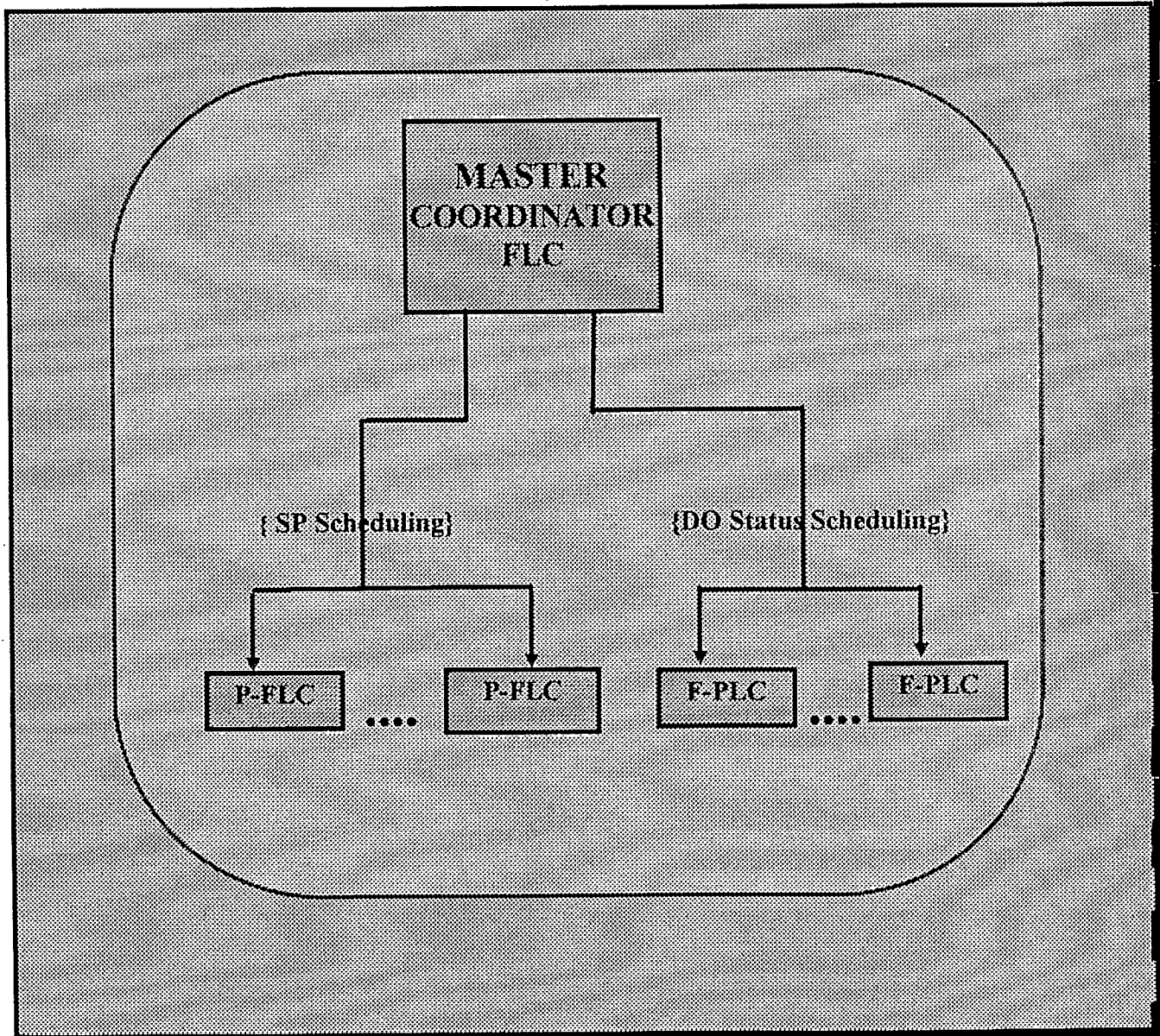
Development of DFCS
(Distributed Fuzzy Control System)
With Automatic KB Generation and Tuning

Development of Fuzzy Monitoring System

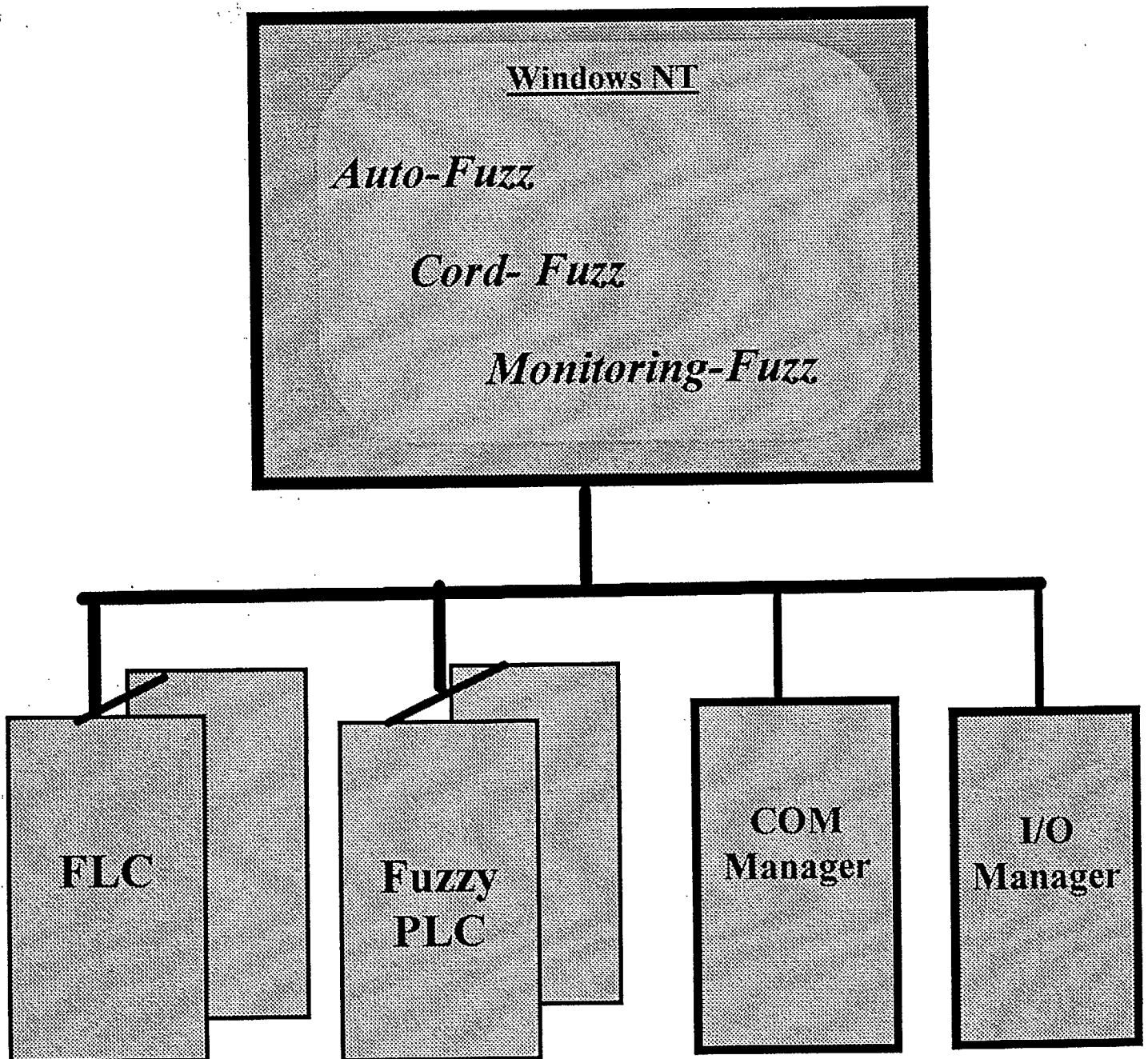
Development of Fuzzy Expert System for
Production Management, Planning and
Scheduling

“Quick-Fuzz/ Cord -Fuzz”

**Expert System For The Configuration and
Co-ordination of Multiple FLCs and Fuzzy PLCs**

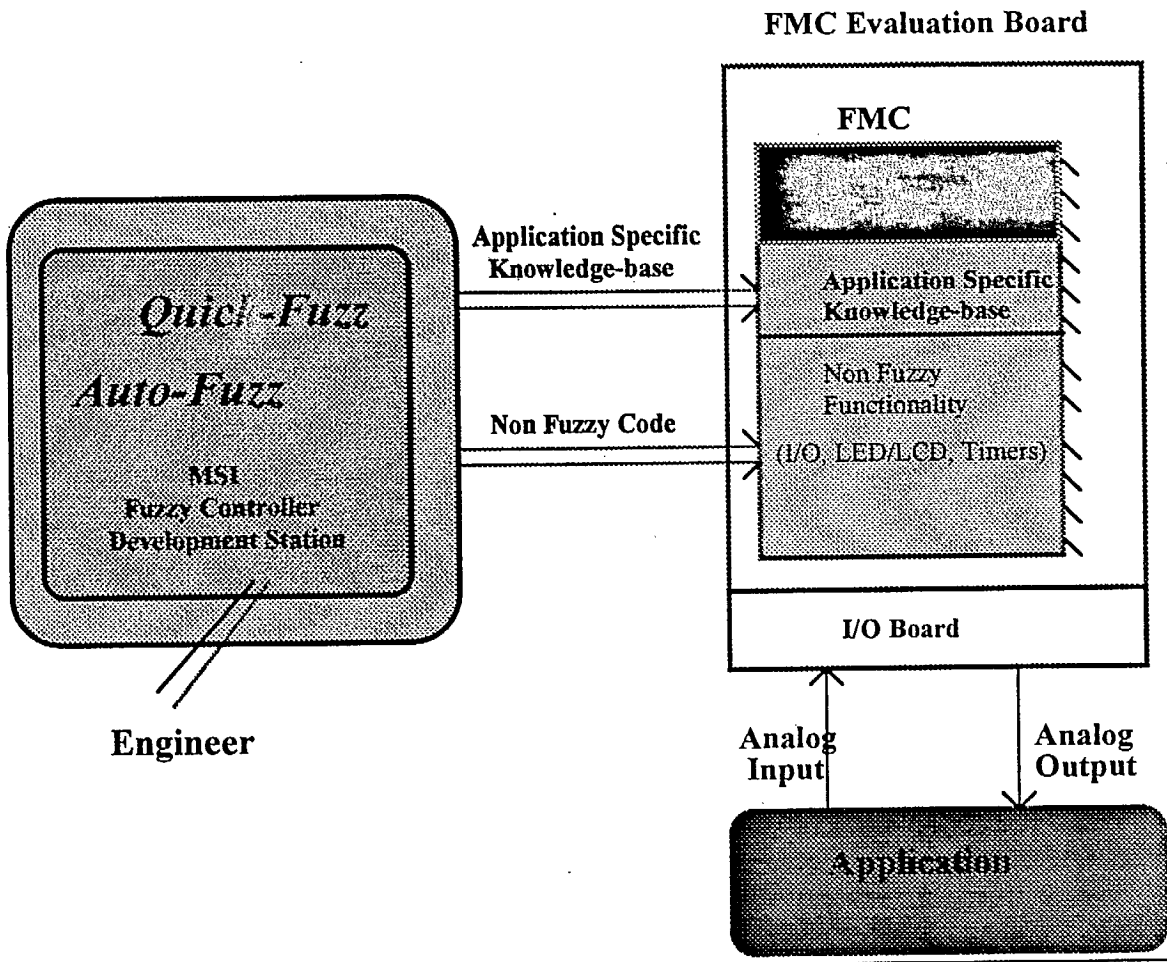


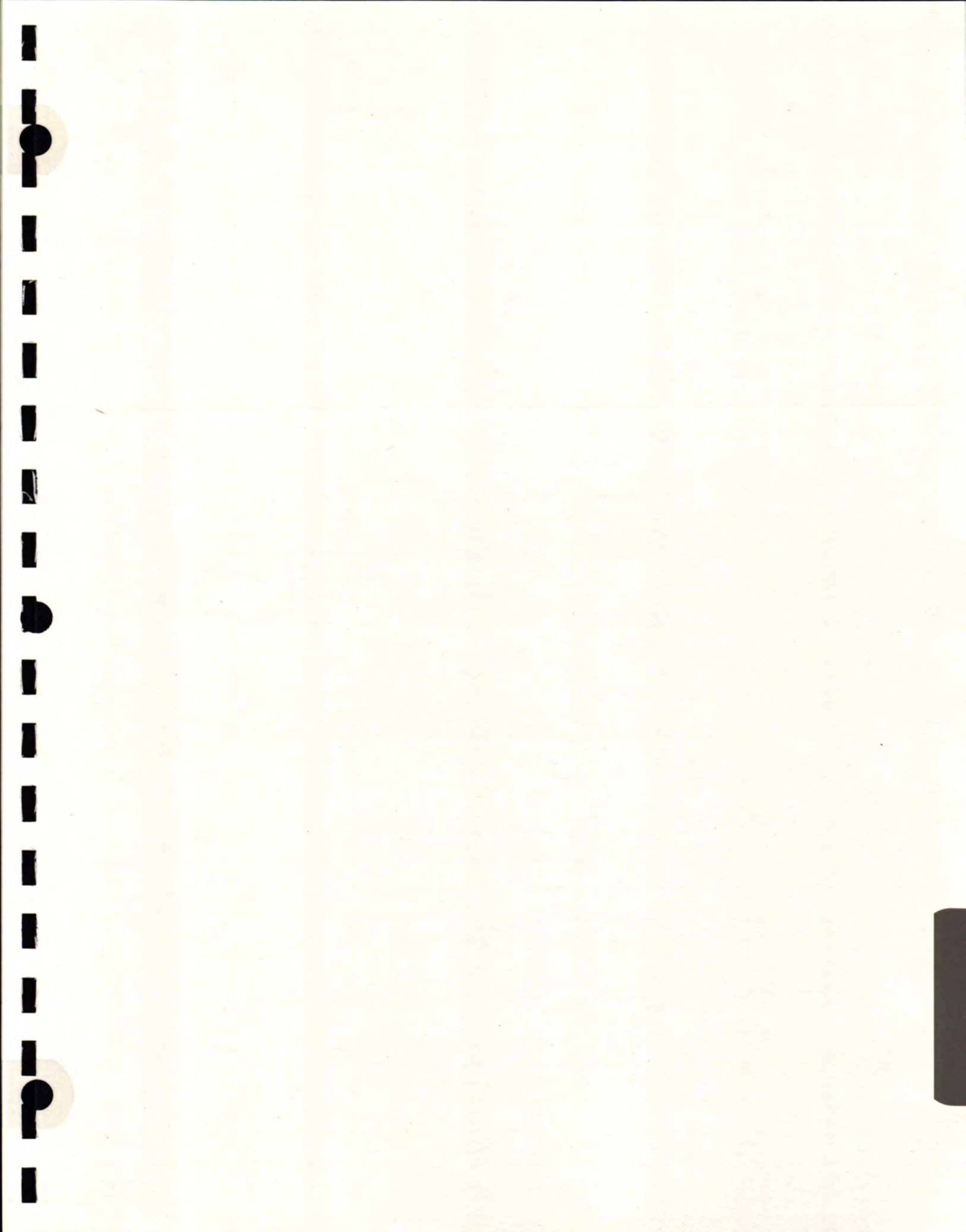
DFCS - Distributed Fuzzy Control System



MSI Fuzzy Technology Products for the Process Control Industry (1994)

| Product Code | Product Designation |
|--|---|
| <p><i>MSI-Fuzz</i></p> <p><i>Auto-Fuzz</i></p> <p><i>Quick-Fuzz</i></p> <p><i>Monitor-Fuzz</i></p> | <p><i>Expert Systems for The Process Industry</i></p> <p>Fuzzy Controller Design System for the Controller Customization and Evaluation</p> <p>Fuzzy Controller KB Auto-Generation and Auto Tuning Expert System</p> <p>Multiple Fuzzy Controller Configuration and Co-ordination System (P-FLC, F-PLC, and M-FLC).</p> <p>Monitoring System for the Fuzzy Distributed Control System (FDCS).</p> |
| <p>FLC-VME</p> <p>FLC- STD-32</p> <p>FLC- PC BUS</p> <p>ISBX</p> | <p><i>Fuzzy Controllers for Standard Bus Systems</i></p> <p>Fuzzy Controller Board for VME BUS</p> <p>Fuzzy Controller Board for STD 32 BUS</p> <p>Fuzzy Controller Board for PC BUS</p> <p>Fuzzy Controller for Intel SBX</p> |
| <p>DFCS</p> | <p>Distributed Fuzzy Control System with Standard BUS and Configuration System</p> |
| <p>FLCB-HPC</p> <p>FLCB-MHC11</p> <p>FLCB-I8751</p> | <p><i>Fuzzy Controller Boards "Flex-Fuzz" Series</i></p> <p>Fuzzy Controller Board with NSC HPC FMC</p> <p>Fuzzy Controller Board with Motorola HC11 FMC</p> <p>Fuzzy Controller Board with Intel I8751 FMC</p> |





LOGIQUE FLOUE EN FABRICATION

EXEMPLE D'APPLICATION DE LA LOGIQUE FLOUE POUR LE CHOIX DES CONDITIONS DE COUPE EN TOURNAGE

Présenté par

**Marek Balazinski
Professeur adjoint**

**ÉCOLE POLYTECHNIQUE
Campus de l'Université de Montréal
2900, rue Édouard Montpetit
C.P. 6079, succursale «Centre-ville»
Montréal (Québec) H3C 3A7
Téléphone : (514) 340-4015
Télécopieur : (514) 340-5867**

Subvention CRSNG OGP1N 013

Mars 1994

INTRODUCTION

1. OBJECTIF

- Concevoir un logiciel de choix de conditions de coupe simple, efficace, bon marché et destiné principalement aux PME.

2. POURQUOI LA LOGIQUE FLOUE?

- Efficacité dans des conditions incertaines;
- possibilité unique d'exprimer la connaissance qualitative d'un expert en forme linguistique proche du langage courant (exemple : si le matériau est dur et si la profondeur de coupe est petite, ALORS la vitesse de coupe sera grande;
- compression des données et grande vitesse d'exécution.

BASE THÉORIQUE DU LOGICIEL FUZZY-FLOU

1. MOTEURS D'INFÉRENCE

$$U' = (A', B', \dots, C') \circ R \quad (1)$$

- où : U' - conclusion
 A', B' - variables linguistiques (observations)
 \circ - règle de composition d'inférence
 R - base de règles (connaissances)

LE LOGICIEL FUZZY-FLOU PEUT UTILISER QUATRE MOTEURS D'INFÉRENCE

$$U'(u) = \max_r \sup_{\substack{x \in X \\ y \in Y \\ z \in Z}} \min \left[\min(C'(z), \dots, B'(y), A'(x)), \min(A_i^{(r)}(x), B_j^{(r)}(y), \dots, C_p^{(r)}(z), U_k^{(r)}(u)) \right] \quad (2)$$

représenté symboliquement par MAX-SUPMIN-MIN-MIN (abrégé par MA-SMI-MI)

$$U'(u) = \max_r \sup_{\substack{x \in X \\ y \in Y \\ z \in Z}} \left[(C'(z) \cdot \dots \cdot B'(y) \cdot A'(x)) \cdot (A_i^{(r)}(x) \cdot B_j^{(r)}(y) \cdot \dots \cdot C_p^{(r)}(z) \cdot U_k^{(r)}(u)) \right] \quad (3)$$

représenté par MAX-SUPPROD-PROD-PROD (abrégé par MA-SPR-PR)

$$U'(u) = \sum_r \sup_{\substack{x \in X \\ y \in Y \\ z \in Z}} \min \left[\min(C'(z), \dots, B'(y), A'(x)), \min(A_i^{(r)}(x), B_j^{(r)}(y), \dots, C_p^{(r)}(z), U_k^{(r)}(u)) \right] \quad (4)$$

représenté par SUM-SUPMIN-MIN-MIN (abrégé par SU-SMI-MI)

$$U'(u) = \sum_r \sup_{\substack{x \in X \\ y \in Y \\ z \in Z}} \left[(C'(z) \cdot \dots \cdot B'(y) \cdot A'(x)) \cdot (A_i^{(r)}(x) \cdot B_j^{(r)}(y) \cdot \dots \cdot C_p^{(r)}(z) \cdot U_k^{(r)}(u)) \right] \quad (5)$$

représenté respectivement par SUM-SUPPROD-PROD-PROD (abrégé par SU-SPR-PR).

LOGICIEL FUZZY-FLOU

MATÉRIEL NÉCESSAIRE

- IBM AT 286, 386, 486 et compatibles
- carte graphique EGA, VGA

CAPACITÉS

- 4 moteurs d'inférence
- 300 règles au maximum
- Chaque règle peut contenir jusqu'à **5 conditions** et **2 conclusions indépendantes**.
- Chaque condition et conclusion peut utiliser jusqu'à **11 variables linguistiques**.
- «Defuzzification» par le centre de gravité.

CE LOGICIEL PEUT ÊTRE UTILISÉ COMME

- système d'aide à la décision et
- contrôleur.

EXEMPLE DE CHOIX ET DE MODIFICATIONS DES CONDITIONS DE COUPE EN TOURNAGE

CHOIX DES CONDITIONS DE COUPE

(données d'entrée selon Machining Data Handbook)

- dureté du matériau à usiner
- profondeur de coupe
- contenu en carbone
- usinabilité

CONCLUSIONS

- vitesse de coupe
- avance de coupe

**MODIFICATIONS DES CONDITIONS DE COUPE
POUR LES ADAPTER AU SYSTÈME
«MACHINE-PIÈCE-OUTIL» PARTICULAIRE**

DONNÉES D'ENTRÉE

- qualité de la machine
- rigidité du système «machine-pièce-outil»
- précision d'usinage désirée

CONCLUSIONS

- facteur multiplicatif de vitesse de coupe
- facteur multiplicatif de l'avance

FUZZY DECISION SUPPORT SYSTEM SHELL
FUZZY-FLOU ver. 0.1

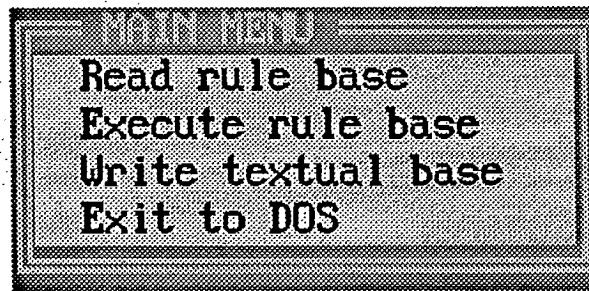
Marek BALAZINSKI, Martin BELLEROSE,

**Ecole Polytechnique de Montreal,
C.P. 6079, Montreal, Qc, CANADA, H3C 3A7**

Ernest CZOGALA

**Technical University of Silesia,
Akademicka 16, 44-101 Gliwice, POLAND**

PAGE TITRE DU SYSTÈME AIDE À LA DÉCISION FUZZY-FLOU



MENU PRINCIPAL DU LOGICIEL FUZZY-FLOU

PROCESSING OPTIONS

INFERENCE: MA-SMI-MI MA-SPR-PR
 SU-SMI-MI SU-SPR-PR

INPUT:
From : keyboard file
 interface
Value: crisp fuzzy

SCREEN OUTPUT
 graphics textual results
 control value run in continue

FILE OUTPUT
 observations
 control value
Actions: all fired

OPTIONS D'UTILISATION DU LOGICIEL FUZZY-FLOU

EXEMPLE DES DONNES ET DES REGLES "coupeang.dat"

| | |
|------------------------------------|------------------|
| # 1 Hardness (Bhn) | (3 2 2 1 7 7) |
| (100 175 0 50 1 very soft) | (3 3 2 1 6 9) |
| (225 275 50 50 1 soft) | (4 1 2 1 6 1) |
| (325 375 50 50 1 medium) | (4 2 2 1 5 4) |
| (425 475 50 50 1 hard) | (4 3 2 1 3 6) |
| (525 575 50 0 1 very hard) | (5 2 2 1 4 1) |
| # 1 Depth of cut (mm) | (5 2 2 1 2 2) |
| (0.05 1.5 0 2.5 1 finishing) | (5 2 2 1 1 4) |
| (3 5 2 3 1 semi-finish.) | (1 1 1 2 9 2) |
| (7 9 3 6 1 roughing) | (1 2 1 2 8 7) |
| (14 16 6 0 1 power rough.) | (1 3 1 2 7 9) |
| # 1 Carbon content (%) | (1 4 1 2 6 10) |
| (0.05 0.25 0 0.05 1 low) | (2 1 1 2 8 2) |
| (0.30 0.50 0.05 0.07 1 medium) | (2 2 1 2 7 7) |
| (0.60 0.90 0.08 0.00 1 high) | (2 3 1 2 6 9) |
| # 1 Usinability | (2 4 1 2 5 10) |
| (0 25 0 50 1 Improved) | (2 1 2 2 8 2) |
| (75 100 50 0 1 normal) | (2 2 2 2 7 7) |
| - 1 Speed (m/min) | (2 3 2 2 6 9) |
| (31 35 0 2 1 sl) | (2 4 2 2 4 10) |
| (37 43 2 3 1 el) | (3 1 2 2 7 2) |
| (46 52 3 4 1 vl) | (3 2 2 2 6 6) |
| (56 64 4 5 1 l) | (3 3 2 2 5 7) |
| (70 78 5 6 1 ml) | (4 1 2 2 5 1) |
| (86 96 6 7 1 med.) | (4 2 2 2 4 4) |
| (105 119 7 8 1 mh) | (4 3 2 2 3 6) |
| (129 147 8 9 1 high) | (5 1 2 2 4 1) |
| (158 182 9 10 1 v.high) | (5 2 2 2 2 2) |
| (195 225 11 12 1 ext.high) | (5 3 2 2 1 4) |
| (240 280 12 0 1 sup.high) | (2 1 3 2 8 2) |
| - 1 Feedrate (mm/rev) | (2 2 3 2 7 7) |
| (0.11 0.14 0.0 0.02 1 sl) | (2 3 3 2 5 9) |
| (0.17 0.19 0.02 0.02 1 el) | (2 4 3 2 4 10) |
| (0.21 0.23 0.02 0.03 1 vl) | (3 1 3 2 7 2) |
| (0.26 0.28 0.03 0.03 1 l) | (3 2 3 2 6 6) |
| (0.32 0.36 0.04 0.03 1 ml) | (3 3 3 2 4 7) |
| (0.40 0.45 0.05 0.03 1 med.) | (4 1 3 2 5 1) |
| (0.50 0.56 0.05 0.04 1 m.high) | (4 2 3 2 4 4) |
| (0.62 0.70 0.06 0.04 1 high) | (4 3 3 2 3 6) |
| (0.78 0.86 0.07 0.05 1 v.high) | (5 1 3 2 4 1) |
| (0.95 1.09 0.10 0.00 1 ext.high) | (5 2 3 2 2 2) |
| | (5 3 3 2 1 4) |
| (1 1 1 1 1 1 2) | |
| (1 2 1 1 1 0 7) | |
| (1 3 1 1 8 9) | |
| (1 4 1 1 7 1 0) | |
| (2 1 1 1 1 1 2) | |
| (2 2 1 1 1 0 7) | |
| (2 3 1 1 9 9) | |
| (2 4 1 1 7 1 0) | |
| (1 1 2 1 1 0 2) | |
| (1 2 2 1 9 7) | |
| (1 3 2 1 8 9) | |
| (1 4 2 1 7 1 0) | |
| (2 1 2 1 9 2) | |
| (2 2 2 1 8 7) | |
| (2 3 2 1 7 9) | |
| (2 4 2 1 6 1 0) | |
| (3 1 2 1 8 2) | |

EXEMPLE DES DONNES ET DES REGLES EN FORME LINGUISTIQUE "coupeang.reg"

PREMISSE Hardness (Bhn)
very soft = (100 175 0 50 1 very soft)
soft = (225 275 50 50 1 soft)
medium = (325 375 50 50 1 medium)
hard = (425 475 50 50 1 hard)
very hard = (525 575 50 0 1 very hard)

PREMISSE Depth of cut (mm)
finishing = (0.05 1.5 0 2.5 1 finishing)
semi-finish. = (3 5 2 3 1 semi-finish.)
roughing = (7 9 3 6 1 roughing)
power rough. = (14 16 6 0 1 power rough.)

PREMISSE Carbon content (%)
low = (0.05 0.25 0 0.05 1 low)
medium = (0.3 0.5 0.05 0.07 1 medium)
high = (0.6 0.9 0.08 0 1 high)

PREMISSE Usinability
Improved = (0 25 0 50 1 Improved)
normal = (75 100 50 0 1 normal)

CONCLUSION Speed (m/min)
sl = (31 35 0 2 1 sl)
el = (37 43 2 3 1 el)
vl = (46 52 3 4 1 vl)
l = (56 64 4 5 1 l)
ml = (70 78 5 6 1 ml)
med. = (86 96 6 7 1 med.)
mh = (105 119 7 8 1 mh)
high = (129 147 8 9 1 high)
v.high = (158 182 9 10 1 v.high)
ext.high = (195 225 11 12 1 ext.high)
sup.high = (240 280 12 0 1 sup.high)

CONCLUSION Feedrate (mm/rev)
sl = (0.11 0.14 0 0.02 1 sl)
el = (0.17 0.19 0.02 0.02 1 el)
vl = (0.21 0.23 0.02 0.03 1 vl)
l = (0.26 0.28 0.03 0.03 1 l)
ml = (0.32 0.36 0.04 0.03 1 ml)
med. = (0.4 0.45 0.05 0.03 1 med.)
m.high = (0.5 0.56 0.05 0.04 1 m.high)
high = (0.62 0.7 0.06 0.04 1 high)
v.high = (0.78 0.86 0.07 0.05 1 v.high)
ext.high = (0.95 1.09 0.1 0 1 ext.high)

RULE 1
IF Hardness (Bhn) is very soft
AND Depth of cut (mm) is finishing
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is sup.high
AND Feedrate (mm/rev) is el

RULE 2
IF Hardness (Bhn) is very soft

AND Depth of cut (mm) is semi-finish.
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is ext.high
AND Feedrate (mm/rev) is m.high

RULE 3
IF Hardness (Bhn) is very soft
AND Depth of cut (mm) is roughing
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is high
AND Feedrate (mm/rev) is v.high

RULE 4
IF Hardness (Bhn) is very soft
AND Depth of cut (mm) is power rough.
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is mh
AND Feedrate (mm/rev) is ext.high

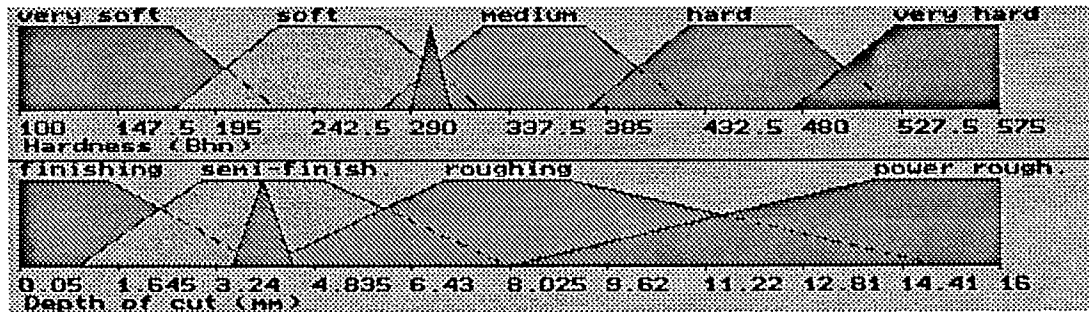
RULE 5
IF Hardness (Bhn) is soft
AND Depth of cut (mm) is finishing
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is sup.high
AND Feedrate (mm/rev) is el

RULE 6
IF Hardness (Bhn) is soft
AND Depth of cut (mm) is semi-finish.
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is ext.high
AND Feedrate (mm/rev) is m.high

RULE 7
IF Hardness (Bhn) is soft
AND Depth of cut (mm) is roughing
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is v.high
AND Feedrate (mm/rev) is v.high

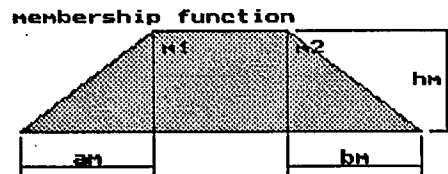
RULE 8
IF Hardness (Bhn) is soft
AND Depth of cut (mm) is power rough.
AND Carbon content (%) is low
AND Usinability is Improved
THEN Speed (m/min) is mh
AND Feedrate (mm/rev) is ext.high

RULE 9
IF Hardness (Bhn) is very soft
AND Depth of cut (mm) is finishing
AND Carbon content (%) is medium

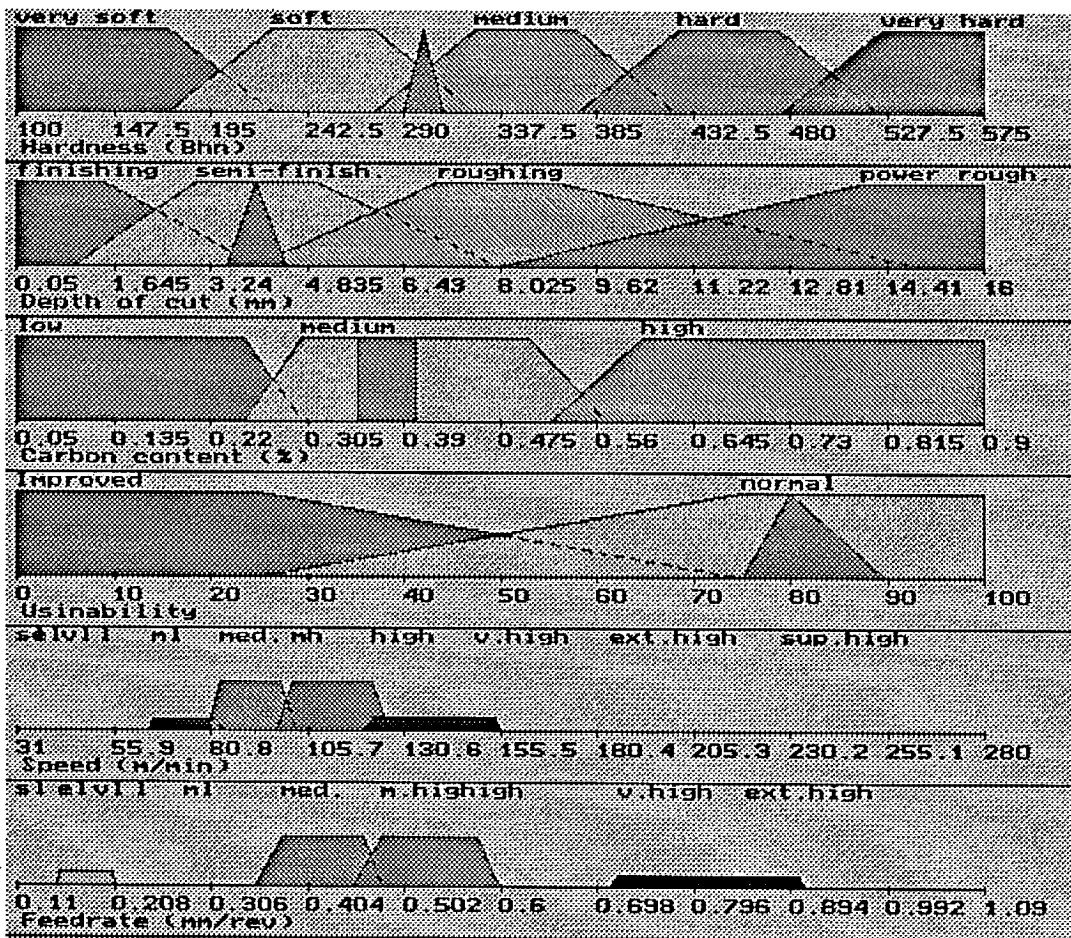


Input observation 2 Depth of cut (mm)

m1= 4
m2= 4
am= 0.5
bm= 0.5
hm= 1

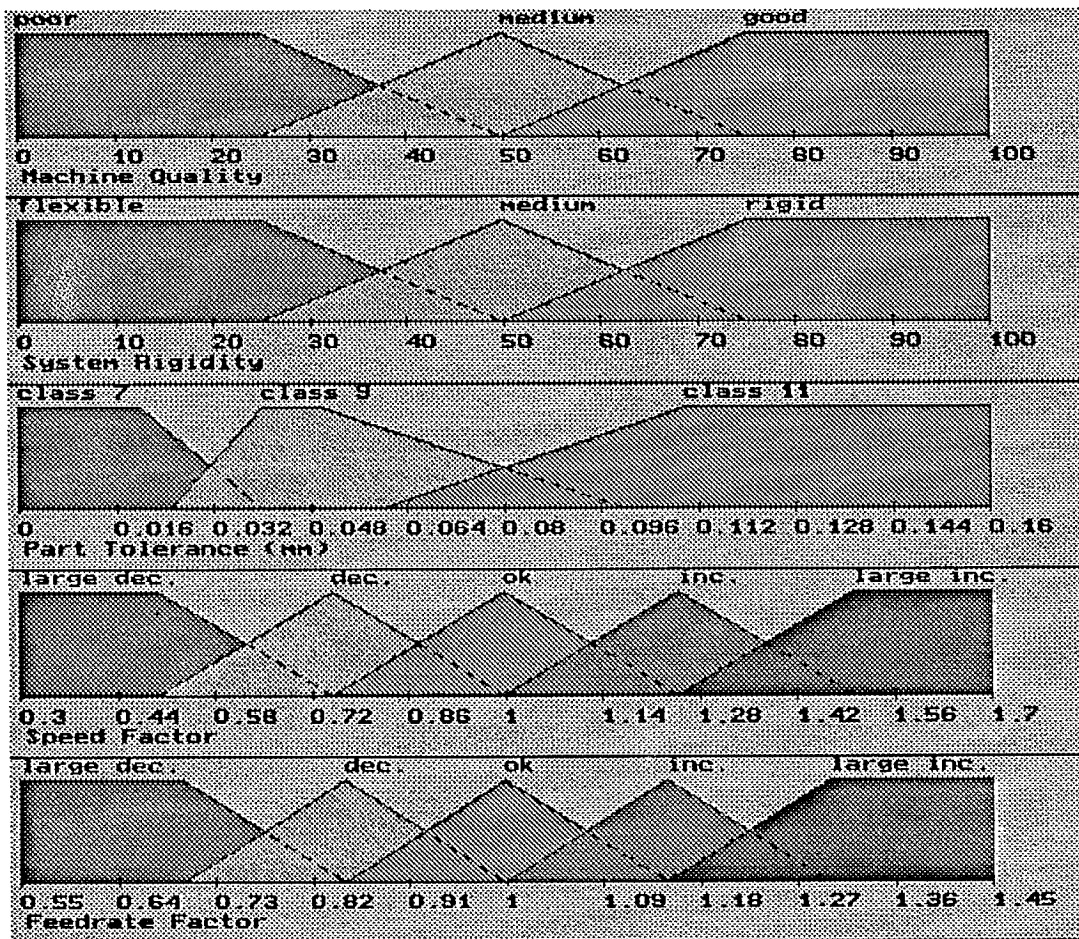


**EXEMPLE D'INTRODUCTION DES OBSERVATIONS
POUR LE CHOIX DES CONDITIONS DE COUPE**

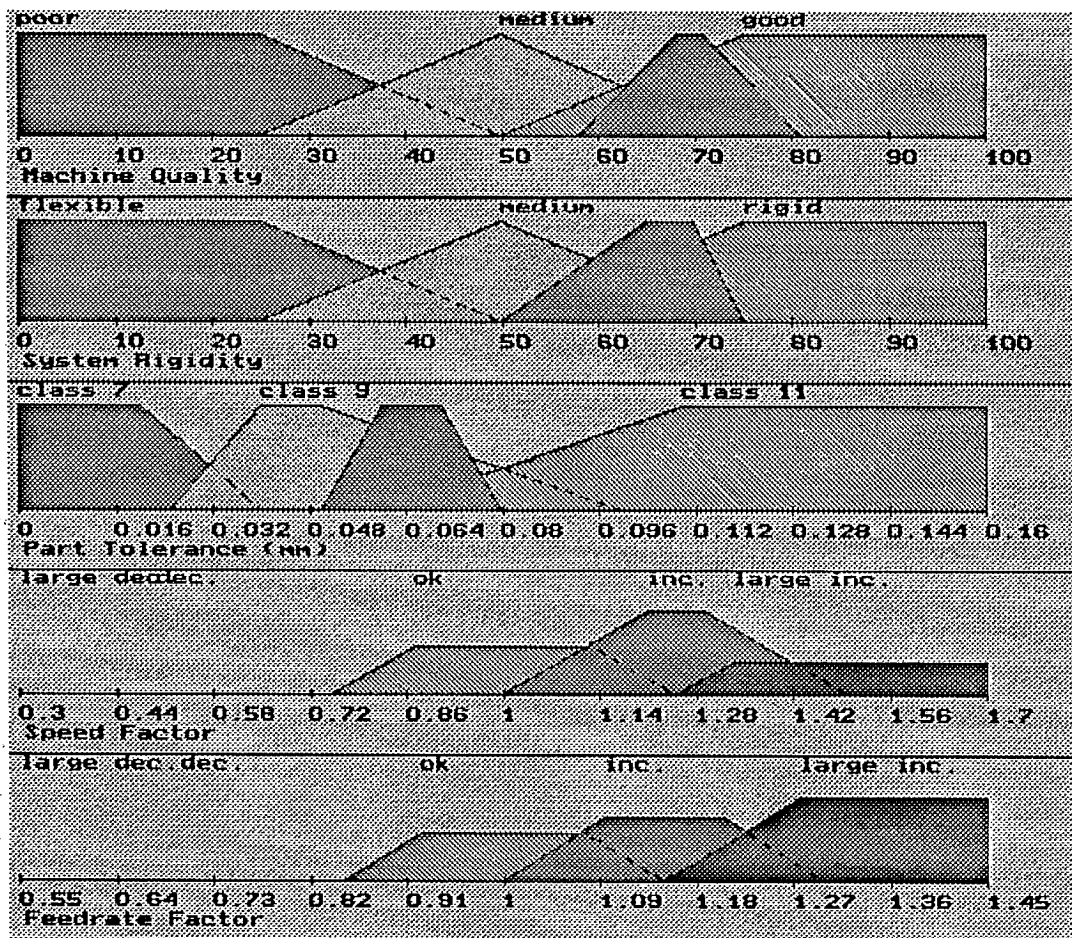


| | |
|---------------------------------------|---------|
| Control value of, Speed (m/min) : | 106.8 |
| Control value of, Feedrate (mm/rev) : | 0.51318 |

EXEMPLE DE CHOIX DES CONDITIONS DE COUPE
 CONCLUSIONS EN FORME LINGUISTIQUE ET NUMÉRIQUE



REPRÉSENTATION GRAPHIQUE DES VARIABLES LINGUISTIQUES
DES CONDITIONS ET DES CONCLUSIONS
POUR LA CORRECTION DES CONDITIONS DE COUPE



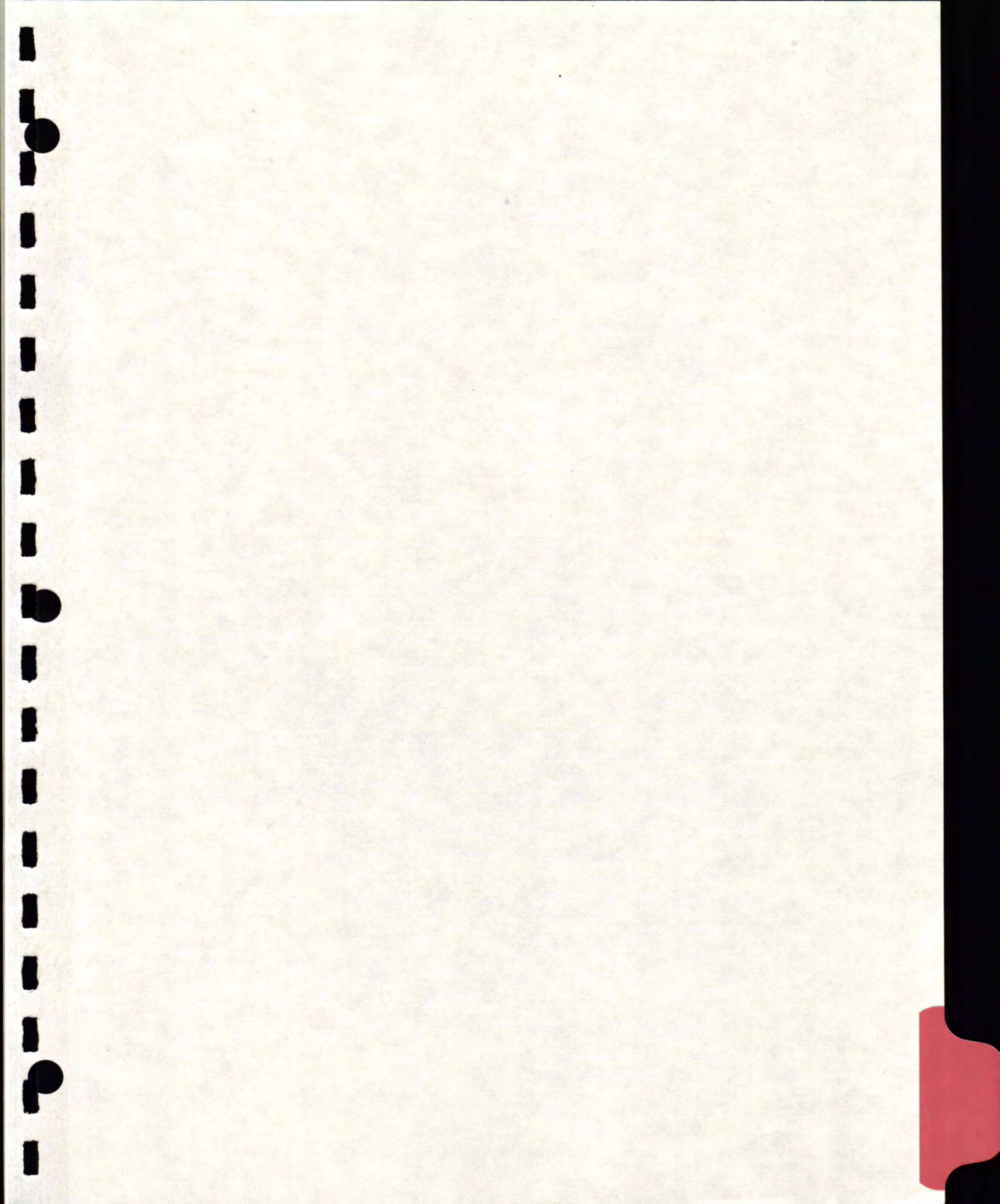
Control value of, Speed Factor : 1.2276
 Control value of, Feedrate Factor : 1.193

EXEMPLE DE LA CORRECTION DES CONDITIONS DE COUPE
 CONCLUSIONS EN FORMES LINGUISTIQUE ET NUMÉRIQUE

CONCLUSION

L'exemple présenté montre que la logique floue est un outil approprié pour traiter les problèmes de fabrication :

- La méthode de raisonnement approximatif est appropriée pour le problème du choix des conditions de coupe parce qu'elle permet d'utiliser la connaissance heuristique disponible dans les ateliers de fabrication.
- Les performances et la robustesse de cette méthode sont adéquates pour les applications pratiques dans les ateliers de fabrication.
- Grâce à la compression des données, le nombre de règles est considérablement réduit.
- L'utilisation des variables linguistiques simplifie la préparation de la base de connaissances et facilite la consultation.



@ AutoSoft

AutoSoft

5655, Élie Avenue, #404
St. Hubert, (Québec)
J3Y 6P3

*Specialist in ind.
control*

SYSTÈMES DE CONTRÔLES - LOGIQUE FLOUE
CONTROL SYSTEMS - FUZZY LOGIC

Bruno Arnold
Stéphane Brûlé
Mario Deschênes
Jean-François Ouellet

9 mars 1994

AutoSoft

5655, av. Élie, #404
Saint-Hubert, (Québec)
J3Y 6P3
Tél.:(514) 656-2323
Fax:(514) 656-1009

Bruno Arnold
Stéphane Brulé
Mario Deschênes
Jean-François Ouellet

RÉSUMÉ D'EXPOSÉ

1. Description du projet

Notre projet est le développement d'algorithmes d'adaptation autour de la logique floue afin de la rendre auto-corrective.

Le projet vise à rehausser significativement le calibre des régulateurs analogiques avec l'approche S.I.F.A.N.A.

Ces techniques logicielles sont ensuite intégrées dans l'automate AutoSoft. Elles permettent alors d'agir concrètement sur un procédé quelconque.

2. Survol de la logique floue classique

Il s'agit d'une approche intuitive contrairement à une approche de modélisation. Son but est de quantifier des phénomènes dont nous ne possédons qu'une perception qualitative du fonctionnement.

L'annexe "A" du plan d'affaires peut être considéré comme référence de base.

La logique floue apporte cependant quelques contraintes à l'utilisateur car les ajustements sont très longs et ne s'effectuent que par "essais et erreurs", d'où le besoin d'un système adaptatif.

3. Sommaire du SIFANA

Le mot SIFANA signifie : **S**ystème d'**i**nférence flou à noeuds adaptatifs.

L'approche SIFANA :

- est intuitive
- possède très peu de paramètres à configurer
- est à la portée d'un opérateur averti
- est auto-adaptative
- accepte plus d'un capteur en entrée et en sortie

Ce système est applicable autant pour les procédés qui sont linéaires ou non, peu ou non connus, chaotiques et dont la dynamique peut varier.

Le schéma bloc décrit son architecture de fonctionnement.

4. Résultats obtenus

Exemple d'un pendule inverse :

- quelle approche doit prendre un utilisateur de SIFANA;
- apprentissage : résultats des antécédences et des conséquences;
- essai d'un asservissement type avec un angle de 10 degrés;

5. Avantages majeurs

- 1- réduction du temps de mise en oeuvre;
- 2- protège contre les impondérables;
- 3- ouvre de nouvelles avenues au contrôle de procédés complexes.

6. Impacts sociaux

- 1- Le SIFANA permet d'augmenter la popularité des technologies à logique floue afin de viser une certaine reconnaissance ou acceptance de la part de l'industrie du contrôle.
- 2- Libère l'ingénieur des contraintes de modélisation et d'optimisation.

7. Marchés visés

Industriels : - neutralisation du pH;
- neutralisation du pH simultanément avec la régulation du chlore;
- contrôle des générateurs d'ozone haute puissance d'Envitech Inc.;
- régulation de procédés chimiques;
- régulation générale et/ou formation en systèmes flous.

Commerciaux (contrôle du bâtiment) :

- aide à l'optimisation des économies d'énergie avec les experts en contrôle du bâtiment de Contrologie Inc.

8. Impacts du projet sur l'entreprise en phase de démarrage

Phases du projet :

- 1) Étude de faisabilité
- 2) Recherche théorique et choix des méthodes
- 3) Orientation du projet vers un SIFANA
- 4) Développements mathématiques et théoriques du système
- 5) Programmation et premiers essais du système
- 6) Tests avec procédés simulés
- 7) Tests avec des procédés réels (pendule inverse et pH-cl)
- 8) Mise en marché et support des clients (formation, etc.)

Seules les étapes 7 et 8 restent à compléter.

Ce projet s'intègre dans le système de contrôle actuel d'AutoSoft et devrait apporter une croissance et des emplois intéressants tel qu'estimé dans le plan d'affaires.

@AutoSoft

Bruno Arnold
Stéphane Brûlé
Mario Deschênes
Jean-François Ouellet

AutoSoft

5655, Elle ave., #404
St. Hubert (Québec)
J3Y 6P3
Tel.:(514) 656-2323
Fax:(514) 656-1009

ABSTRACT

1. Project Description

This project consists in the development of adaptation algorithms to modify actual fuzzy logic techniques into a general adaptive regulation control system.

The main goal is to significantly increase performance and grade of analog regulators with the Adaptive Network-based Fuzzy Inference System - ANFIS - approach.

Our physical control system, named AutoSoft, applies those sophisticated software techniques. Once combined, they generate all necessary concrete actions on a process.

2. Overview of classical fuzzy logic

The control approach under fuzzy logic is intuitive, rather than modelling as in common design approach. Fuzzy concept's goal is to quantify phenomena of which we only have qualitative perception.

Appendix A, contained in the business plan, can be considered a basic reference.

In spite of its advantages, fuzzy logic imposes many constraints on the user in the adjustment of fuzzy sets: the longest part of a fuzzy startup. Furthermore, these settings can only be done on a "trial and error" basis, reinforcing the need for an adaptive system.

3. Adaptive Network-based Fuzzy Inference System (ANFIS)

The ANFIS approach:

- is intuitive
- has only a few parameters to configure
- is self-adaptive
- accepts many inputs as well as outputs

ANFIS is suitable for processes being either linear or non-linear, either well known, misunderstood or chaotic, and of which dynamics may vary.

4. Results obtained

Example of an inverted pendulum:

- the approach the ANFIS' user should take;
- results of the final antecedents and the final consequences;
- attempting a closed-loop control with a starting angle of 10 degrees;

5. Major advantages

- 1- reduced start up time;
- 2- protection against imponderables;
- 3- new possibilities for complex processes.

6. Social impacts

- 1- Increased acceptance of fuzzy technologies brought by ANFIS could reach a point of global recognition in industrial control.
- 2- Relieves engineers of the modelling and optimization burden.

7. Target markets

Industrial: - pH neutralization;
 - pH neutralization and chlorination regulation simultaneously;
 - high power ozone generator control;
 - chemical process regulation;
 - fuzzy system training and seminars.

Commercial (building environment control): - help in optimizing energy savings.

8. Competitive situation

In our opinion, AutoSoft is the absolute leader in its field. There is no other similar system currently on the market. However, a definite trend towards fuzzy logic is predictable as some of the largest controller manufacturers show interest in it. Moreover, no one offers self-adaptive features in their fuzzy products.

9. Consequences of this project on our starting company

Project's steps: 1) Feasibility study
 2) Theoretical research and orientation on the ANFIS approach
 3) System development, programming and system's first tries
 4) Tests with a simulated process
 5) Tests with real processes (inverted pendulum and pH-Cl)
 6) Production, sales and customer support (training, etc.)

We are now at step 5.

This project is part of AutoSoft's control system. As shown in our business plan, it should achieve above average growth and create many employments.

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Block diagram of ANFIS (fuzzy controller) and a process

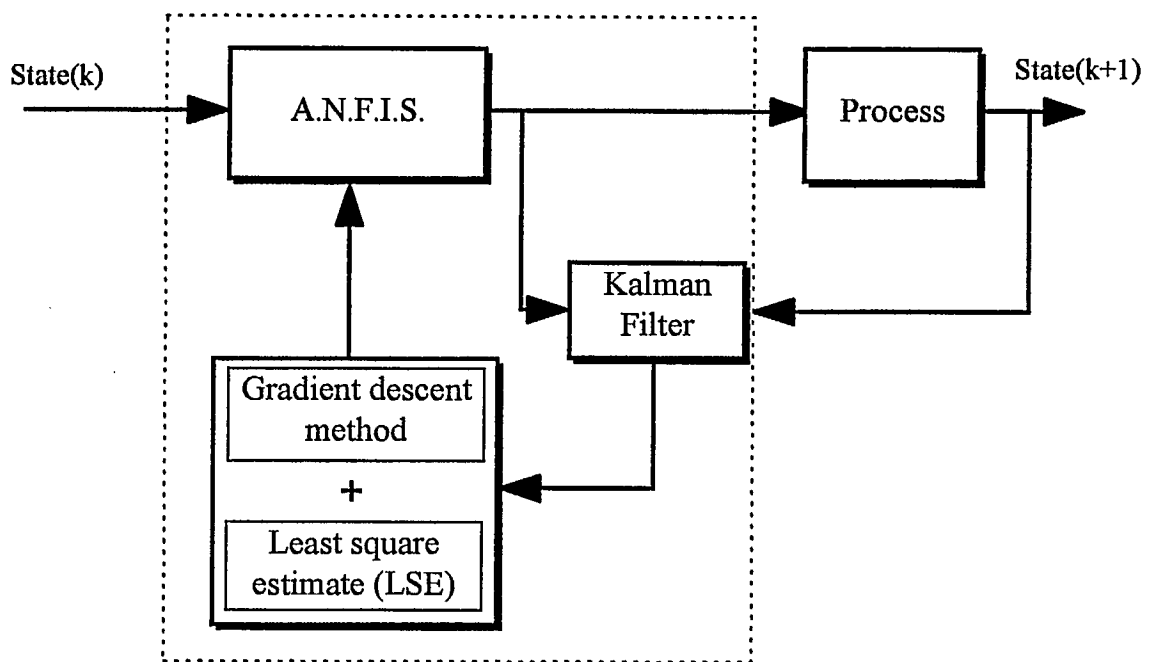


Figure 1

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ANFIS : Adaptive-Network-Based Fuzzy Inference System

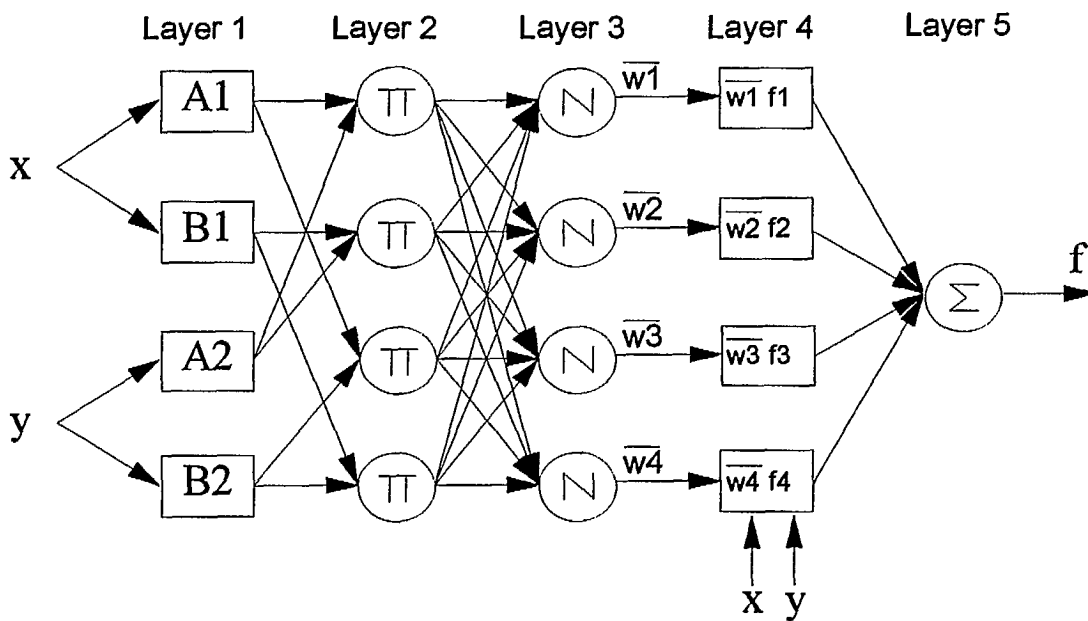


Figure 2

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Example of an inverted pendulum

$$\ddot{\Theta} = \frac{g \cdot \sin \Theta + \cos \Theta * \left(\frac{-F - m * l * \Theta^2 * \sin \Theta}{m_c + m} \right)}{l * \left(\frac{4}{3} - \frac{m * \cos^2 \Theta}{m_c + m} \right)}$$

- theta: angle of the pole
- g: acceleration due to gravity
9.8 m/s²
- m_c: mass of the cart 1.0 kg
- m: mass of pole 0.1 kg
- l: half-length of pole 0.5 m
- F: force applied in newtons

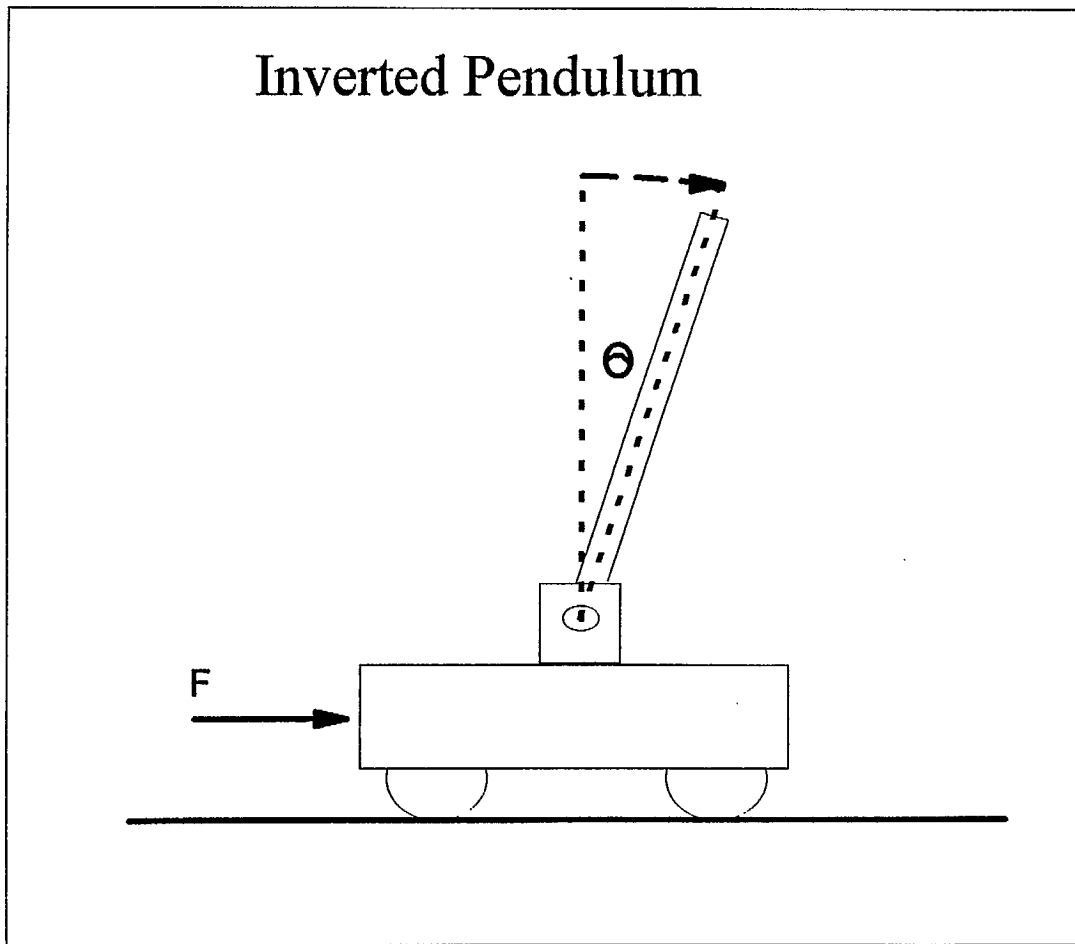


Figure 3



Initial and final fuzzy sets for the inverted pendulum

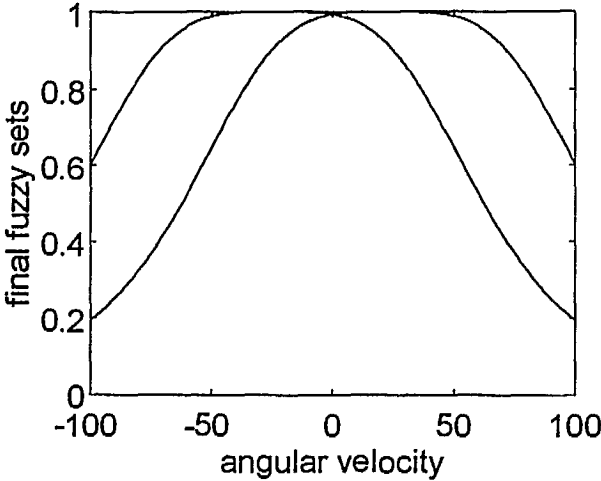
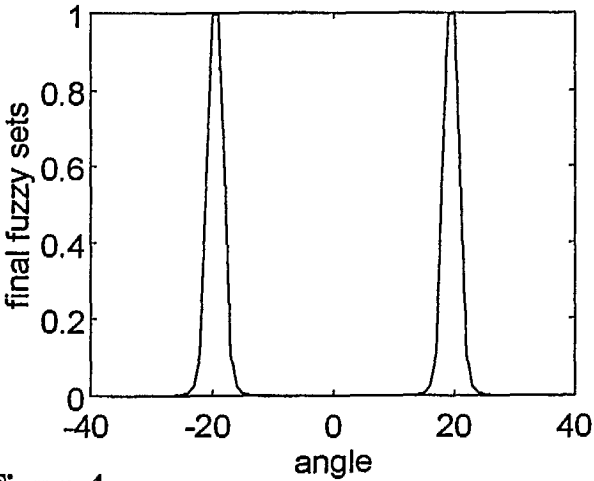
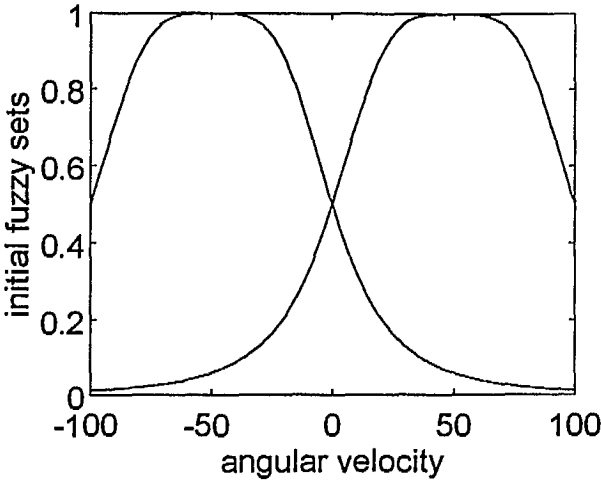
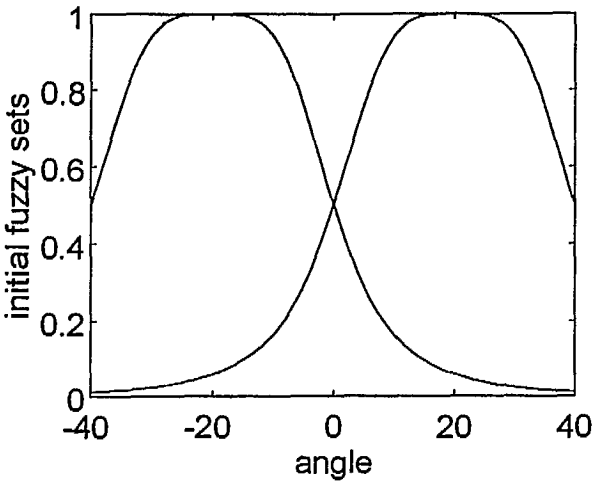


Figure 4



Initial control action surface for the inverted pendulum

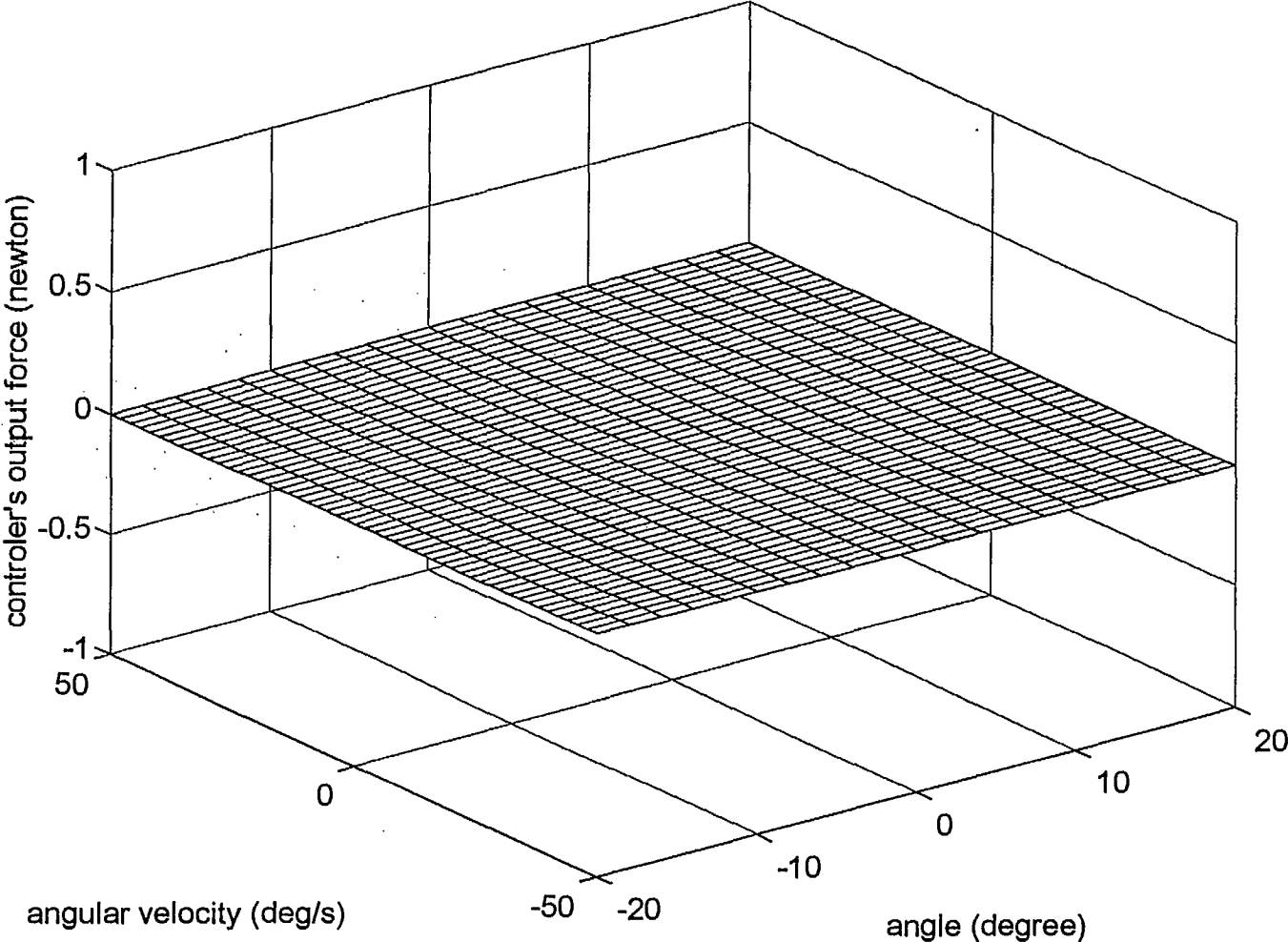


Figure 5



Control action surface after 1 epoch

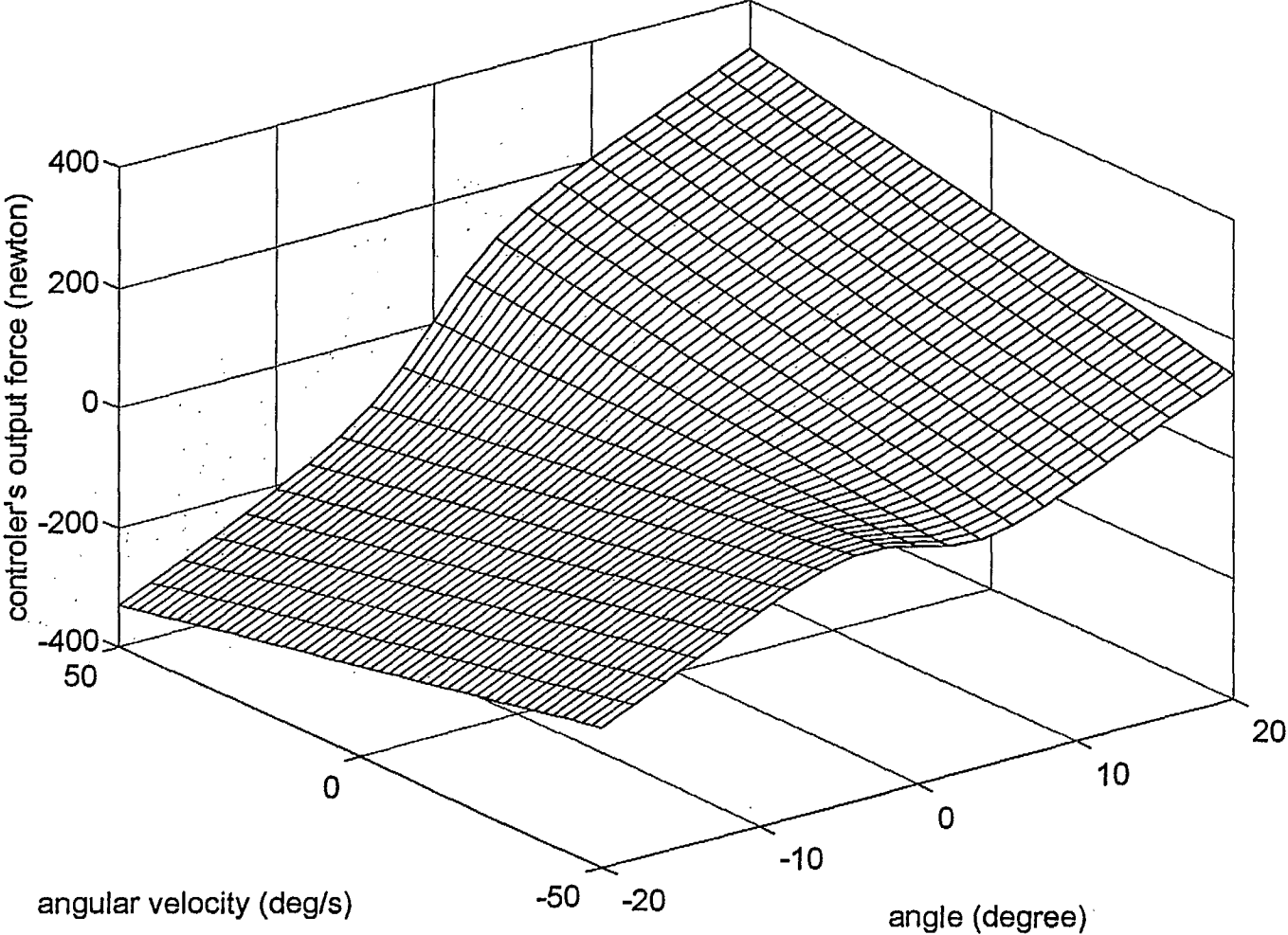


Figure 6



Final control action surface

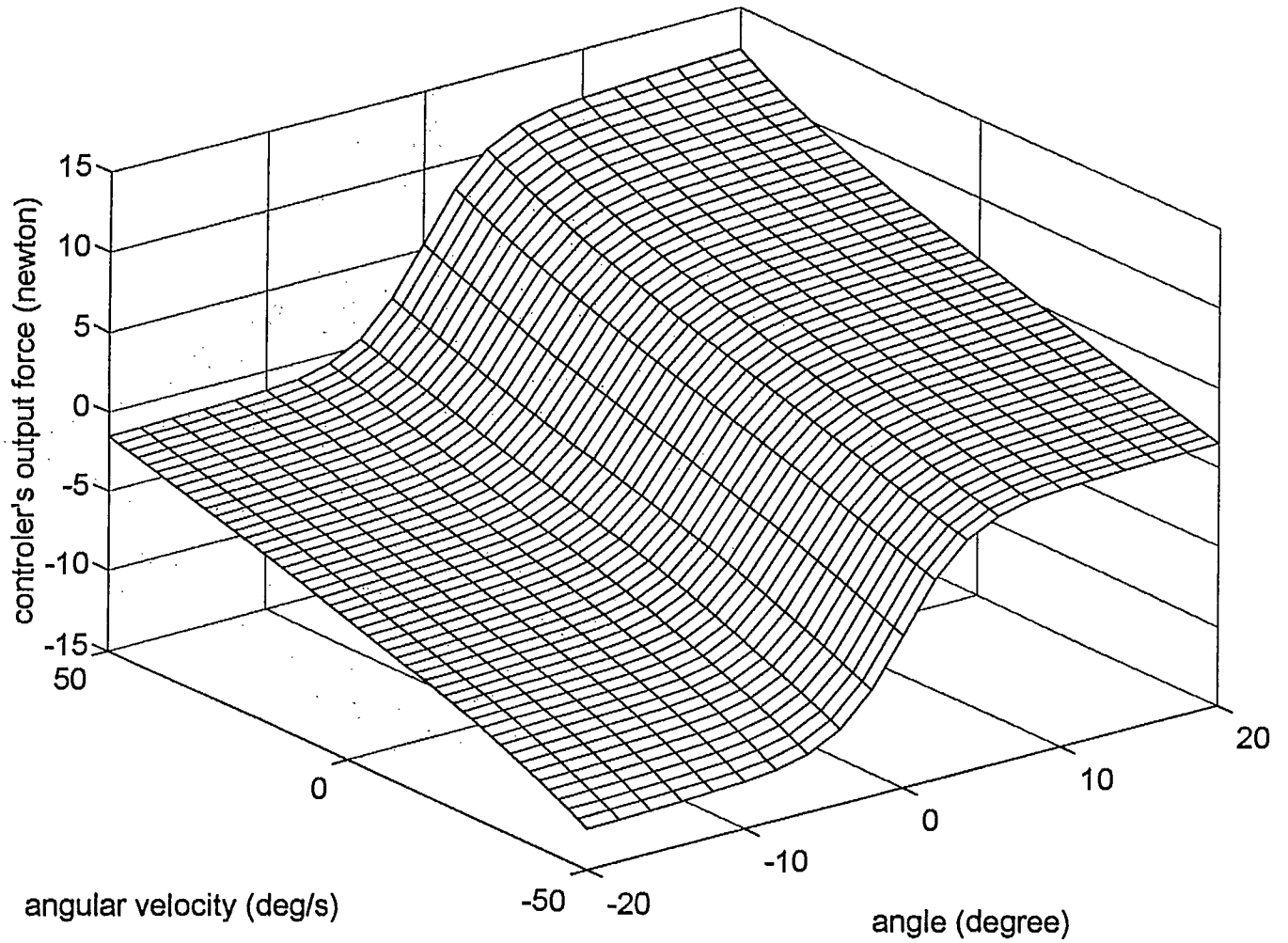


Figure 7



Some results for the inverted pendulum

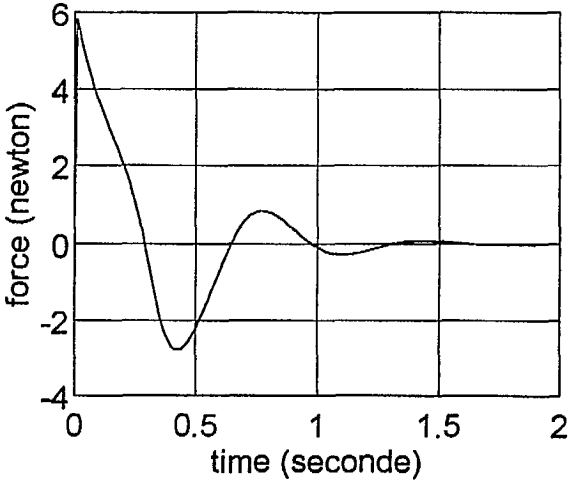
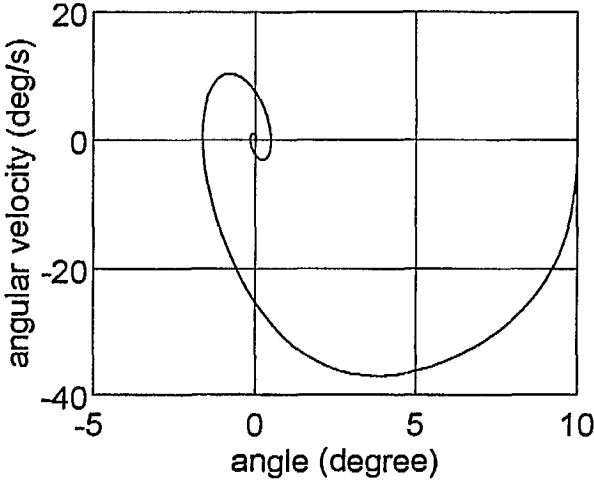
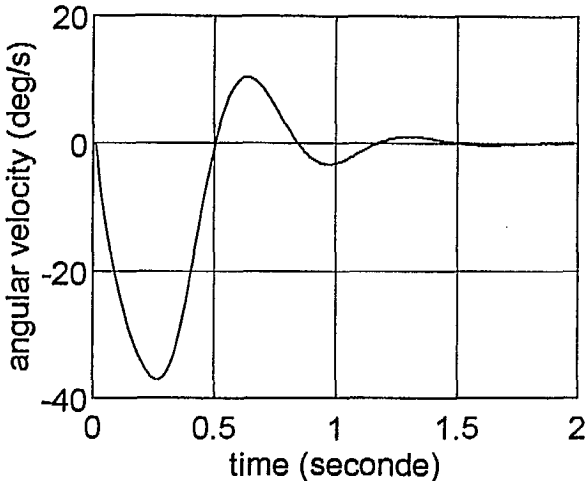
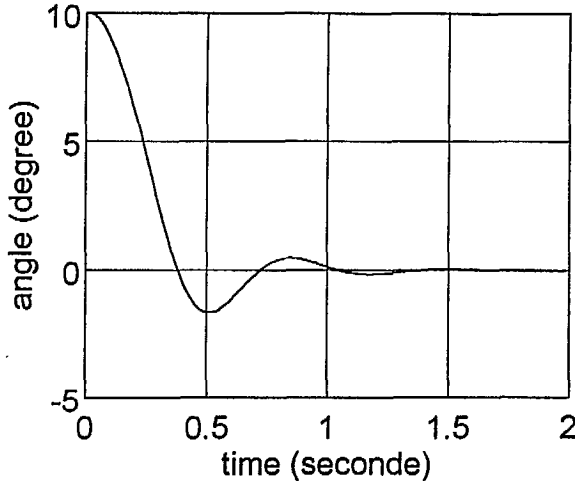


Figure 8



Comparison between 1st order PID controller and ANFIS in ON-LINE learning mode for motor velocity control

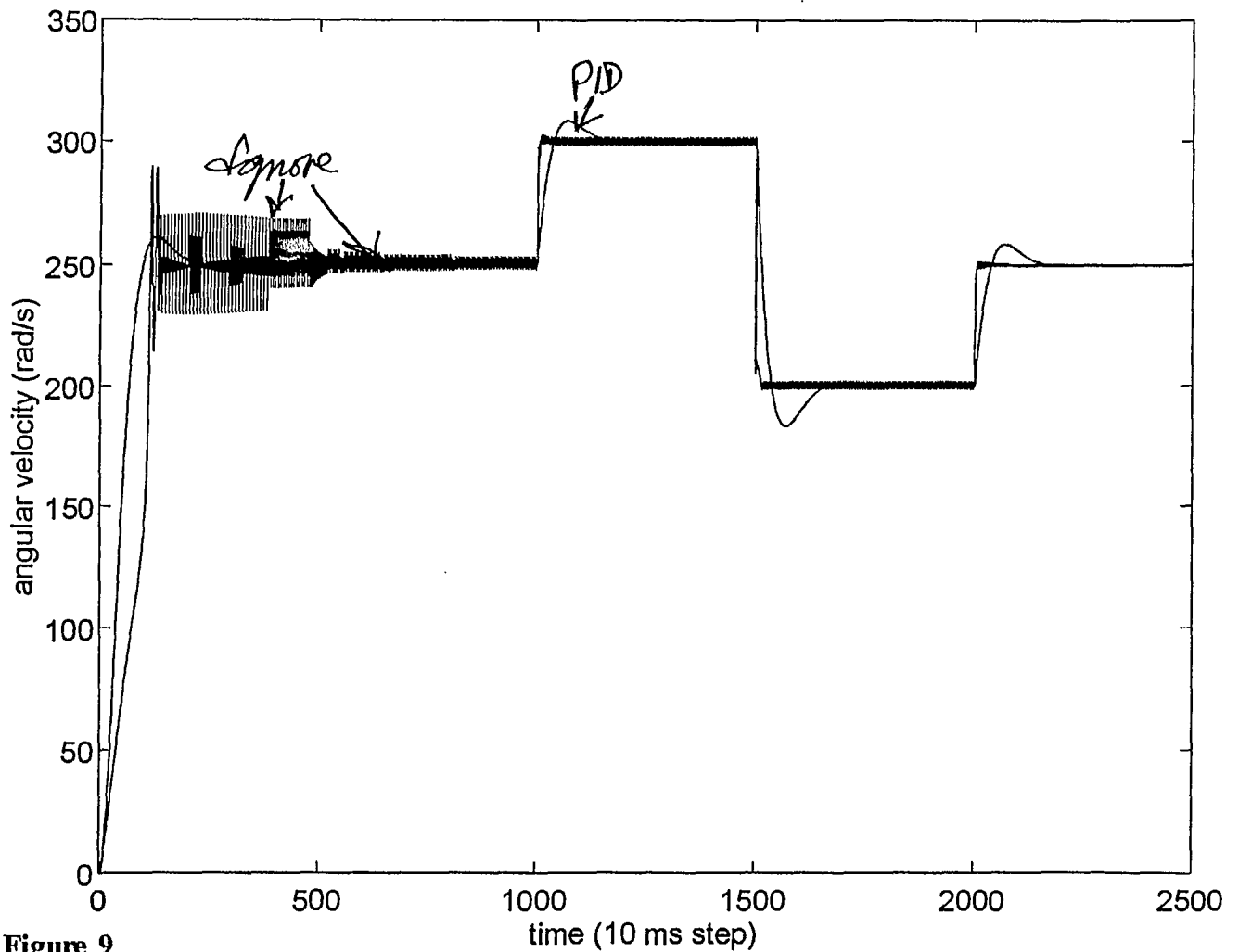


Figure 9

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First Canadian Workshop on F

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